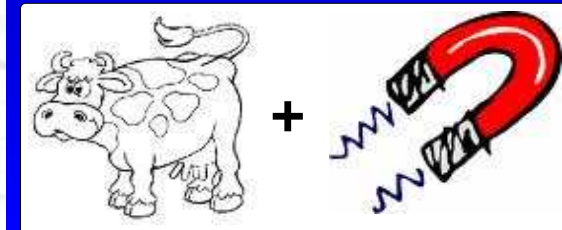


# Lecture I

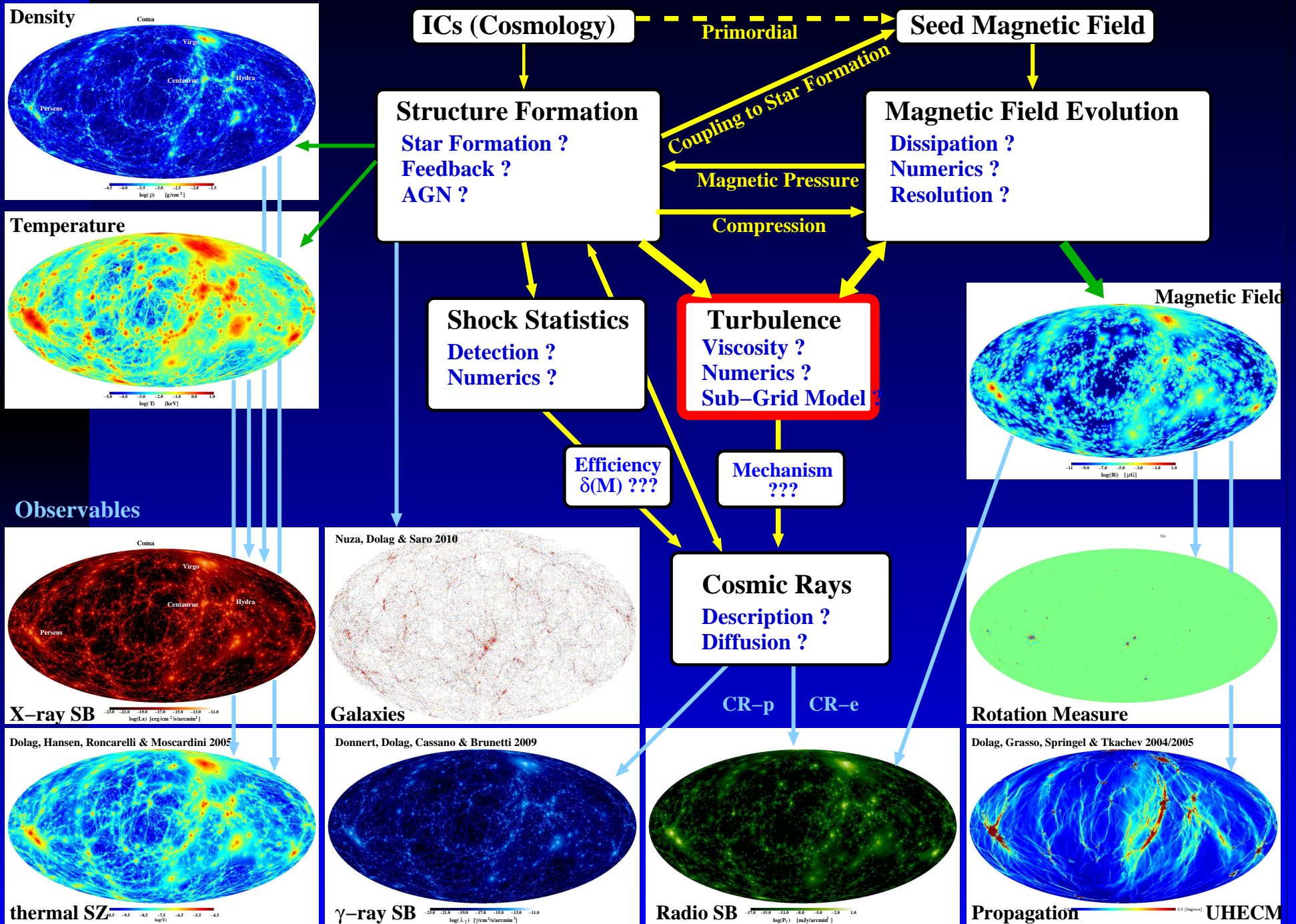
## Magnetic Fields in Clusters RMs and Radio emission

Klaus Dolag

Universitäts-Sternwarte München, LMU

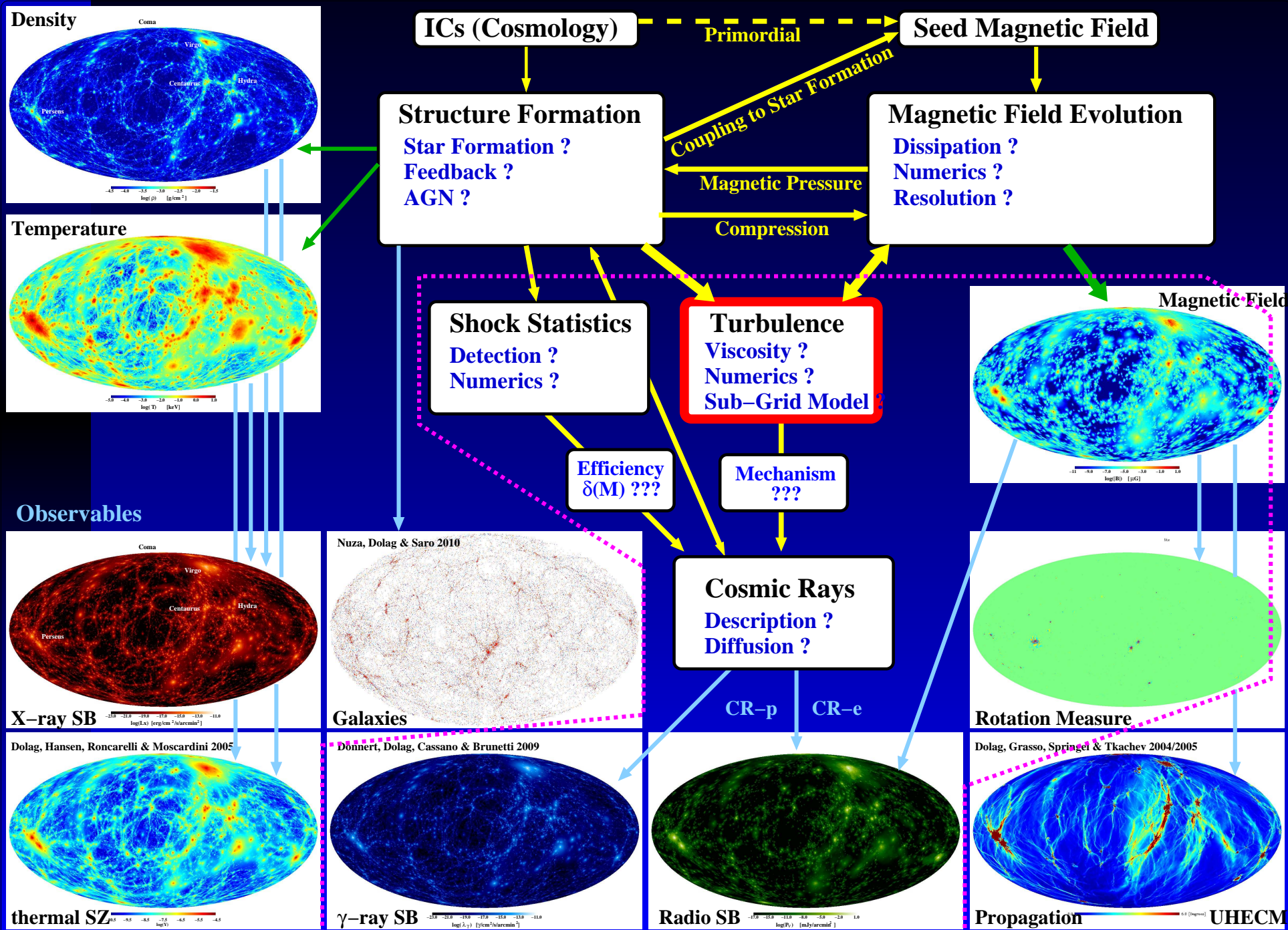


# Process Network








# Process Network



# Outline

- Introduction
  - Historic Milestones (Example: Coma cluster)
  - Observations
  - The Big Picture
  -  part 1
- Faraday Rotation Measures
  - Cluster Samples
  - Individual Clusters
  - Constraining Magnetic Field properties
  -  part 2
- Diffuse Radio emission
  - Radio Haloes
  - Radio Relics
  - Scaling relations
- Summary
  -  part 3





CI 0024+17

NASA, ESA, M.J. Jee and H. Ford (Johns Hopkins University)

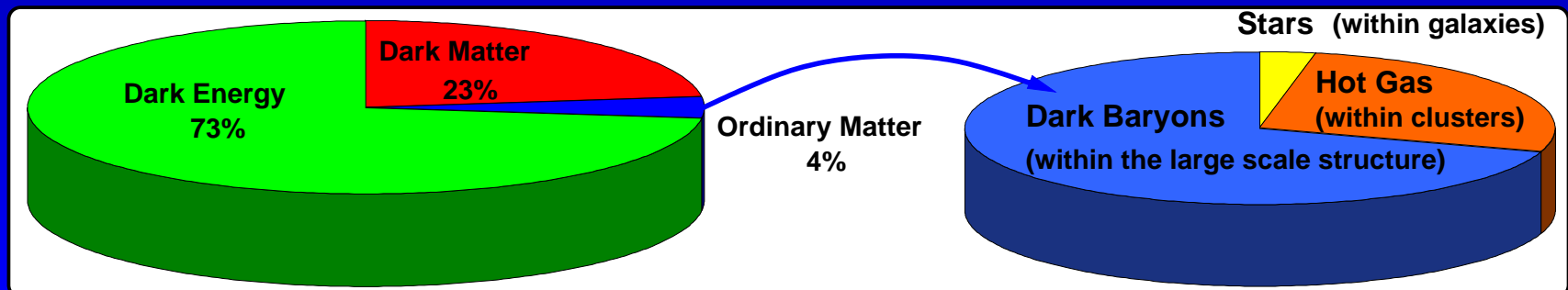
# Galaxy Clusters in Numbers

Galaxy clusters are the largest, gravitationally bound objects in the Universe and represent an almost fair sample of the cosmological composition.

- Up to thousands of galaxies with  $\sigma_{\text{gal}}$  up to 1000 km/s
- Size ( $R_{\text{cluster}}$ ) of several Mpc
- Large Reynolds numbers ( $\Rightarrow$  turbulence)
- Total mass ( $M_{\text{tot}}$ ) up to several  $10^{15} M_{\odot}$  ( $\Rightarrow$  dark matter)
- Nearly cosmic baryon fraction ( $\approx 95\%$ )
- ICM temperatures ( $T_{\text{ICM}}$ ) higher than  $10^8 \text{K}$

Observed to be virialized:

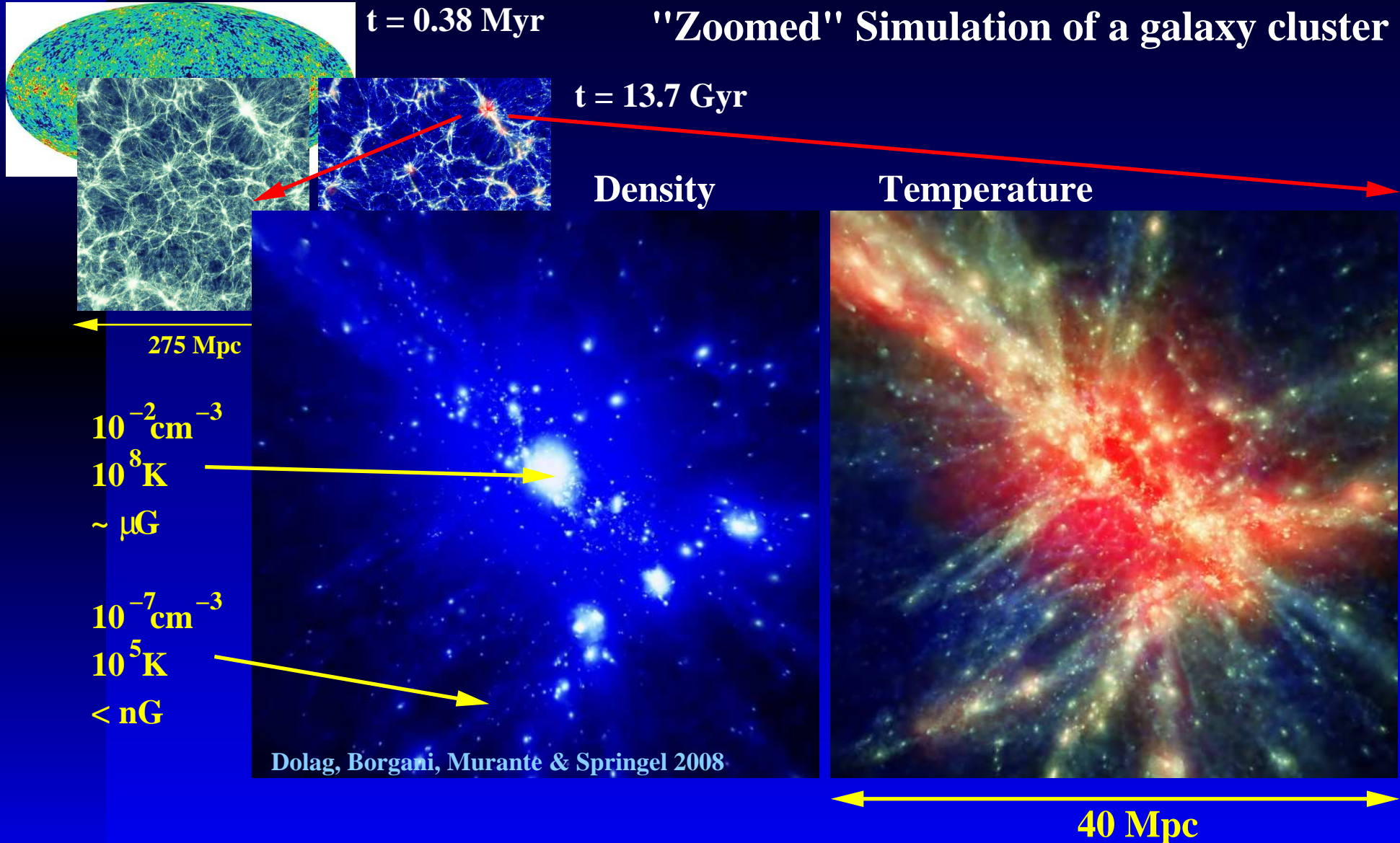
$$3\sigma_{\text{galaxies}}^2 \approx \frac{GM_{\text{tot}}}{R_{\text{cluster}}} \approx \frac{3kT_{\text{ICM}}}{2\mu m_p}$$





# Galaxy Clusters in Numbers

Clusters form at the nodes of the cosmic web and may be utilized to investigate the physical state of diffuse baryons.

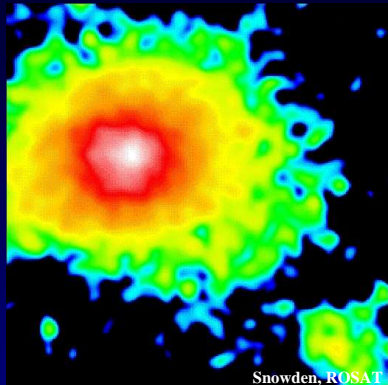


$$v_{\text{sound}} \approx 1500 > \sigma_{\text{gal}} \approx 1000 > v_{\text{turb}} \approx 300 > v_{\text{Alfven}} \approx 100 \text{ km/s}$$



# Galaxy Clusters in Numbers

Observations ( $\Rightarrow$ ), Simulations ( $\Leftarrow$ ) and the role of  $\vec{B}$ :



ICM (X-ray,  $T \approx 10^8$  K, Bremsstrahlung):

$\Rightarrow$  Dynamical state of ICM

$\Leftarrow$  Non thermal **pressure** support

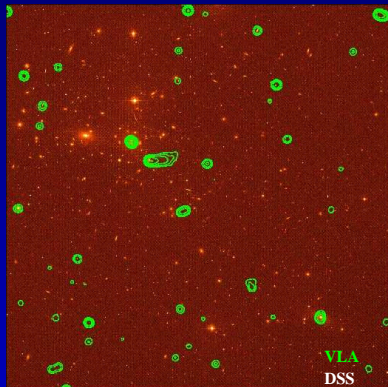
$\Leftarrow$  **Turbulence, Viscosity**, Shocks

Galaxies (optical, radio,  $N_{\text{gal}} > 1000$ ):

$\Rightarrow$  Interaction with the ICM

$\Leftarrow$  Galaxies in dense environment (**stripping**, distribution of metals)

$\Leftarrow$  Magnetic field **seeding** (outflows)

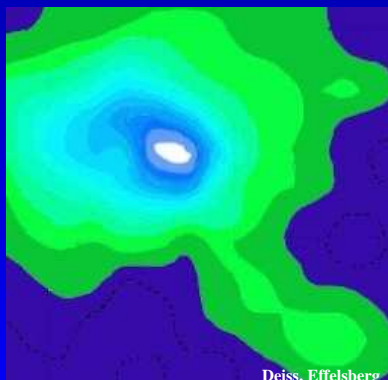


ICM (radio, synchrotron radiation, RM):

$\Rightarrow$  Distribution of  $\vec{B}$ , CRs (diffuse + RM)

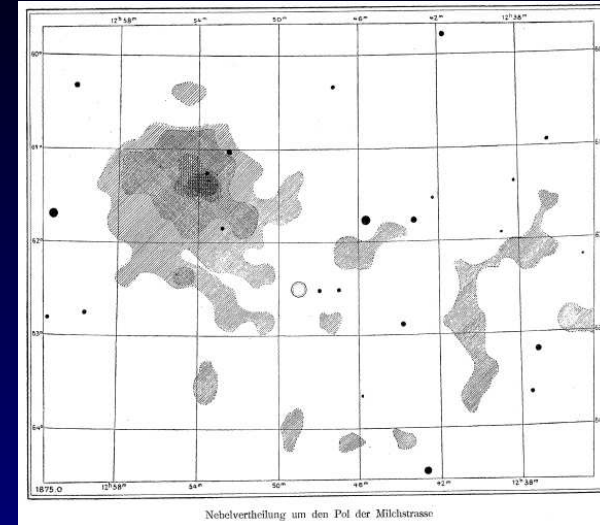
$\Leftarrow$  **Evolution** and **buildup** of  $\vec{B}$

$\Leftarrow$  **Acceleration** and **propagation** of CRs



# 110 Years Coma Cluster

	0"	50"	58"	57"	56"	55"	54"	53"	52"	51"	50"	49"	48"	47"	46"	45"	44"	43"	42"	41"	40"	39"	38"	37"	36"	35"
59° 15'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
60° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
61° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
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30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
62° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
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63° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
64° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
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Max Wolf, 1901/1902

## Ein merkwürdiger Haufen von Nebelflecken.

Auf zwei mit dem Bruce-Teleskop genommenen Aufnahmen vom 24. März dieses Jahres, welche die Umgebung von 31 Comae Berenices darstellen, findet sich eine sehr interessante Gegend des Himmels. Um die Stelle

$$\alpha = 12^{\text{h}} 52^{\text{m}} 6^{\text{s}} \quad \delta = +28^{\circ} 42' (1855.0)$$

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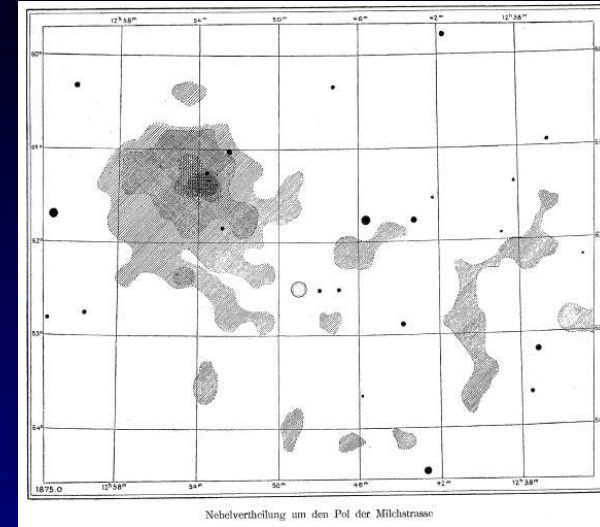
Heidelberg, 1901 März 27.

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30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
60° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
61° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
62° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
63° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
30	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
45	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
64° 0'	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—



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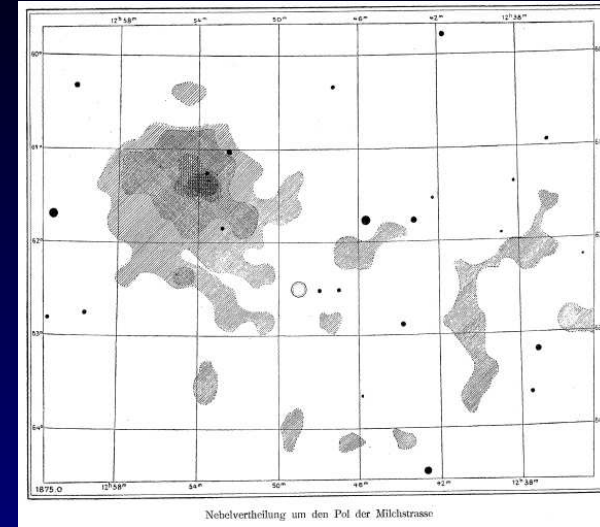
Max Wolf.

numerous small nebulae are standing such close together, that once literally frightens in sight of the remarkable appearance of this cluster of nebulae.



# 110 Years Coma Cluster

	0"	59"	58"	57"	56"	55"	54"	53"	52"	51"	50"	49"	48"	47"	46"	45"	44"	43"	42"	41"	40"	39"	38"	37"	36"	35"		
59° 15'	—	—	—	—	1	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	—	—	—		
30	—	—	—	—	0	0	2	1	3	1	2	1	3	2	1	1	2	0	0	2	1	0	0	—	—	—		
45	—	—	—	0	1	4	2	0	1	1	3	1	0	1	2	0	1	2	0	1	1	0	0	1	—	—		
60° 0'	—	—	—	0	0	2	1	0	1	1	2	2	1	0	2	3	0	1	3	5	0	0	2	0	0	—		
15	—	—	0	0	2	3	3	7	3	5	5	2	1	4	1	3	1	2	0	0	0	3	5	0	1	0	0	
30	—	—	0	2	3	4	3	2	3	5	3	1	3	0	0	2	4	1	0	0	0	3	2	0	0	2	0	
45	0	1	4	5	9	16	12	15	5	3	1	4	2	1	4	1	2	1	1	0	1	2	4	0	1	0	0	
61° 0'	0	1	5	15	19	10	23	15	19	8	4	3	4	2	1	0	1	1	1	0	1	1	1	2	0	0	4	
15	0	0	9	17	11	14	36	68	10	7	3	7	0	2	1	2	3	1	1	3	0	4	4	3	0	2	1	
30	1	2	2	9	6	12	13	17	20	16	6	7	1	2	1	1	1	1	4	1	1	5	3	1	6	3	1	
45	0	5	5	10	8	8	12	9	10	11	4	5	4	2	5	2	6	5	2	1	2	2	1	3	2	2	3	
62° 0'	0	2	1	3	6	8	3	10	7	3	5	4	2	4	6	8	3	2	2	5	0	3	9	10	10	2	2	
15	0	3	1	6	5	10	11	9	1	10	7	1	5	3	4	4	3	2	3	3	6	4	1	5	2	3	1	
30	—	—	0	1	4	4	1	2	4	8	4	2	1	2	1	2	3	4	2	1	3	9	4	3	2	4	5	3
45	—	—	0	1	5	2	3	1	3	6	4	6	2	0	6	2	4	3	5	2	6	10	5	3	1	1	7	6
63° 0'	—	—	0	2	2	2	3	0	0	0	0	1	1	1	1	2	4	0	2	4	2	7	5	0	4	0	2	2
15	—	—	0	1	1	2	0	3	0	8	1	1	0	0	0	2	2	1	0	5	3	5	3	8	4	1	2	1
30	—	—	0	0	4	0	0	8	0	2	0	0	0	0	2	4	3	3	4	4	2	8	2	2	2	0	0	0
45	—	—	0	0	2	0	1	4	1	1	1	6	4	2	0	0	5	4	2	1	5	1	1	3	0	—	—	
64° 0'	—	—	—	—	0	3	0	0	0	0	1	7	1	2	6	4	3	7	2	4	0	0	0	—	—	—	—	
15	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	



Max Wolf, 1902

**the regular behavior within the arrangement of these distant worlds**

Es ist sofort zu sehen, wenn man die Tabelle oder die Tafel betrachtet, dass das Zusammendrängen der Nebel immer stärker wird, je weiter man in's Innere der Hauptinsel eindringt. Je näher man dem Punkte grösster Dichtigkeit kommt, umso dichter treten auch die Nebel an einander, so dass auf dem innersten Quadratgrad mehr als 320 einzelne Nebelflecken beisammen stehen. An der dichtesten Stelle dieses »Weltpoles« finden sich mehr als 70 Nebel auf der Fläche von  $\frac{1}{16}$  Quadratgrad.

Wir finden also hier ein völlig gesetzmässiges Verhalten in der Anordnung dieser fernen Welten; und dieser ungeheure Reichthum führt uns so eine Ordnung im Weltsystem vor Augen, die sicher für die Erkenntniss des Universums von allergrösster Bedeutung ist, von der wir uns aber auch zugestehen müssen, dass wir noch lange keine erschöpfende Erklärung für sie werden finden können. \*)

**of greatest significance for understanding the universe**

# Historical Milestones

## ≈70 Years ago:

Unvisible matter needed to explain cluster dynamics

Zwicky 1936

## ≈50 Years ago:

- Coma C detected as extended radio source

Large, Masthewson & Haslam 1959

- Confirmed to be diffuse radio emission

Willson 1970 ⇒ problem of large extend Jaffe 1977

- Diffuse X-ray emission detected

Meekins, Fritz, Chubb & Friedman 1971

- Faraday Rotation (RM) of ICM detected

Dennison 1979

- No similar emission found in 72 rich clusters

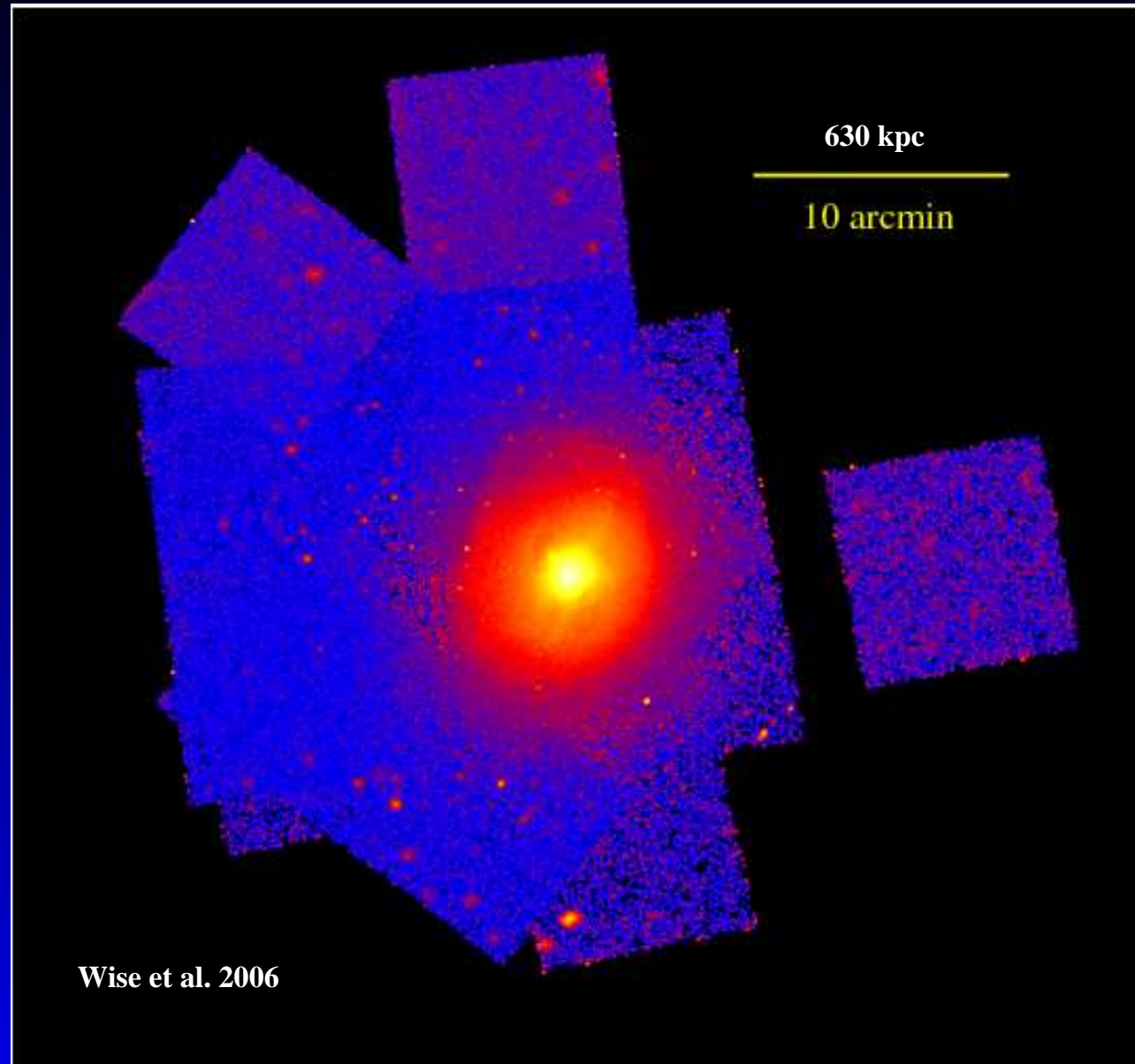
Hanisch 1982

⇒ What is the origin of the magnetic field ?

⇒ What causes the diffuse radio emission ?

⇒ Magnetic fields on larger scales ?

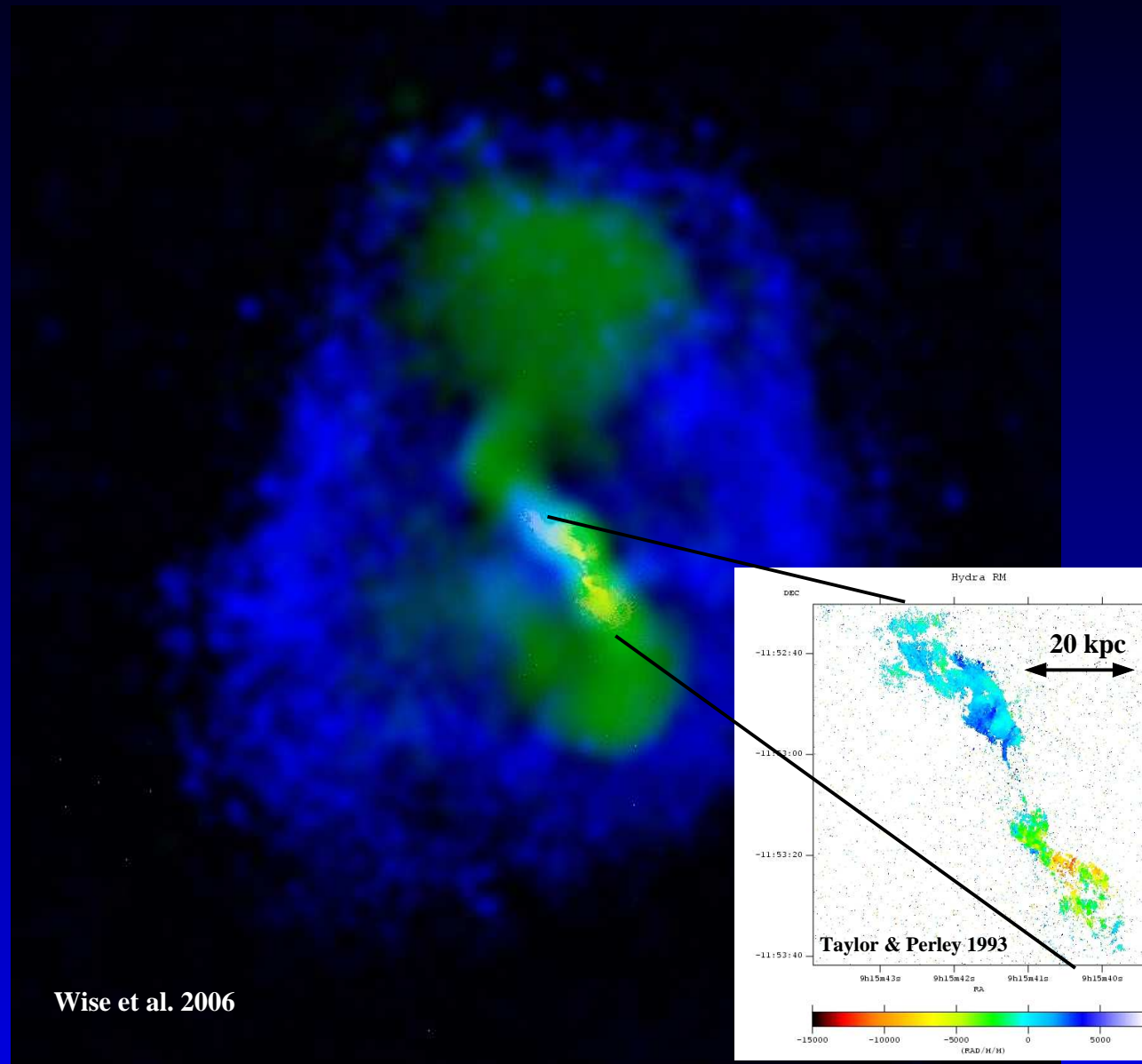
# Cool core clusters



Chandra **X-ray** image (**ICM**) of the Hydra cluster (cool core)

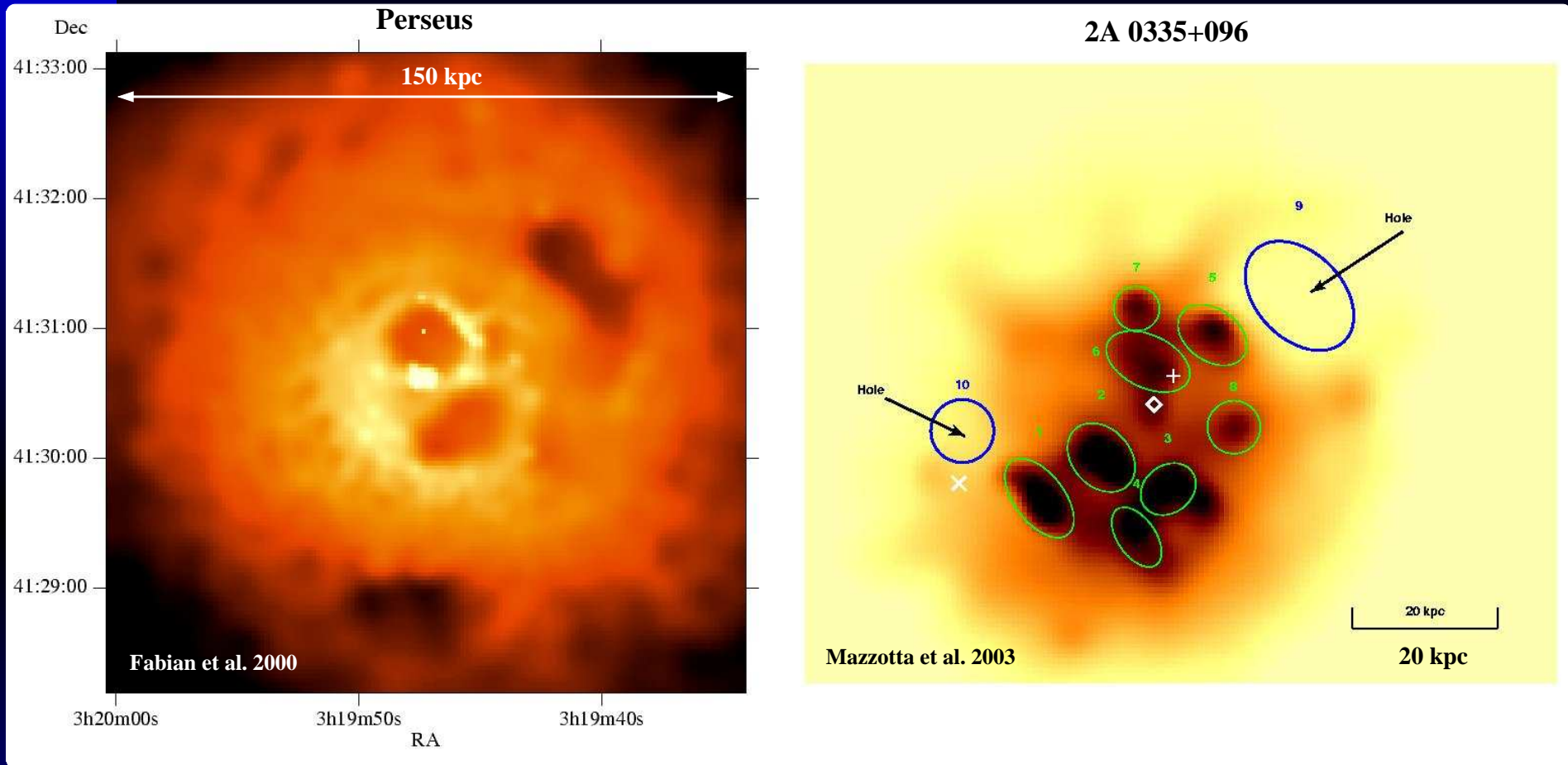


# Cool core clusters



Composite image to illustrate the **connection** between the **X-ray cavity** (blue) and 330Mhz **radio emission** (green).

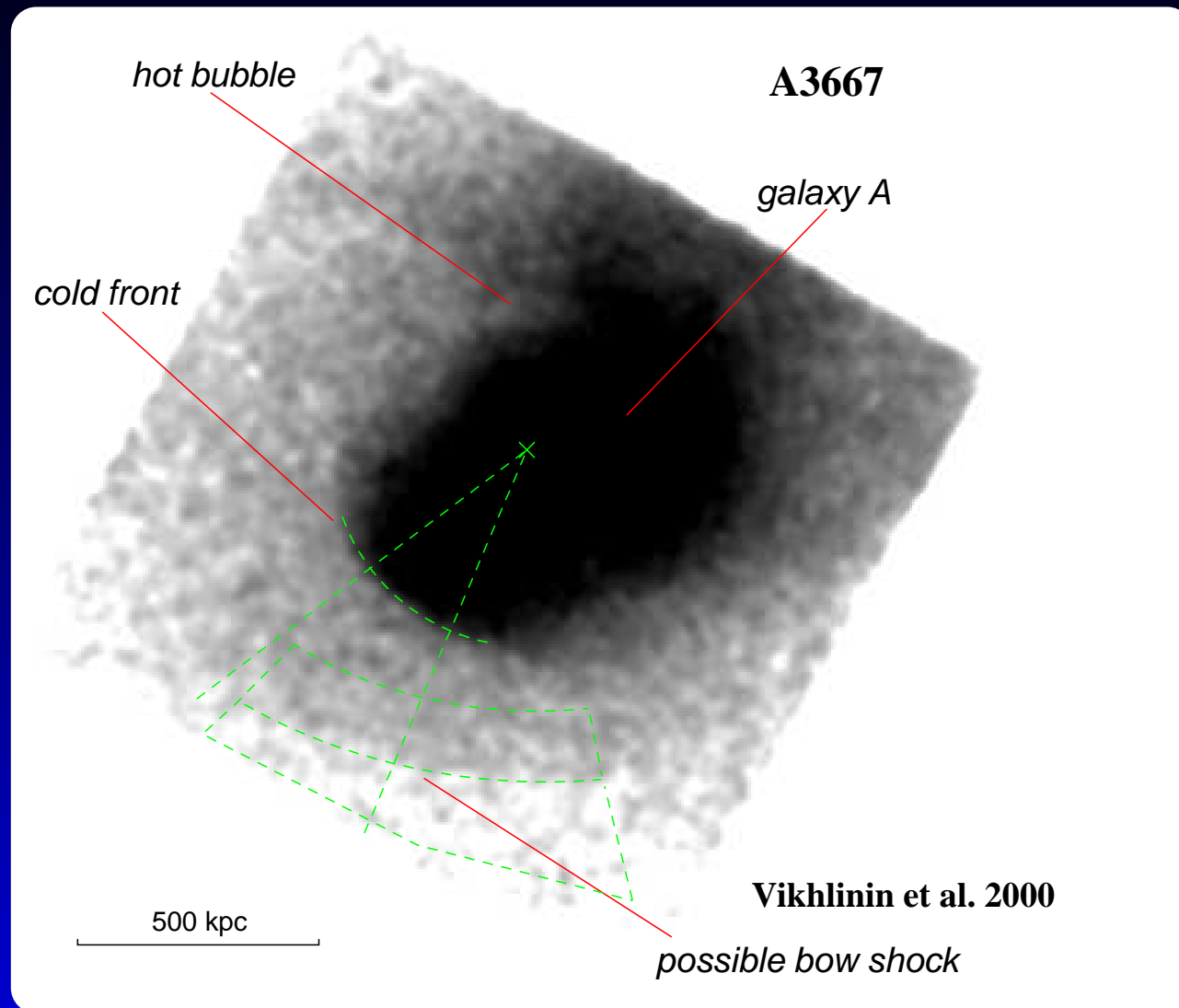
# Cool core clusters



X-ray cavity in the cool core center of Perseus cluster (left) and 2A 0335+096 cluster (right). See work by E. Churazov.

- Does energy injected by the AGN heats the cool core ?
- Does the motion of cores induce mixing ?
- Details remain jet unclear (viscosity, turbulence, instabilities (RT,KH) ...)  $\Rightarrow$  **magnetic field**

# X-ray Clusters

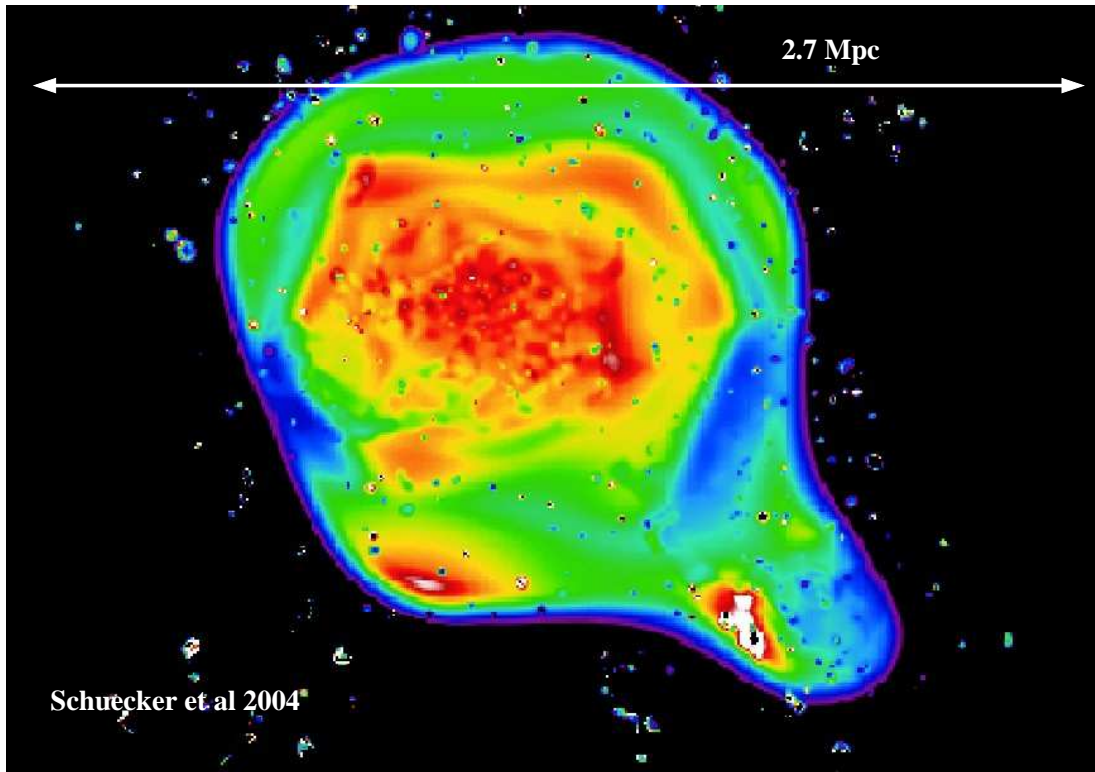


X-ray image of the A3667 cluster, illustrating the sloshing of gas on large scales. Sharp fronts indicate suppression of thermal conduction.  $\Rightarrow$  **magnetic field**

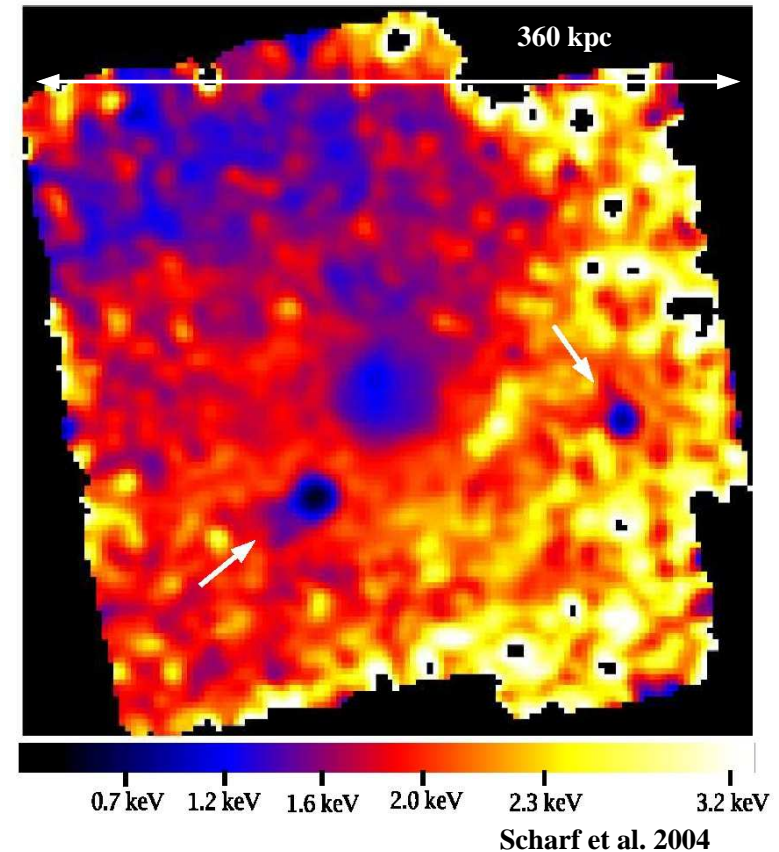


# X-ray Clusters

Coma



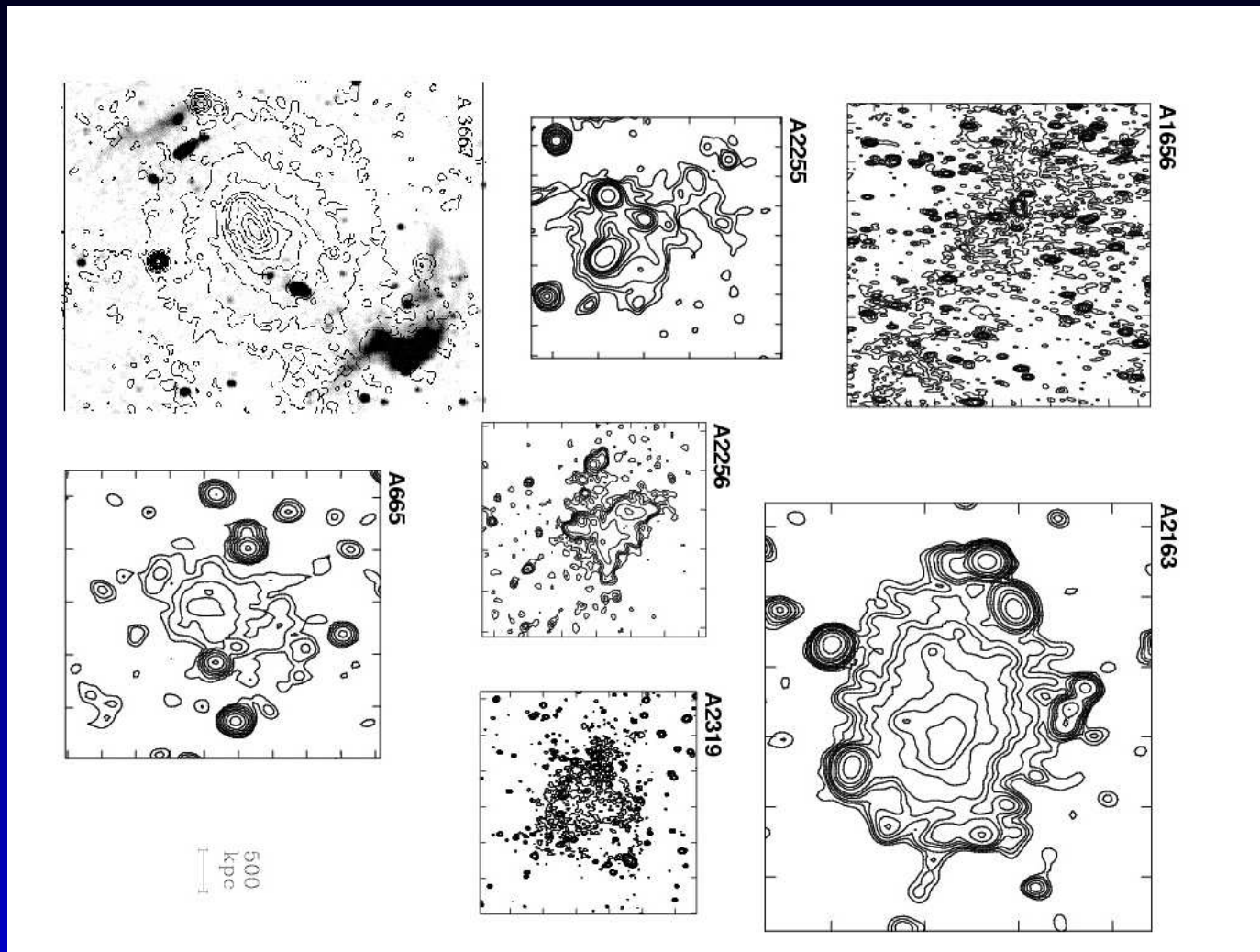
Fornax



X-ray temperature map of Coma (left) and Fornax cluster (right).

- How much turbulence is present in galaxy clusters ?
- How effective does gas stripping work ?
- Details still unexplored, again viscosity and instabilities depend on **magnetic field**

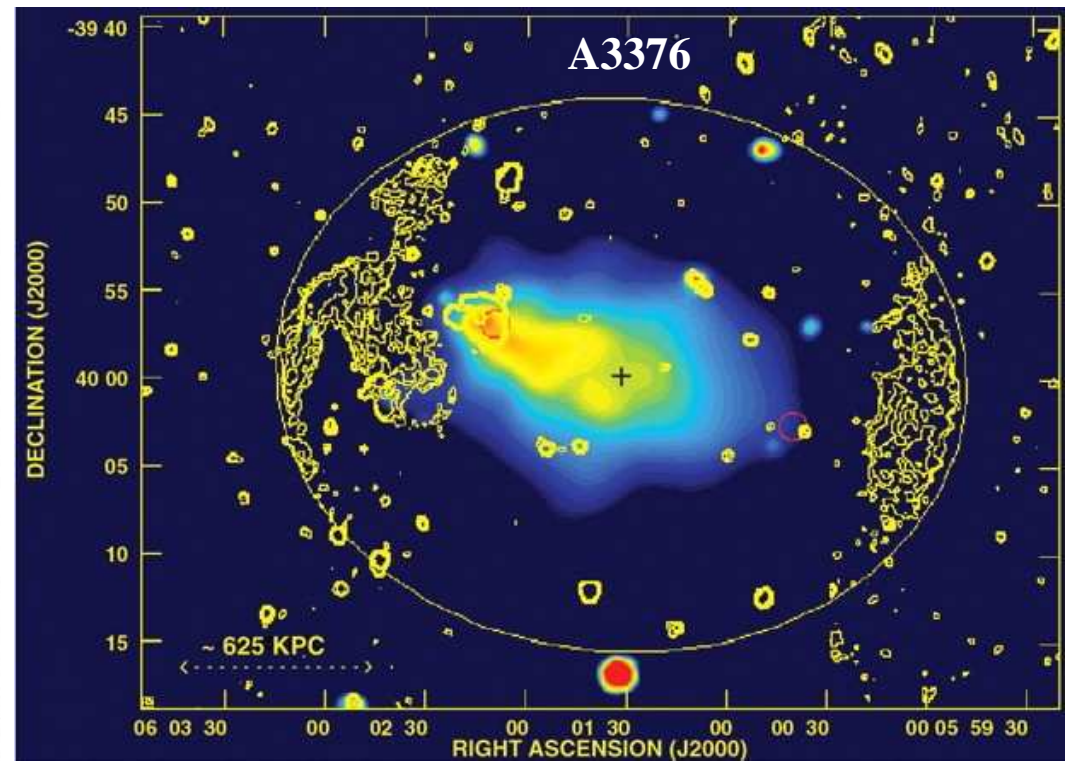
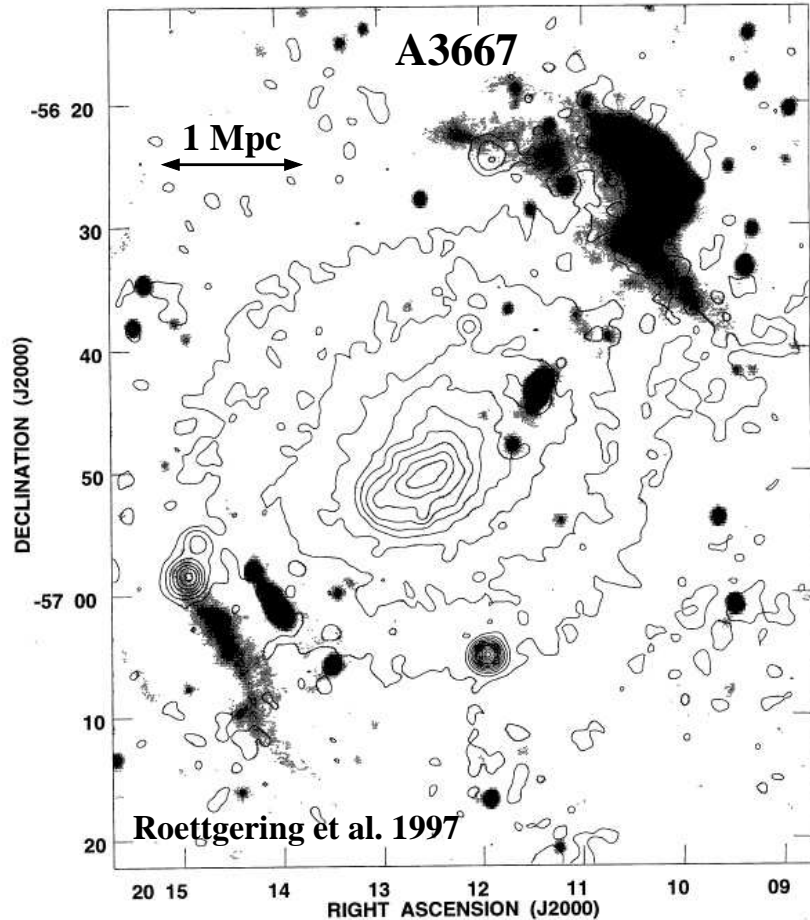
# Radio Clusters



**Cluster wide diffuse synchrotron emission** (radio halos) of relativistic electrons in cluster magnetic fields. **Origin of relativistic electrons** (secondary, shocks, turbulence, ...) ?



# Radio Clusters



Bagchi et al. 2006

**Peripheral synchrotron emission** (radio relics) of A3667 (left) and A3376 (right).

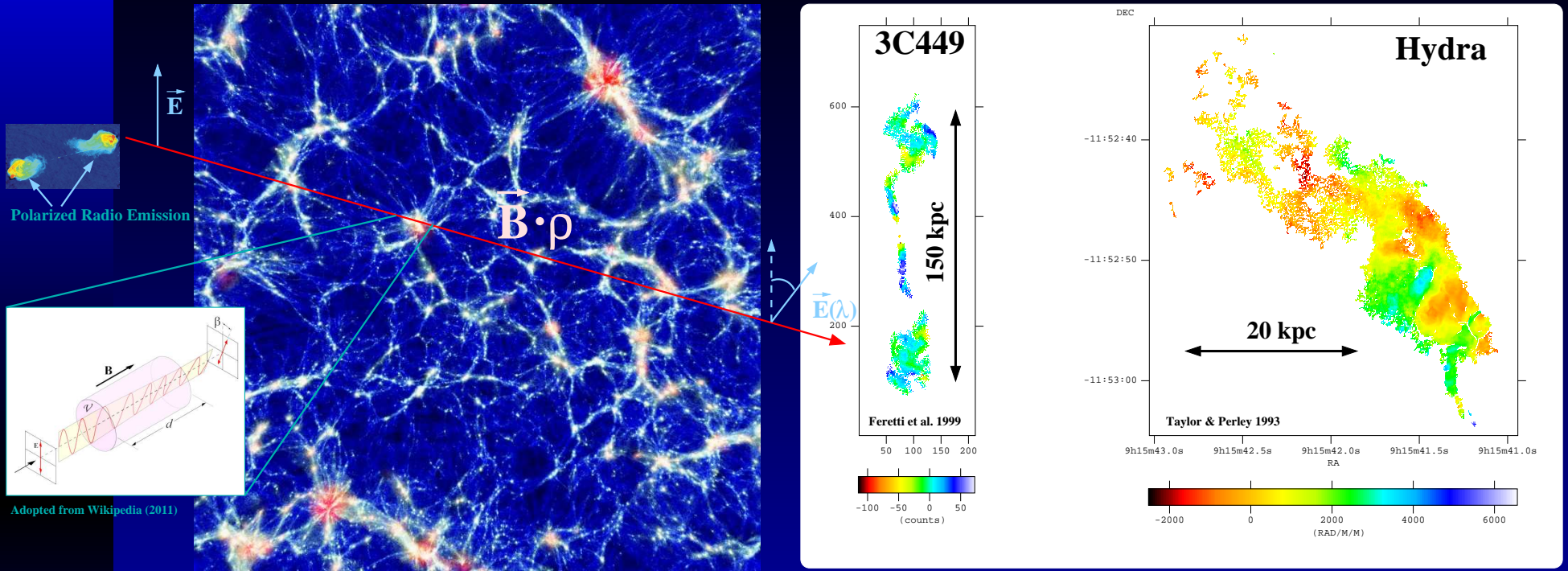
- Related to **merger** or accretion **shock** ?
- Acceleration of electrons in shock ?
- Revival of (old) relativistic plasma ?



# Magnetic Field Questions

- Strength, Structure, Origin, Evolution
- ⇒ Common Origin ?  
Filament vs. Cluster, Cluster vs. cool Core, ...
- ⇒ Relation to other LSS "properties" ?
  - scaling with density ( $\propto \rho^\alpha$ ) ?
  - scaling with temperature/mass ( $\propto T^\beta$ ) ?
  - length scales,  $P_B(k)$  (Filaments, Cluster, cool Core) ?
- ⇒ Relation to dynamics ?
  - Merger, Turbulence, cool Core, Bubbles ?
- Observations:
  - RM in clusters
  - Radio emission (halo and relics)

# What do we know ?



High quality Rotation Measure maps across the lobes of the central radio source in 3C449 (left) and Hydra (right).

$$\text{RM} \propto \int n_e B_{\parallel} dl \approx B_{\parallel} \sqrt{l}$$

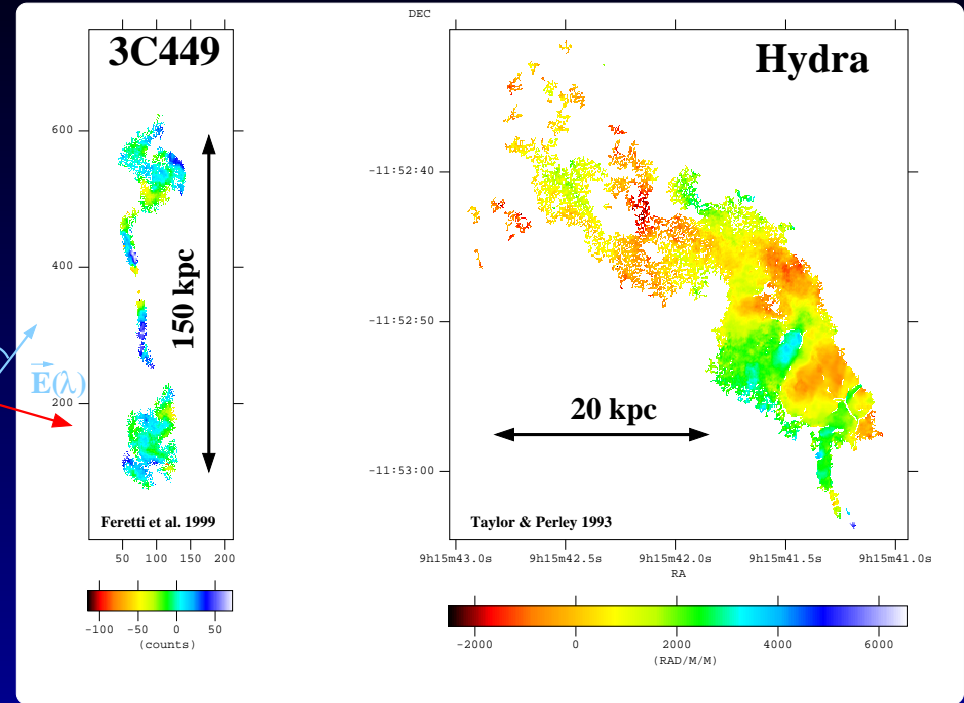
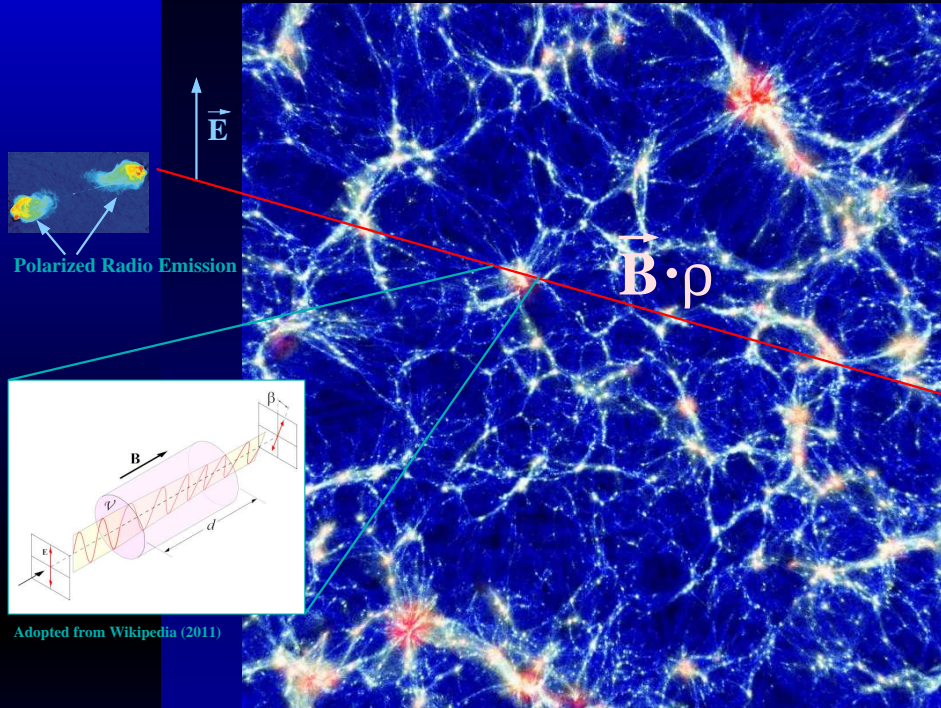
≈ 20 Years ago:

< 10 extended RM sources within clusters

< 100 point sources behind various clusters

⇒ very simplified models:  $\sim (0.1 - 10) \mu\text{G}$ ,  $l \sim (4 - 100) \text{kpc}$ .

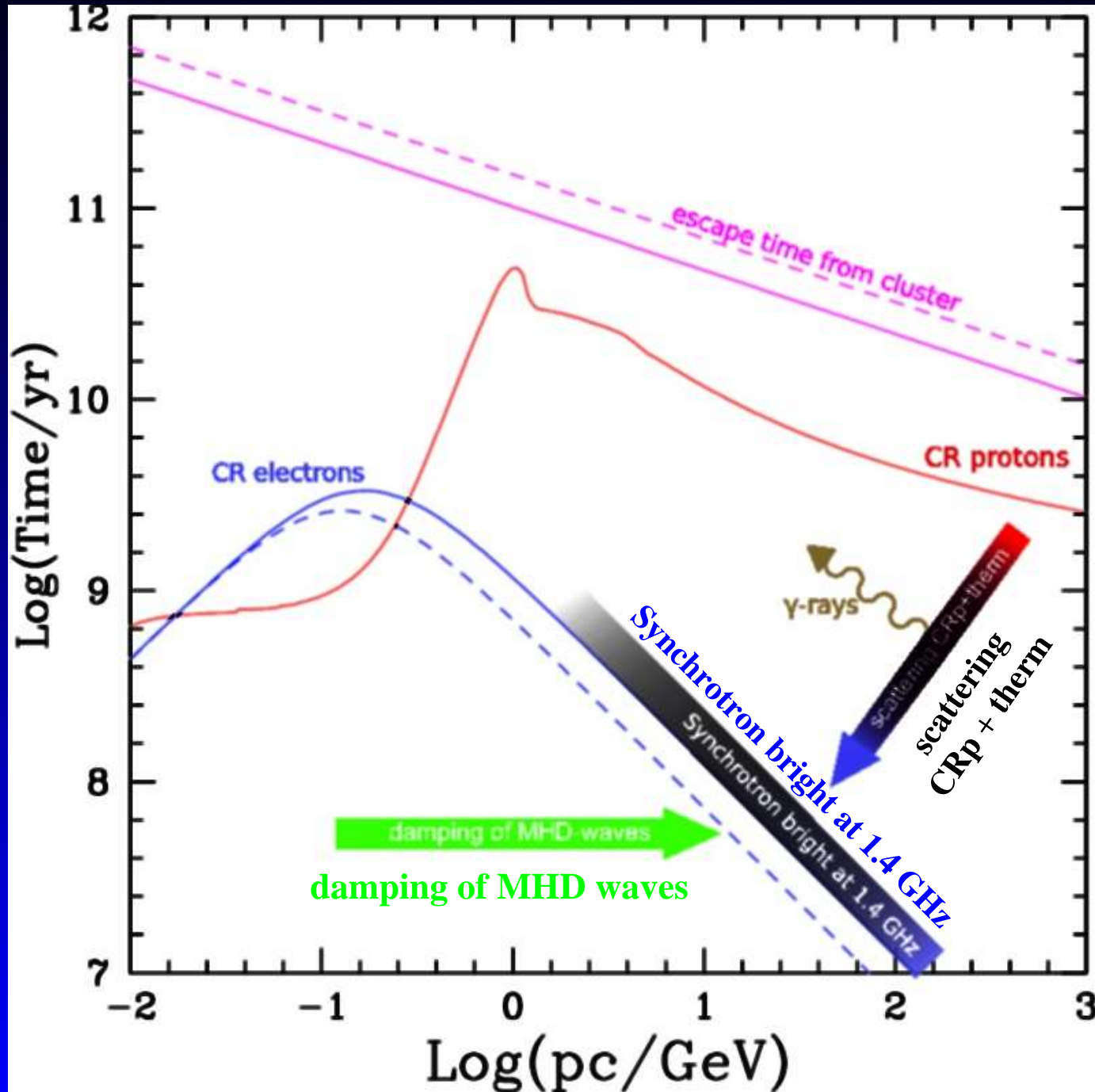
# What do we know ?



- A119:  $\vec{B}$  with **radial declining profile** and **fixed power spectrum** (Murgia et al. 2004)
- Hydra: direct reconstruction of **power spectrum** (e.g.  $|B_k|^2$ ) (Vogt & Ensslin 2005, Kuchar & Ensslin 2010)
- A2255:  $\vec{B}$  with **radial declining profile** and **variable power spectrum** (Govoni et al. 2006)
- Coma: RMs from 7 extended sources constraining **magnetic field** and **power spectrum** (Bonafede et al. 2009)
- A401, A2142, A2065, Ophiuchus: **magnetic field** for clusters with different temperature (Govoni et al. 2009)

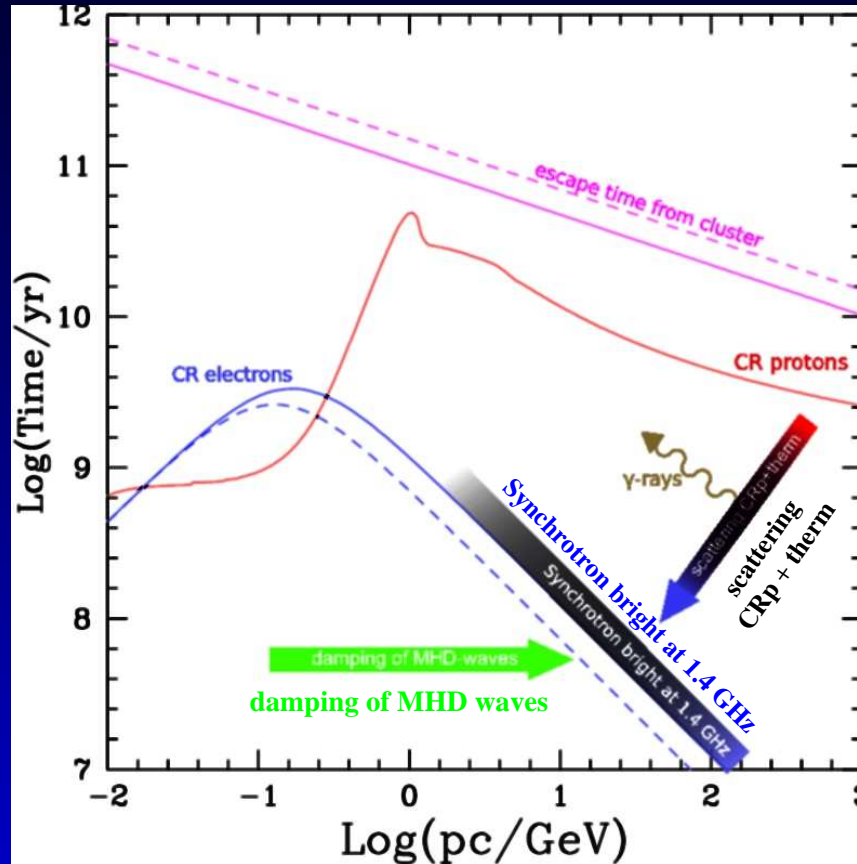


# What do we know ?



# What do we know ?

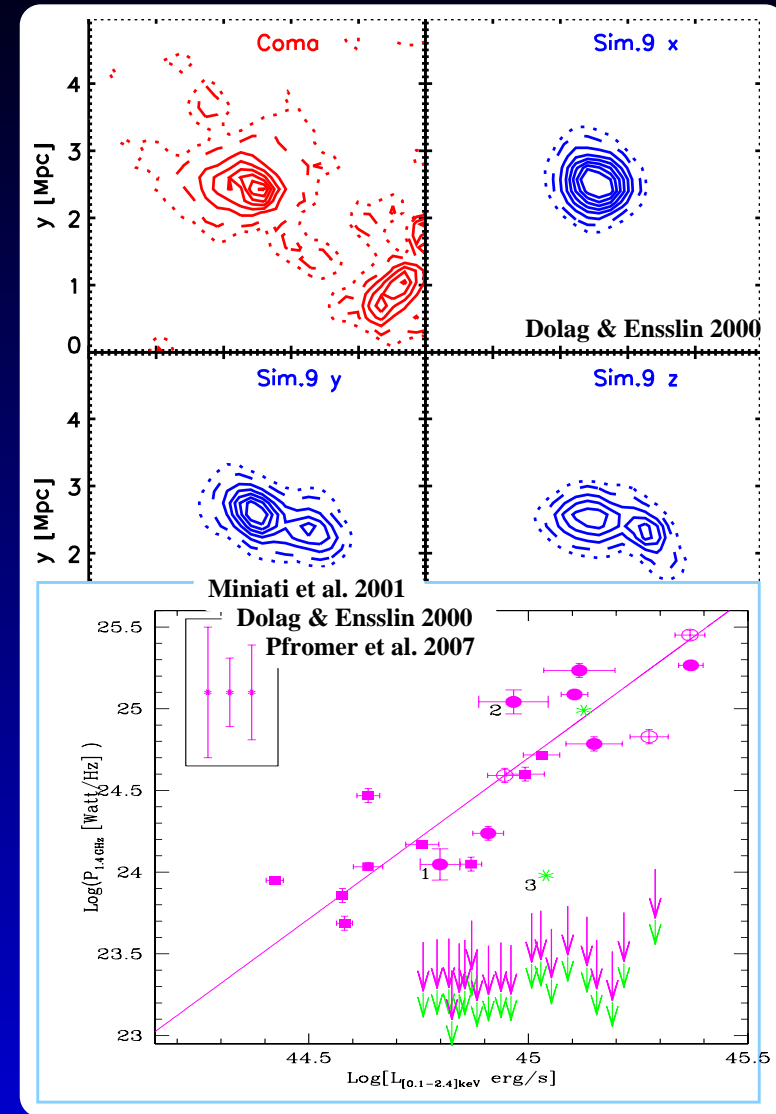
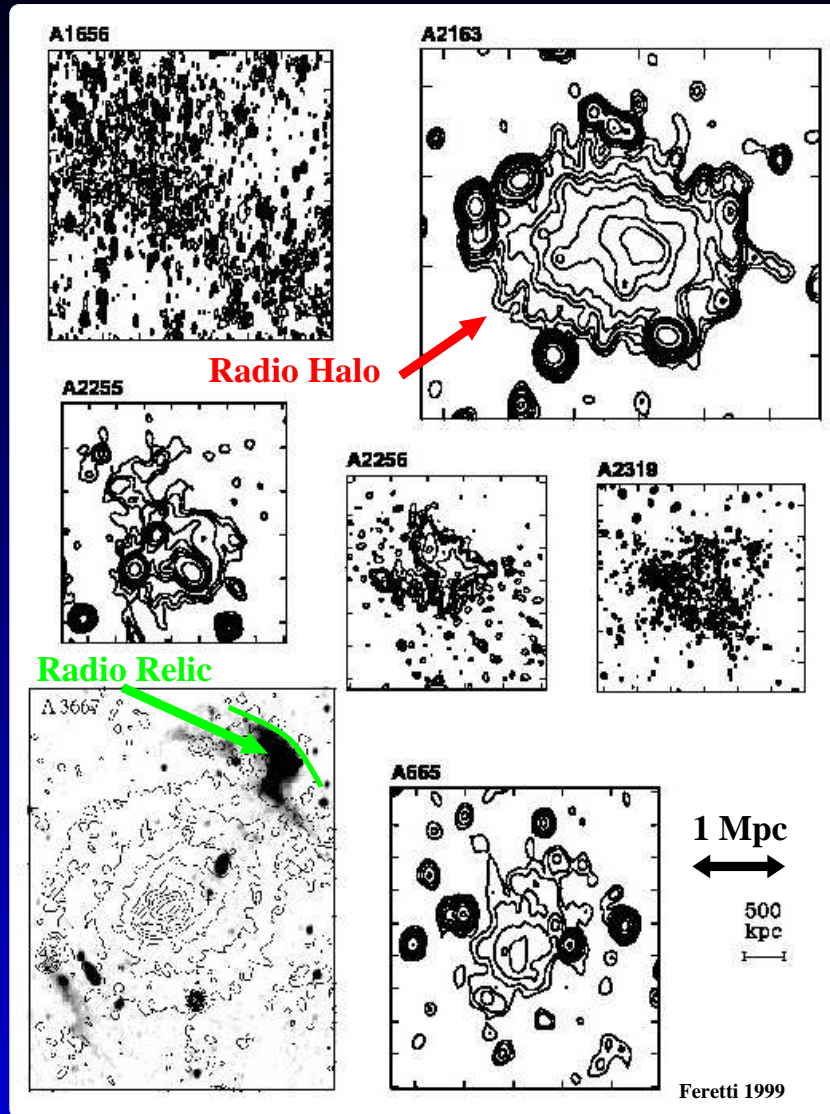
- Early work on radio halos (individual clusters)  
 $\approx 10$  clusters with diffuse emission:  $> (0.05 - 0.5) \mu\text{G}$



⇒ **Increased numbers and complexity:**

- Global spectral index steepening / local index maps
- Radial radio emission profile for many clusters
- **Probability** for clusters to host a **radio halo**

# What do we know ?



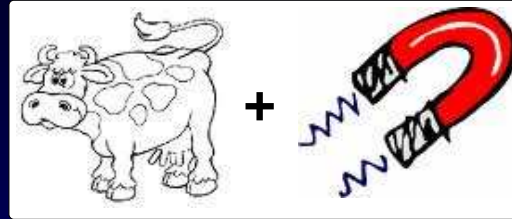
Cluster wide **diffuse synchrotron emission** connected to **merger** events, **periferal** emission directly connected to **shocks**.

- **Radio halo**: Turbulence, shocks, secondary ?
- **Relics**: Primary from shocks or compressed radio plasma ?



# Note on magnetic fields

Always be careful, as things can be much more complicated as you think !



Example: **Magnetic Cows**: “Magnetic alignment in grazing and resting cattle and deer”, Begall et al. 2008

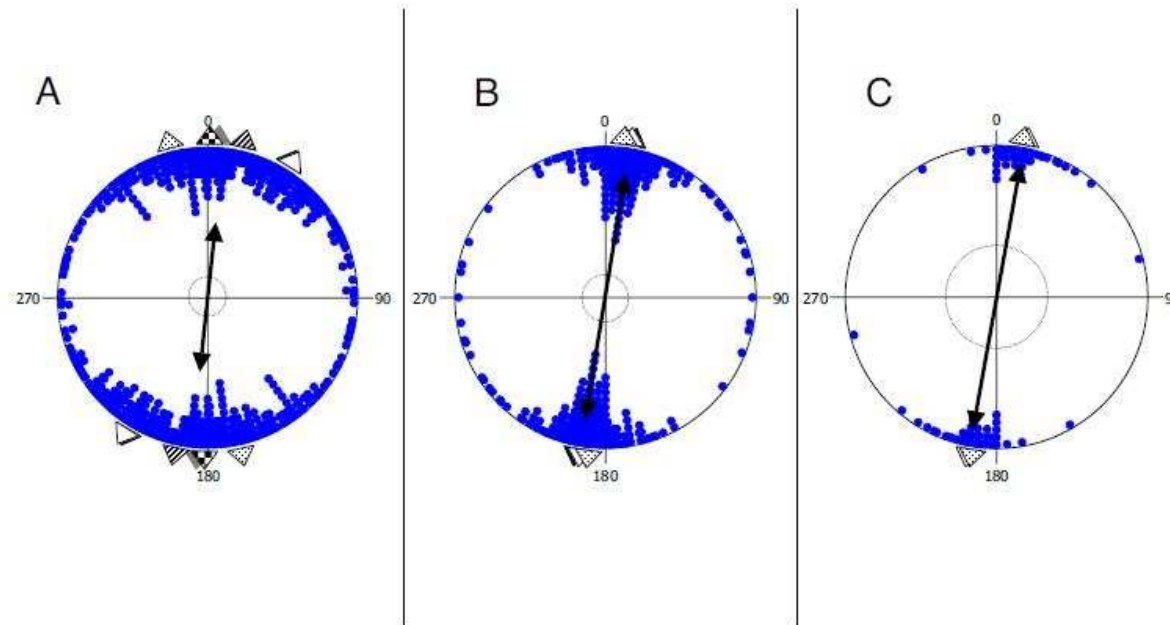
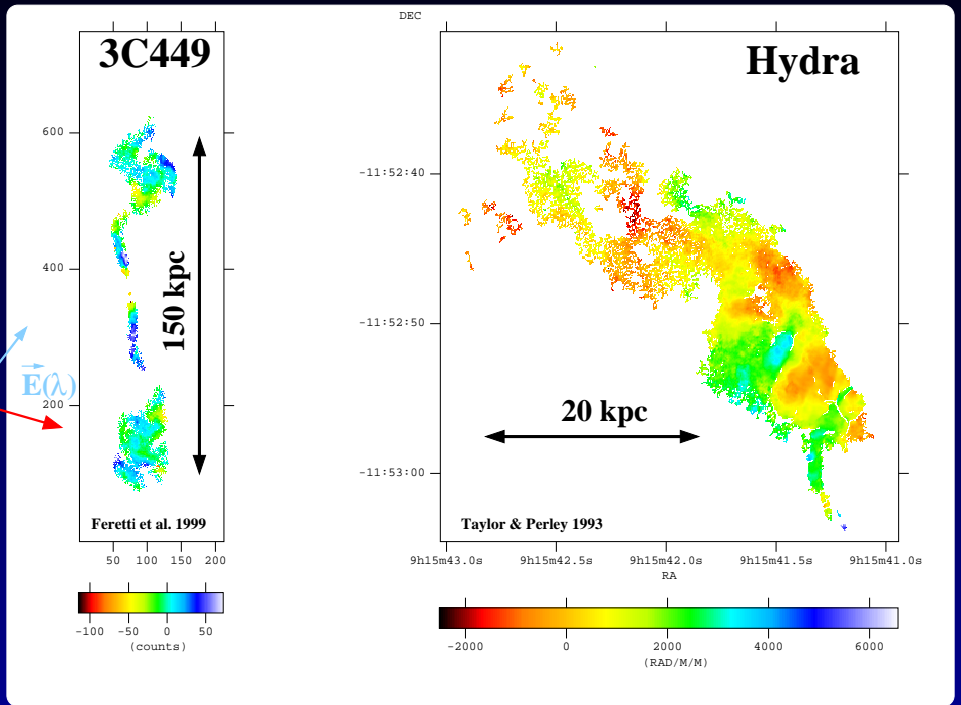
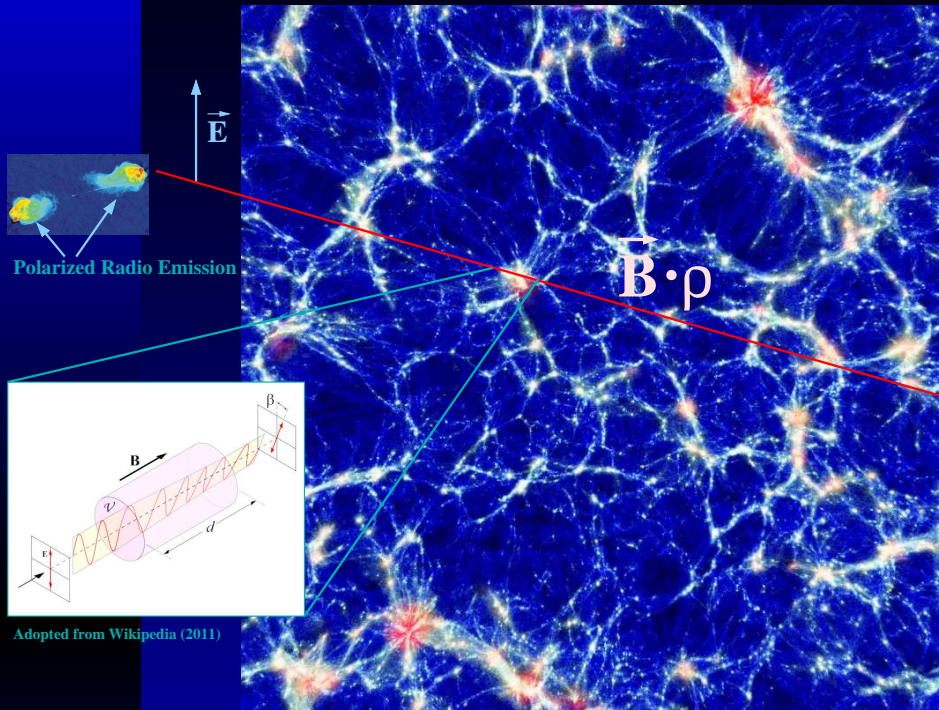


Fig. 1. Axial data revealing the N-S alignment in three ruminant species under study. (A) Cattle. (B) Roe deer. (C) Red deer. Each pair of dots (located on opposite sites within the unit circle) represents the direction of the axial mean vector of the animals' body position at one locality. The mean vector calculated over all localities of the respective species is indicated by the double-headed arrow. The length of the arrow represents the  $r$ -value (length of the mean vector), dotted circles indicate the 0.01-level of significance. Triangles positioned outside the unit circle indicate the mean vectors of the cattle data subdivided into the six continents (dotted: North America; gray: Asia; checkered: Europe; striped: Australia; black: Africa; white: South America) (A) and the mean vectors of resting (black) and grazing (white) deer, and of deer beds (dotted) (B: roe deer; C: red deer).

# Observations

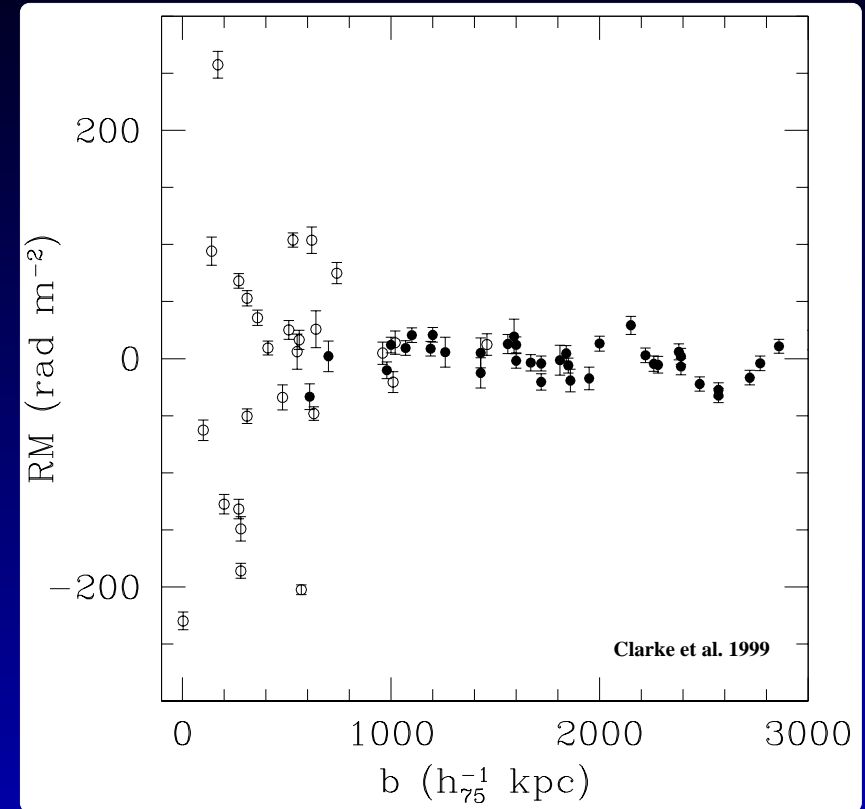
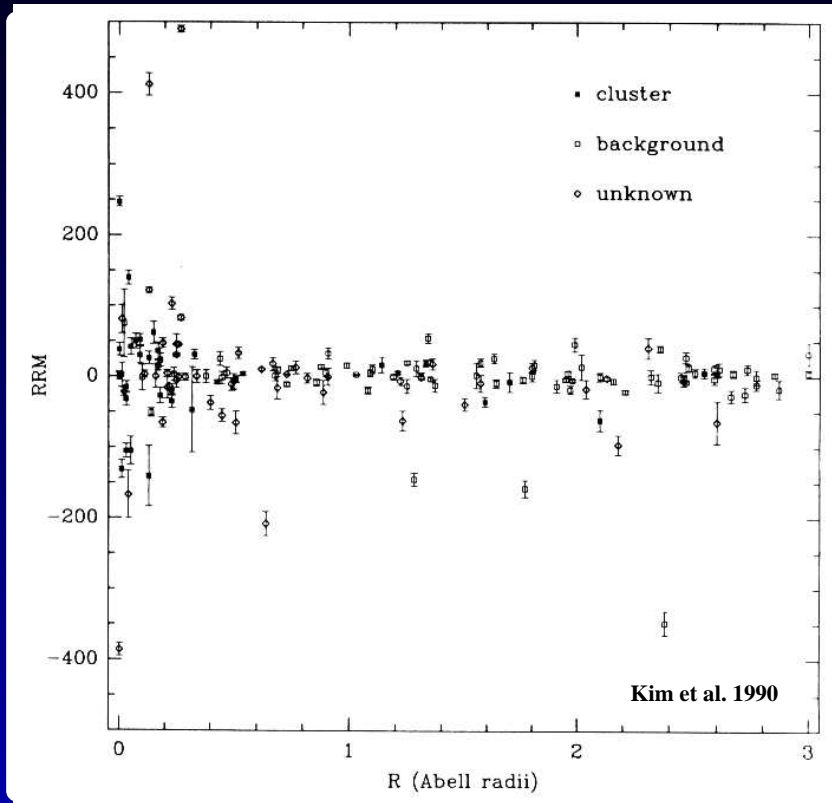


High quality Rotation Measure maps across the lobes of the central radio source in 3C449 (left) and Hydra (right).

$$\text{RM} \propto \int n_e B_{\parallel} dl \approx B_{\parallel} \sqrt{l}$$

- **Simple interpretation**
- **Direct inversion**
- **Modeling**
- **Simulations (Lecture III)**

# Observations



**Rotation Measure** as function of distance to the center of galaxy clusters.

$$\text{RM} = 812 \frac{\text{rad}}{\text{m}^2} \int \frac{n_e}{\text{cm}^{-3}} \frac{B_{\parallel}}{\mu\text{G}} \frac{dl}{\text{kpc}}$$

Clear signature of **cluster magnetic fields** !



# Observations

From HIFLUGCS (Reiprich & Böringer 2002)

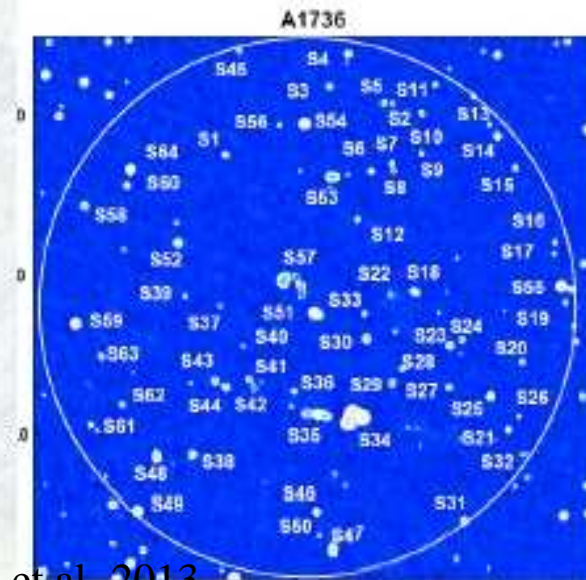
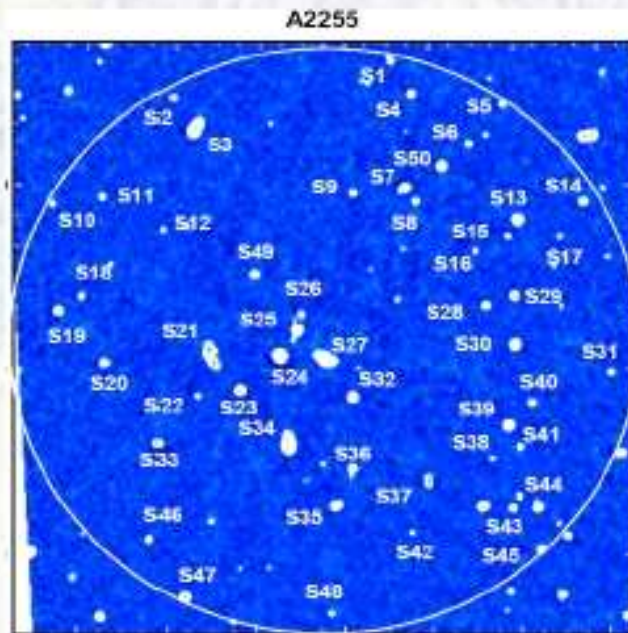
→ clusters with  $L_x > 1.5 \cdot 10^{44}$  erg/s [0.1 – 2.4 keV] –  $M_{200} > 5 \cdot 10^{14} M_\odot$

39 clusters

Radio Images → I Q and U Stokes parameters out of 10 core radii from NVSS

(1.4 GHz, 100 MHz bandwidth)

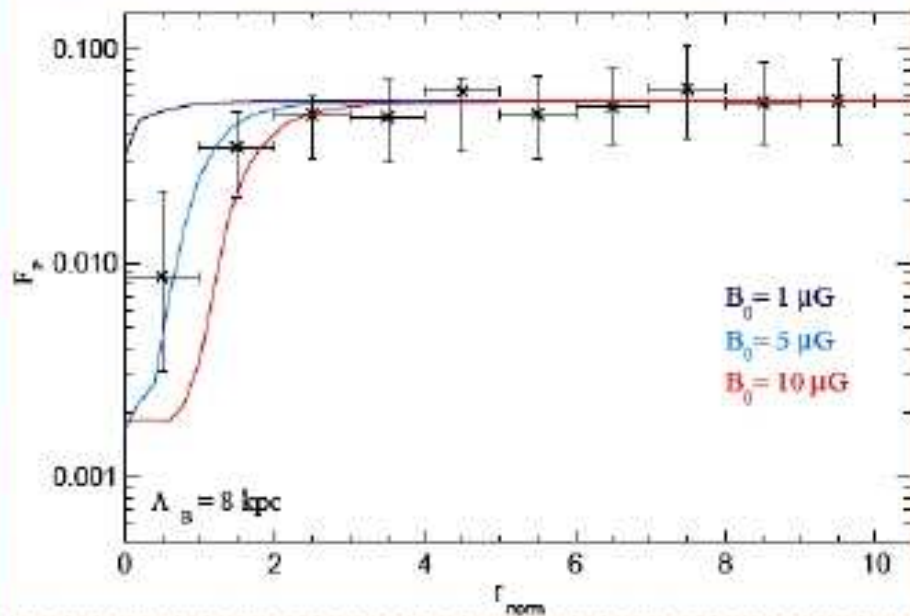
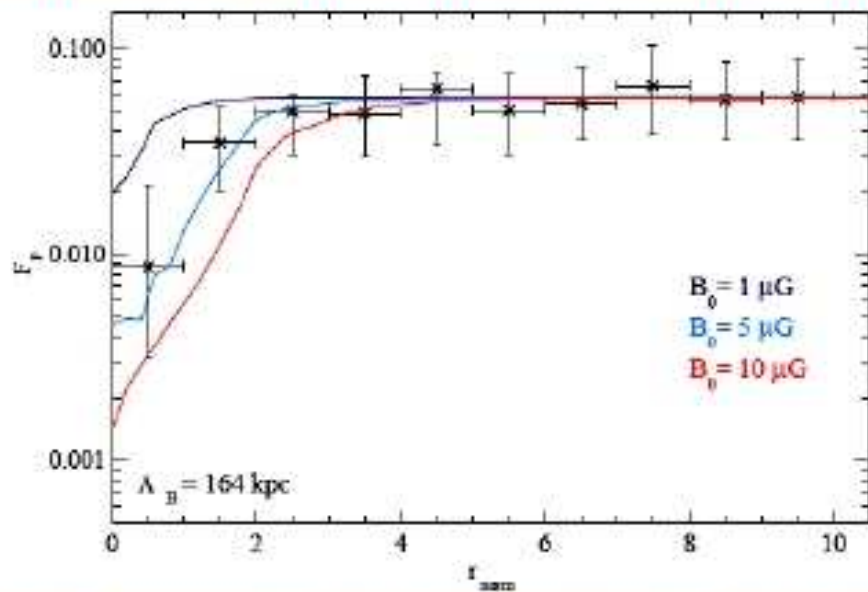
Total sample of **33** clusters



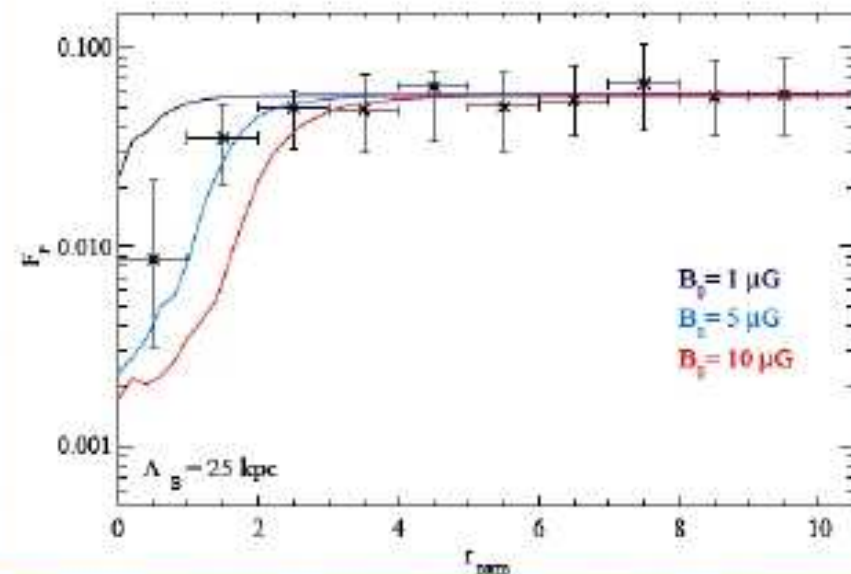
Bonafede et al. 2013

Fractional **polarization** data of radio sources as function of distance to the center of massive galaxy clusters.

# Observations



$$\langle B \rangle(r) = \langle B_0 \rangle \left( \frac{n_e}{n_0} \right)^{0.5}$$



$$\langle B_0 \rangle \approx 5 \mu\text{G}$$

Bonafede et al. 2013

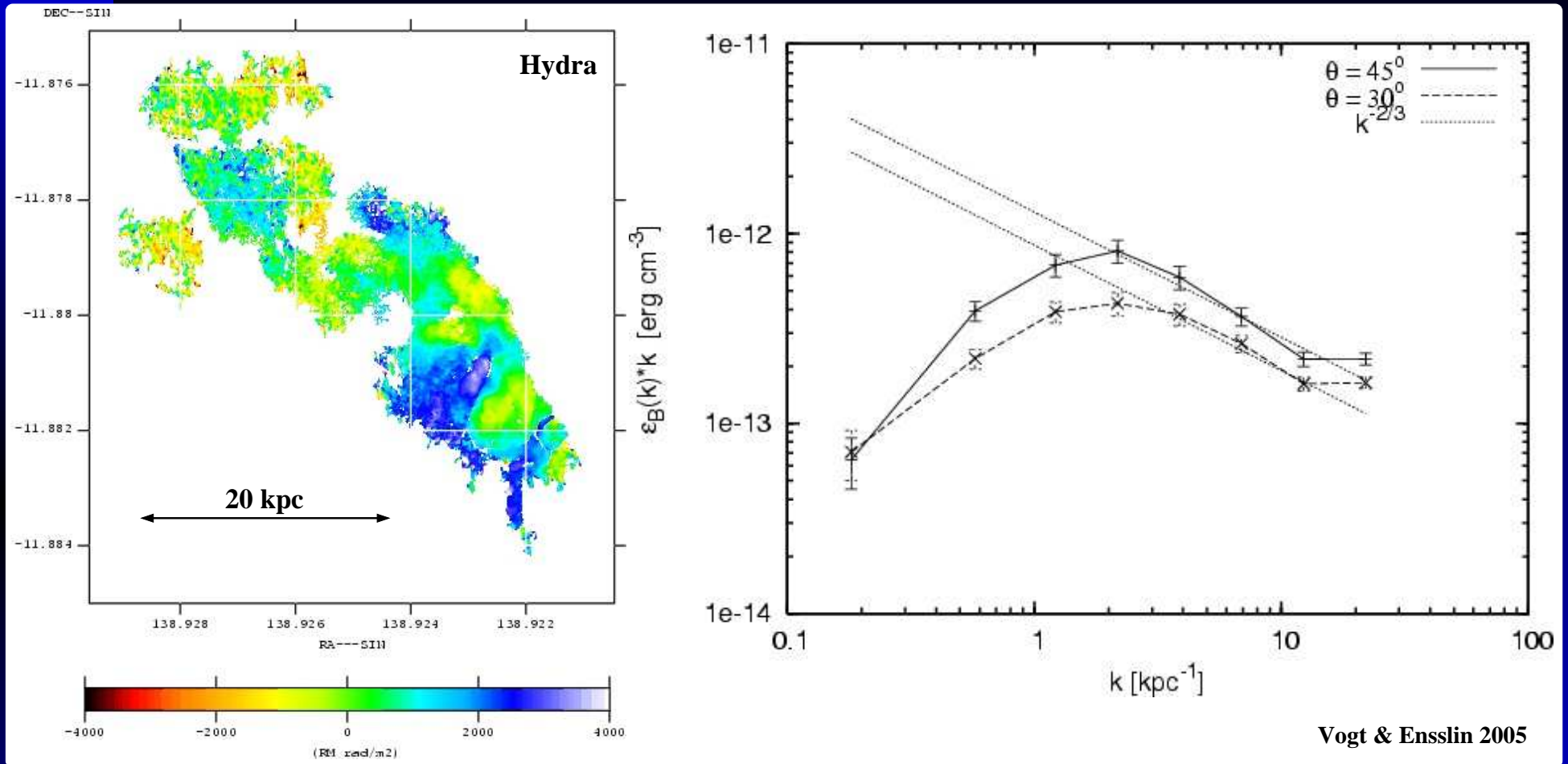
Clear signature of **cluster magnetic fields** !

# Observations

Jets in realistic galaxy clusters environment



# Observations

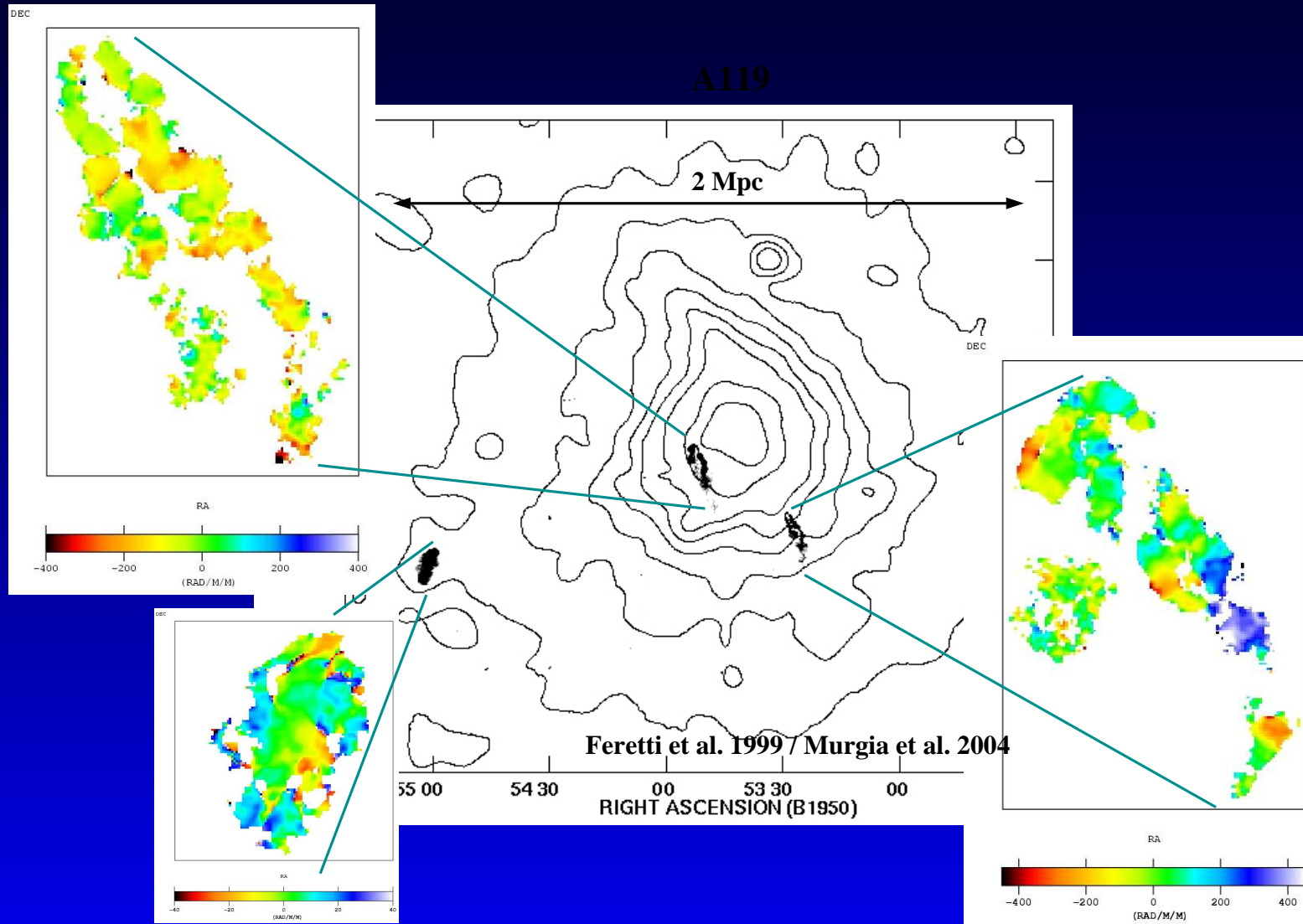


**Rotation Measure** of Hydra (left) and inferred power spectrum of the underlying magnetic field (Vogt & Ensslin 2005).

- Follows a **Kolmogorov-like** power spectrum !
- Magnetic field correlation length  $\approx 3$  kpc !
- Cool core turbulence or cluster wide field ?

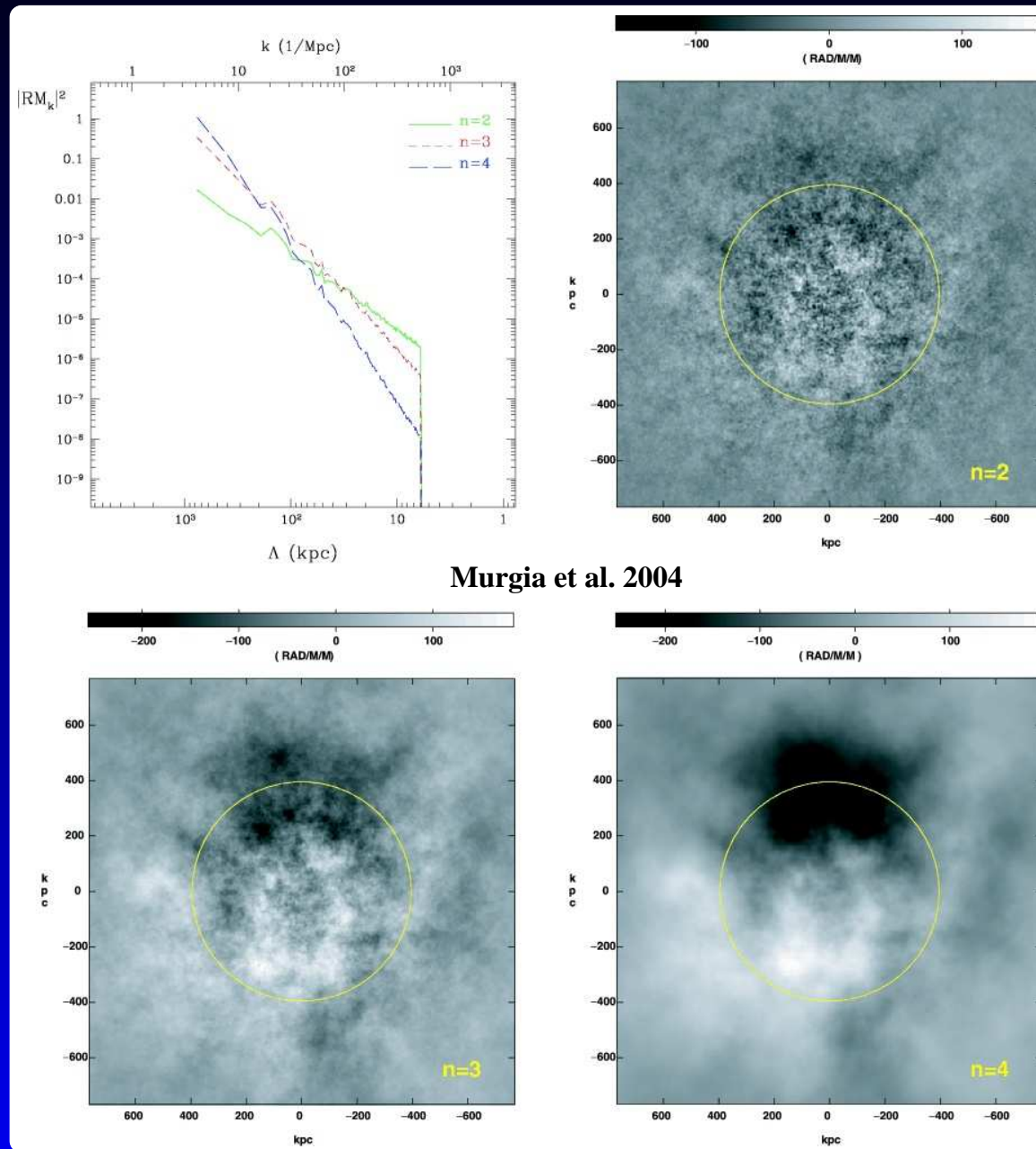
# Observations

$$B(r) = B_0 \left(1 + (r/r_c)^2\right)^{-1.5\eta}, \quad |B_k|^2 \propto k^{-n}$$



Composite of X-ray map and Rotation Measure in 3 extended radio sources in A119.

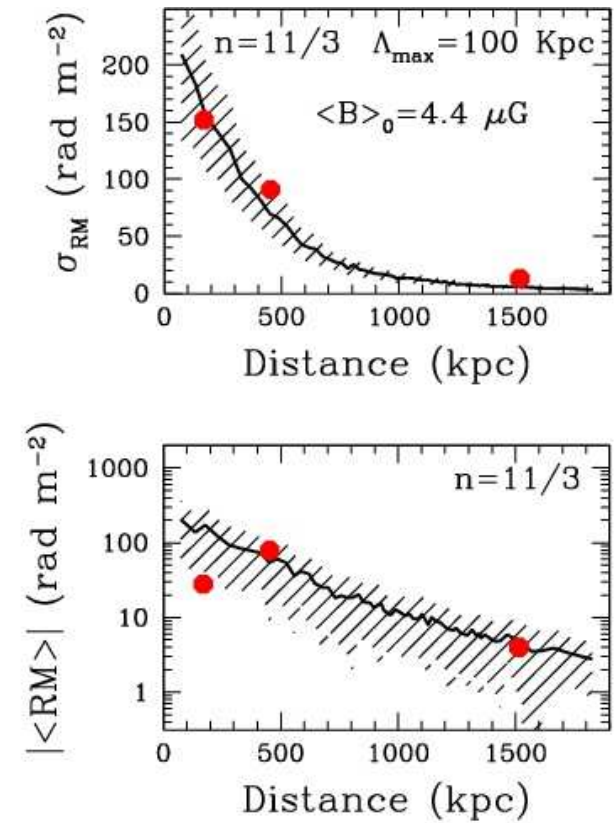
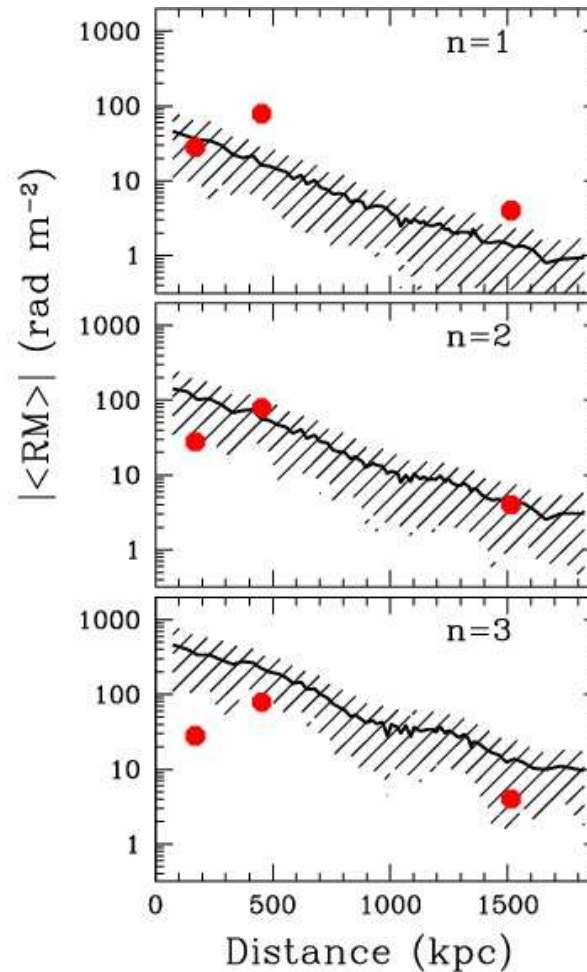
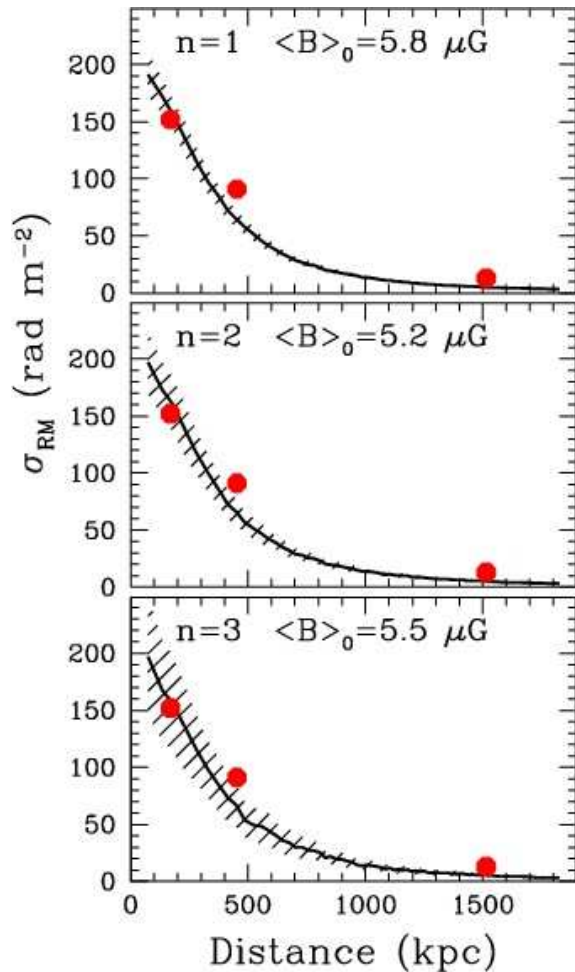
# Observations



Modeling the magnetic field in A119.



# Observations

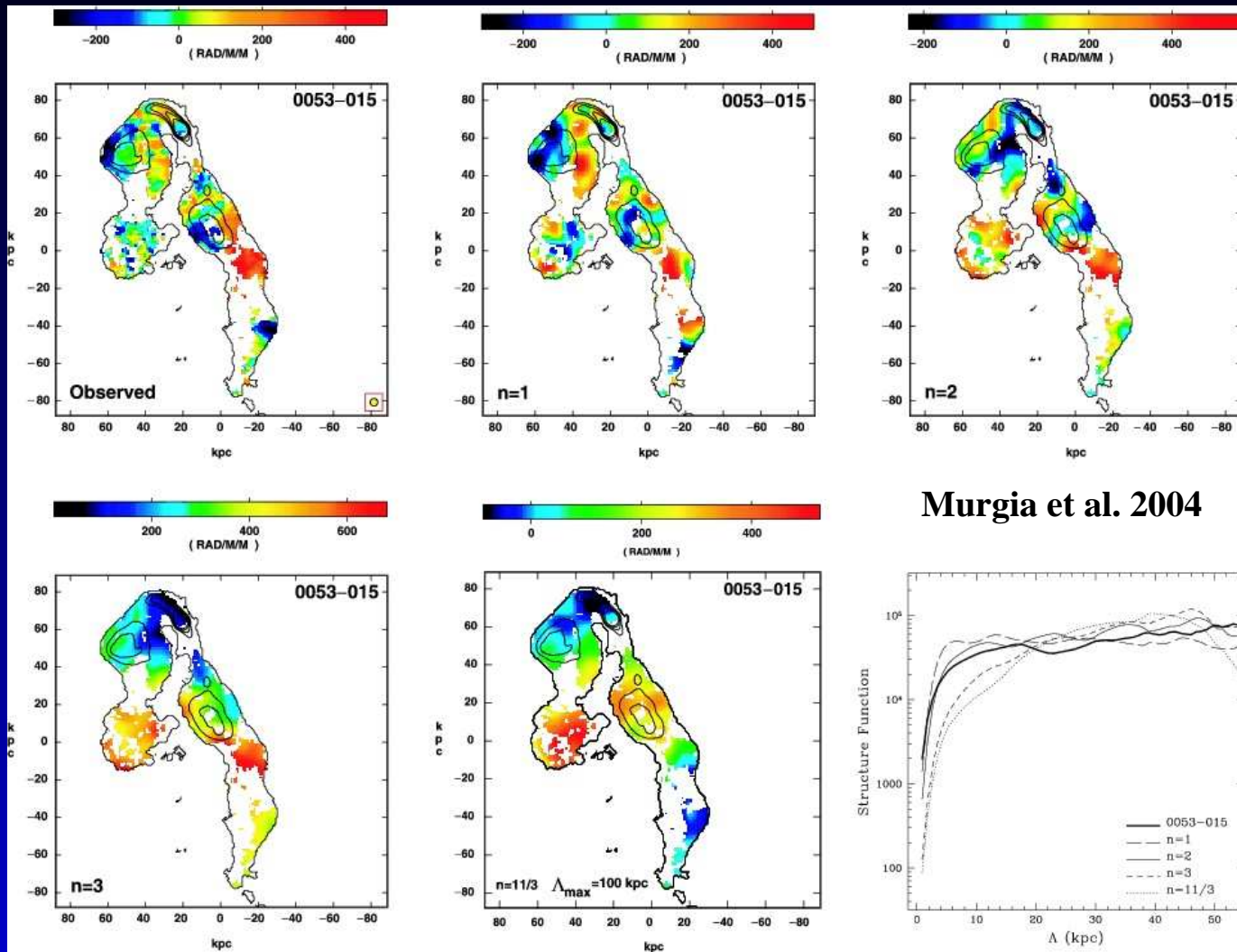


**Murgia et al. 2004**

Profile of  $\sigma$  (left) and  $\langle \rangle$  (middle) Rotation Measure for A119.

- $(\lambda_{\text{min}}, \lambda_{\text{max}}) = (6, 768) \text{ kpc} \Rightarrow n=-2$  best fit !
- Kolmogorov-like  $(-11/3)$  fits only for  $\lambda_{\text{max}} \approx 100 \text{ kpc}$  !

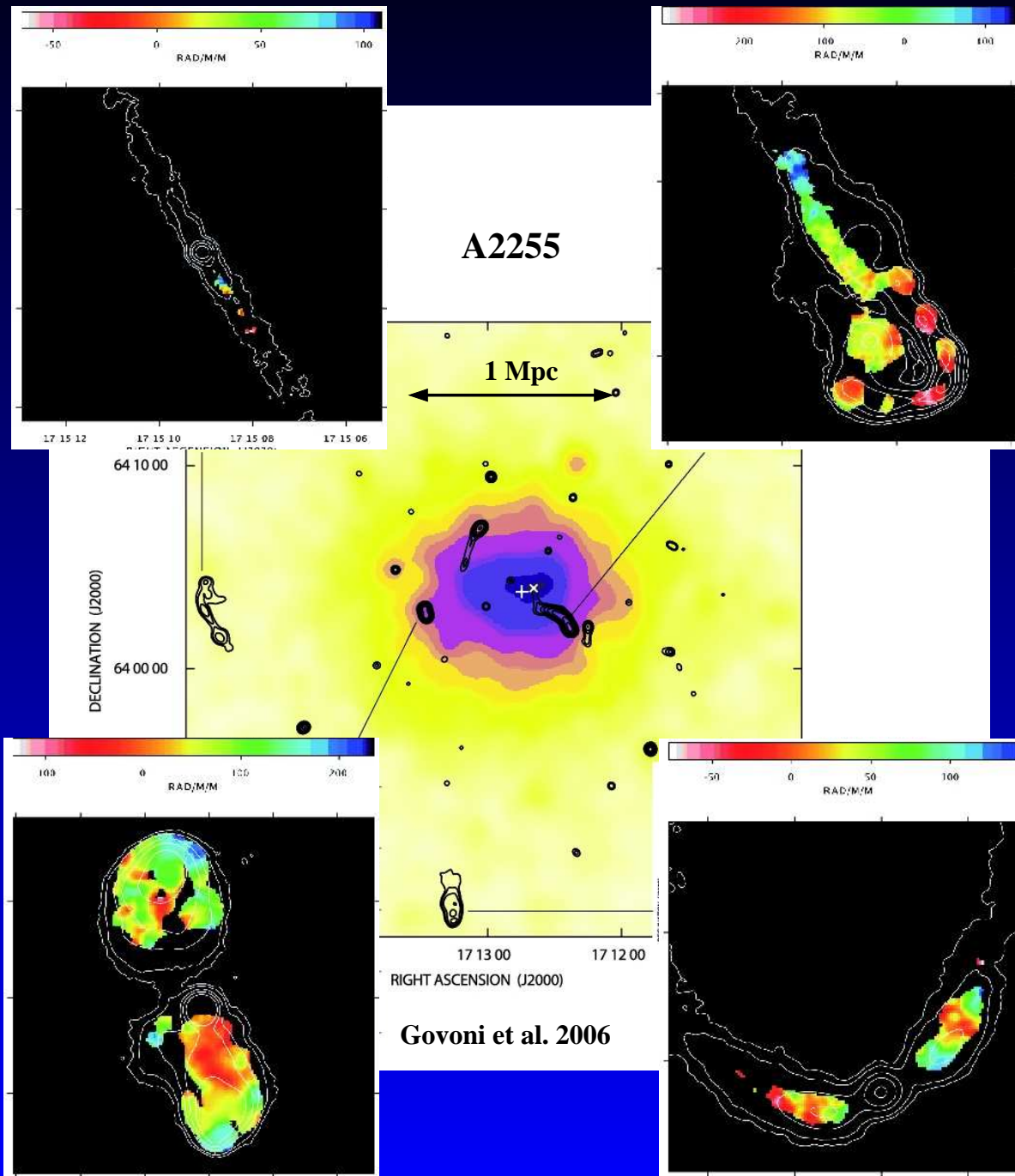
# Observations



Synthetic Rotation Measure maps and structure function.

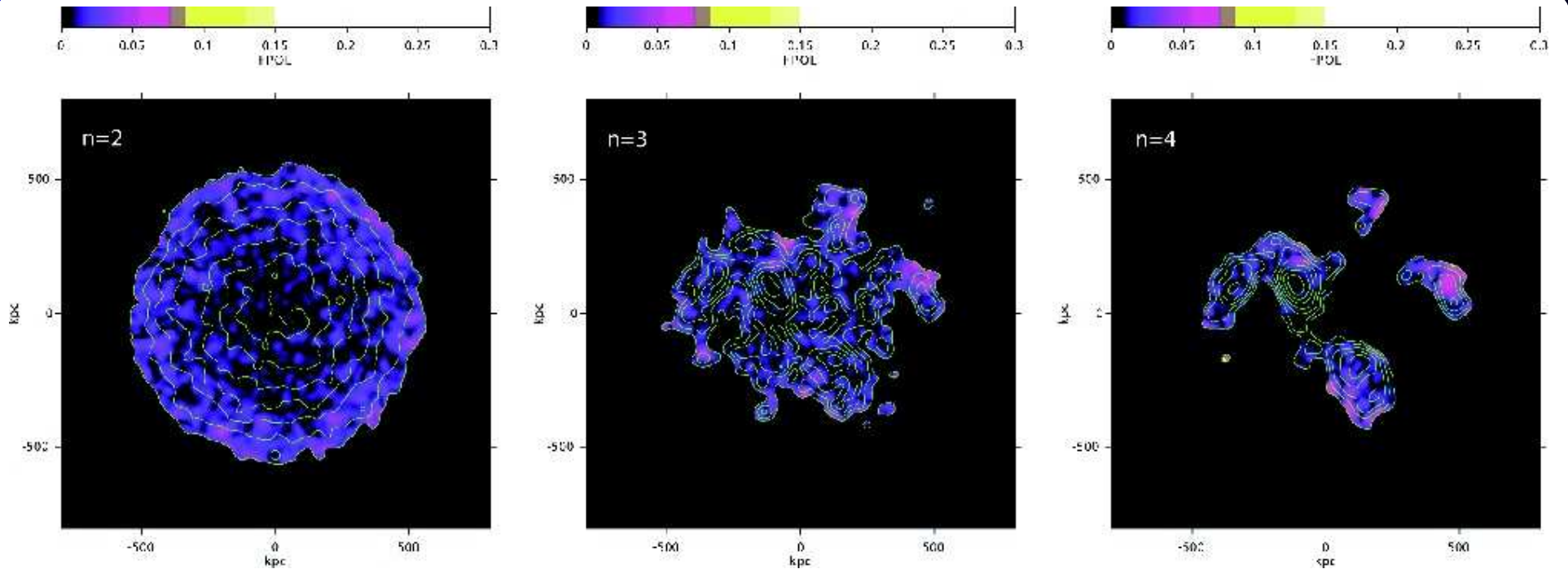
- Prefers  $n=-2$  compared to Kolmogorov-like
- Can we include more observations (e.g. radio halo) ?

# Observations





# Observations

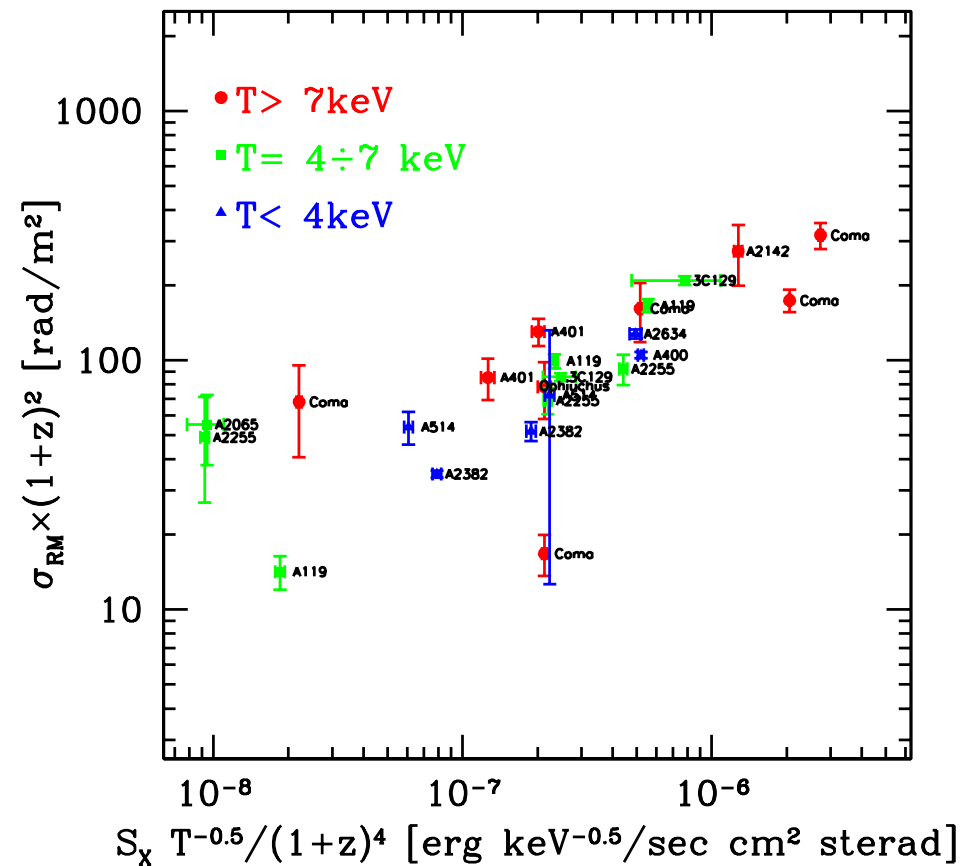
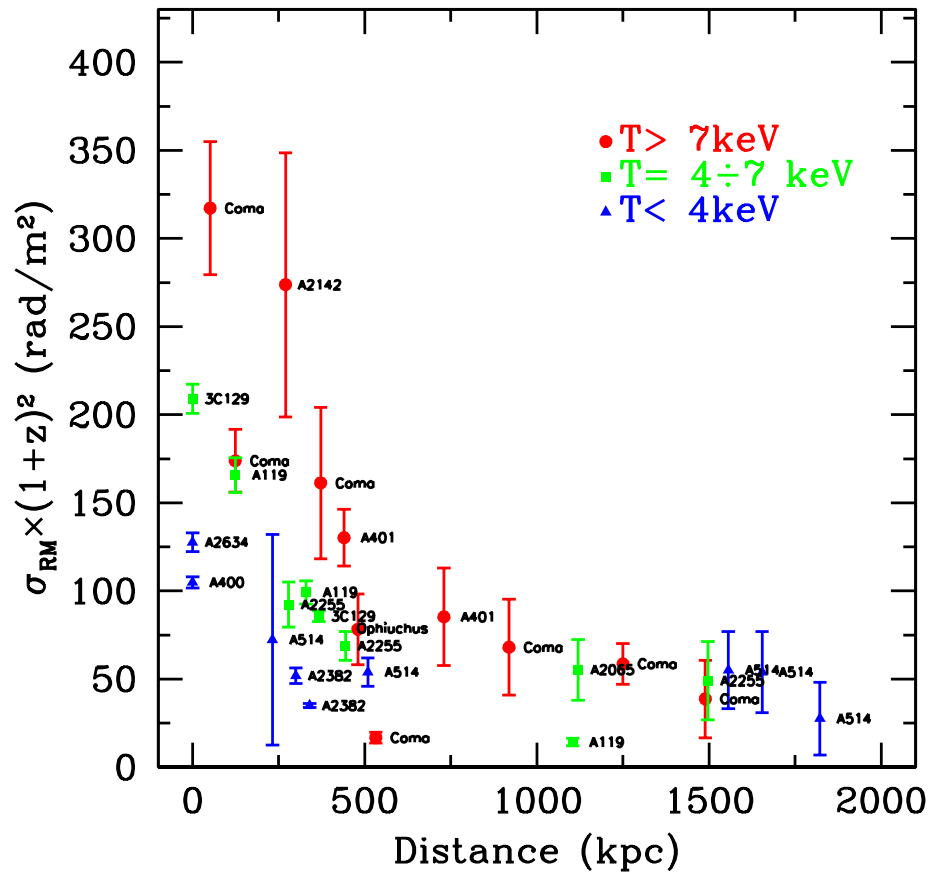


Govoni et al. 2006

Modeled radio halo and fractional polarization for A2255

- **Rotation Measure** alone leads to  $n \approx -3$ .
- **Radio halo** and **polarization** needs varying from -2 to -4 when going from center to periphery.
- Signature of cluster dynamics ?
- Signature of turbulence/decay of magnetic field ?

# Observations

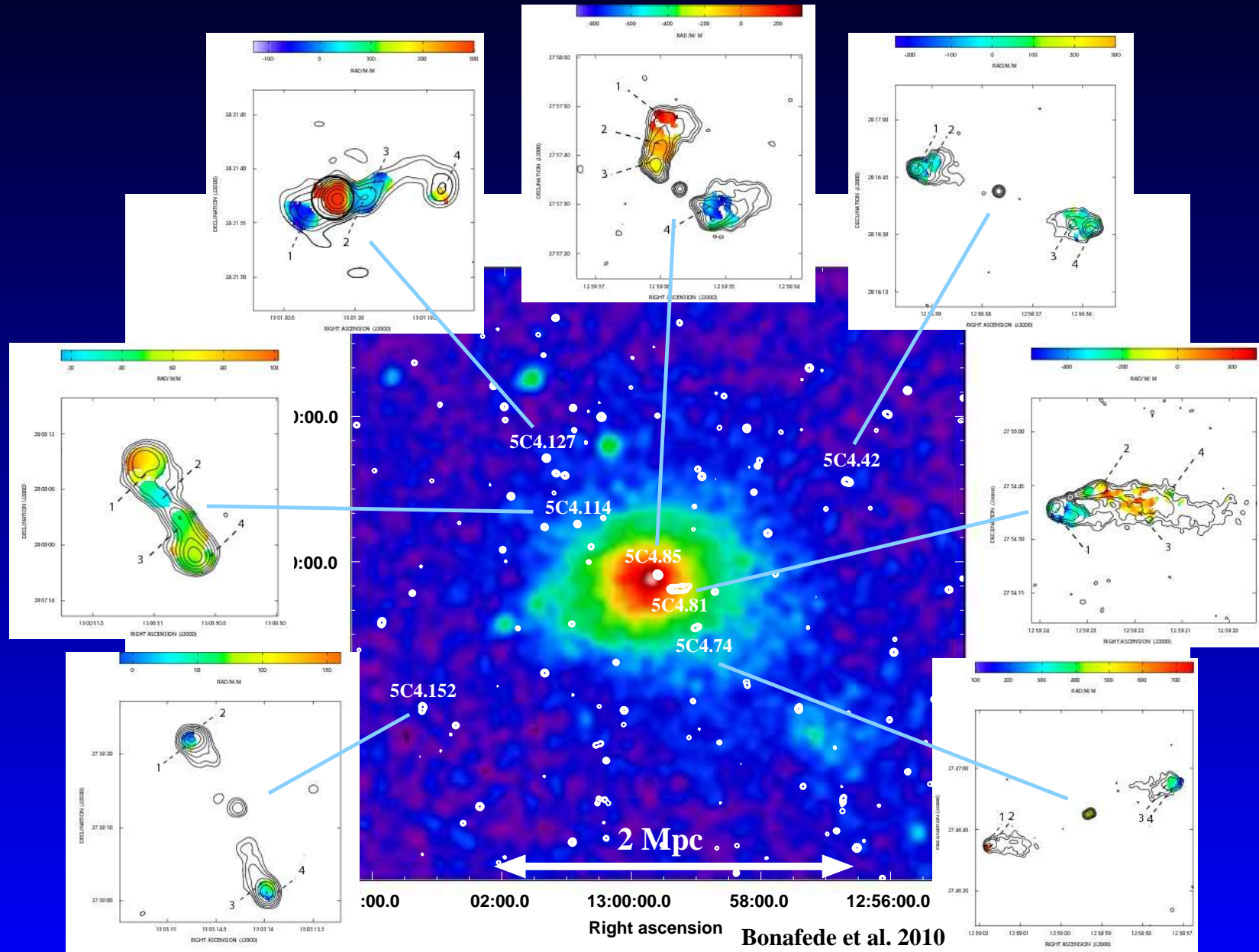


Govoni et al. 2010

- **Combination** of RM measured in **many clusters**.
- How does  $\vec{B}$  scale with cluster temperature ?
- Magnetic Field in Radio quiet/active clusters ?

# Observations

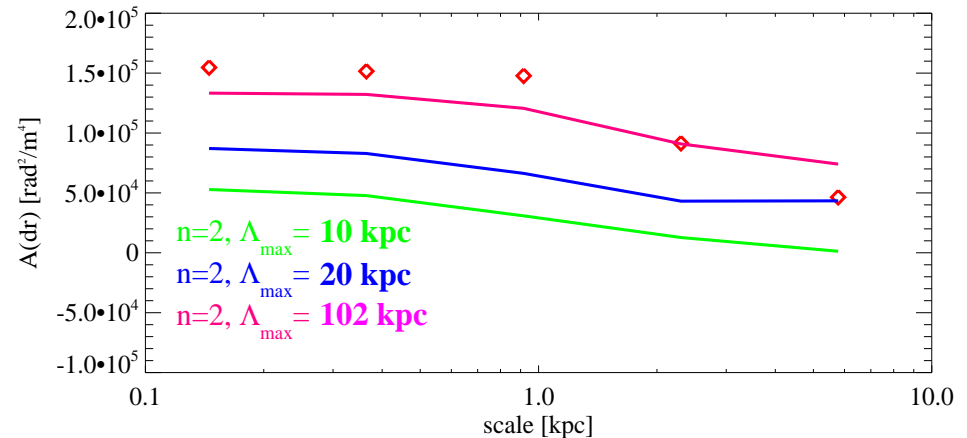
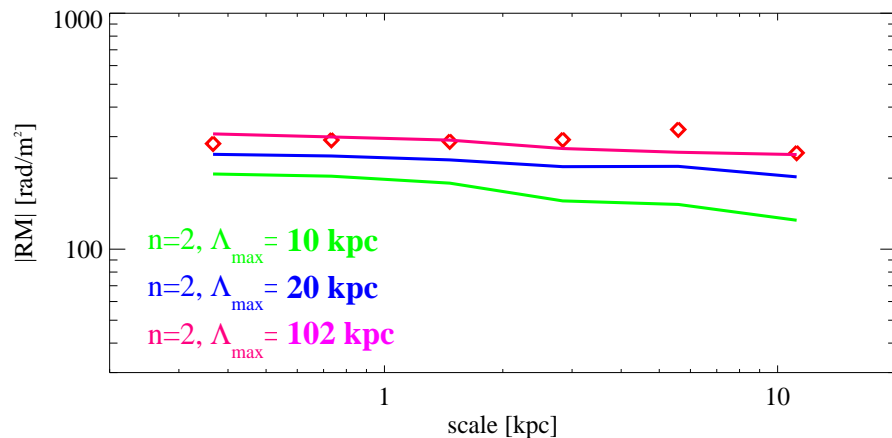
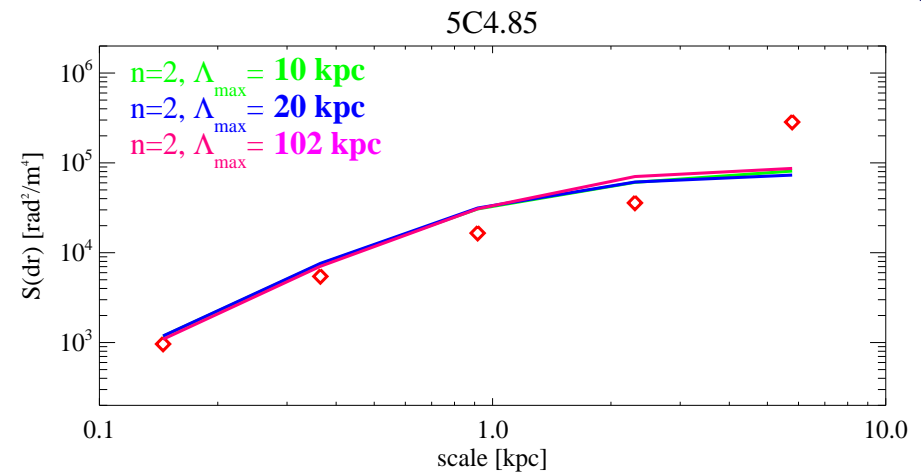
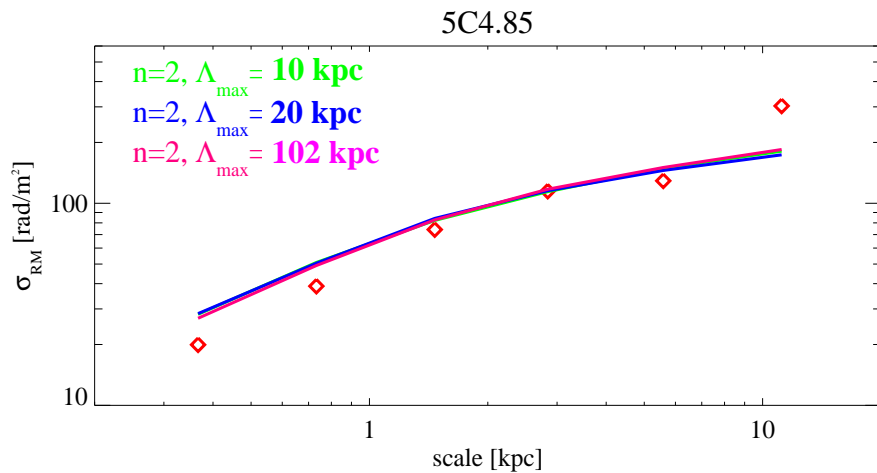
$$B(r) = B_0 \left(1 + (r/r_c)^2\right)^{-1.5\eta}, \quad |B_k|^2 \propto k^{-n}, \quad (k_{\min}, k_{\max})$$





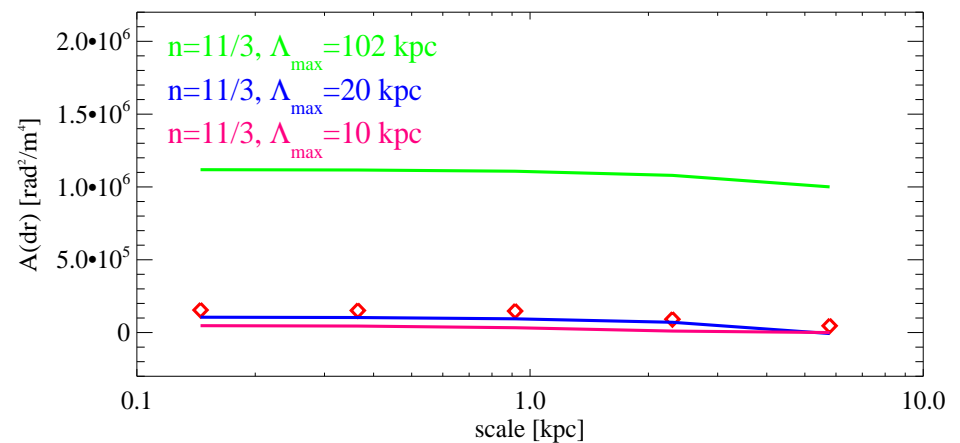
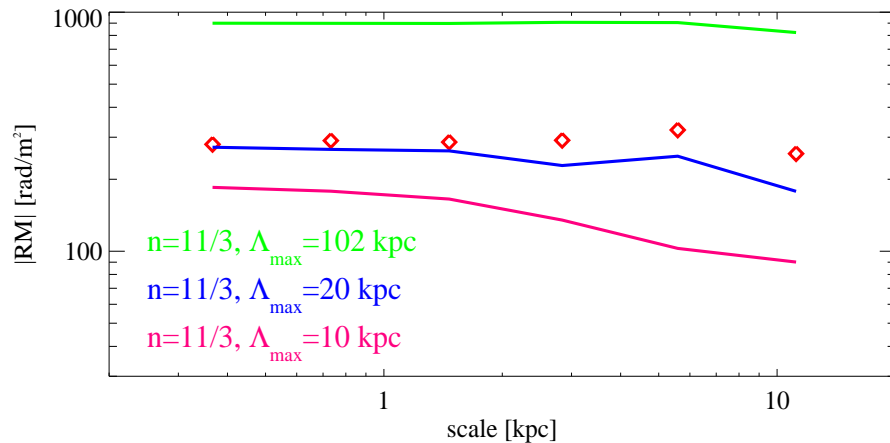
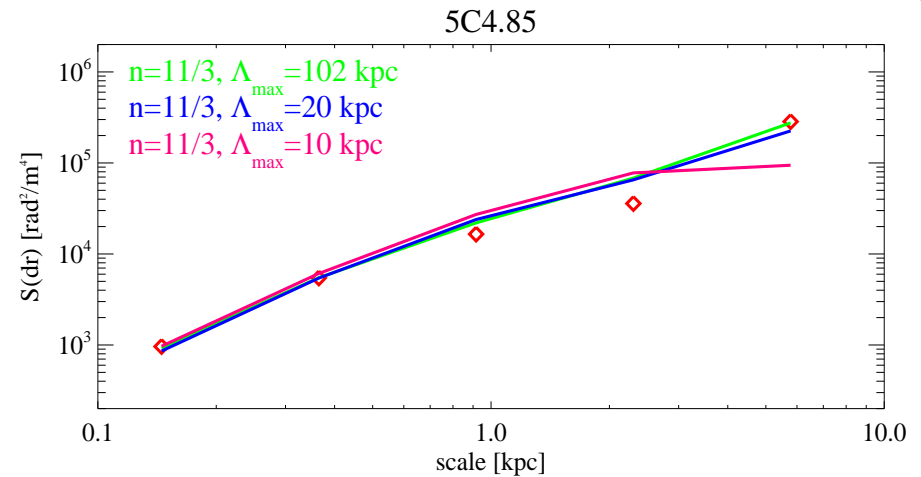
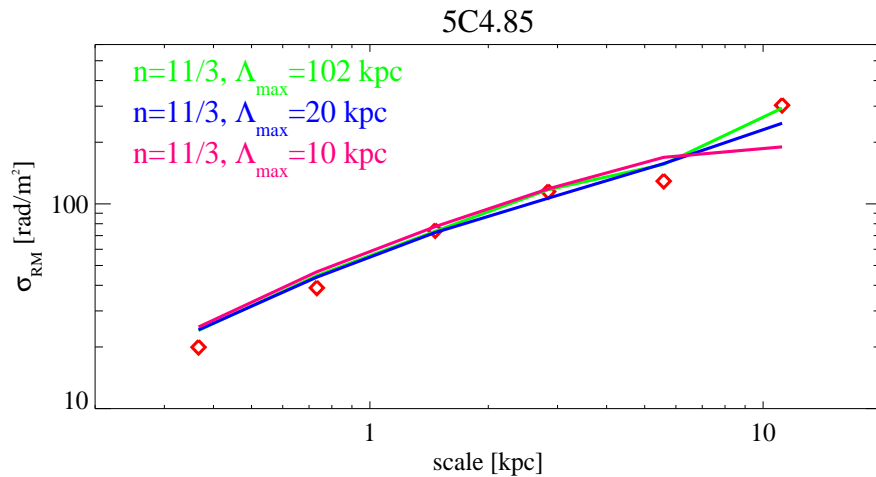
# Observations

- $S(dx, dy) = \langle [RM(x, y) - RM(x + dx, y + dy)]^2 \rangle$
- $A(dx, dy) = \langle RM(x, y) \times RM(x + dx, y + dy) \rangle$
- $\langle |RM| \rangle_{\text{scale}}$ ,  $\langle \sigma_{RM} \rangle_{\text{scale}}$ ,  $n = 2, \Lambda_{\text{max}} = 102 \text{ kpc}$



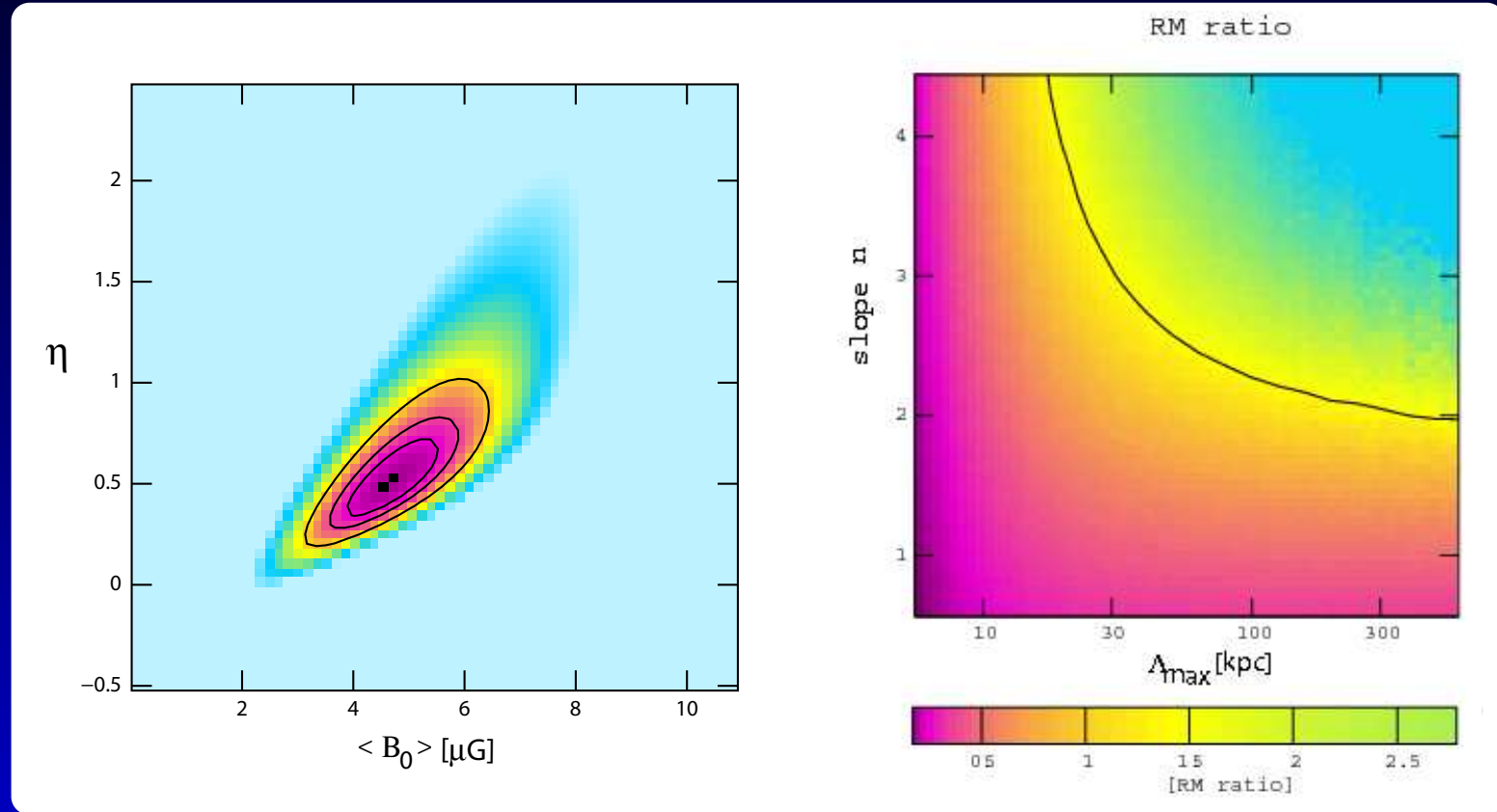
# Observations

- $S(dx, dy) = \langle [RM(x, y) - RM(x + dx, y + dy)]^2 \rangle$
- $A(dx, dy) = \langle RM(x, y) \times RM(x + dx, y + dy) \rangle$
- $\langle |RM| \rangle_{\text{scale}}$ ,  $\langle \sigma_{RM} \rangle_{\text{scale}}$ ,  $n = 11/3$ ,  $\Lambda_{\text{max}} = 24 \text{ kpc}$



# Observations

$$B(r) = B_0 \left(1 + (r/r_c)^2\right)^{-1.5\eta}, \quad |B_k|^2 \propto k^{-n}, \quad (k_{\min}, k_{\max})$$

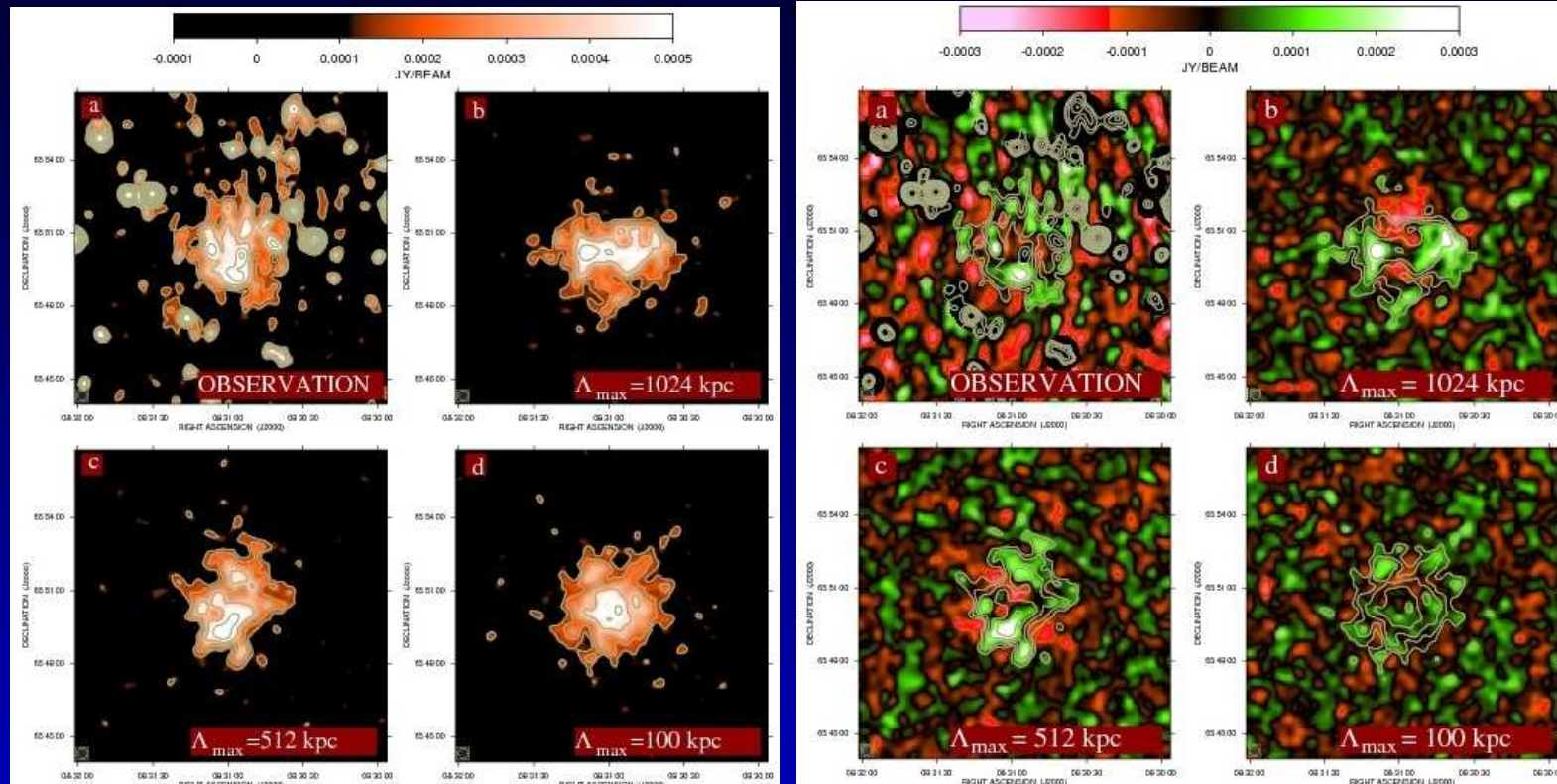


- Degeneration of injection scale  $k_{\min}$  and spectral index  $n$
  - Knowledge of the **spectrum** constrains **magnetic field**
  - How does  $\vec{B}$  scale with cluster temperature ?
- $\Rightarrow$  Cosmological MHD simulations (Lecture III)



# Observations

$$B(r) = B_0 \left(1 + (r/r_c)^2\right)^{-1.5\eta}, \quad |B_k|^2 \propto k^{-n}, \quad (k_{\min}, k_{\max})$$



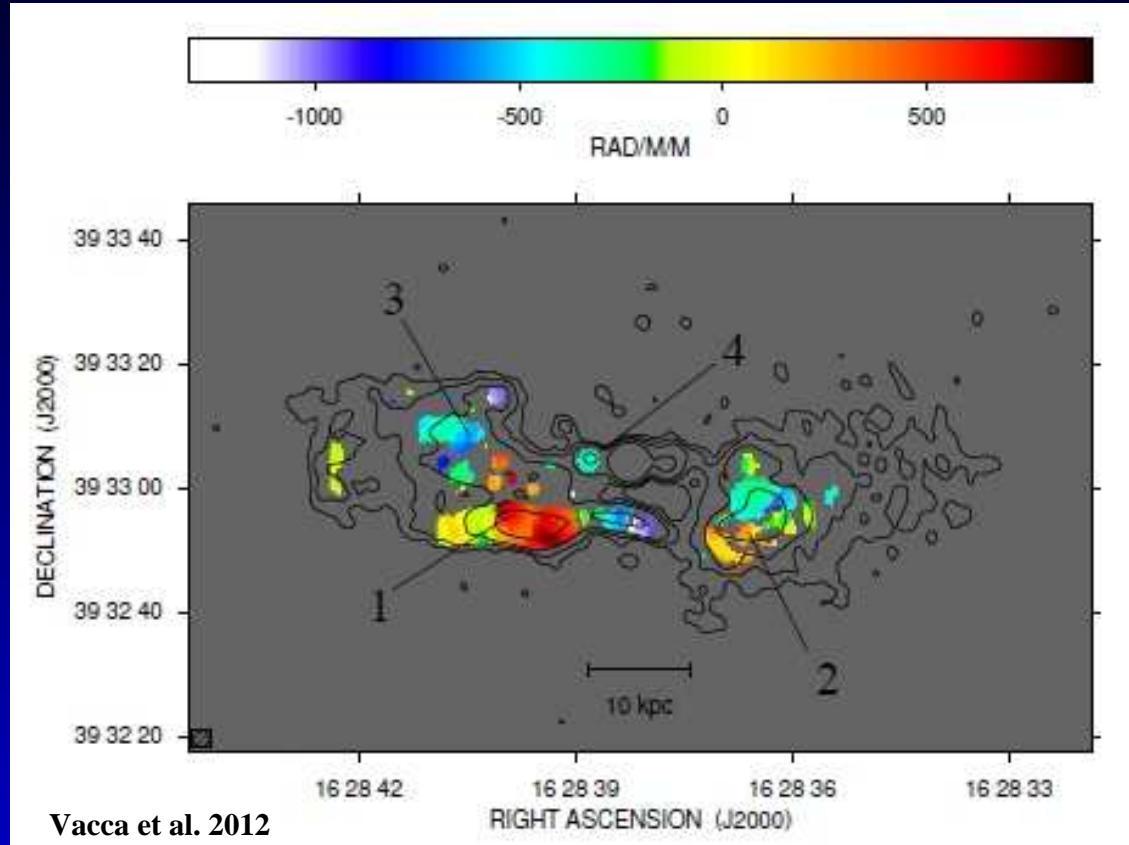
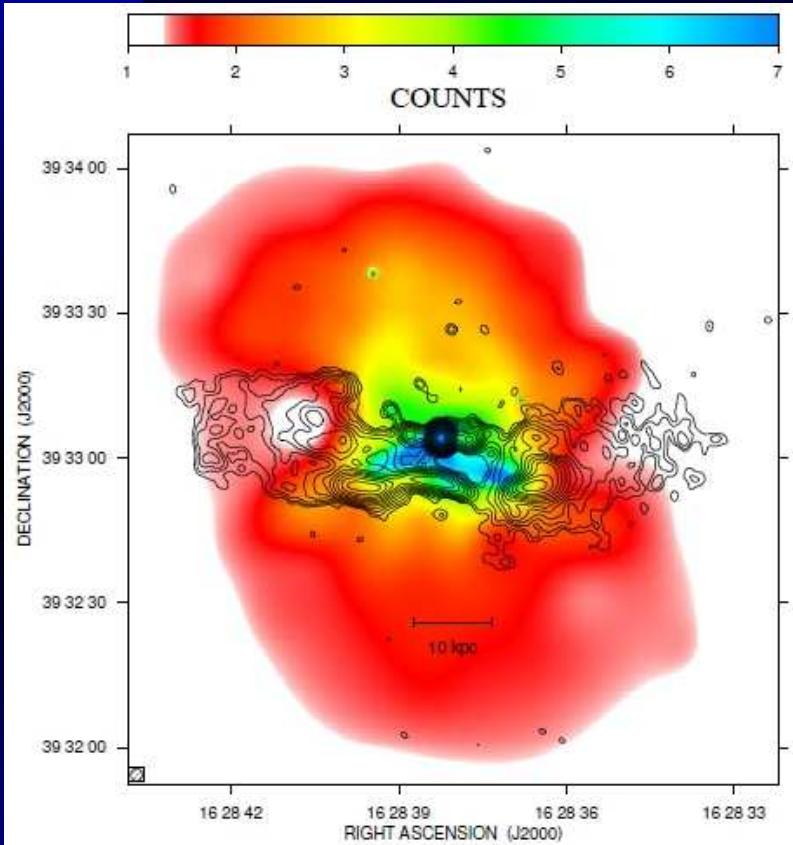
⇒ A655: Inferred outer scale  $\approx 450$  kpc (Vacca et al. 2010) !

- **Depolarization** indicates truncation at small scales !

⇒ **No** fluctuations at **scales below**  $\approx (.1 - .5)$  kpc !

# Observations

$$B(r) = B_0 \left(1 + (r/r_c)^2\right)^{-1.5\eta}, \quad |B_k|^2 \propto k^{-n}, \quad (k_{\min}, k_{\max})$$

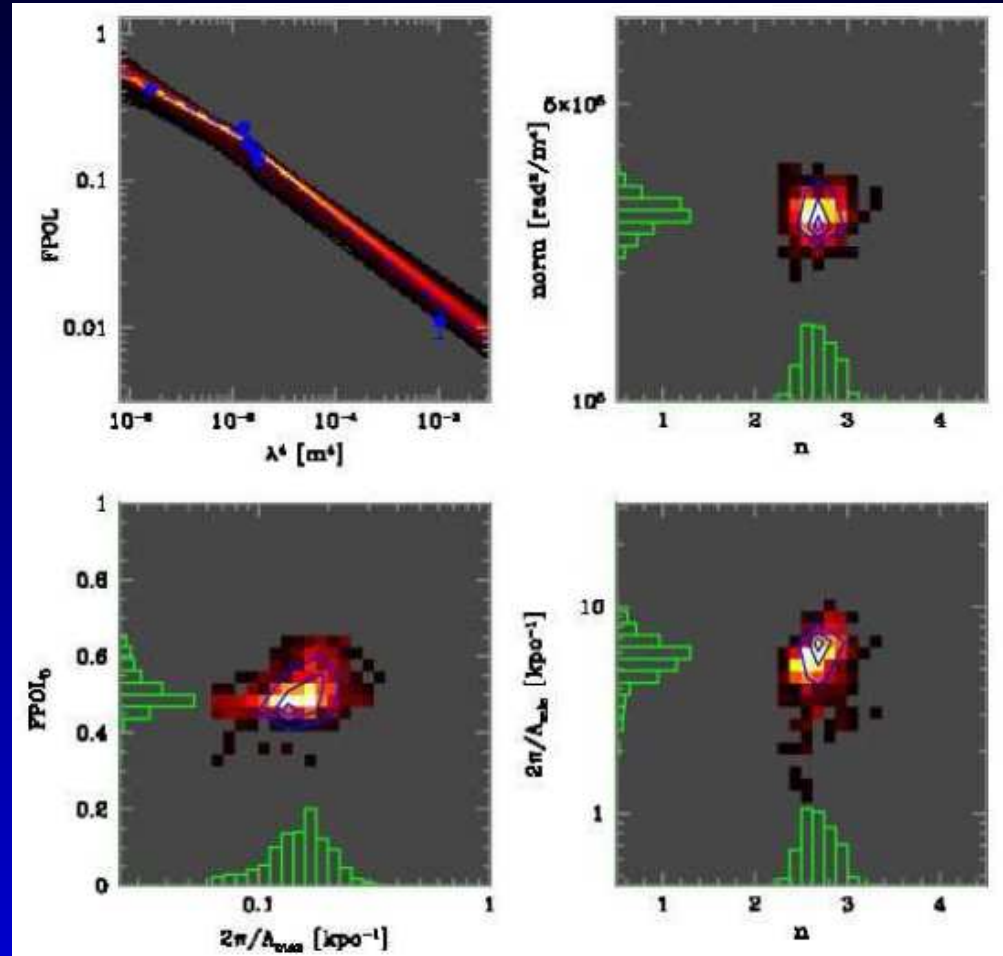
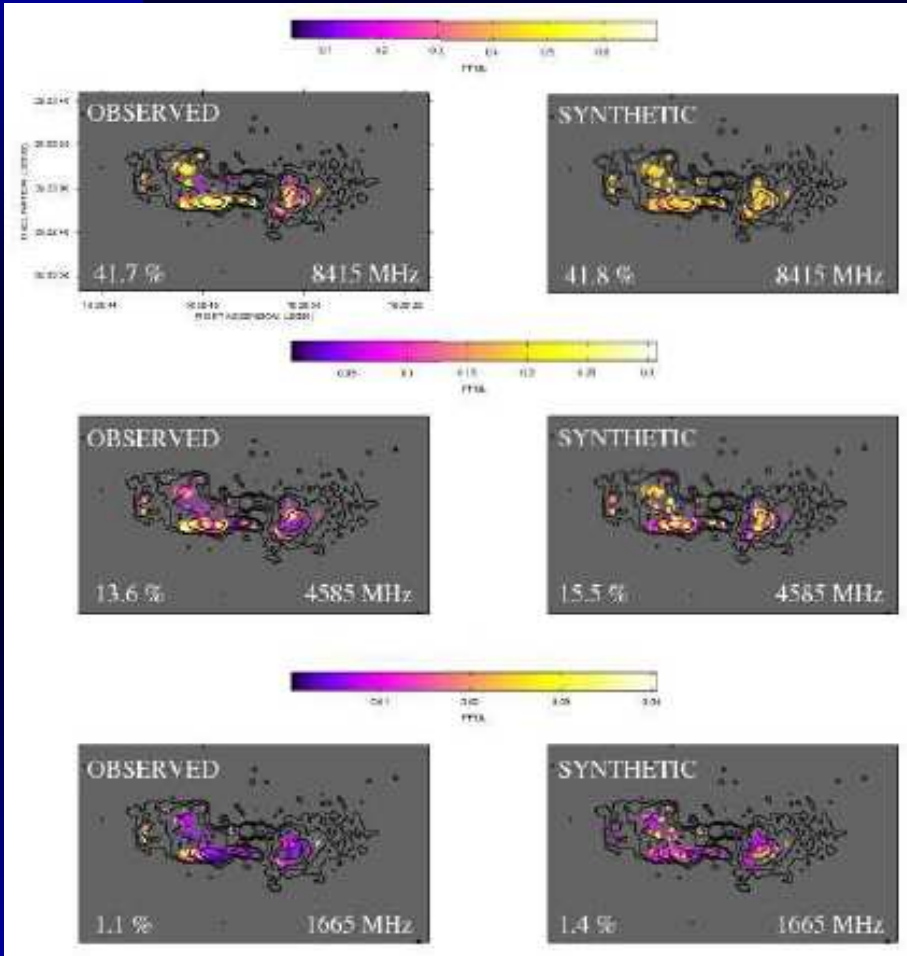


A2199 (Vacca et al. 2012):

- ICM model (double  $\beta$  model)
- Model for cavities
- RM and **depolarization** analysis

# Observations

$$B(r) = B_0 \left(1 + (r/r_c)^2\right)^{-1.5\eta}, \quad |B_k|^2 \propto k^{-n}, \quad (k_{\min}, k_{\max})$$



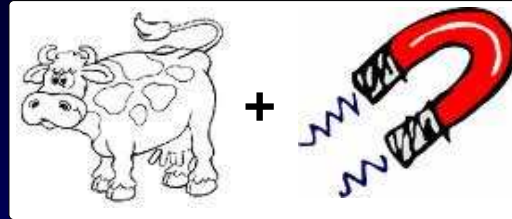
- $B_0 = (11.7 \pm 9.0) \mu\text{G}$
- $n = (2.8 \pm 1.3)$
- $\eta = (0.9 \pm 0.5)$

- Vacca et al. 2012
- $\Lambda_{\max} = (35 \pm 28) \text{kpc}$
  - $\Lambda_{\min} = (0.7 \pm 0.1) \text{kpc}$

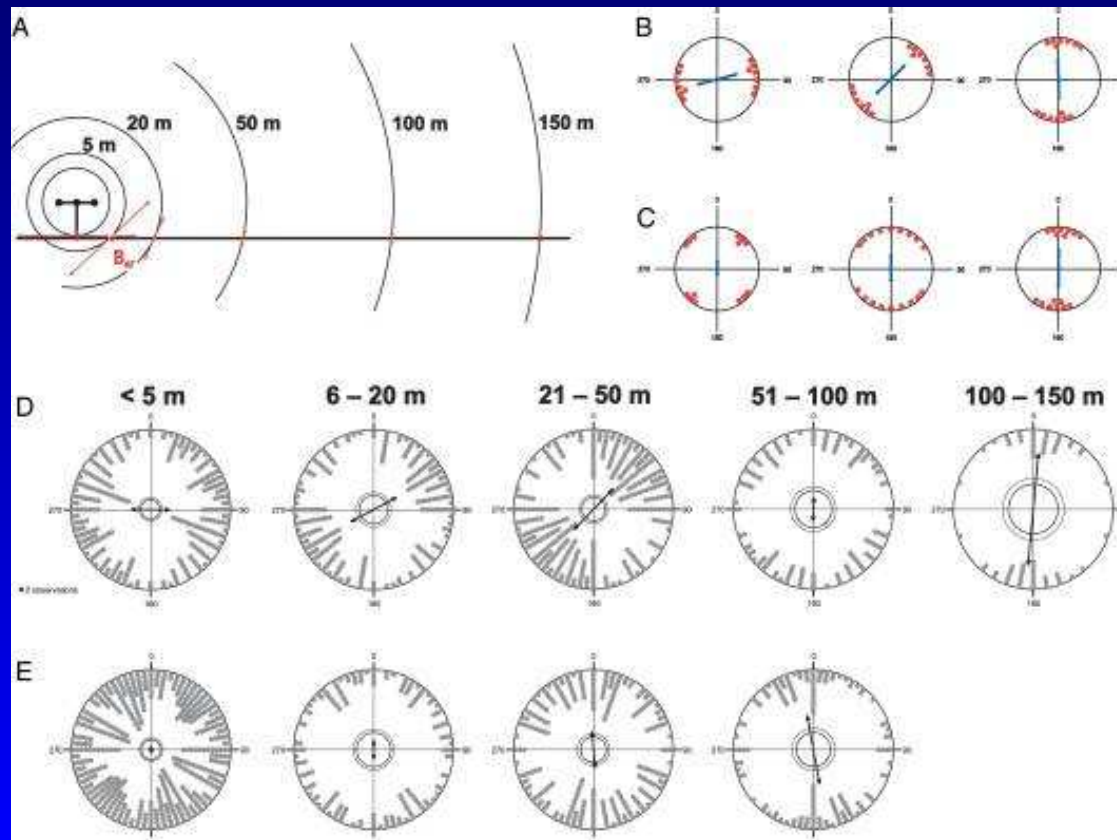


# Note on magnetic field structure

Details in magnetic field structure can reveal interesting effects !



Example **Disturbed Magnetic Cows**: “Extremely low-frequency electromagnetic fields disrupt magnetic alignment of ruminants”



# Cluster non-thermal Emission

Cluster: MACSJ1752.0+4440 X-ray , Optical, Radio

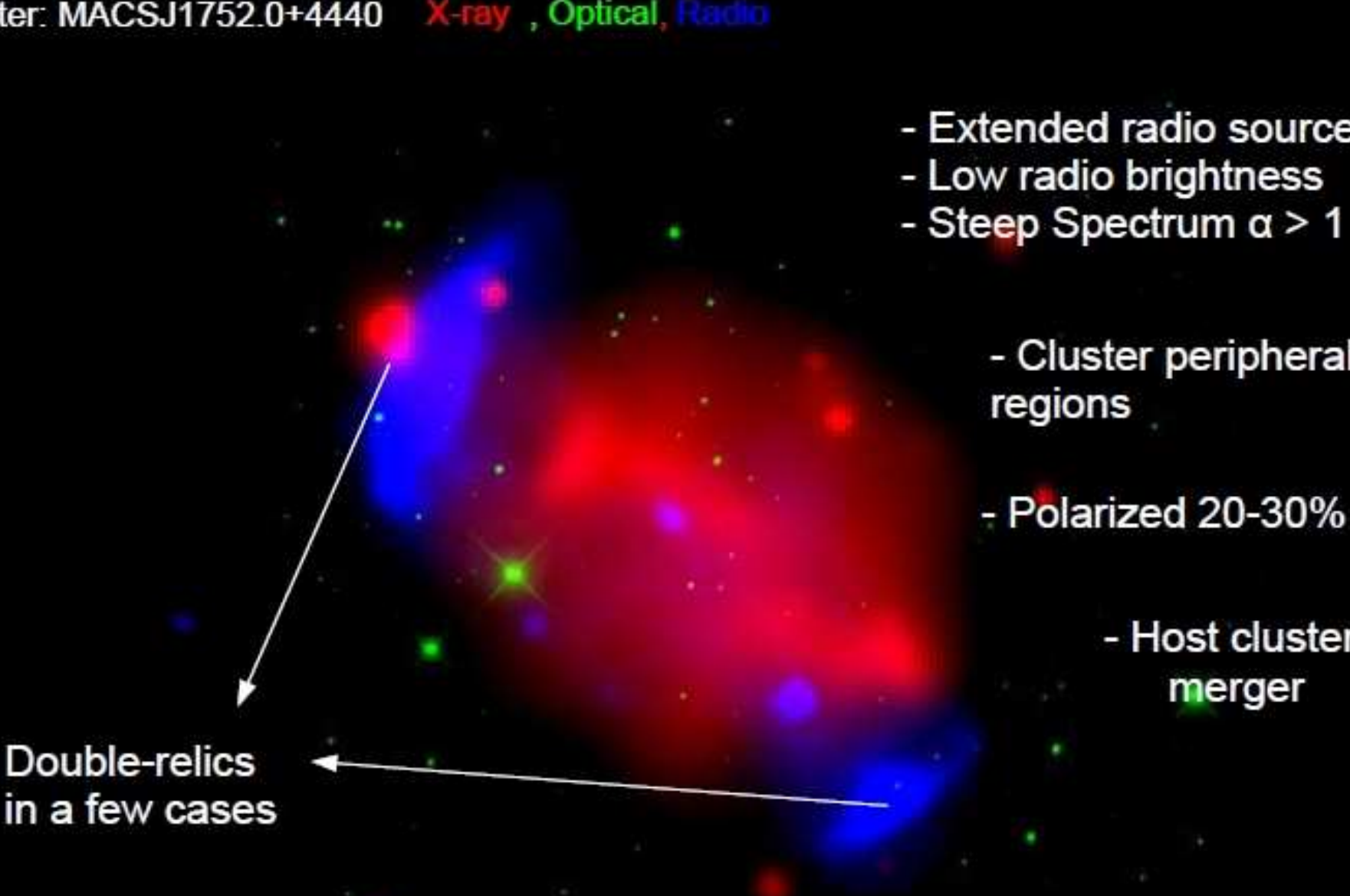
- Extended radio sources
- Low radio brightness
- Steep Spectrum  $\alpha > 1$

- Cluster peripheral regions

- Polarized 20-30%

- Host cluster:  
merger

Double-relics  
in a few cases

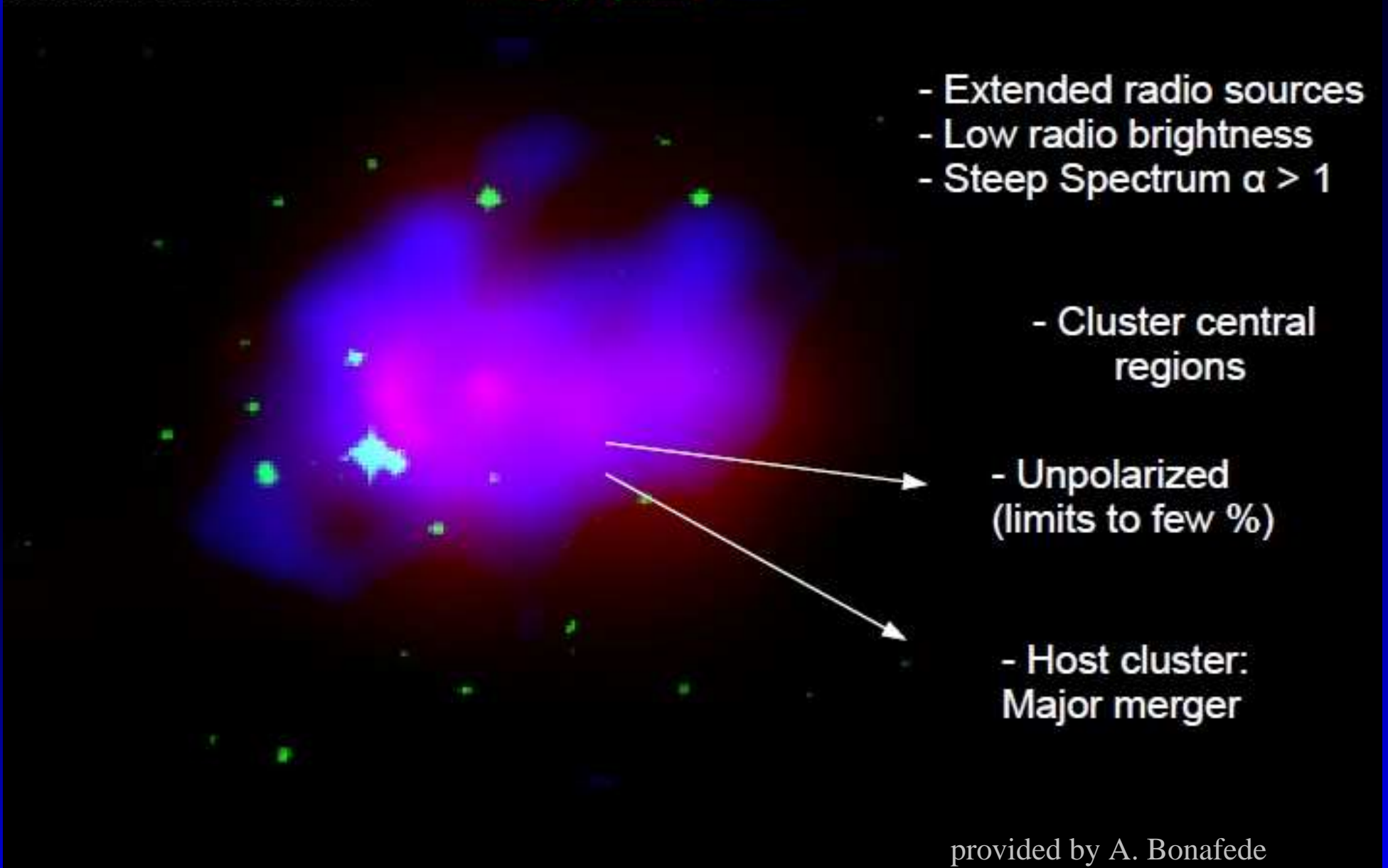


provided by A. Bonafede

# Cluster non-thermal Emission

Cluster: MACSJ0553-33

X-ray , Optical, Radio





# Cluster non-thermal Emission

## Cluster mergers

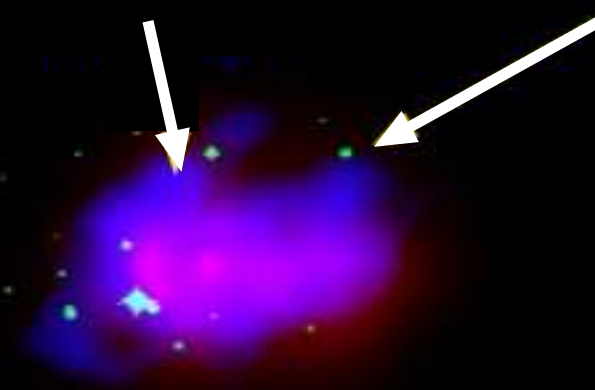
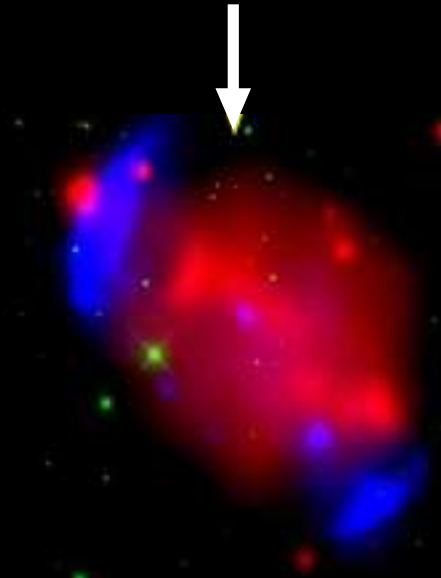
Shock Waves

developing  
Turbulence

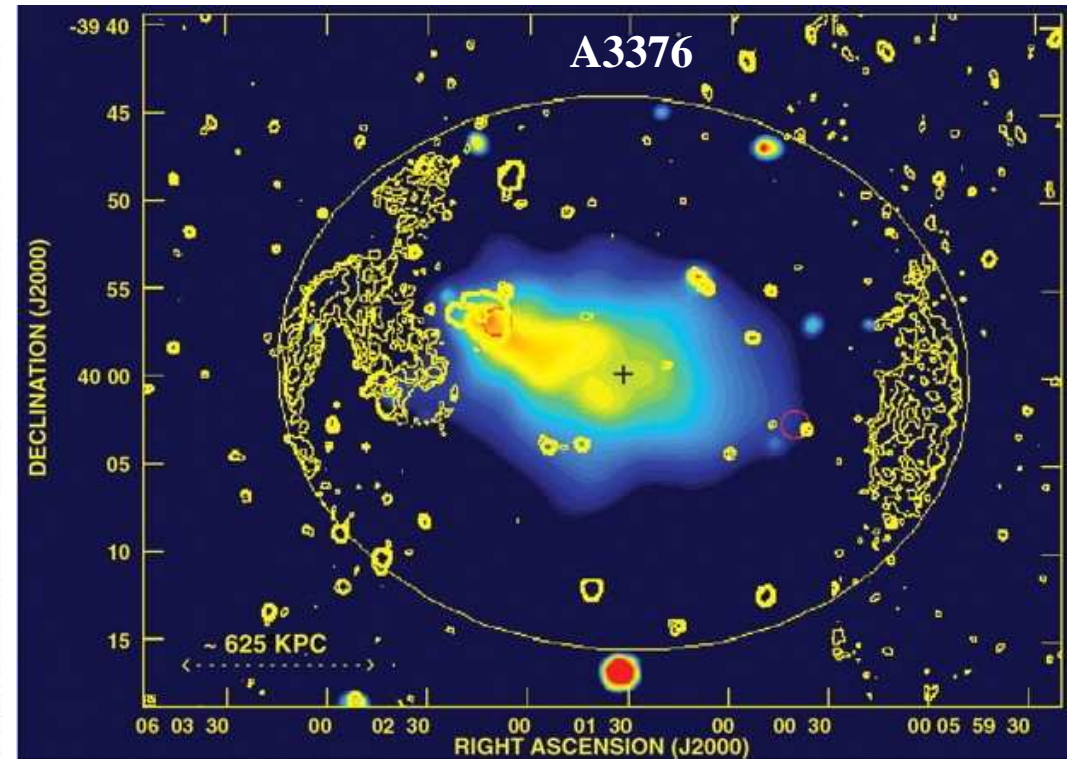
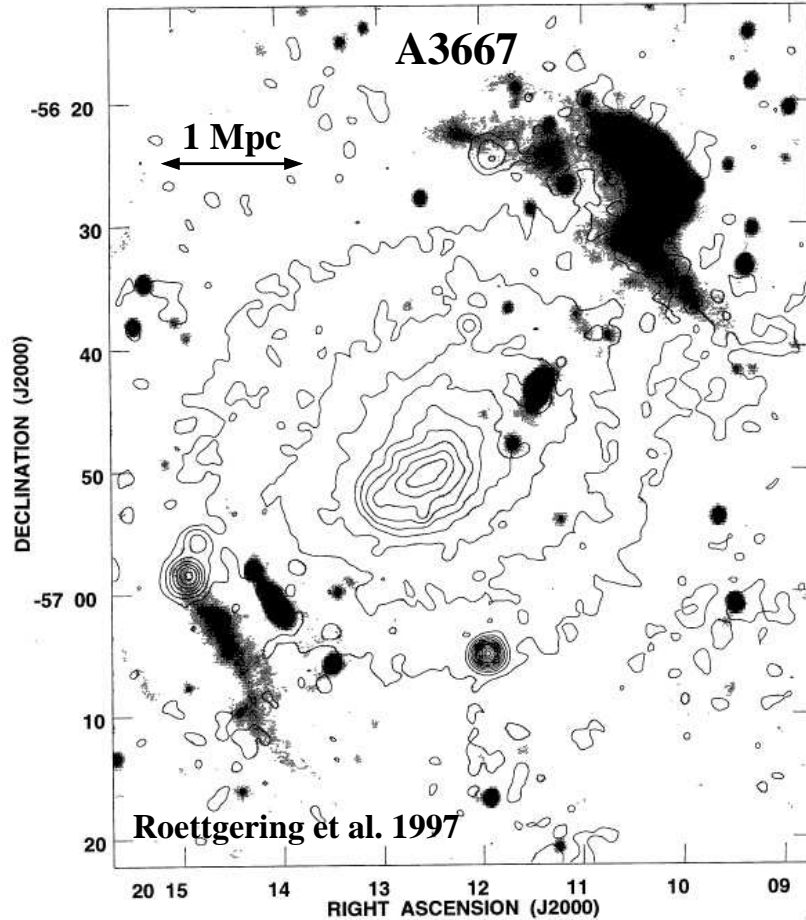
Acceleration of  $e^-$   
compression / ordering  
of Magnetic Fields

Re-acceleration  
of existing  $e^-$

Hadronic  
interaction  
CRp / ICM  
decay to  $e^-$



# Cluster Radio Relics



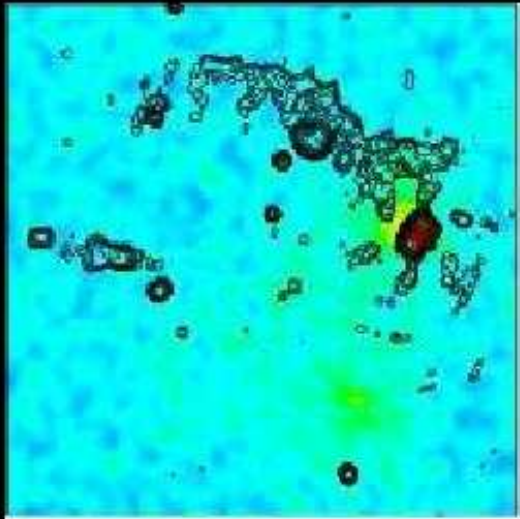
Bagchi et al. 2006

**Peripheral synchrotron emission** (radio relics) of A3667 (left) and A3376 (right).

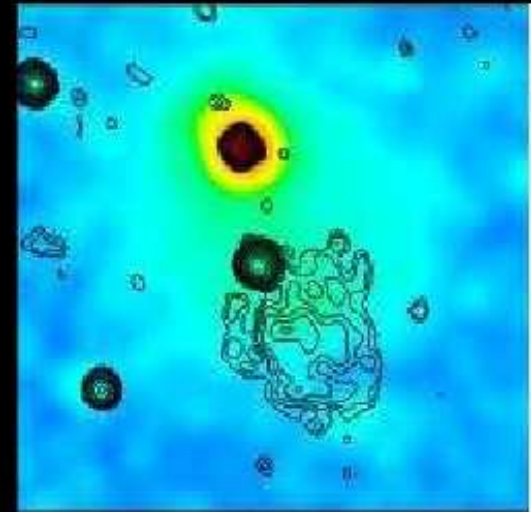
- Modeling of A3667 (Roettgering 1997)
- emission zone width  $\Rightarrow \vec{B} \approx 1 \mu\text{G}$

# Cluster Radio Relics

## Radio relics: morphologies

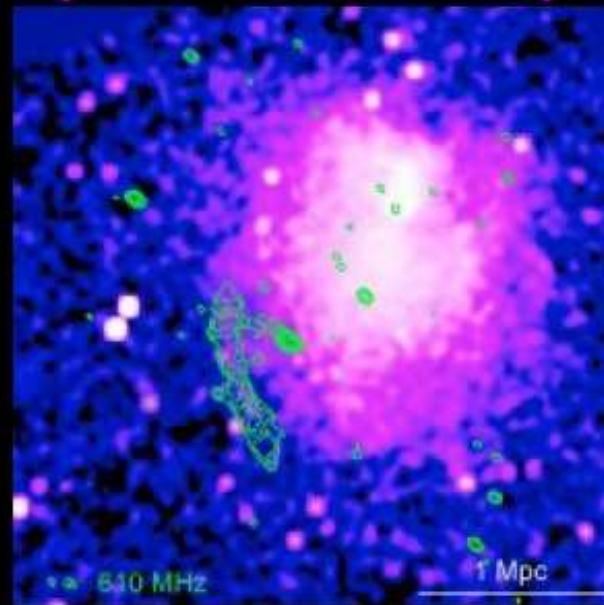


**Abell 115**  
(Govoni et al. 2001)

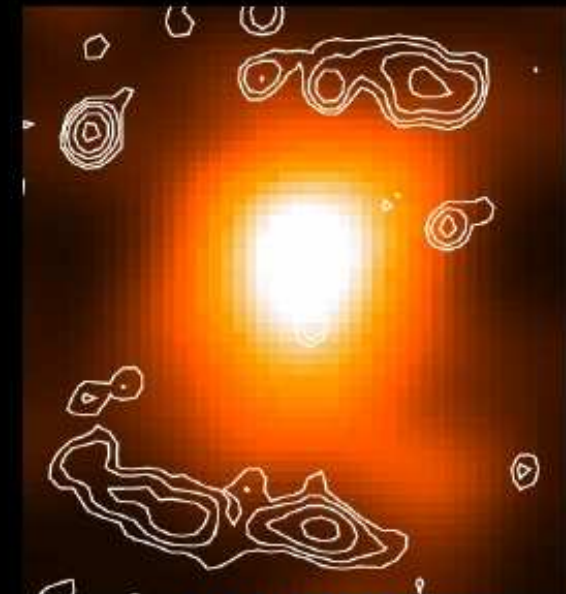
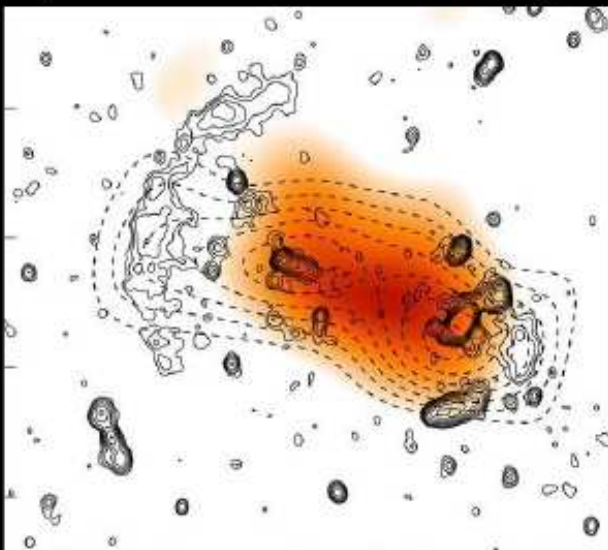


**Abell 1664**  
(Govoni et al. 2001)

**Abell 521**  
(Giacintucci et al. 2008)



**ZwCl 0008.8+5215**  
(van Weeren et al. 2011)

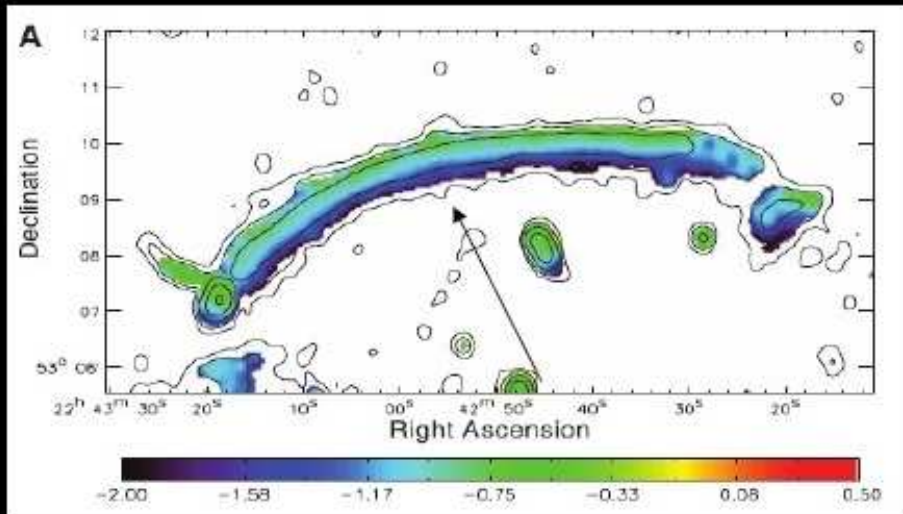


**Abell 1240**  
(Bonafede et al. 2009)

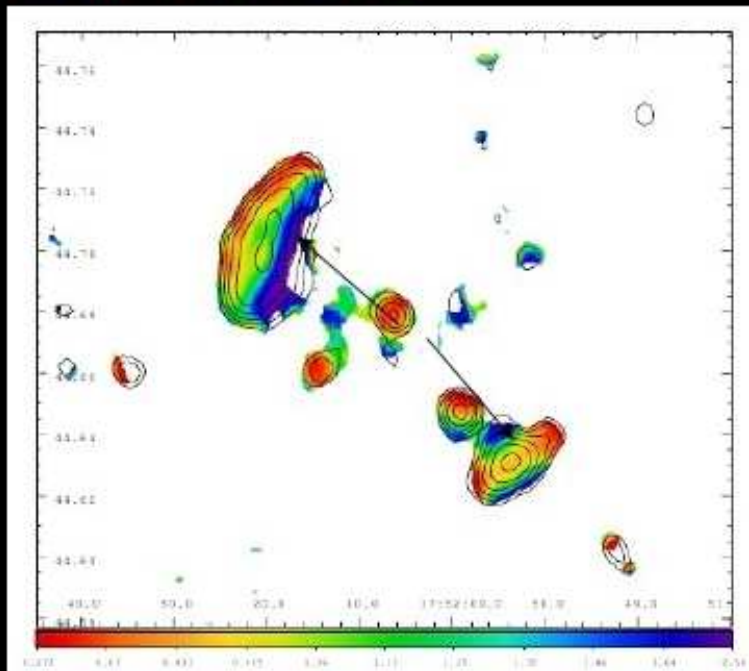


# Cluster Radio Relics

Van Weeren et al. 2010



Bonafede et al. 2012



Spectral steepening

↓  
particle aging

Diffusive Shock  
Acceleration regime

$$\alpha_l = -\frac{1}{2} + \frac{M^2 + 1}{M^2 - 1}$$

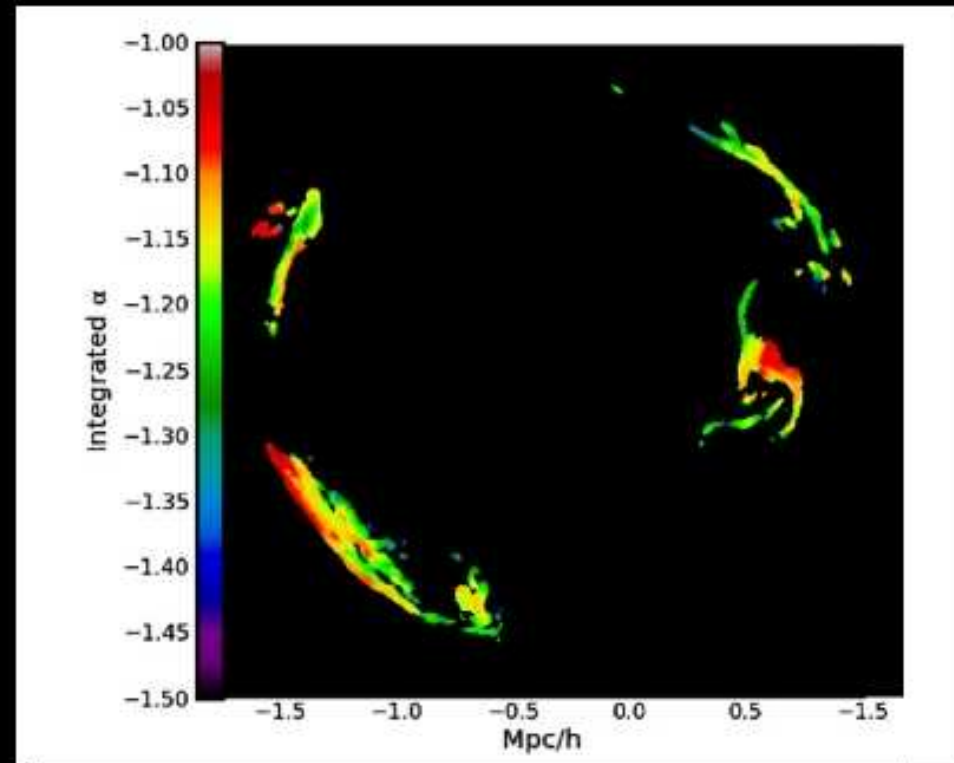
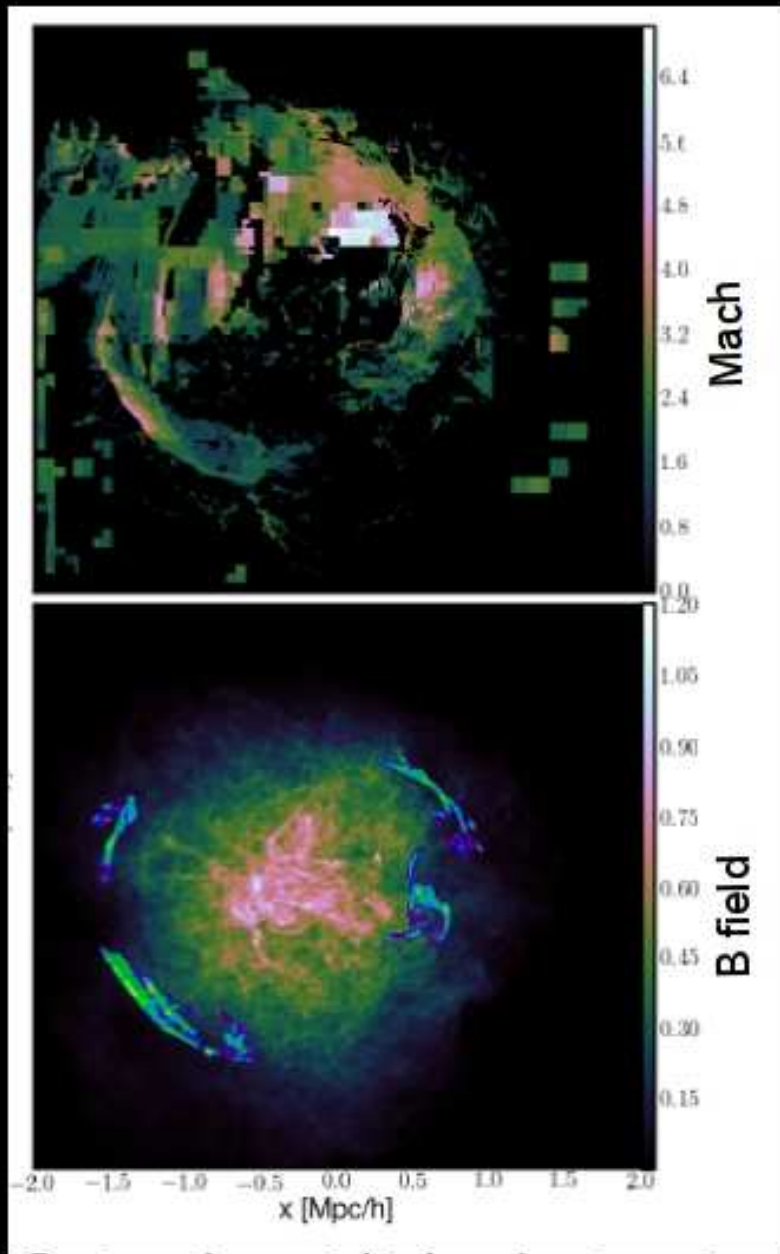
Blandford & Eichler 87

Mach numbers ~  
2 - 4

provided by A. Bonafede

# Cluster Radio Relics

From cosmological simulations

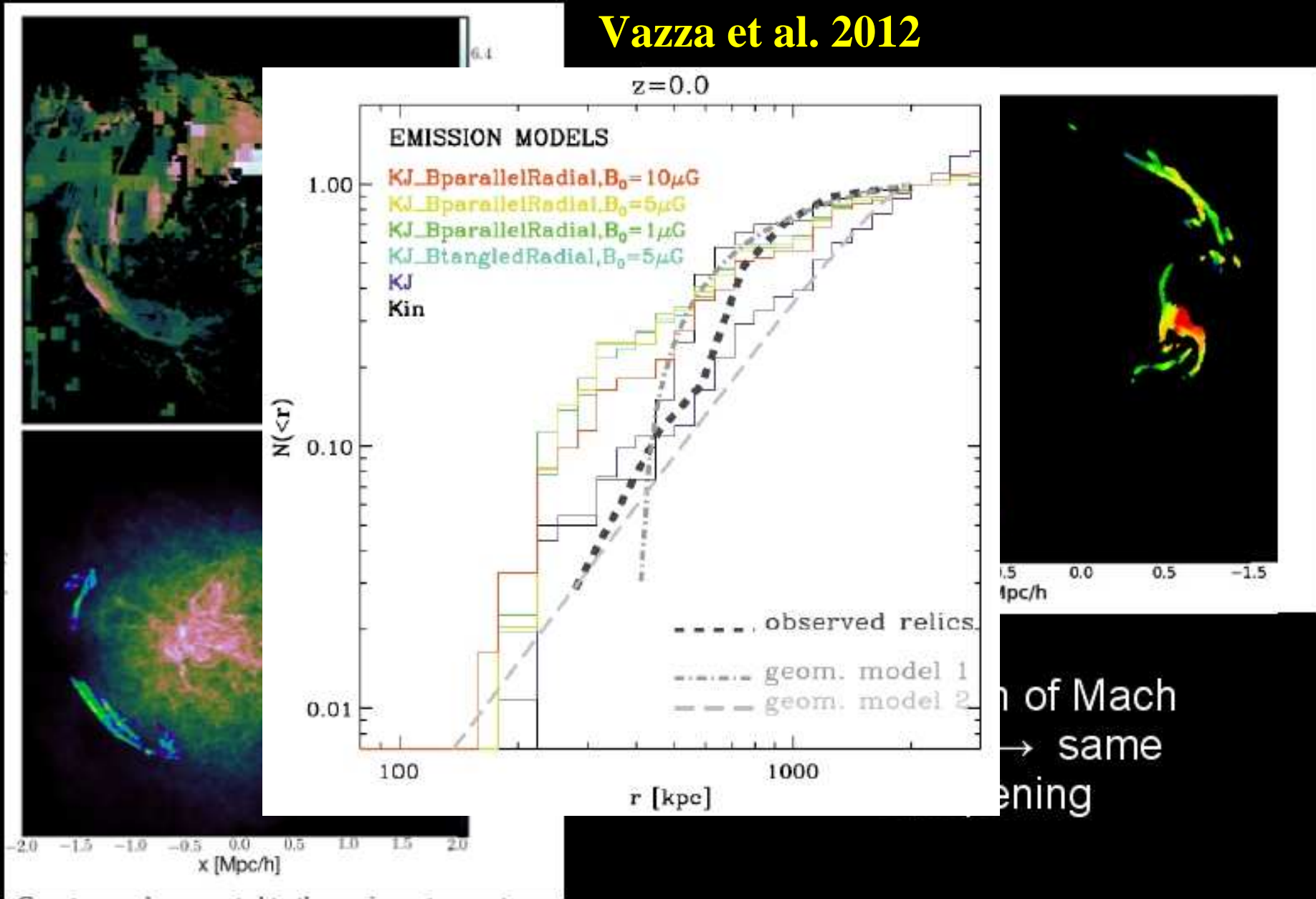


Distribution of Mach numbers  $\rightarrow$  same steepening

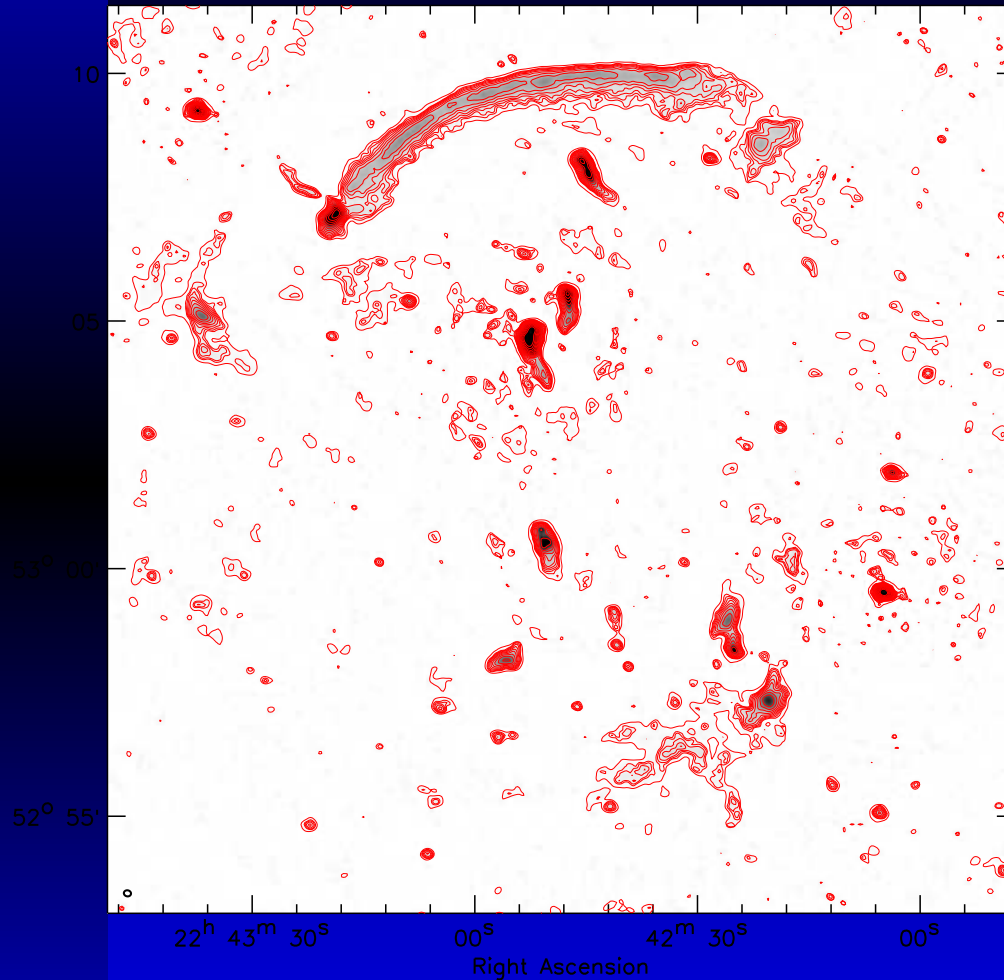
# Cluster Radio Relics

From cosmological simulations

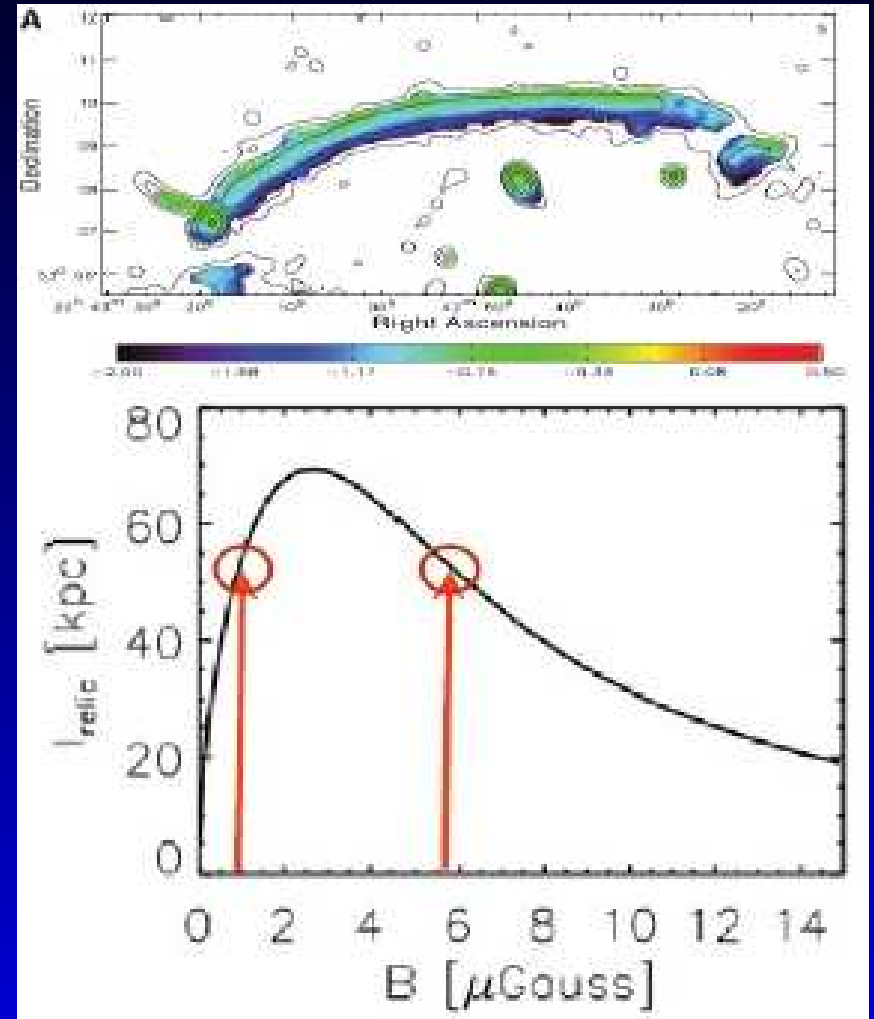
Vazza et al. 2012



# Cluster Radio Relics



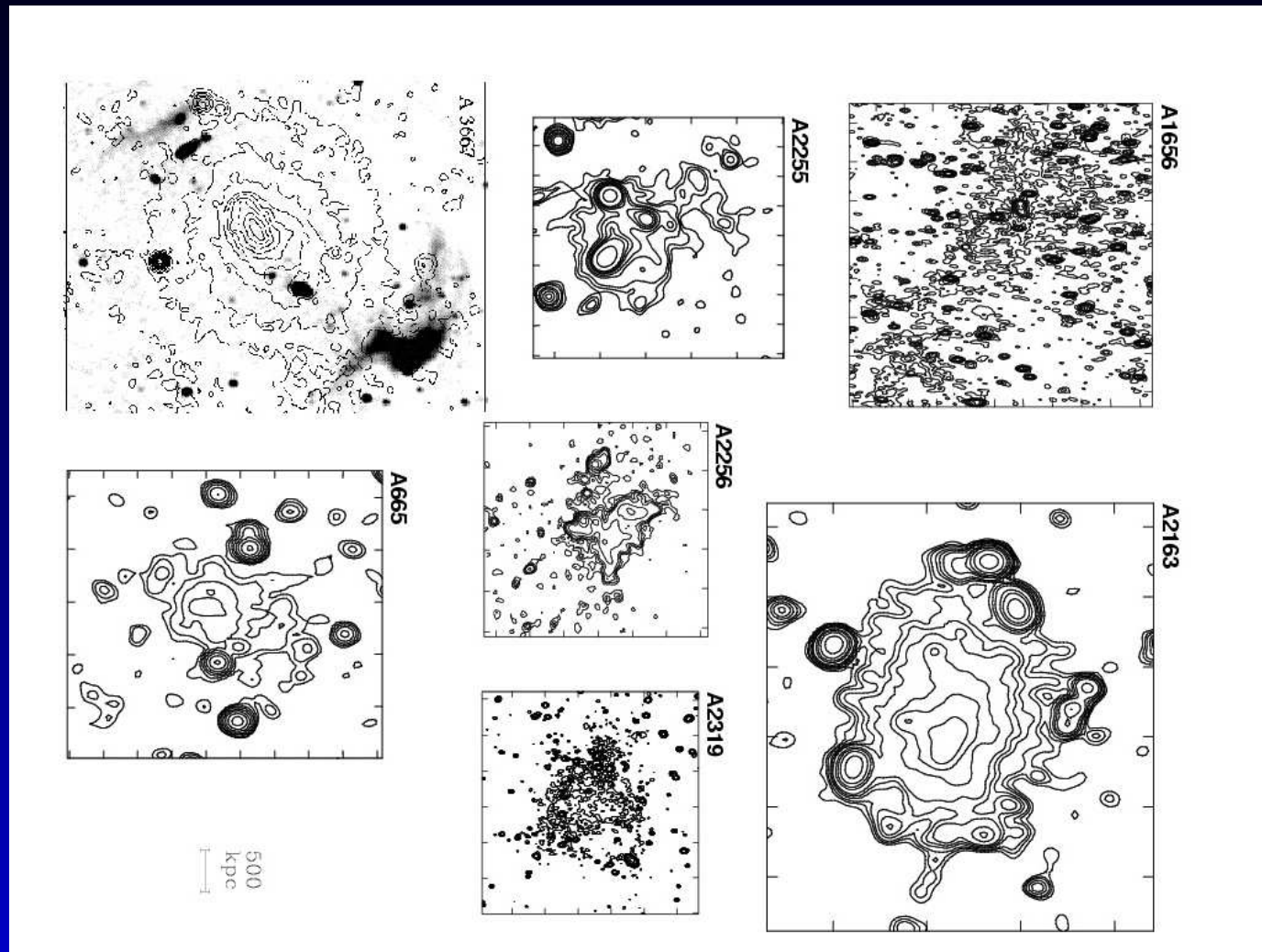
van Weeren et al. 2010



With of the relic suggest  $\vec{B} \approx 1\mu\text{G}$  or  $5 - 7\mu\text{G}$  !

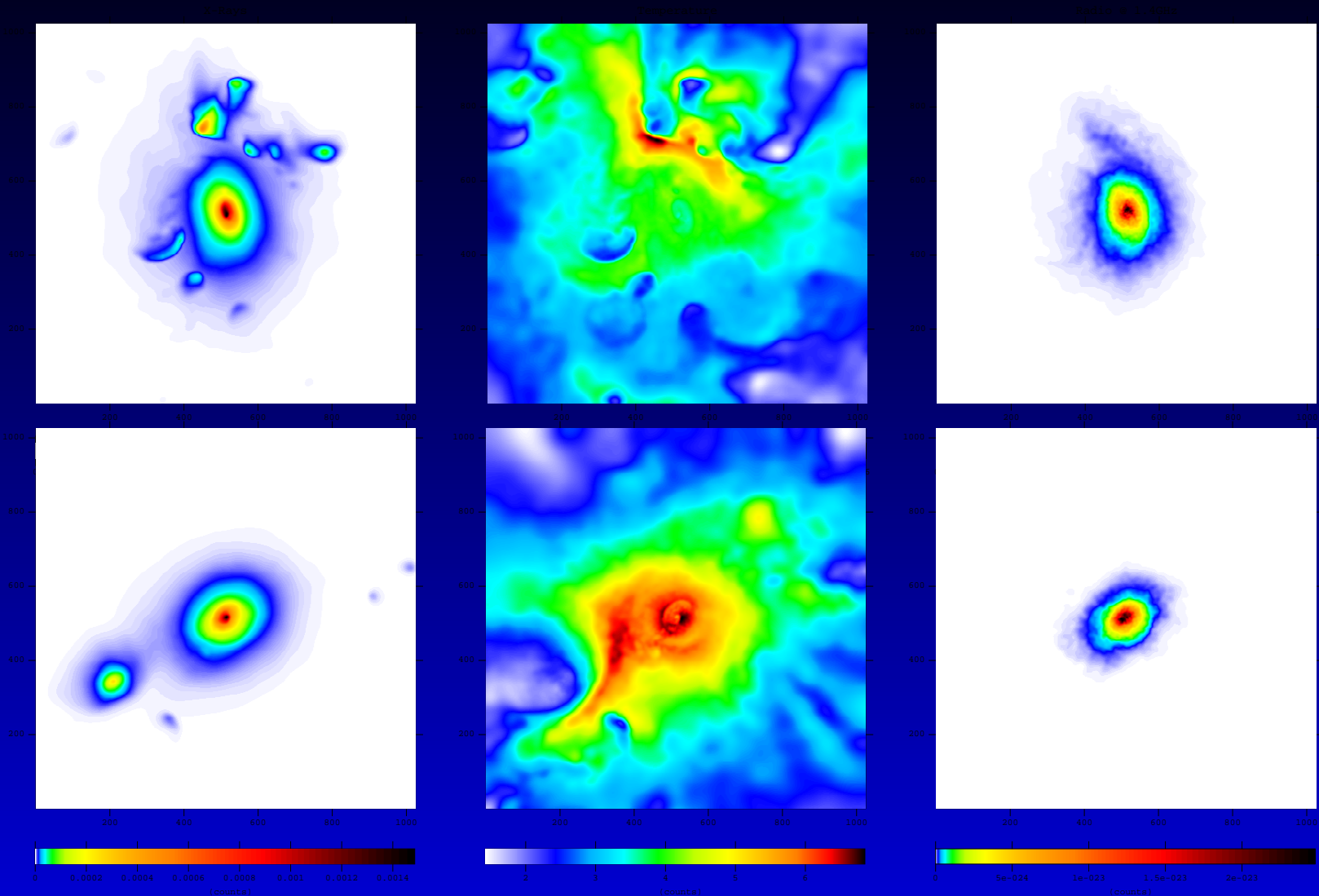


# Cluster Halos (hadronic)



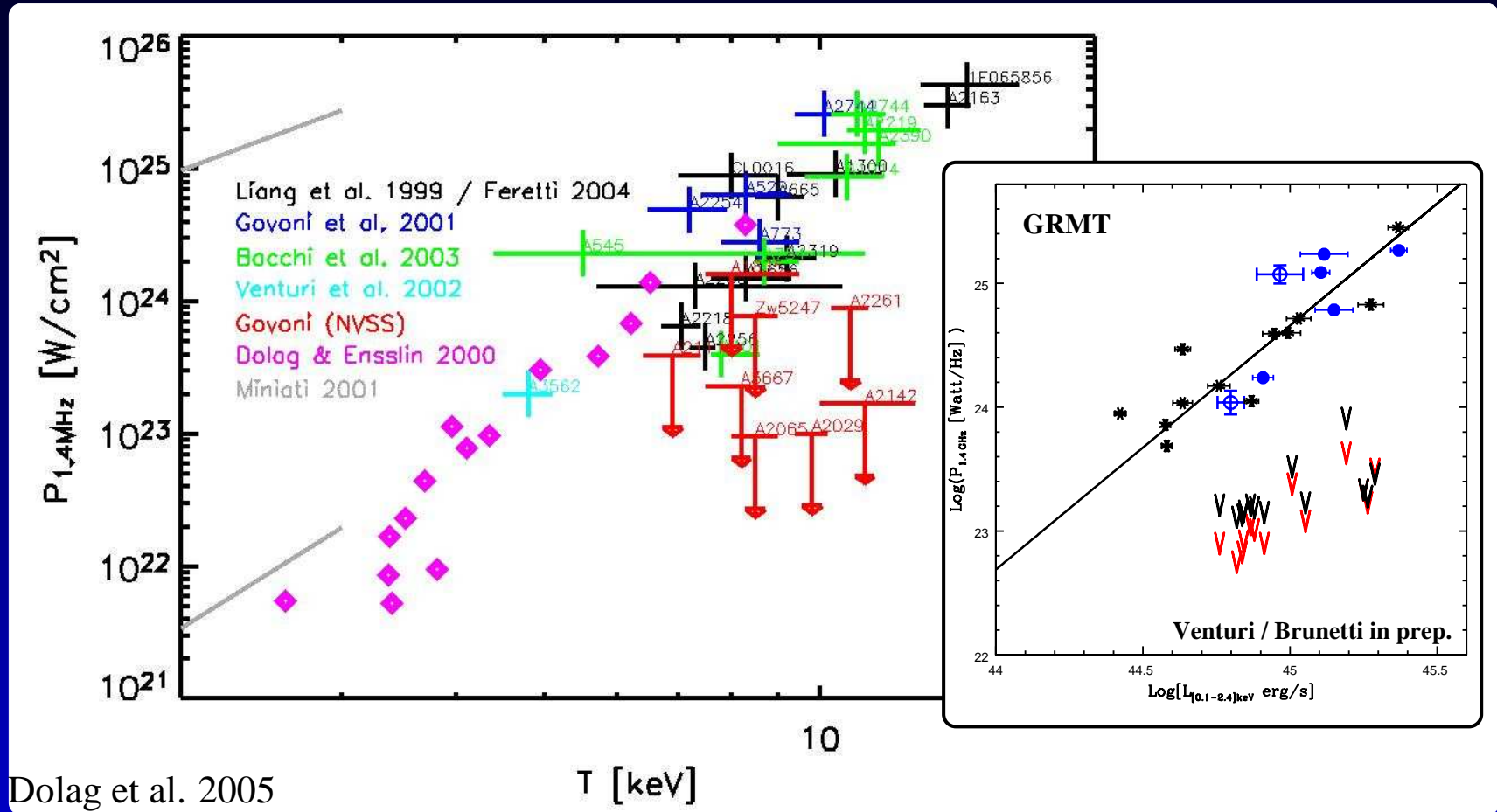
**Cluster wide diffuse synchrotron emission** (radio halos) of relativistic electrons in cluster magnetic fields. **Origin of relativistic electrons** (secondary, shocks, turbulence, ...) ?

# Cluster Halos (hadronic)



X-Ray (left), Temperature (middle) and Radio emission (right) from 2 simulated clusters. Radio emission is derived from **simple secondary model**, see Dolag & Ensslin 2000.

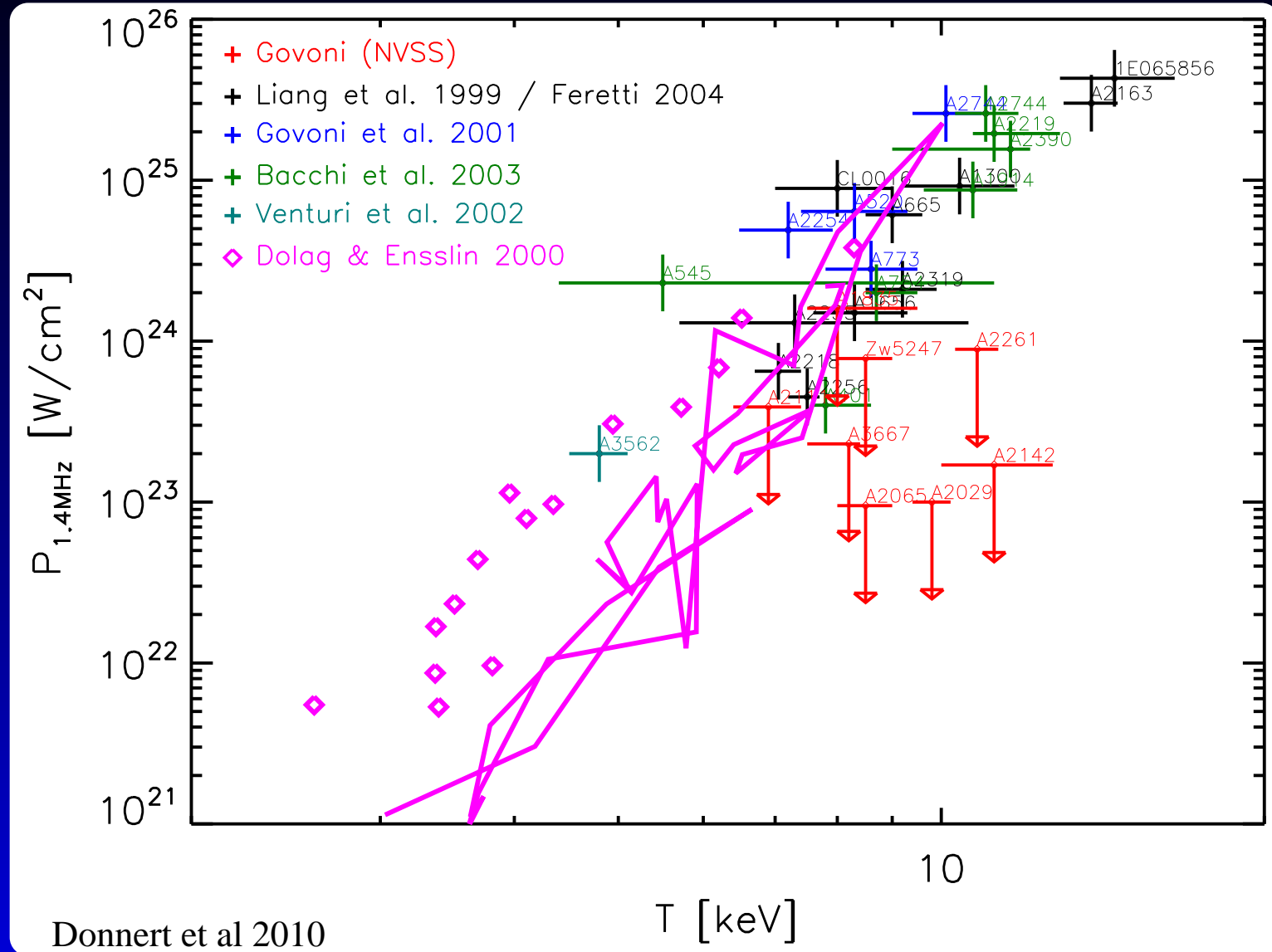
# Cluster Halos (hadronic)



Dolag et al. 2005

- Assuming energy fraction of  $\text{CR}p^+ \propto$  to thermal energy.
- Secondary ( $\text{CR}p^+ \rightarrow \pi^{\pm,0} \rightarrow e^-$ ) **predict correlation !**
- But **fail** to reproduce **probability !**

# Cluster Halos (hadronic)



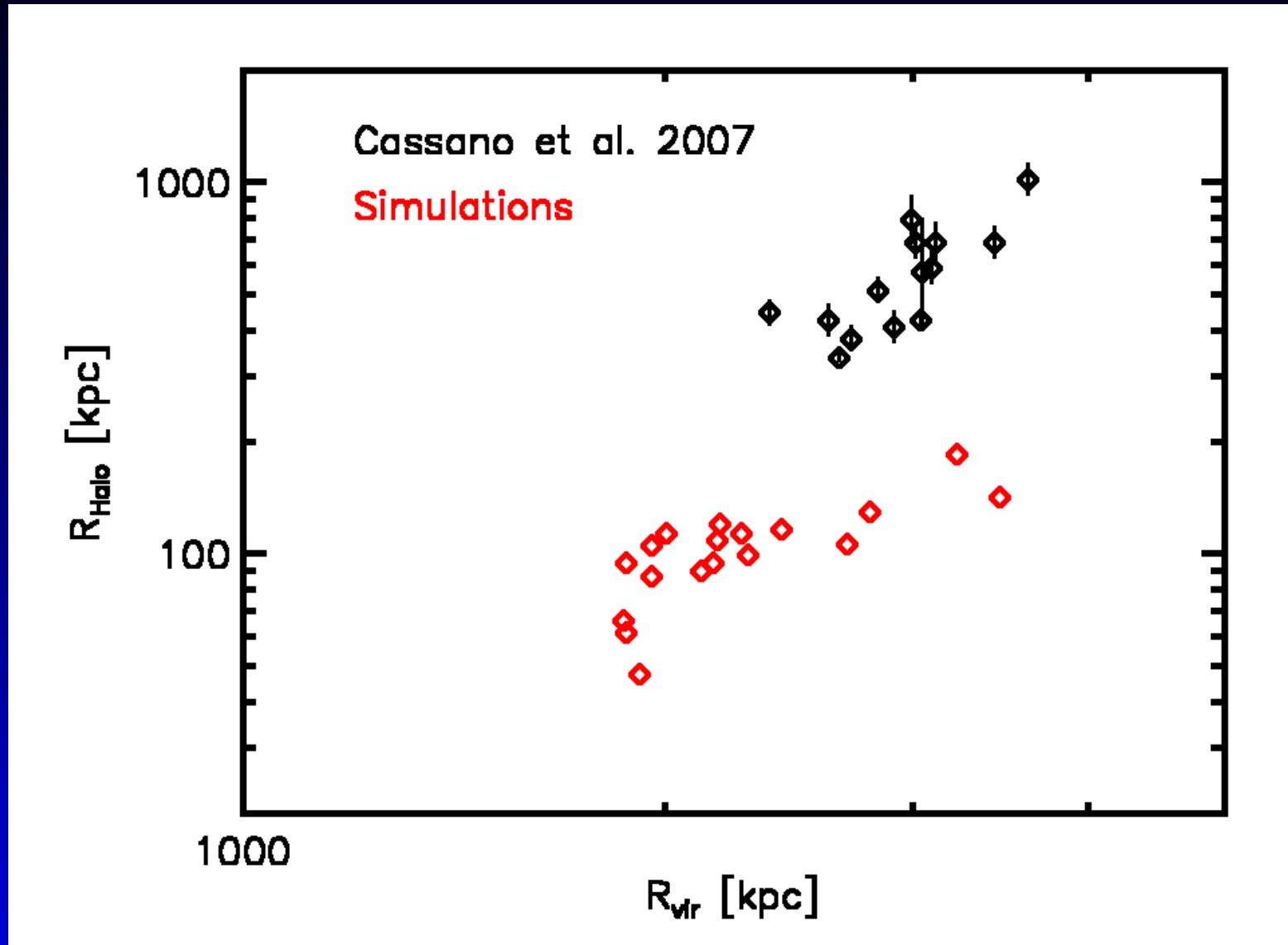
Evolution **track** relative **parallel** to correlation.

⇒ Strong dissipation of magnetic fields is needed for models.

⇒ Or strong diffusion for CRp needed !

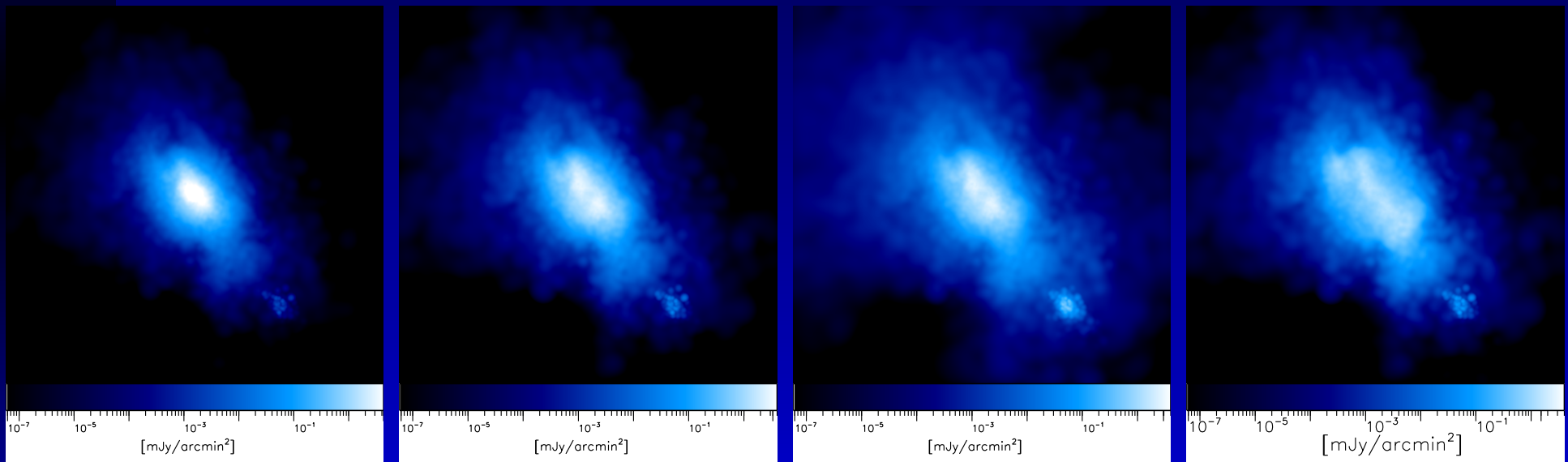
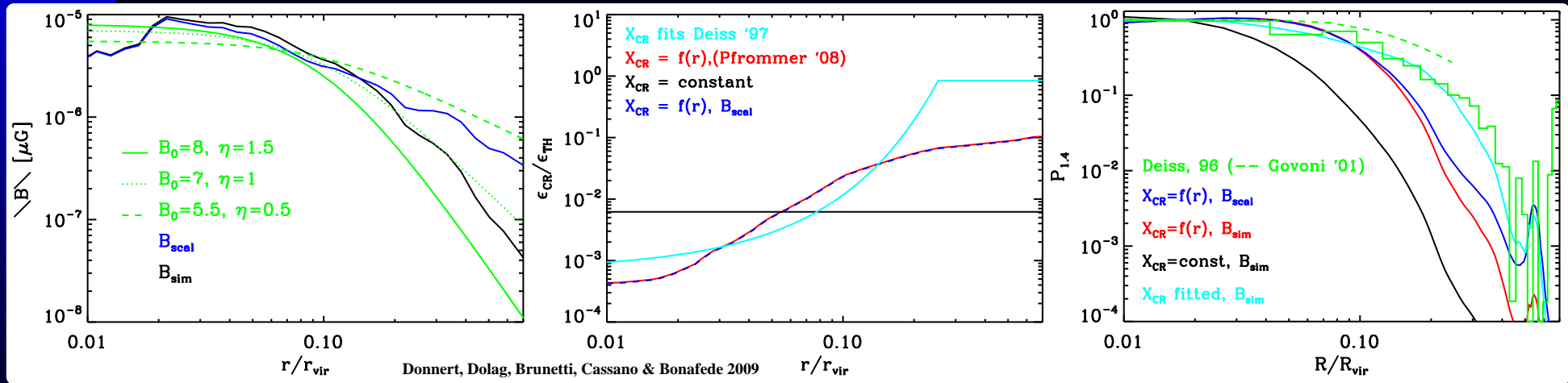


# Cluster Halos (hadronic)



Models also **fail** to predict the observed, **large extension** of the diffuse radio emission.

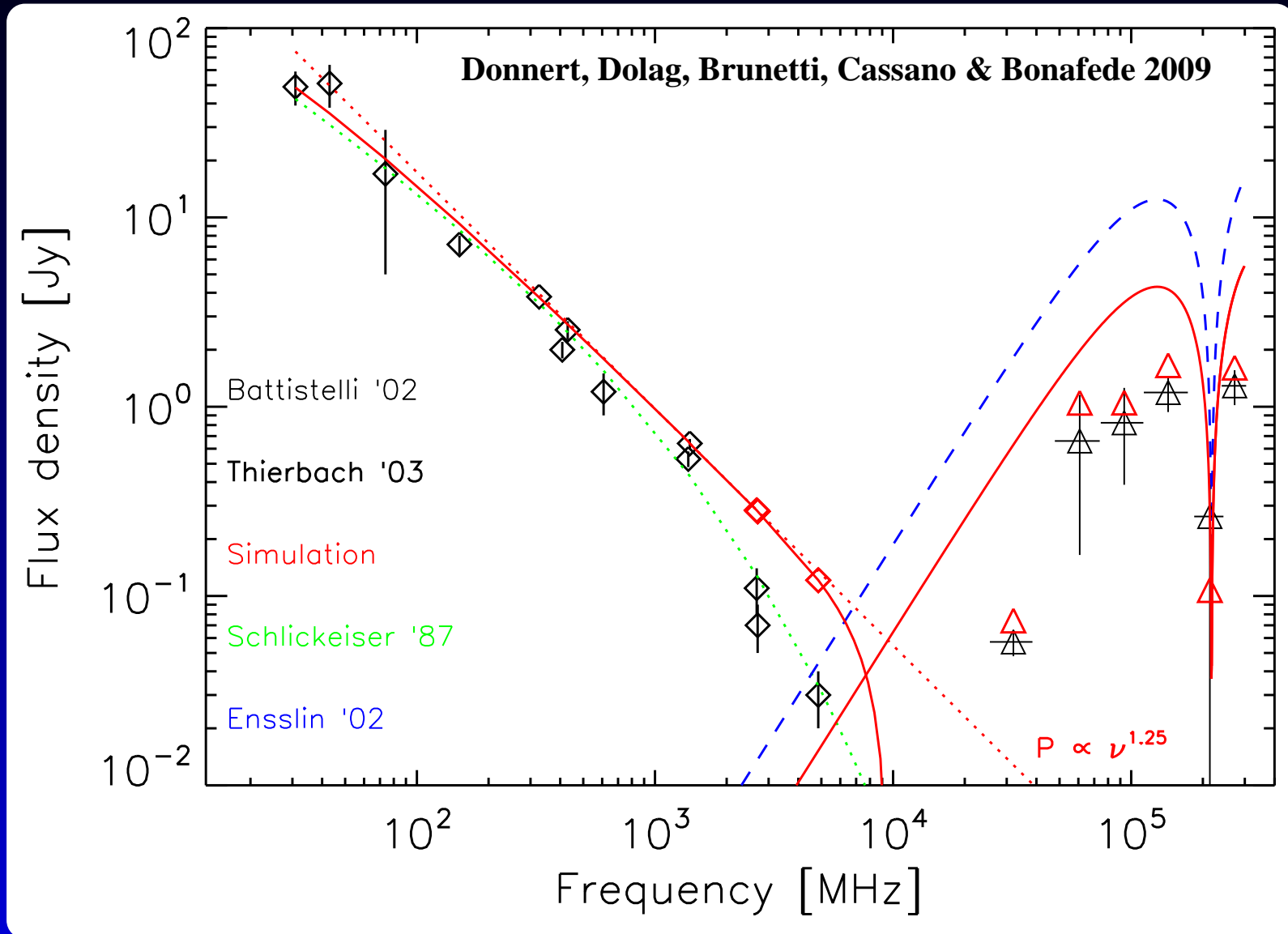
# Cluster Halos (hadronic)



Hadronic interactions of  $\text{CR-}p^+$  ( $>\text{GeV}$ ) with  $\text{ICM-}p^+$  will produce pions. The charged pions decay into secondary electrons producing synchrotron emission.

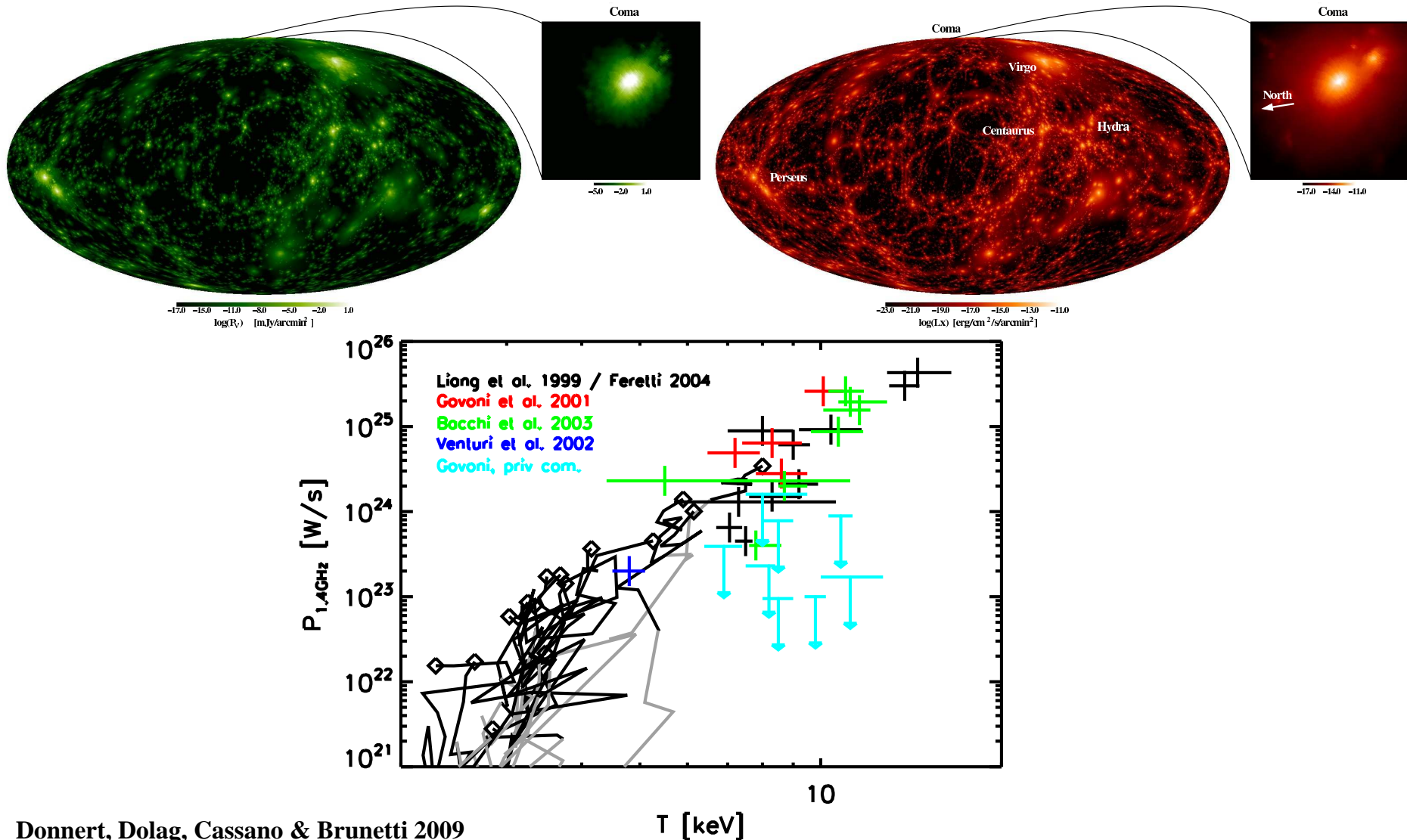
$\Rightarrow$  Radial **energy distribution** / emission **disfavors model** !

# Cluster Halos (hadronic)



CR- $p^+$  will have power law distribution  $\Rightarrow$  power law spectra,  
and negative SZ flux steepens spectra not enough  
 $\Rightarrow$  Sign of aging (e.g. **indicates primary** CR- $e^-$ )

# Cluster Halos (hadronic)



Donnert, Dolag, Cassano & Brunetti 2009

- Evolution track parallel to correlation
- ⇒ Strong evolution in CR- $e^-$  needed
- ⇒ Secondaries from CR- $p^+$  disfavored
- ⇒ Need to investigate **turbulent re-acceleration**



# Cluster Halos (turbulence)

⇒ Solve Fokker-Planck equation for CRe population

$$\frac{\partial n}{\partial t} = \frac{\partial}{\partial p} \left( D_{pp} \frac{\partial n}{\partial p} + H(p)n \right) - \frac{n}{T(t)} + Q(t)$$

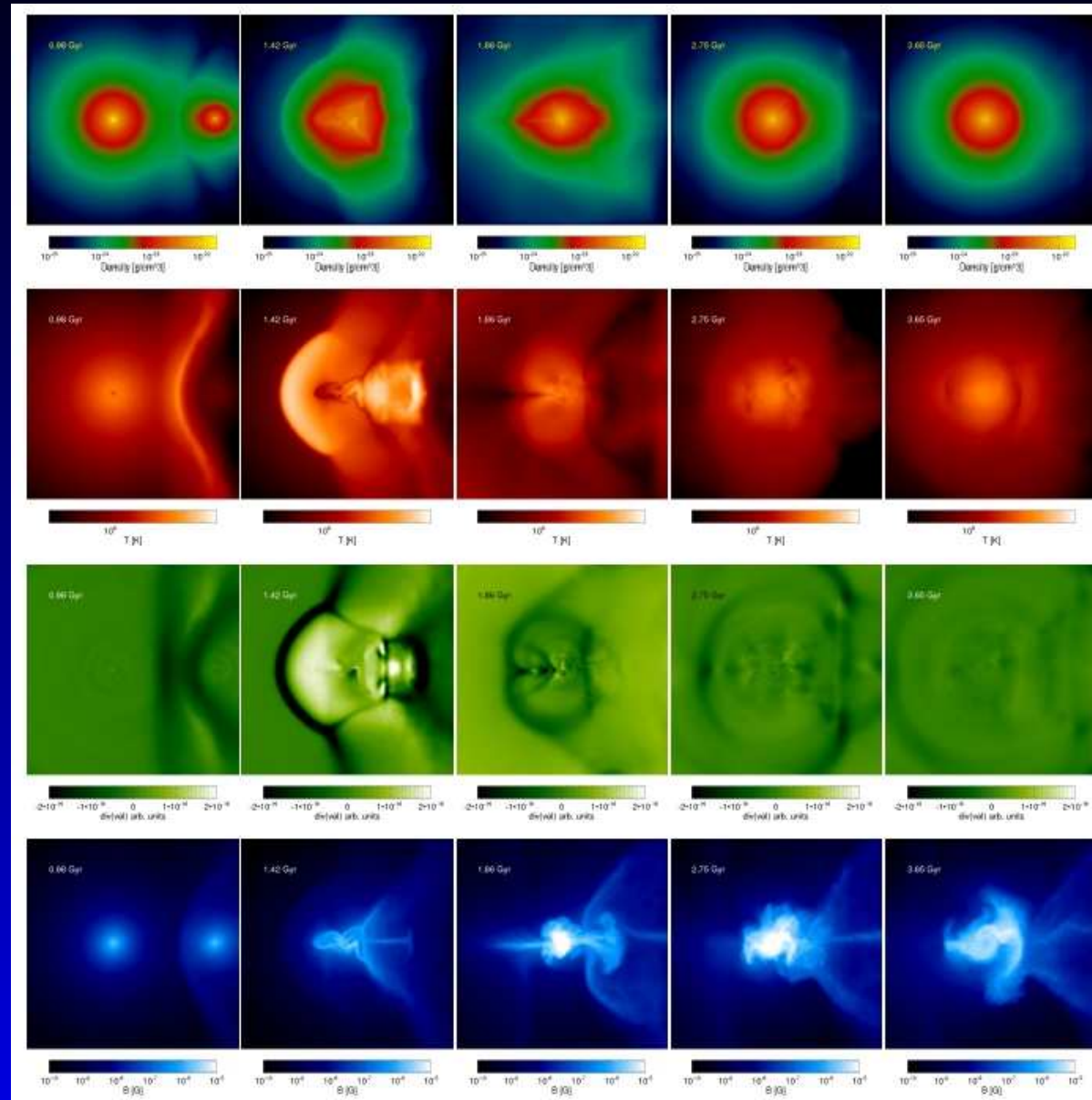
- 10% turbulent energy in fast mhd modes and reacceleration by those only
- Momentum Diffusion Coefficient

$$D_{pp} \propto v_{\text{turb}}^4 / h_{\text{sml}} / c_{\text{sound}}$$

- cooling with inverse compton, synchrotron and bremsstrahlung
- See also Cassano & Brunetti 05, Brunetti & Lazarian 2007
- 1% CRp as seed for CRe (hadronic background)

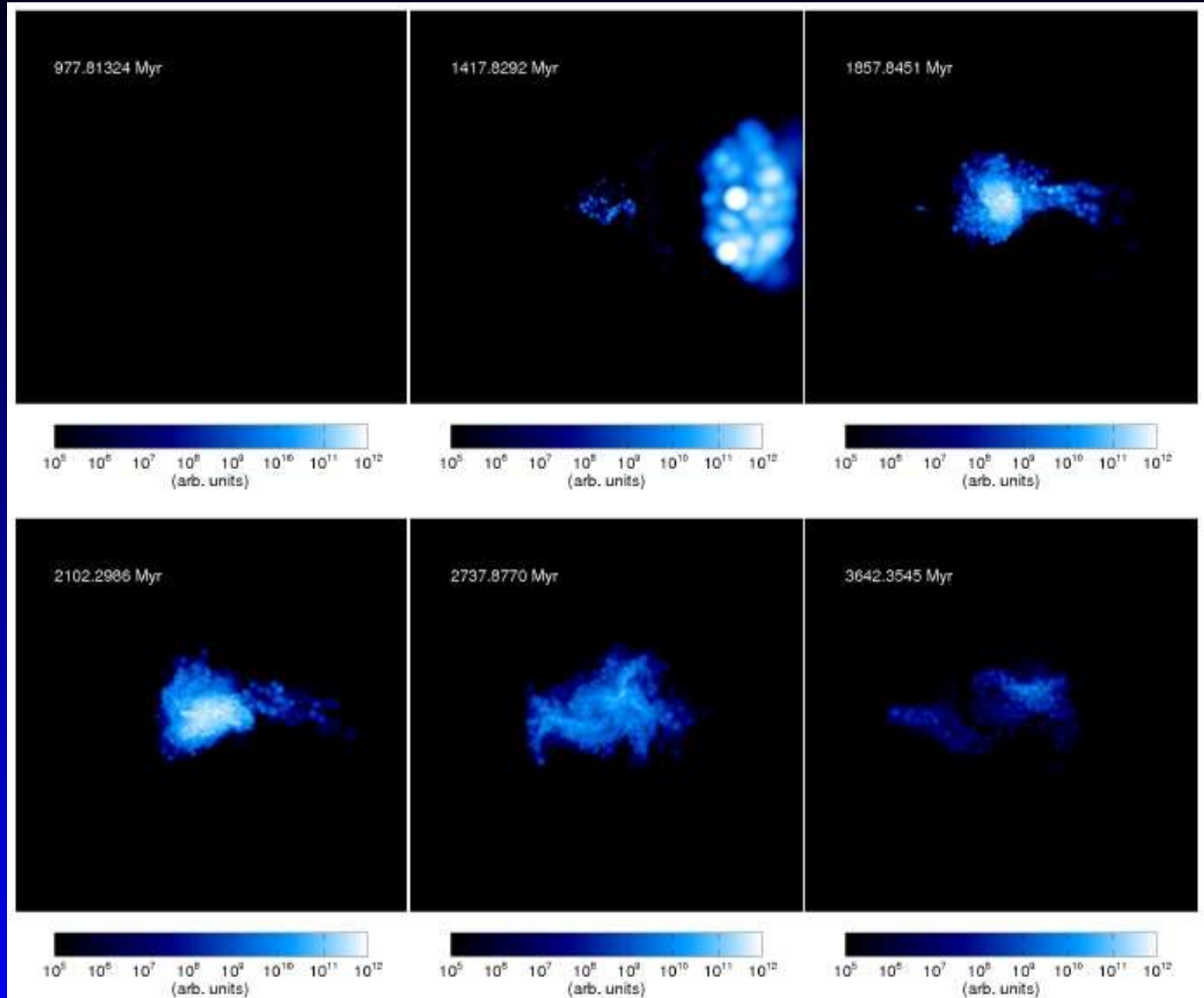
Donnert et al. 2012

# Cluster Halos (turbulence)



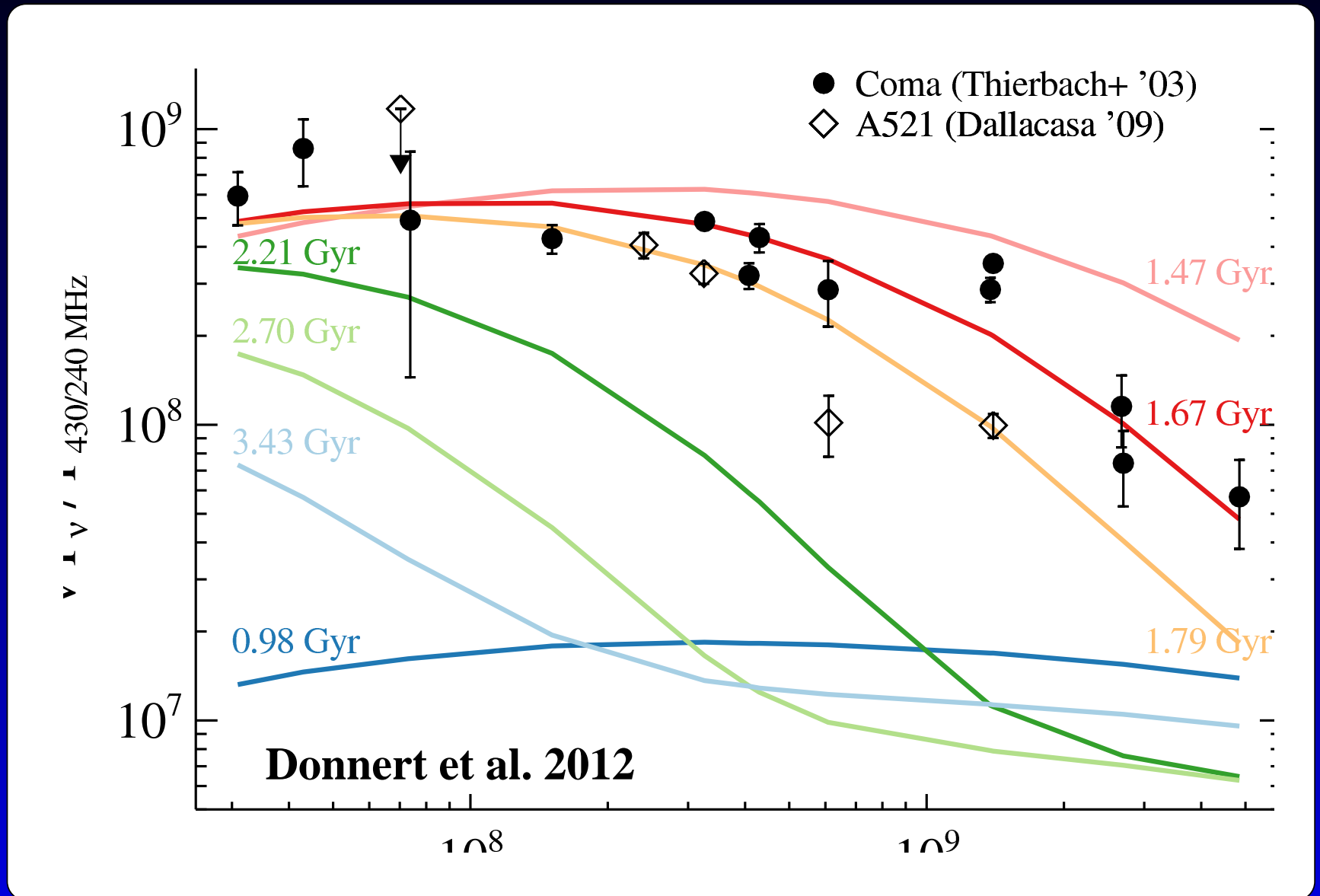
Idealized 1:4 merger, solving Fokker-Planck equation for all particles ( $2 \times 128^3$ ) (Donnert et al. 2012)

# Cluster Halos (turbulence)



Evolution of synthetic radio emission (Donnert et al. 2012)

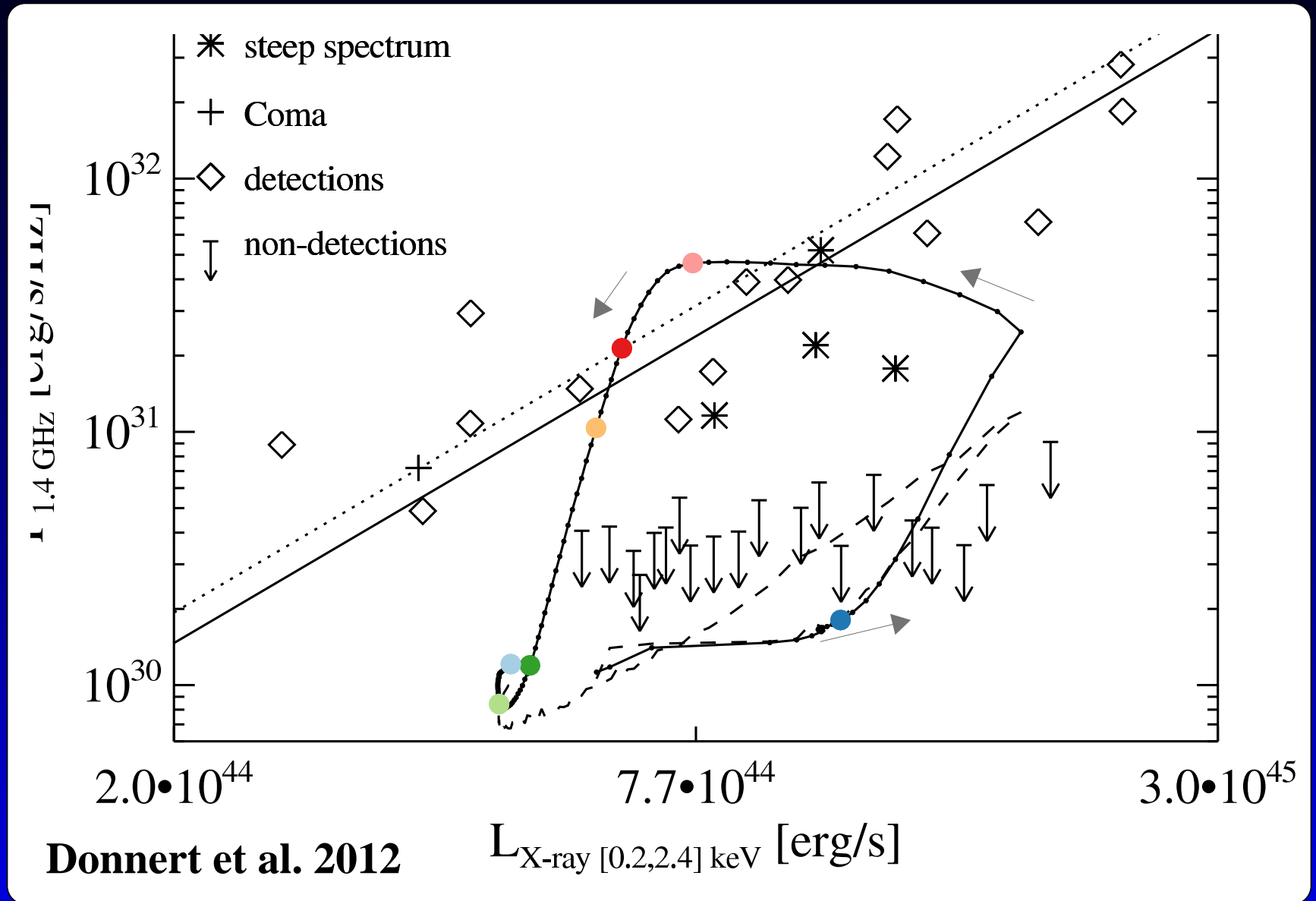
# Cluster Halos (turbulence)



Evolution of the spectrum of the radio emission (Donnert et al. 2012)

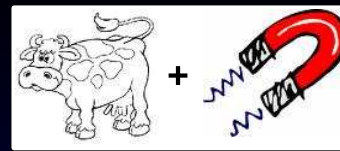


# Cluster Halos (turbulence)



Evolution of the  $L_x$ - $P_{1.4}$  relation (Donnert et al. 2012)

# Are we done ?



- *“Magnetic alignment in grazing and resting cattle and deer”*, Begall et al. 2008
- *“Extremely low-frequency electromagnetic fields disrupt magnetic alignment of ruminants”*, Burda et al. 2009
- *“No alignment of cattle along geomagnetic field lines found”*, Hert et al. 2011a
- *“Further support for the alignment of cattle along magnetic field lines: reply to Hert et al.”*, Begall et al. 2011
- *Authors’ response*, Hert et al. 2011b

**COW MAGNETS**

**What are Cow Magnets?**

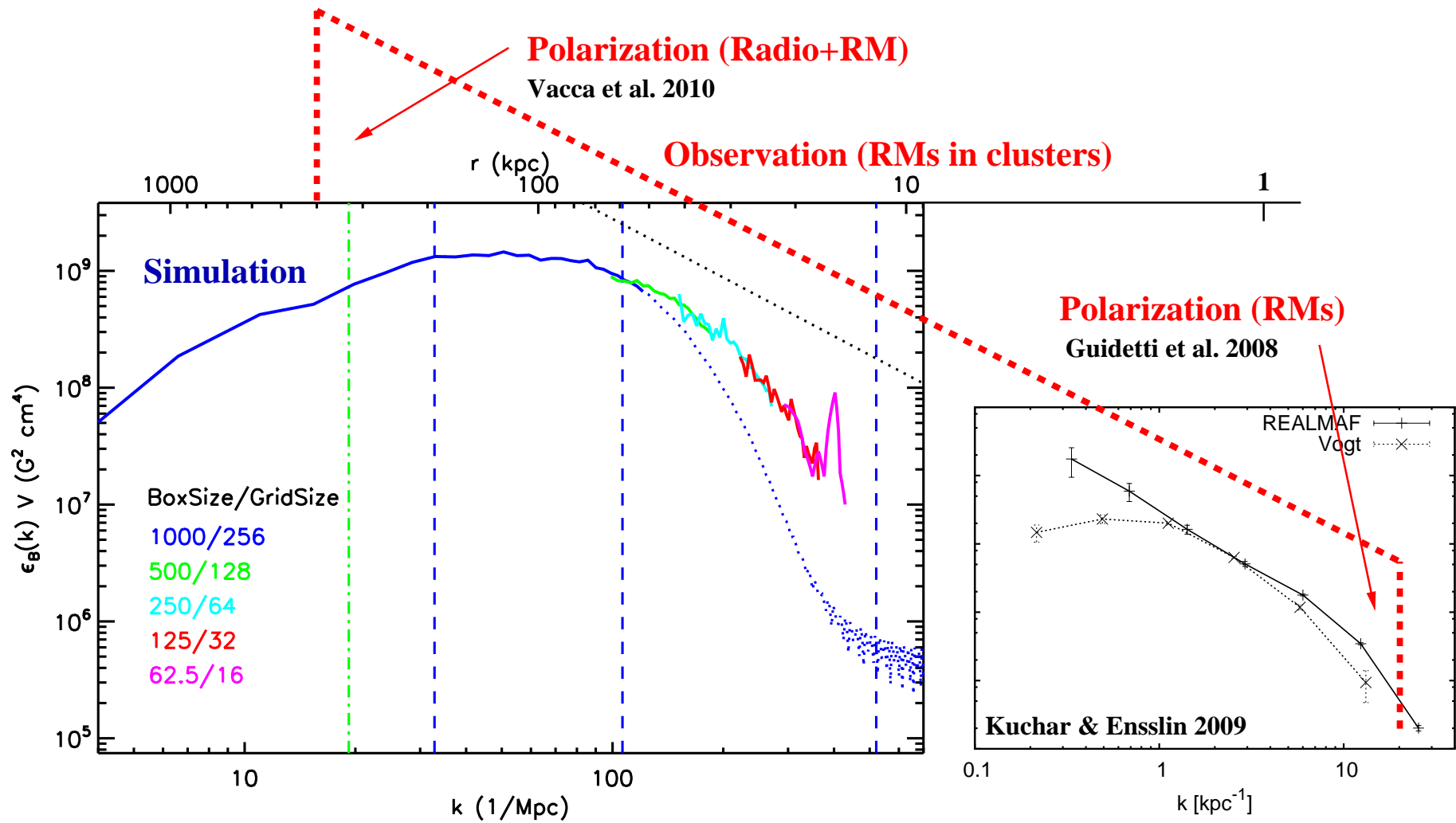
Cow magnets are popular with dairy farmers and veterinarians to help prevent Hardware Disease in cattle. While grazing, cows eat everything from grass and dirt to nails, staples and bits of baling wire (referred to as tramp iron). Tramp iron tends to lodge in the honeycombed walls of the reticulum, threatening the surrounding vital organs and causing irritation and inflammation, known as Hardware Disease. The cow loses her appetite and decreases milk output (dairy cows), or her ability to gain weight (feeder stock). Cow magnets help prevent this disease by attracting stray metal from the folds and crevices of the rumen and reticulum. One magnet works for the life of the cow!

**[Purchase Cow Magnets at Our Online Store.](#)**

A grey silhouette of a cow. A blue speech bubble points to the cow's stomach area, containing a black and white striped cylindrical cow magnet.

- **Science for Europe** (US farmers feed cow magnets to their cattle)

# Summary (I)



- Measurement of magnetic field power spectra
- Clear indication of magnetic field topology
- Indications for minimum/maximum length scale

# Summary (2)

## Radio Relics:

- Diffuse, periferal emission
- Related to shocks from mergers
- Spectral index relates to Mach number
- Polarization indicates magnetic field alignment
- Width of emission region constrains  $\vec{B}$

## Radio Halos:

- Diffuse, central emission
- Related to merger events
- Morphology related to thermal gas
- Secondary model disfavored
- Most likely driven by turbulent re-acceleration