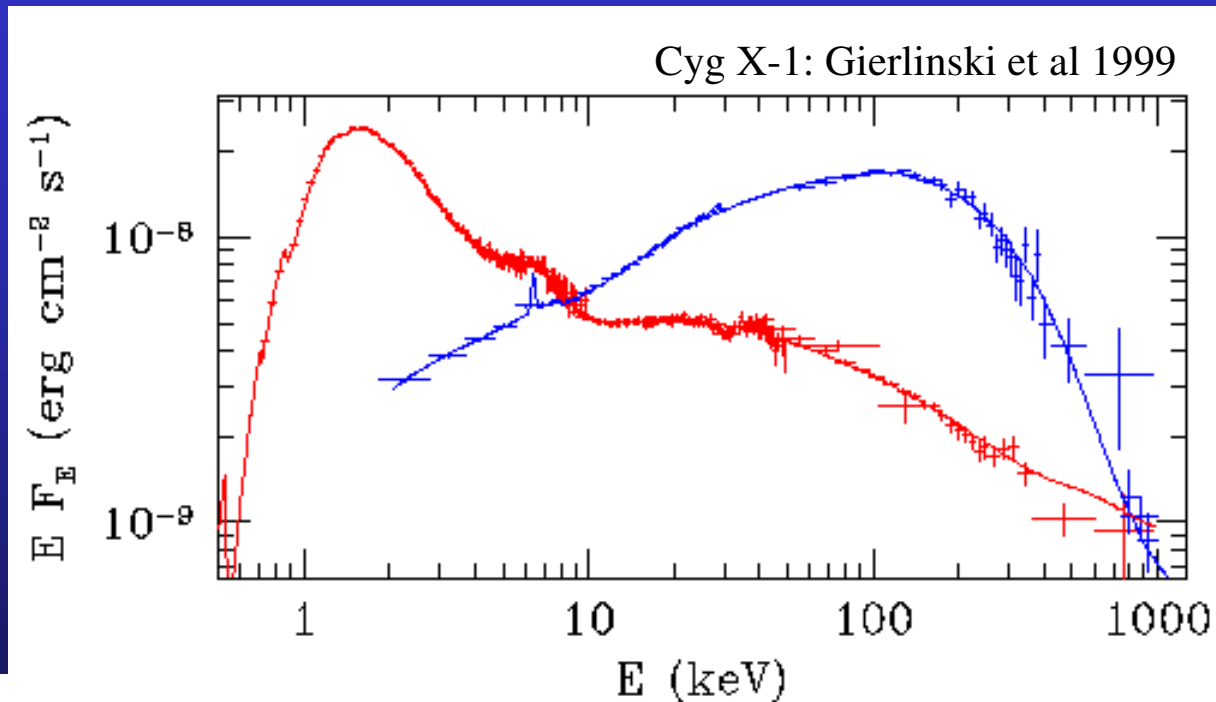


How to make high energy spectra!

Chris Done
University of Durham

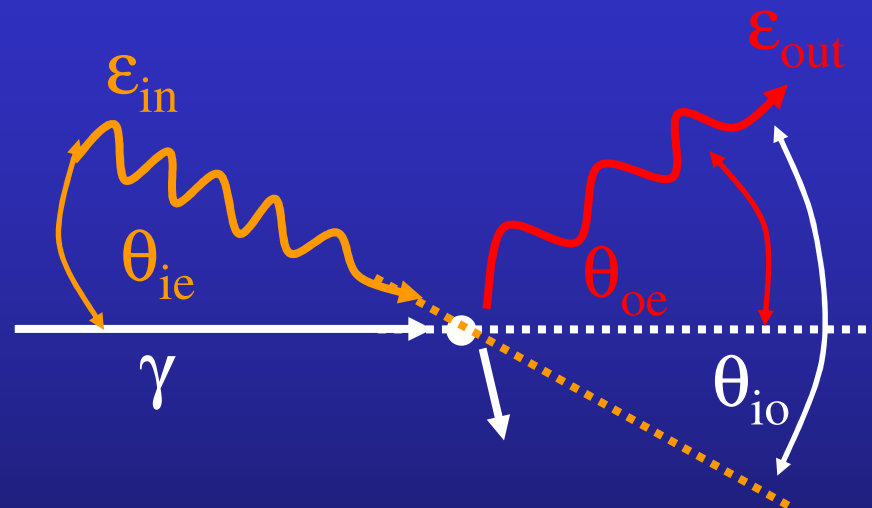
Observations



- Low state spectra peak at 100 keV. Well modelled by thermal electron distribution
- High state spectra need predominantly non-thermal electron distribution

Compton scattering theory

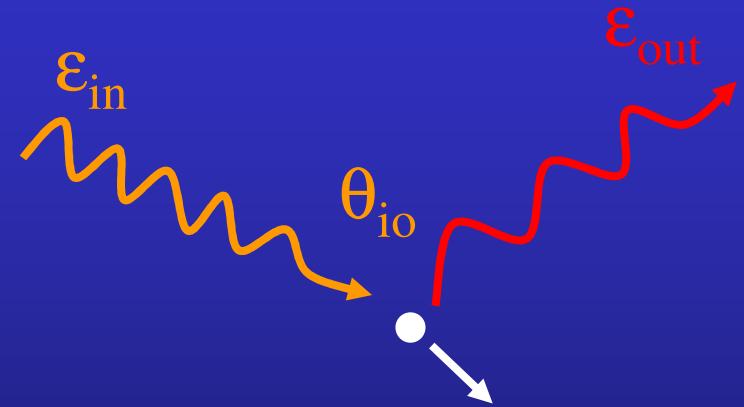
- Collision – redistribute energy
- If photon has more energy than electron then it loses energy – downscattering
- If photon has less energy than electron then it gains energy – upscattering
- Easiest to talk about if scale energies to mc^2 so electron energy γmc^2 just denoted γ while photon energy becomes $\epsilon = h\nu/mc^2 = E/511$ for E (keV)



$$\epsilon_{out} = \frac{\epsilon_{in}(1 - \beta \cos \theta_{ei})}{1 - \beta \cos \theta_{eo} + (\epsilon_{in}/\gamma)(1 - \cos \theta_{io})}$$

Downscattering: electron at rest

- Always downscatter in electron rest frame as electron must recoil from collision
- Rest frame so $\beta=0$, $\gamma=1$,
- Lose very little energy for $\epsilon_{\text{in}} \ll 1$ $\epsilon_{\text{out}} \approx \epsilon_{\text{in}}(1 - \epsilon_{\text{in}})$
- Lose almost all energy for $\epsilon_{\text{in}} \gg 1$ $\epsilon_{\text{out}} \sim 1$

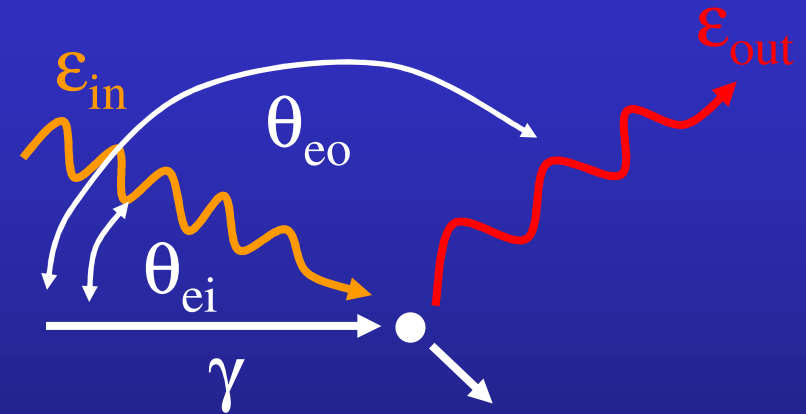


$$\epsilon_{\text{out}} \sim \frac{\epsilon_{\text{in}}}{1 + \epsilon_{\text{in}} (1 - \cos\theta_{\text{io}})}$$

Thermal compton upscattering:

- If $\epsilon_{in} \ll \Theta$ then electron has most energy so loses it to photon
- Average over angle for isotropic electron and photon distribution.
- Integrate over Maxwellian distribution of γ to get :
$$\epsilon_{out} = (1 + 4\Theta + 16\Theta^2) \epsilon_{in}$$

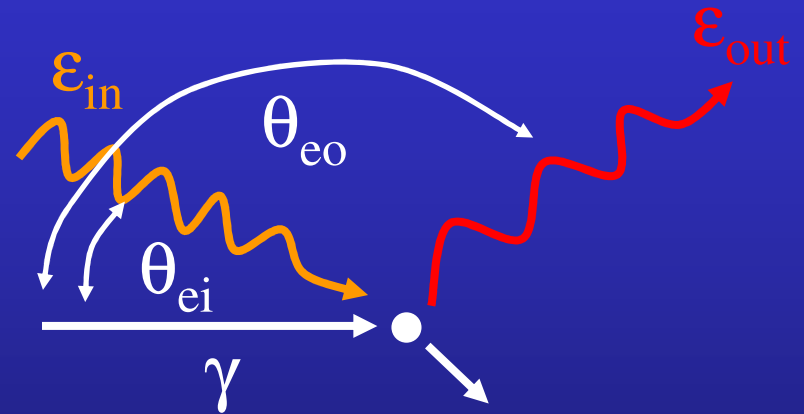
where $\Theta = kT_e/mc^2$



$$\epsilon_{out} \sim \frac{\epsilon_{in}(1 - \beta \cos \theta_{ei})}{1 - \beta \cos \theta_{eo}}$$

Limits

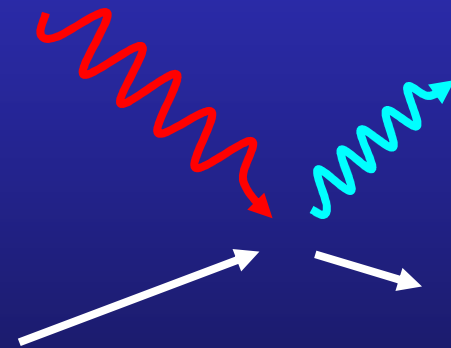
- Can't get more energy out than put in: $\epsilon_{\text{out}} < \epsilon_{\text{in}} + \gamma$
- If upscattering then just reach electron energy limit so for thermal $\epsilon_{\text{out}} \sim 3\Theta$



$$\epsilon_{\text{out}} \sim 3\Theta$$

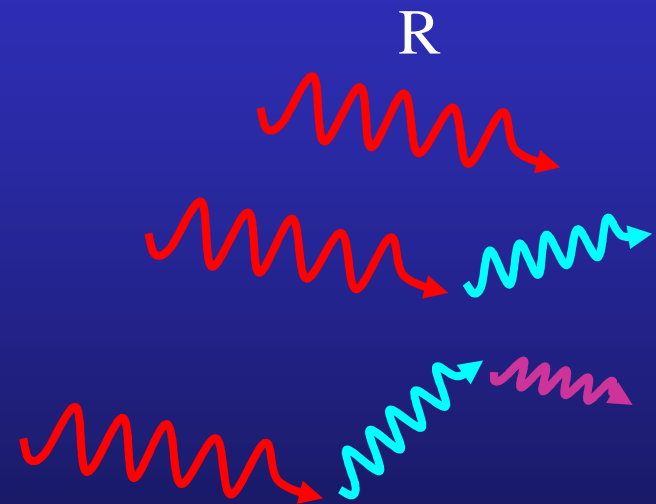
How much scattering ?

- Compton scattering seed photons from accretion disk. Photon energy boosted by factor $\Delta\epsilon/\epsilon \sim 4\Theta + 16\Theta^2$ if thermal in each scattering.



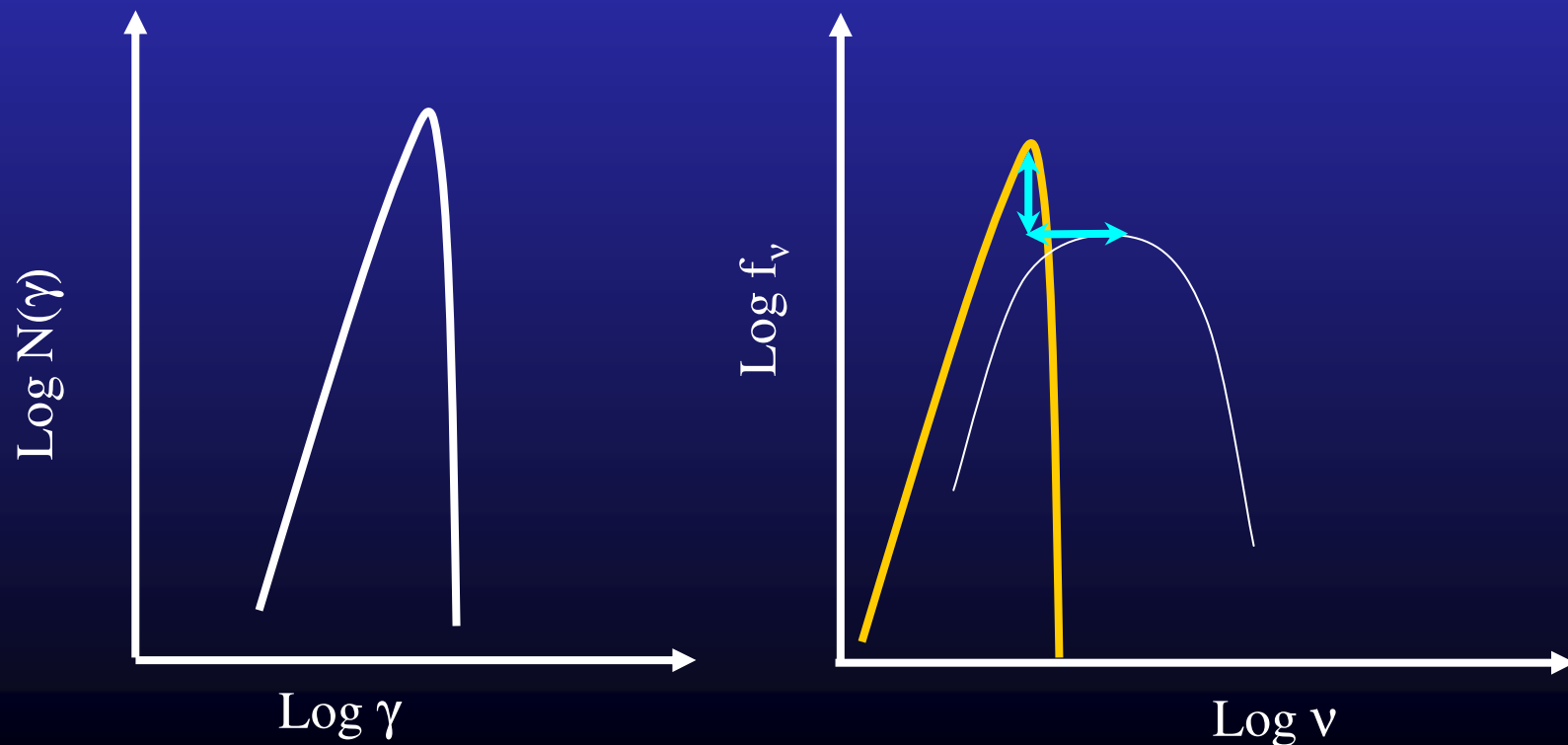
How much scattering ?

- Number of times scattered given by optical depth, $\tau = \sigma n R$
- Scattering probability $\exp(-\tau)$
- Optically thin $\tau \ll 1$ prob $\sim \tau$
average number $\sim \tau$
- Optically thick $\tau \gg 1$ prob ~ 1
and average number $\sim \tau^2$
- Total fractional energy gain =
frac.gain in 1 scatt x no.scatt
- Compton $y = (4\Theta + 16\Theta^2) (\tau + \tau^2)$
 $\sim 4\Theta\tau^2$ for $\Theta < 1$ $\tau > 1$



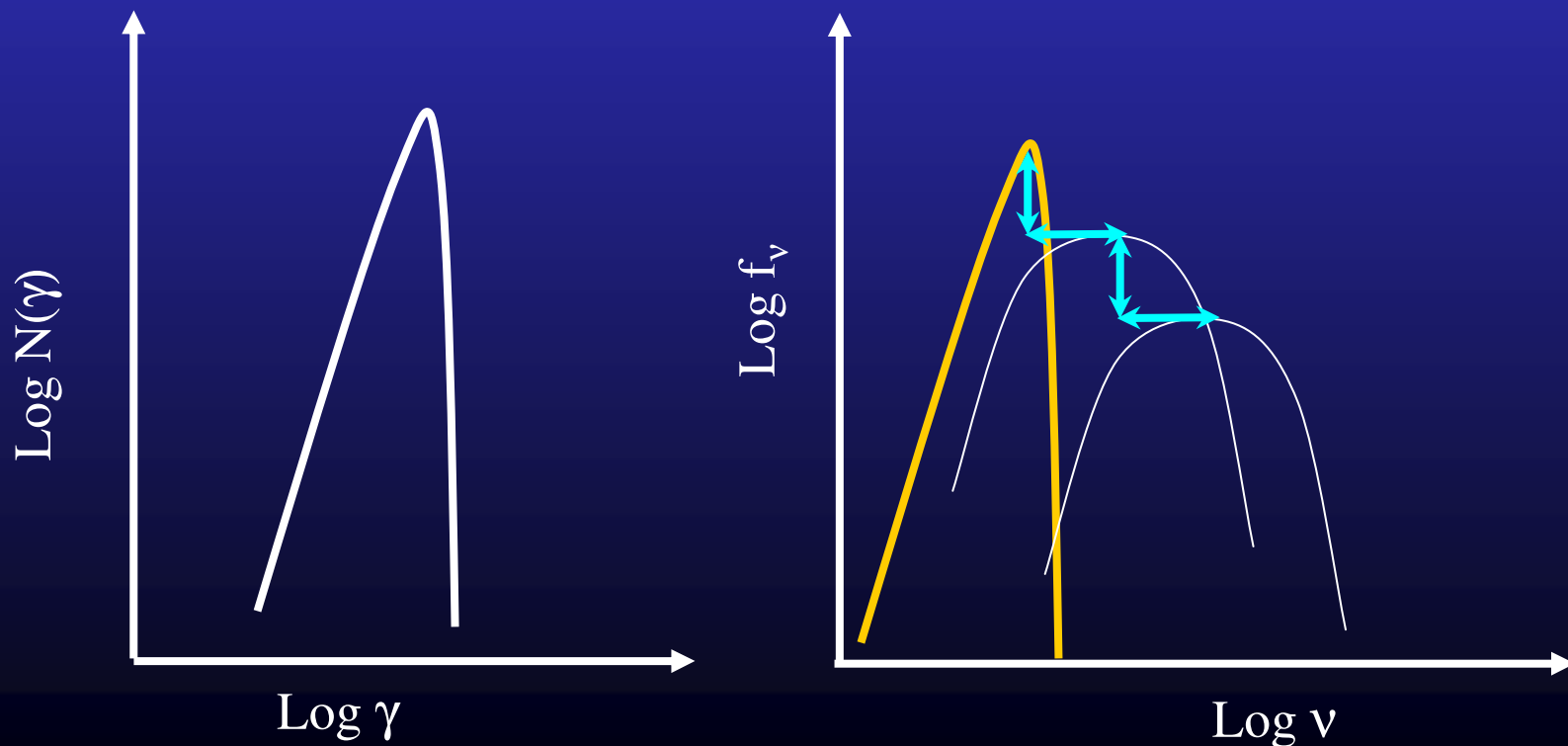
Optically thin thermal compton

- power law by multiple scattering of thermal electrons
- Number of photons $dN/dE dE = E dN/dE d\text{Log } E = f(\epsilon) d\log \epsilon \propto \epsilon^{-\alpha}$
- For $\tau < 1$ scatter τ photons each time to energy $\epsilon_{\text{out}} = (1 + 4\Theta + 16\Theta^2)\epsilon_{\text{in}}$
- index $\alpha = \log(\text{prob}) / \log(\text{energy boost}) \sim -\log \tau / \log (1 + 4\Theta + 16\Theta^2)$



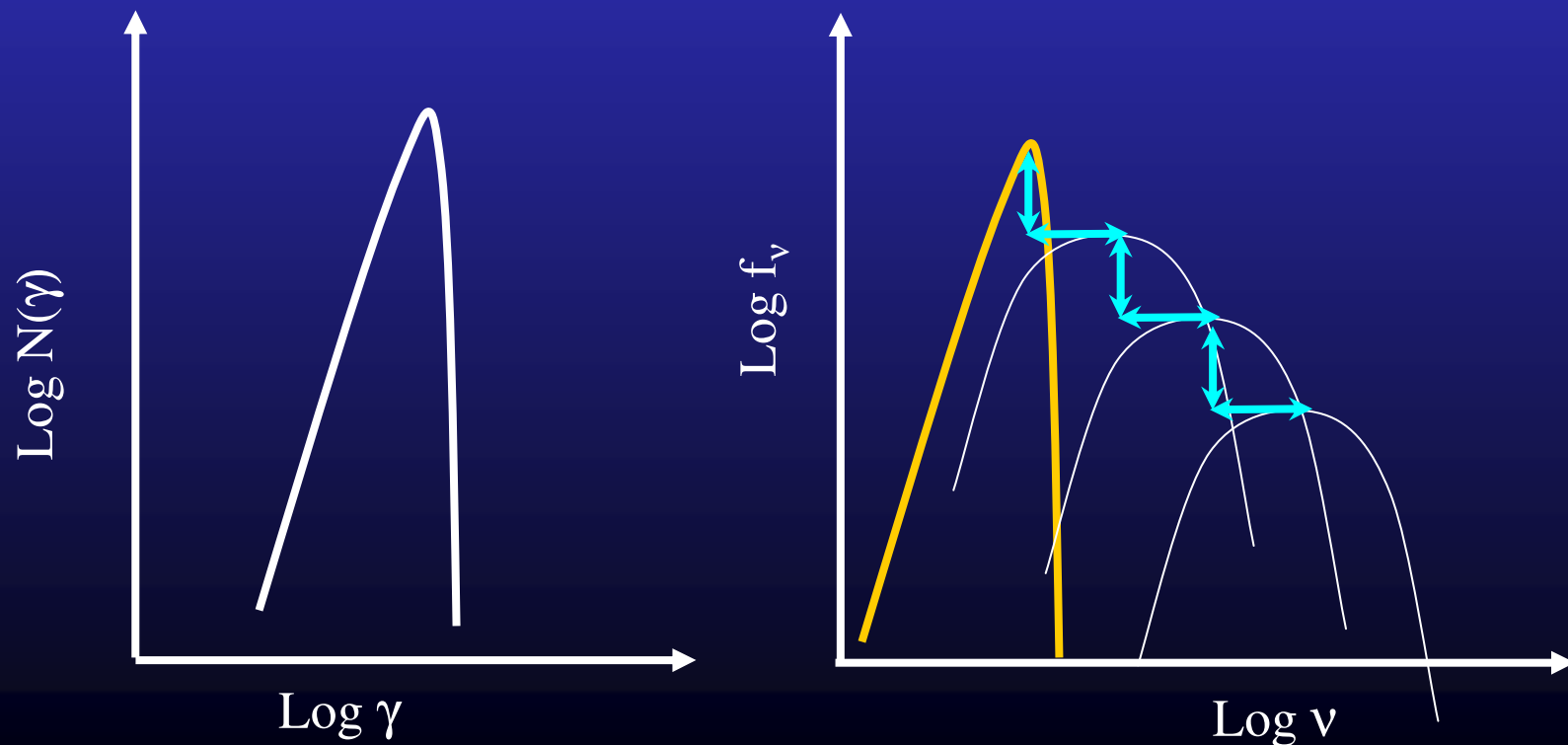
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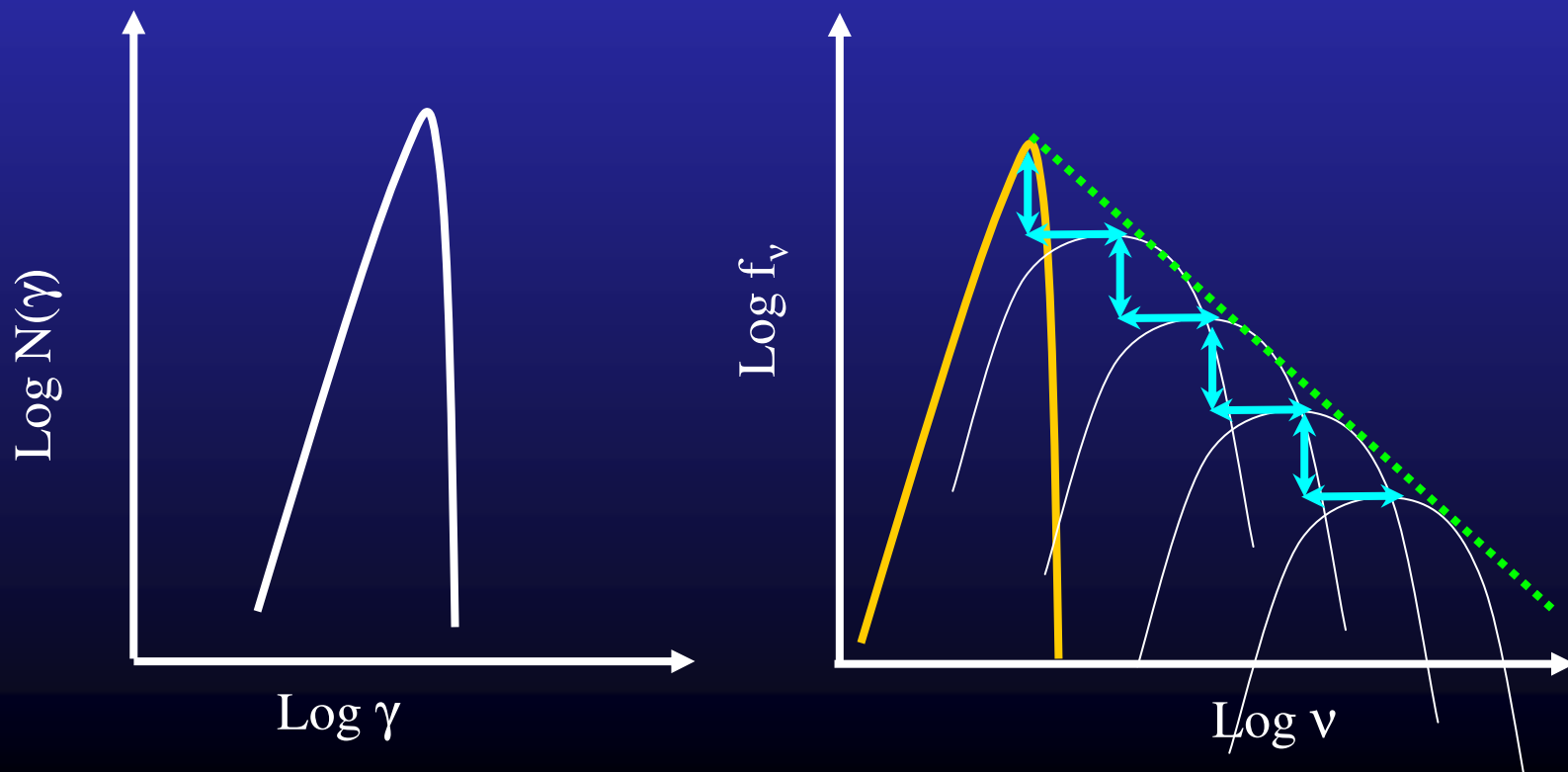
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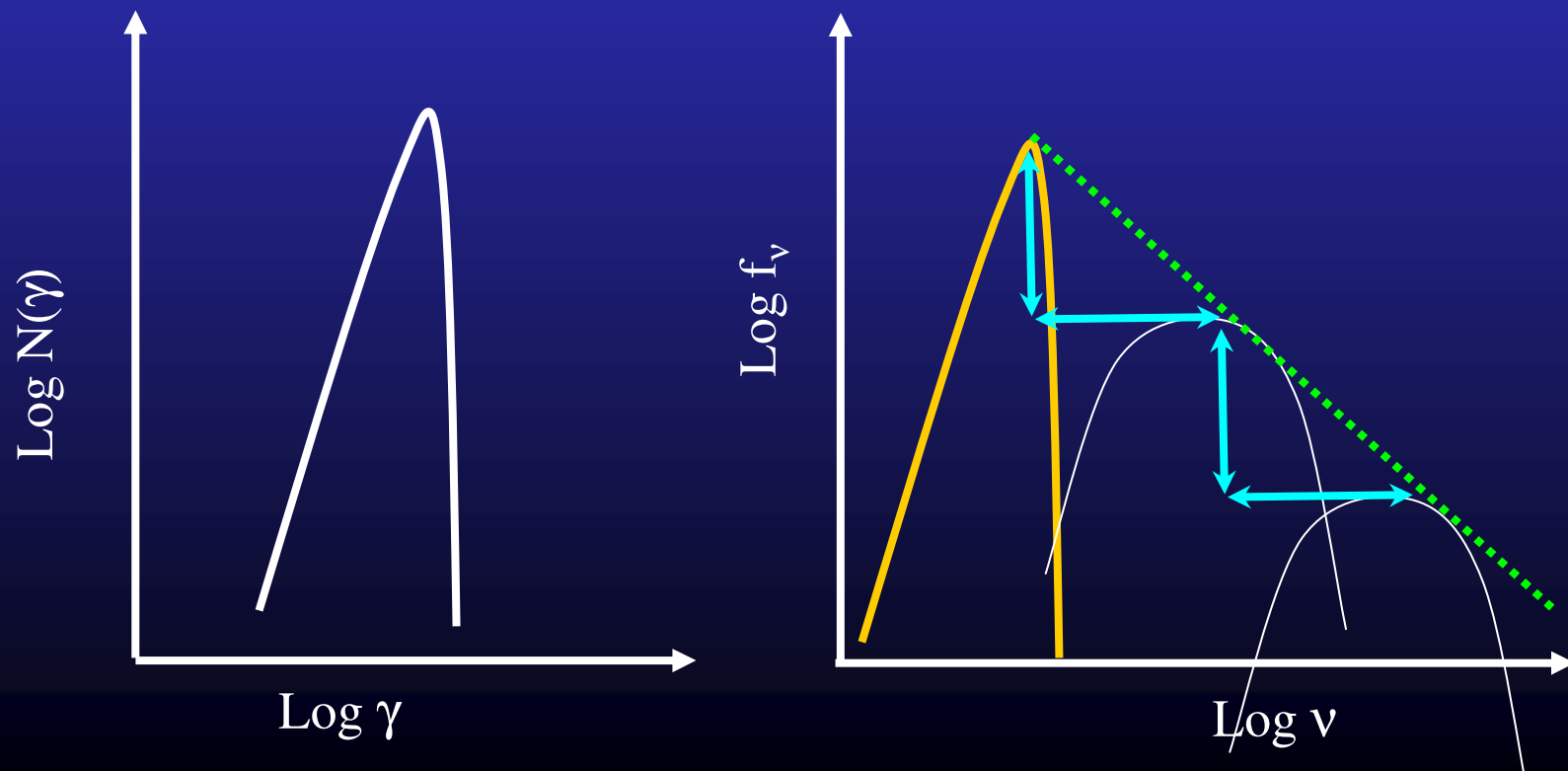
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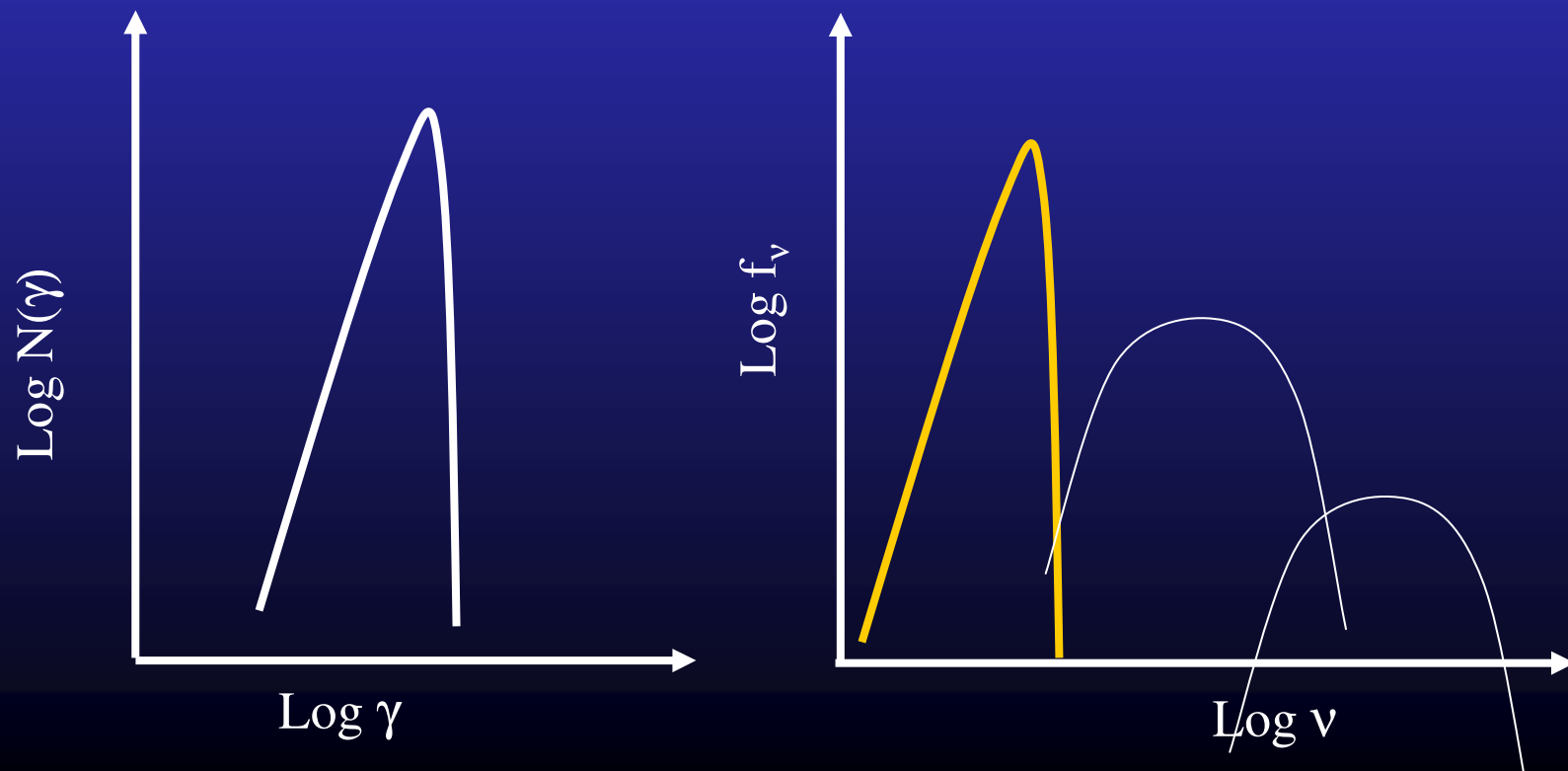
Optically thin thermal compton

- index $\alpha = \log(\text{prob}) / \log(\text{energy boost}) \sim -\log \tau / \log(1 + 4\Theta + 16\Theta^2)$
- Same index for lower τ higher Θ
- BUT BUMPY spectrum if $\tau \ll 1$



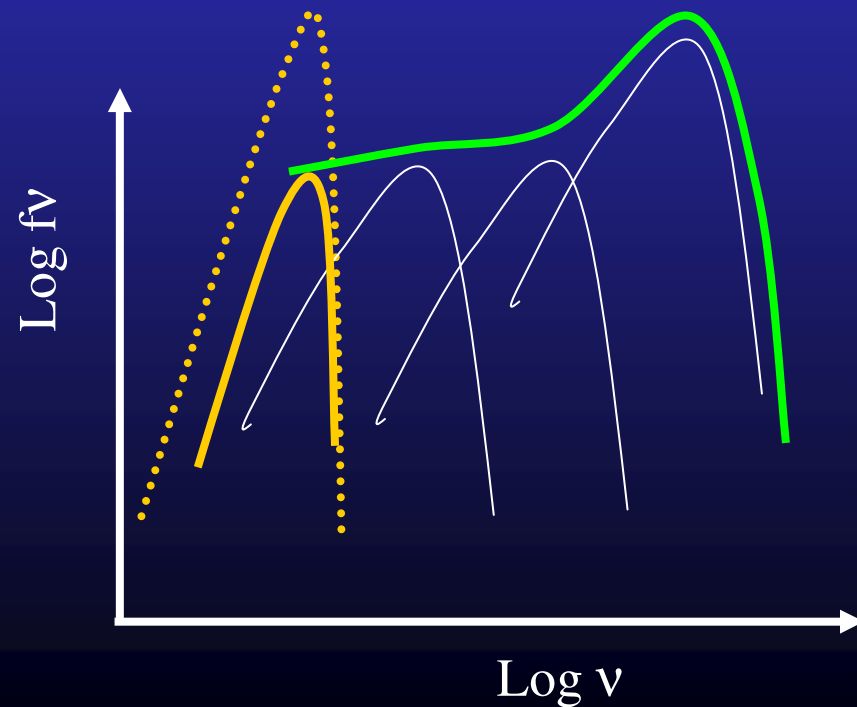
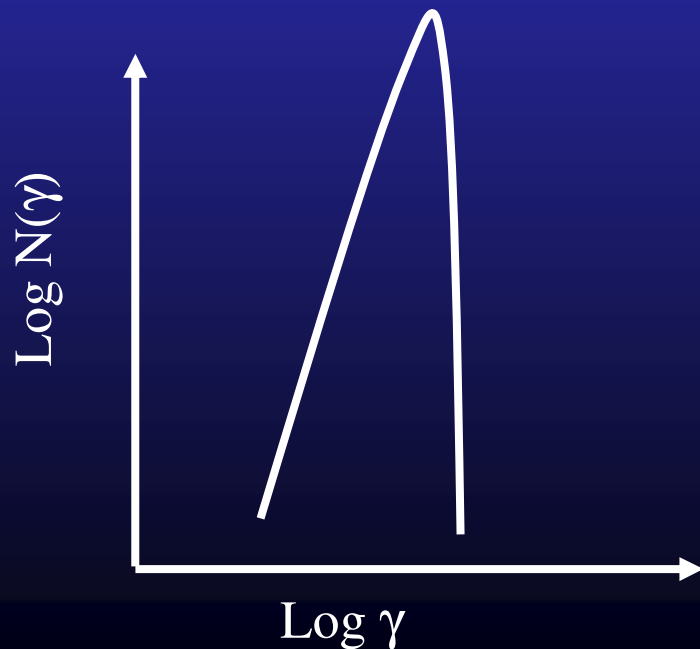
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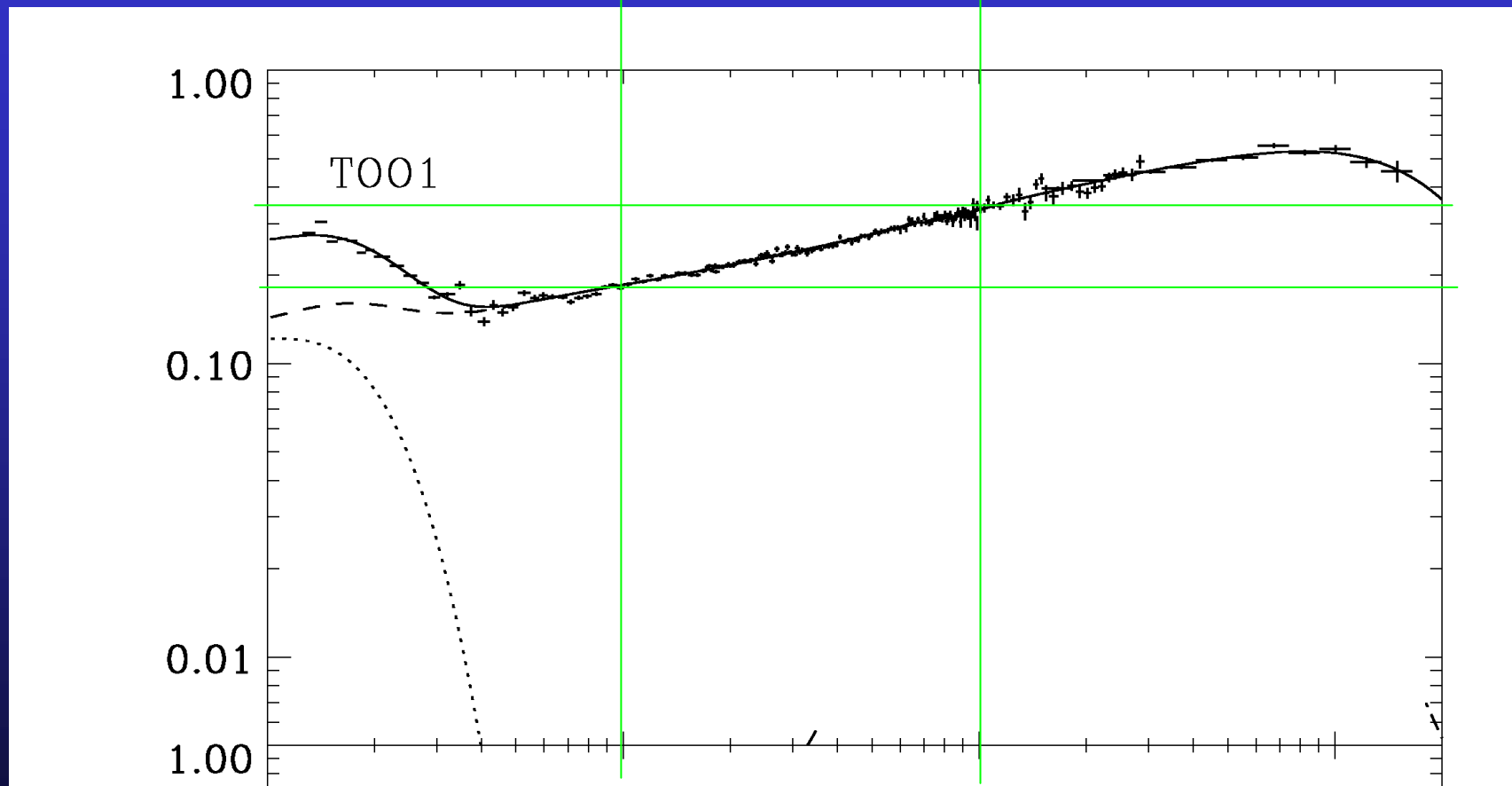


Optically thick thermal

- Optical depth $\tau > 1$, multiple scattering – average $N \sim \tau^2$
- Not much left of original seed photon spectrum $\exp(-\tau)$
- if $(1+4\Theta)^N \epsilon_{in} > 3\Theta$ ($y \gg 1$) then majority of photons reach 3Θ
- Can't go any higher so they pile up – try to thermalise but little true absorption so still comptonised. Wien peak.

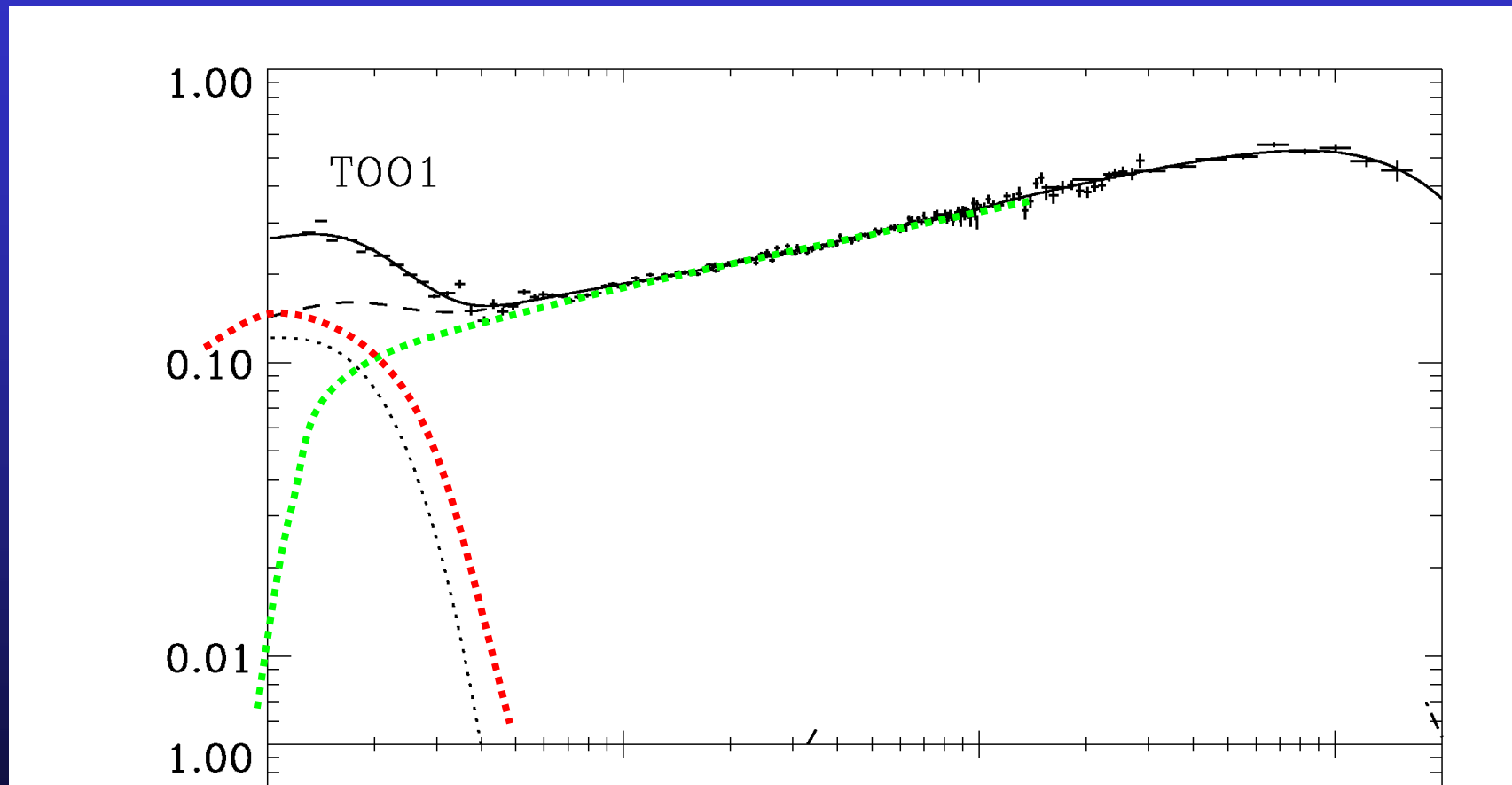


Practice!! Mystery object



- Estimate Θ and τ

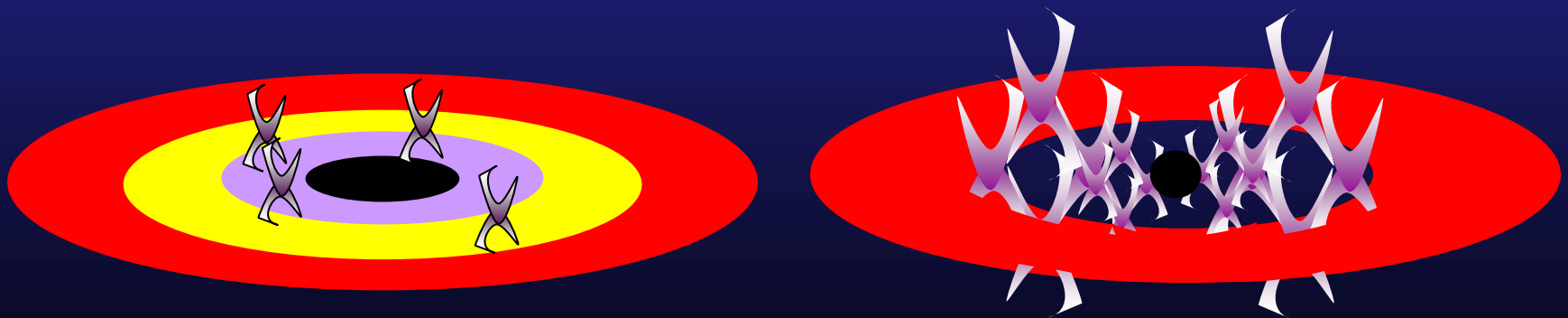
Seed photons



- Need more soft emission than $\exp(-\tau)$
- Not all disc comptonised! Patchy corona or truncated disc

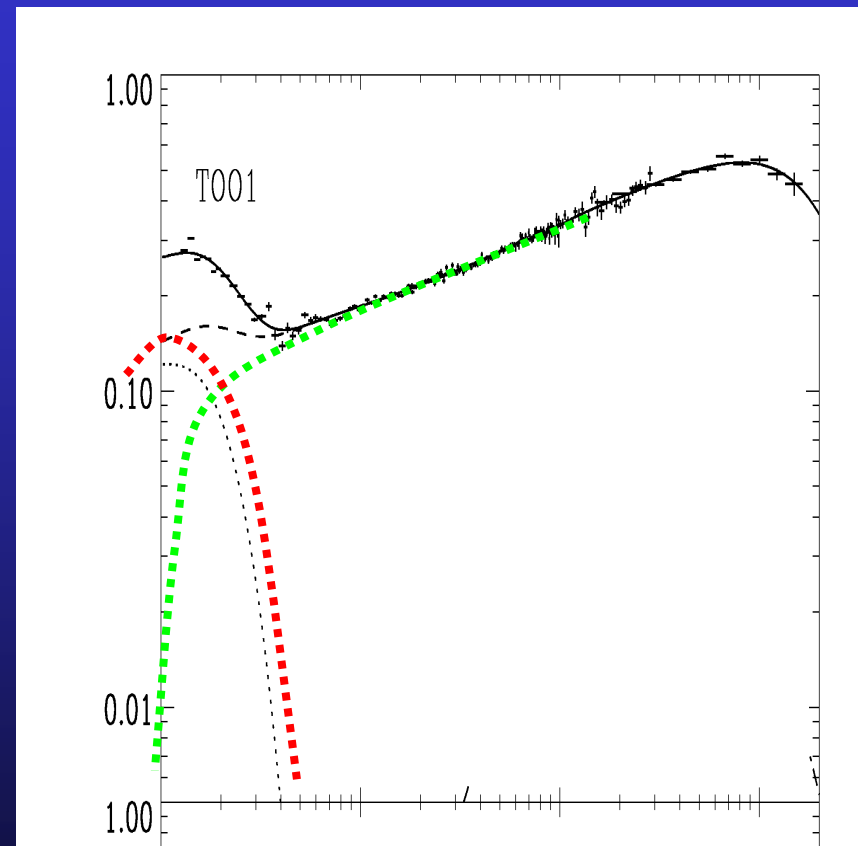
Energetics!

- Seed photon power illuminating flow L_s
- Heating of electrons gives comptonisation power L_h
- $L_h \gg L_s$ to get hard spectrum
- Easy to see how in truncated disc. Less easy in corona (see L5)



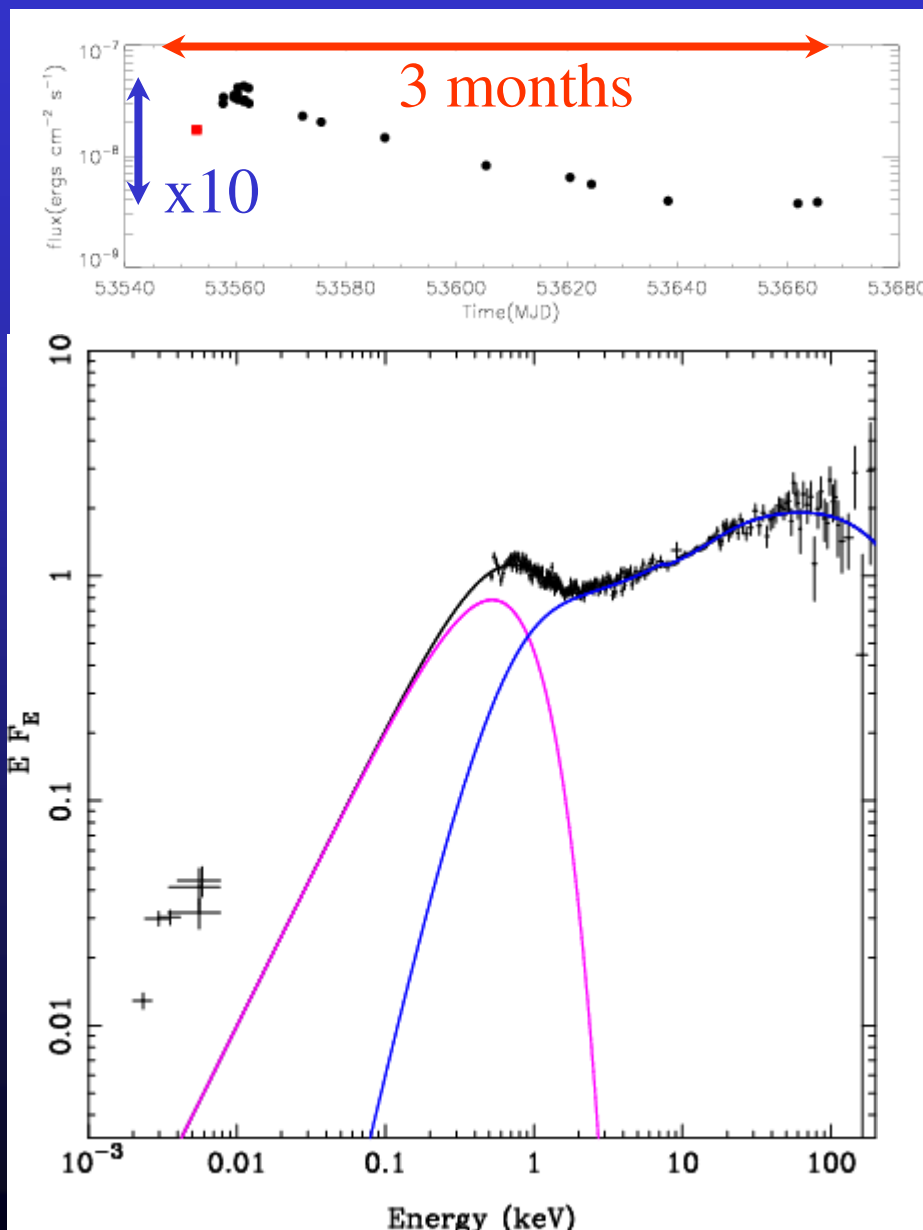
Energetics!

- Seed photon power illuminating flow L_s
- Heating of electrons gives comptonisation power L_h
- y axis τL_s to L_h , x axis from ϵ_{in} to 3Θ
- Get self consistent Θ from energetics



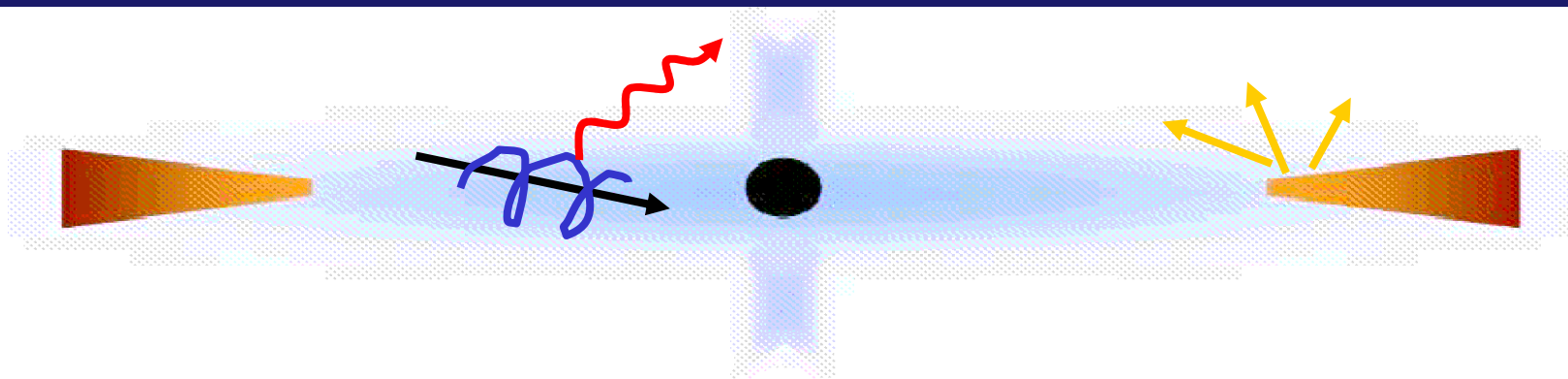
Seed photons in low/hard state

- Low/hard state outburst
- Swift optical/UV/X-ray plus RXTE 3-200 keV
- Low N_h ($2 \times 10^{21} \text{ cm}^{-2}$)
- Factor 10 \downarrow in 3 months
- Seed photons disc at peak
- Probably cyclo-sync later



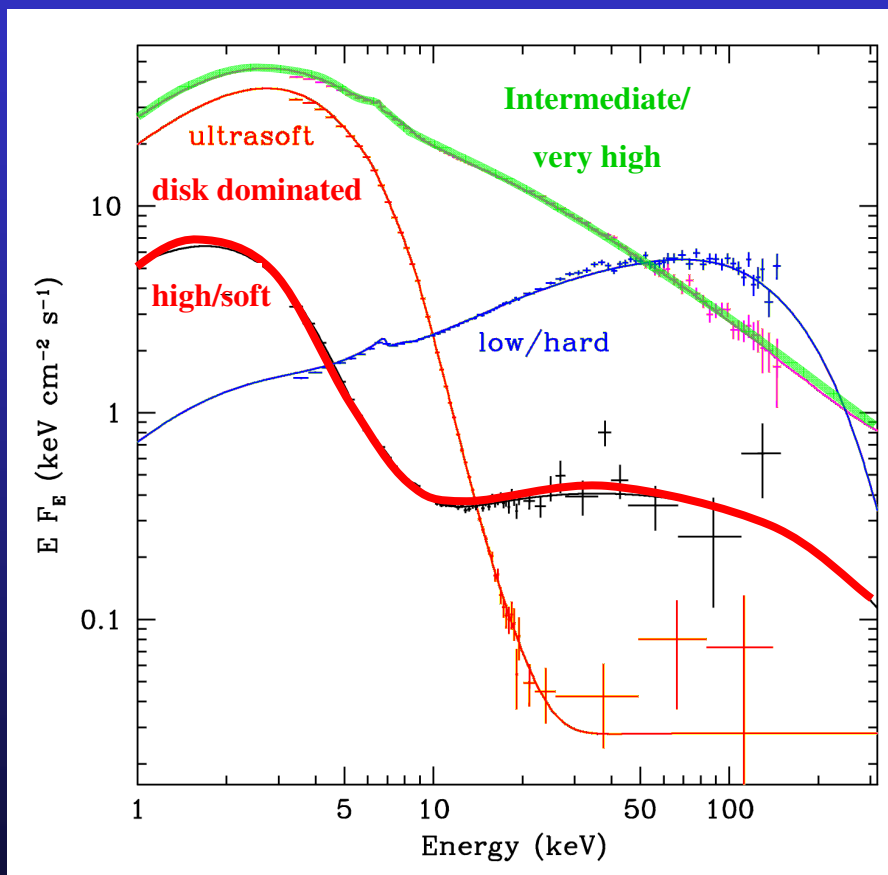
Seed photons in low/hard state

- Most photons from disc don't intercept hot flow
- So $L_s \ll L_h$ and predict very HARD spectra
- Never see this!
- So need another source of seed photons
- Got B field and hot electrons – the thermal electrons can spiral around the B field lines and give cyclo-synchrotron in the flow itself so it makes its own seed photons!



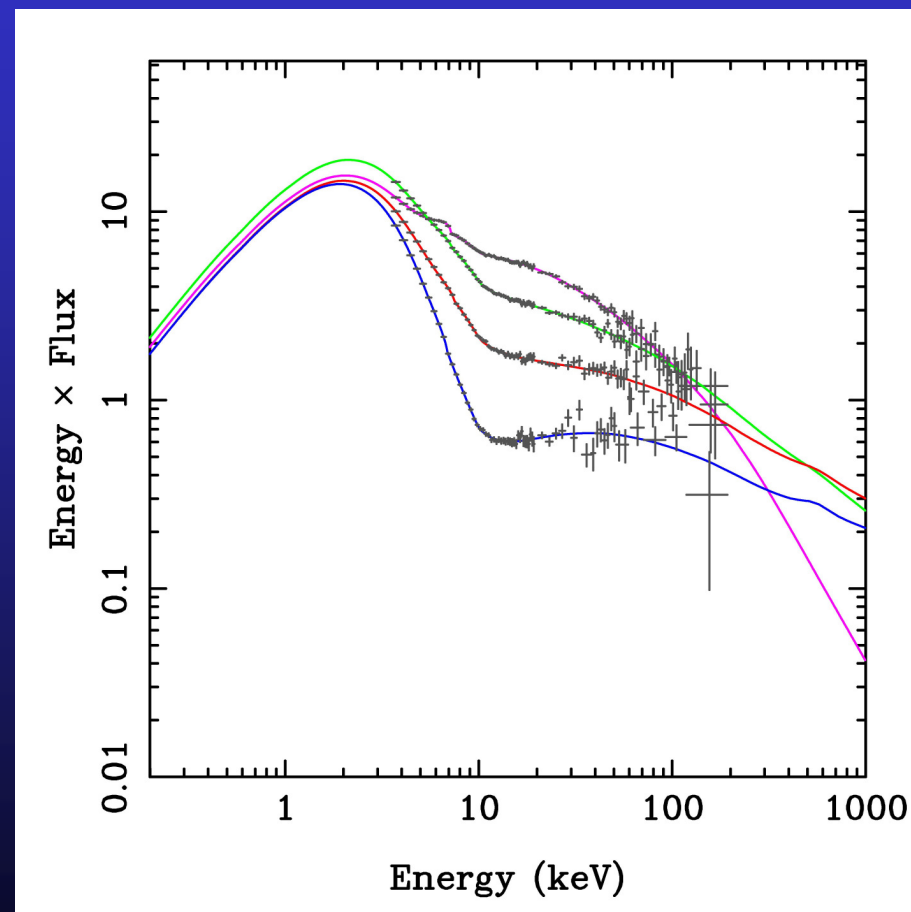
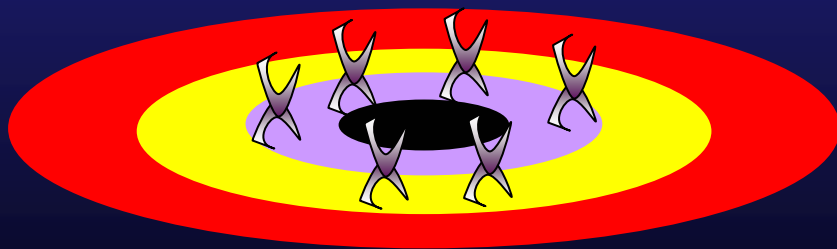
Spectral states

- Dramatic changes in continuum – single object, different days
- Underlying pattern in all systems
- High L/L_{Edd} : soft spectrum, peaks at kT_{max} often disc-like, plus tail
- Lower L/L_{Edd} : hard spectrum, peaks at high energies, not like a disc (McClintock & Remillard 2006)



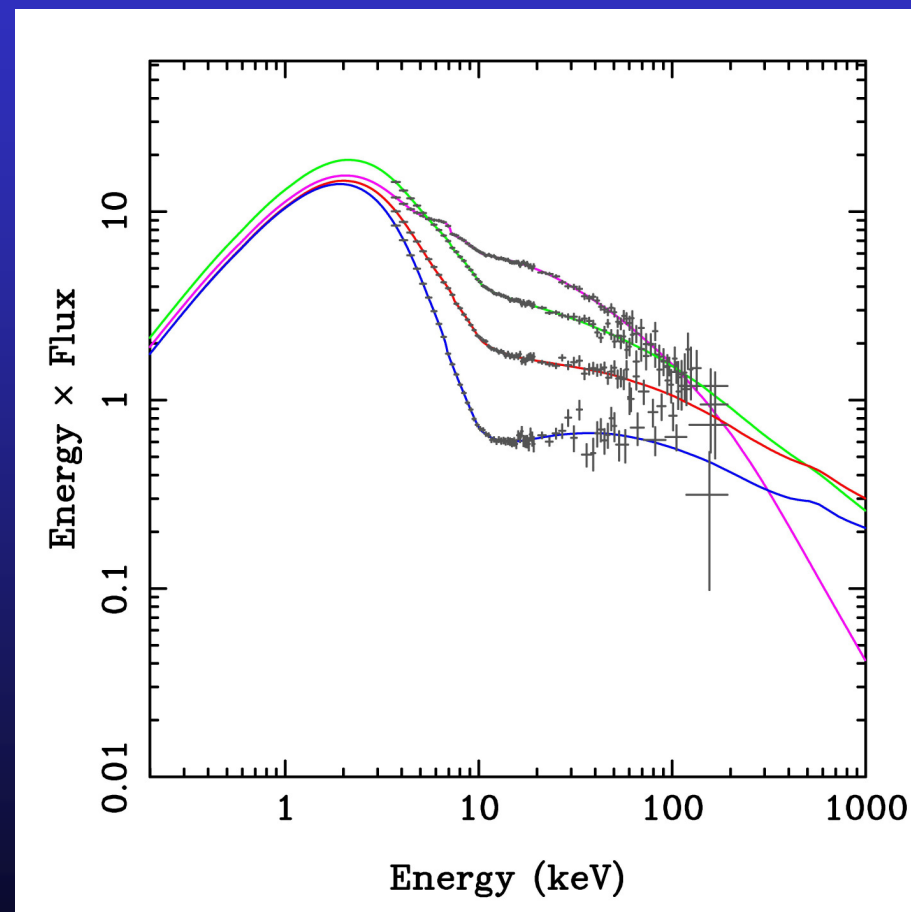
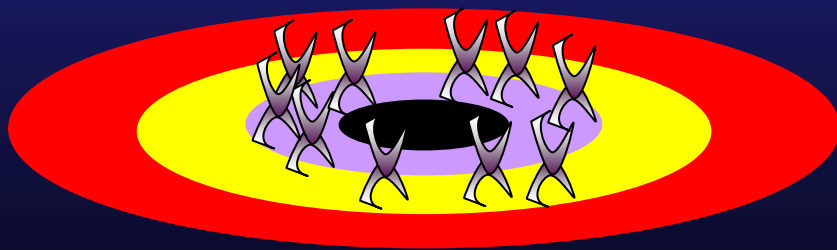
X-ray spectra at high L/L_{Edd} are not always disc dominated

- Disc dominated spectra tail – either small t or small covering fraction
- Merge smoothly onto VHS
- Most extreme show no clear disc rise – high optical depth AND high covering fraction



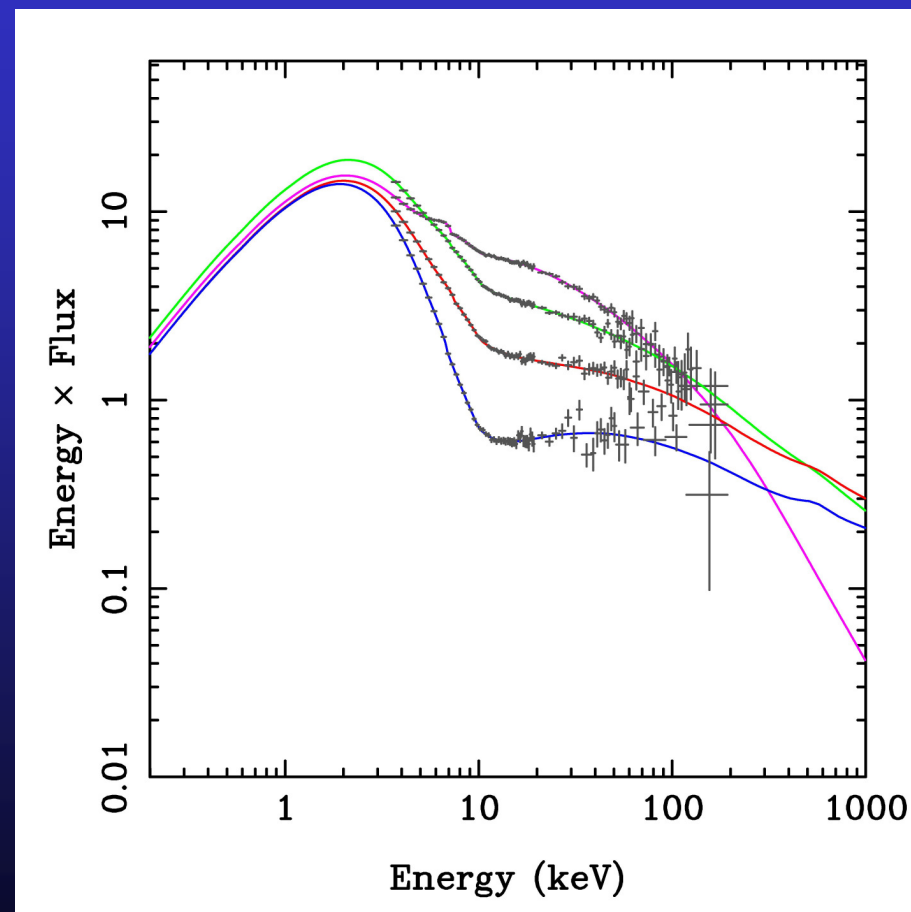
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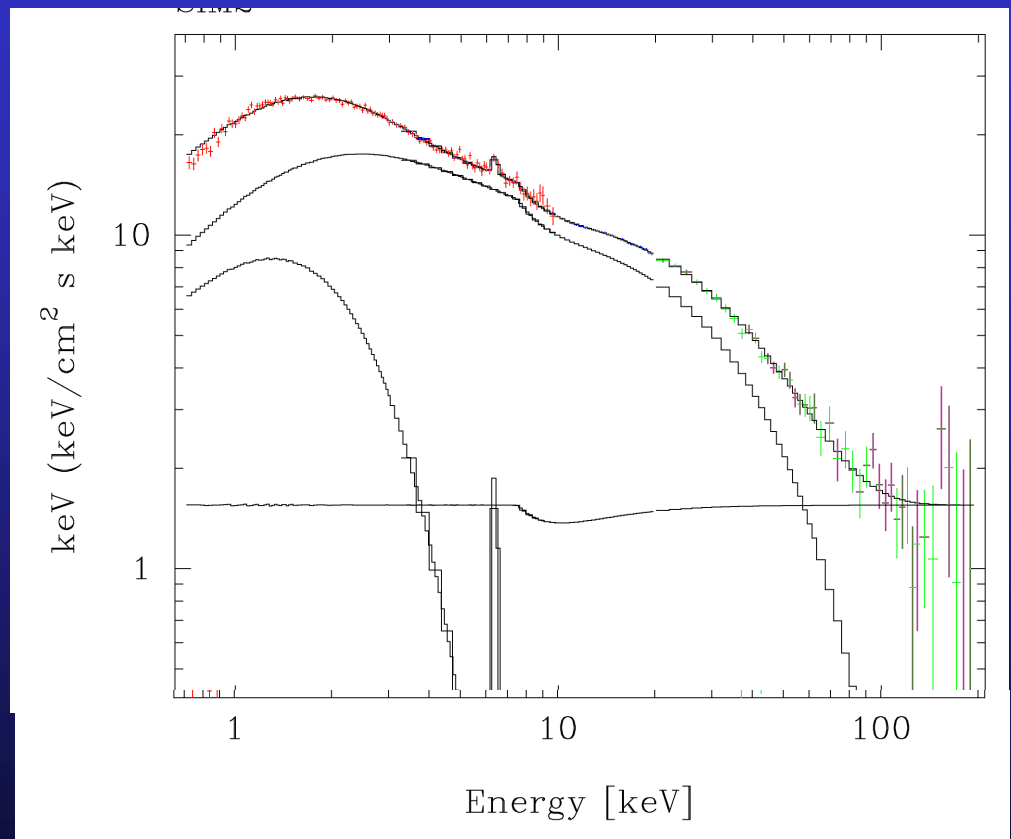
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Very high state

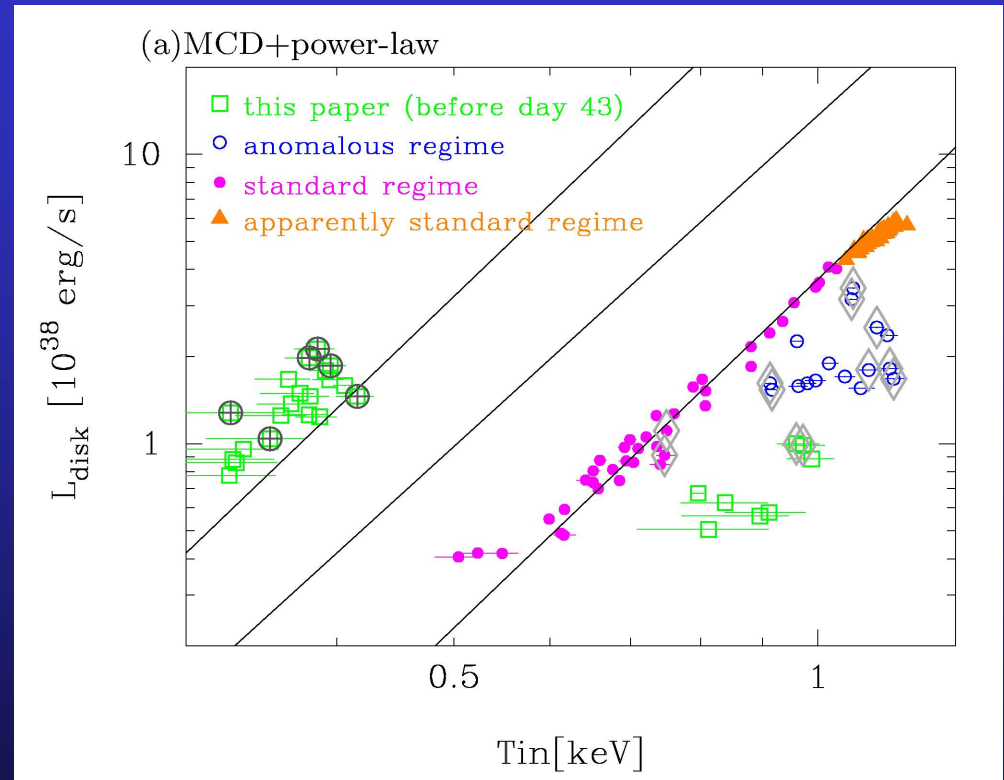
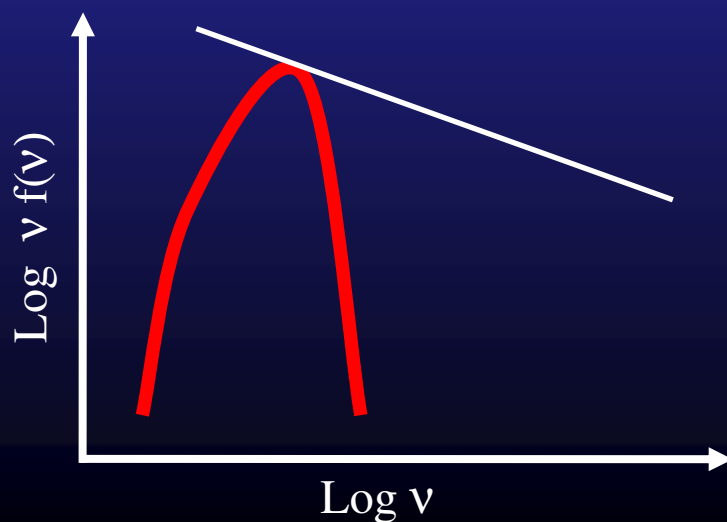
- Disk does not dominate!
- Sometimes hard to see as separate component from continuum – optically thick comptonisation completely covering inner disc
- $kT_e \sim 10\text{-}20\text{ keV}$, $\tau \sim 2$
optically thick Kubota et al 2001; Kubota & Done 2004



Very High State: Spectrum

Kubota & Done 2004

- Disc AND tail have roughly equal power. BE CAREFUL!!!
- Now depends on models - Comptonized spectrum is NOT a power law close to seed photons!

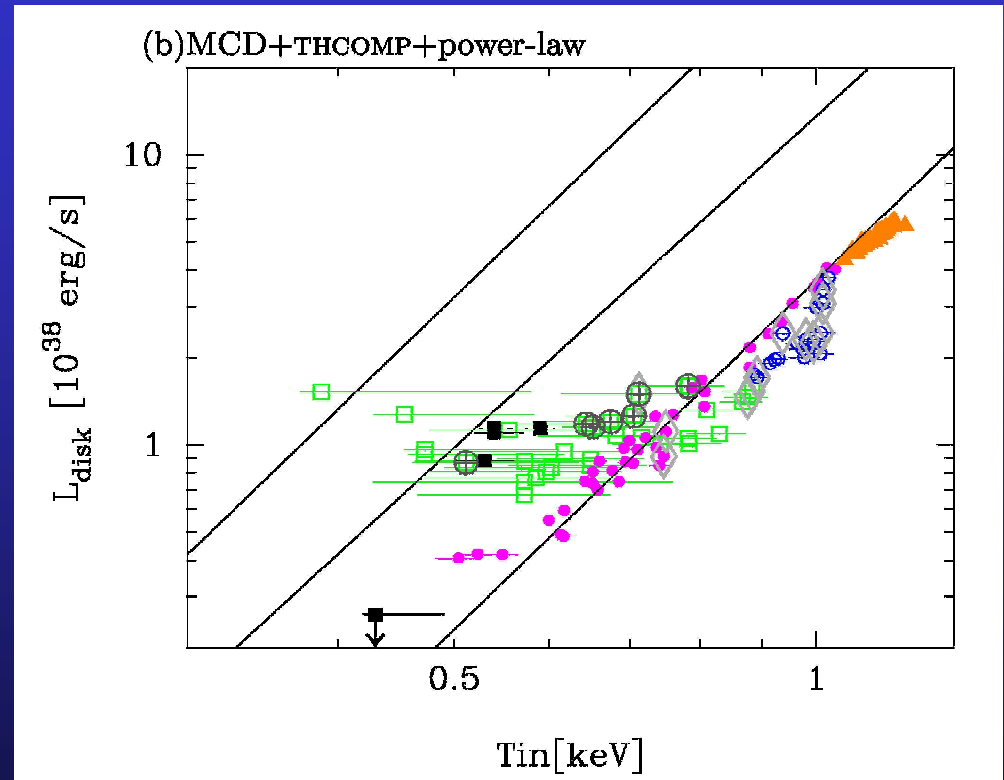
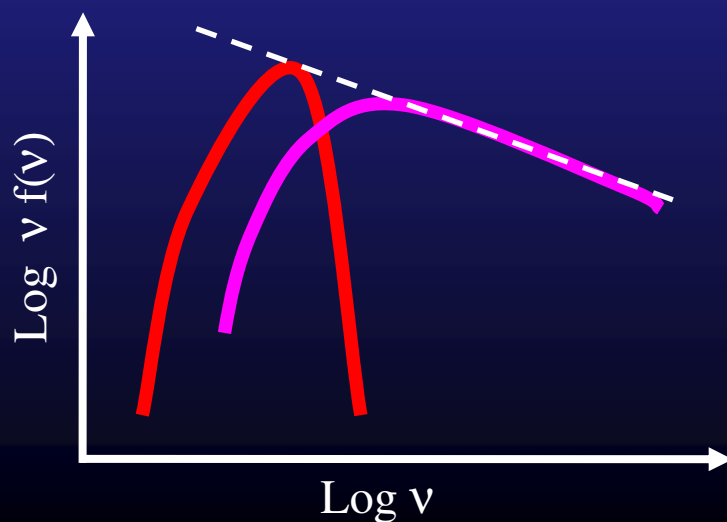


- Disc dominated (low L / high L)
- Very high state (comp < disc)
- Very high state (comp > disc)

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Kubota & Done 2004

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- Now depends on models - Comptonized spectrum is NOT a power law close to seed photons!

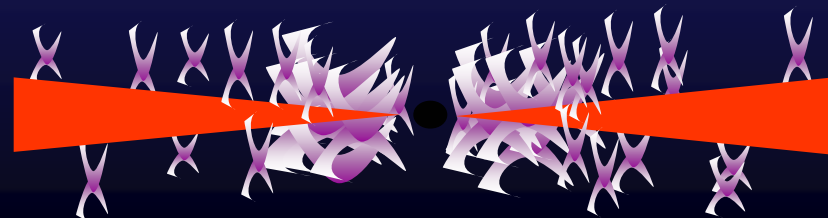
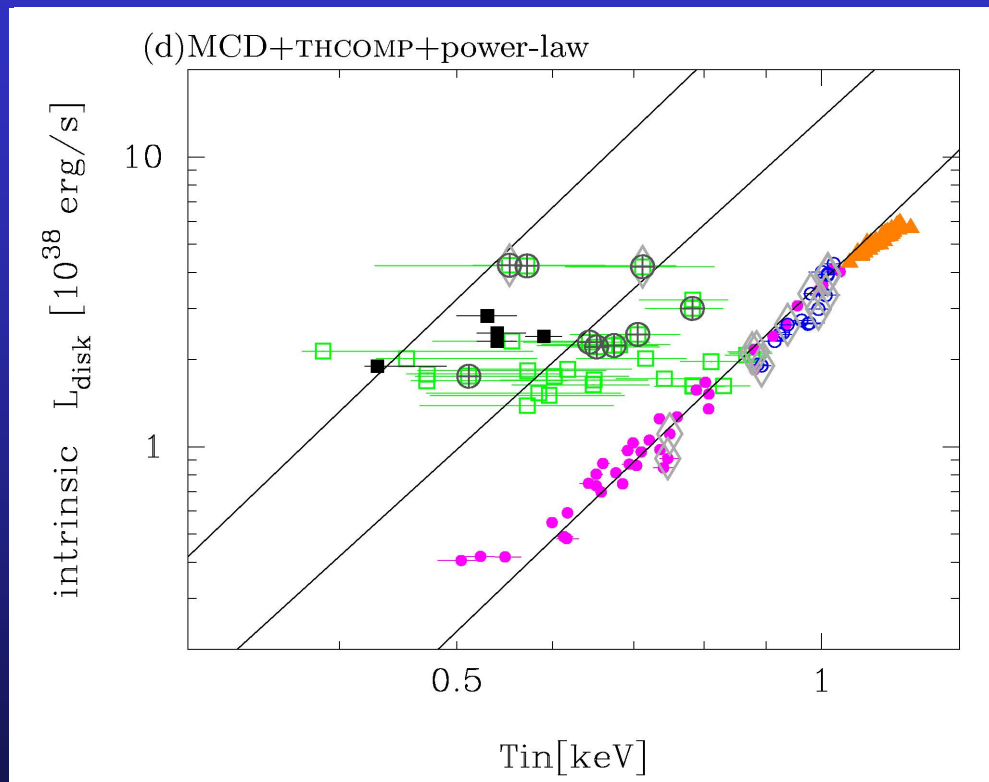
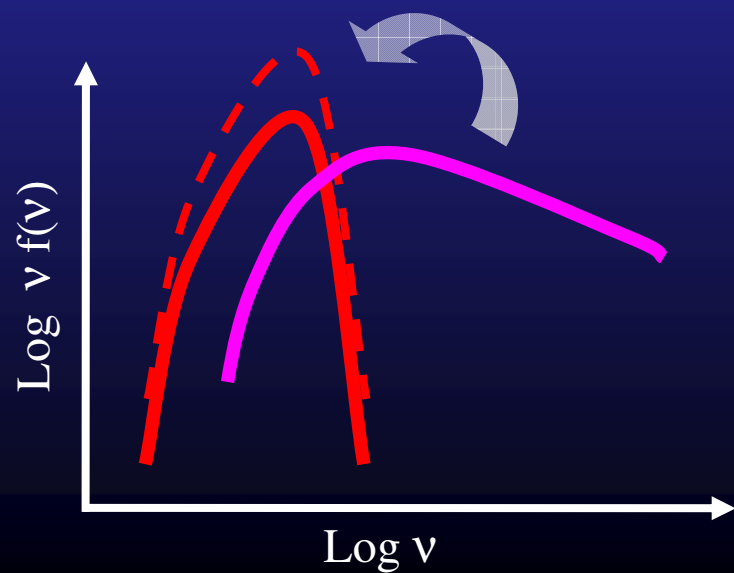


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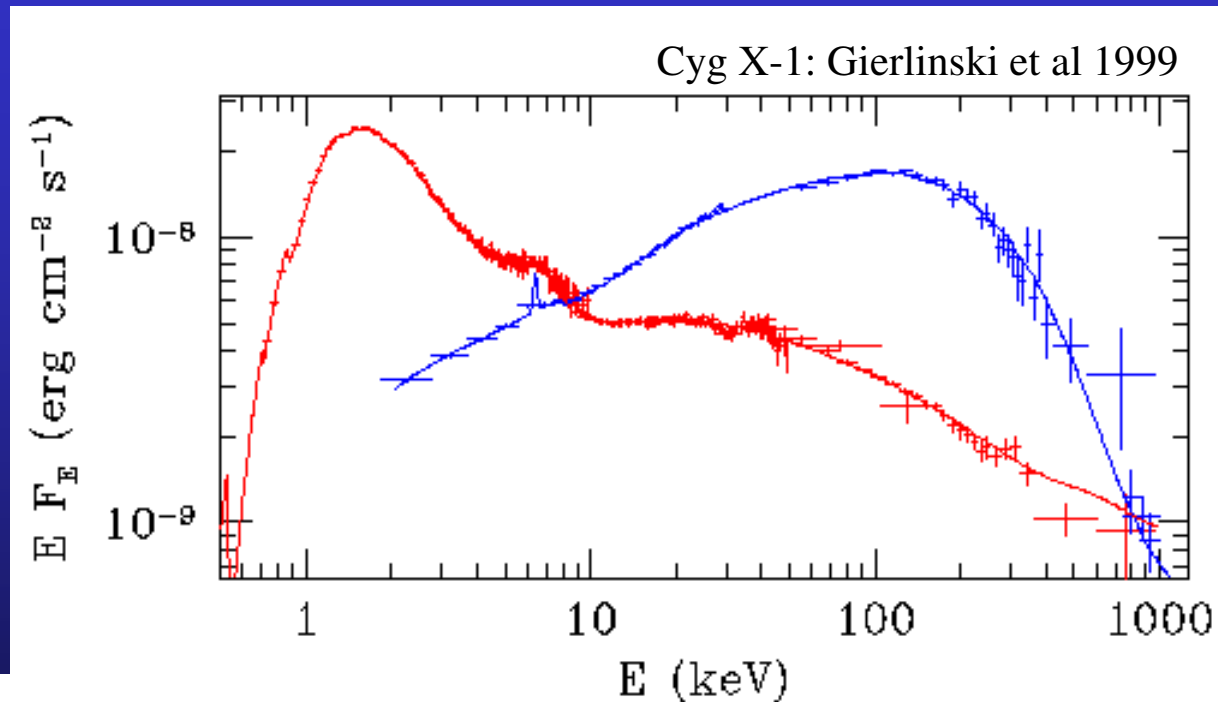
Very High State: photons

Kubota & Done 2004

- But Comptonised photons come from the disc – optically thick so suppresses apparent disc emission
- Correct for this



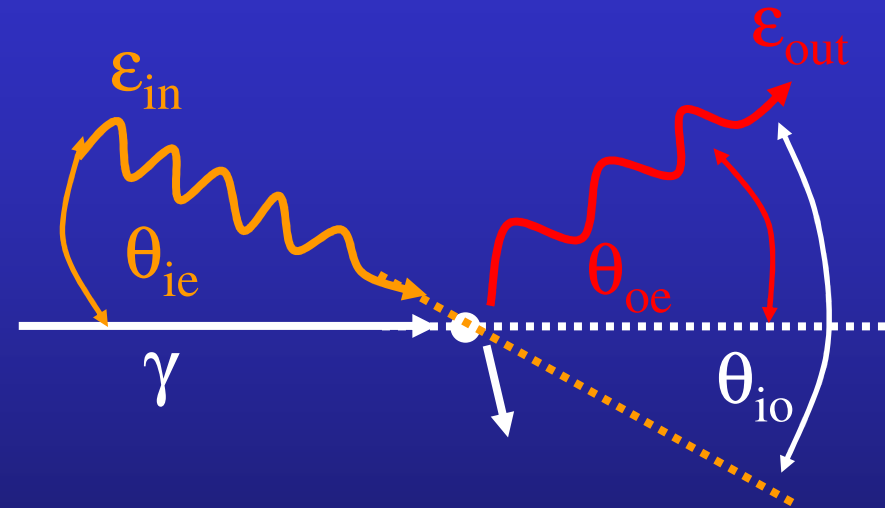
Observations



- Low state spectra peak at 100 keV. Well modelled by thermal electrons
 $\Theta \sim 0.1 - 0.2$ $\tau \sim 1$
- High state spectra need predominantly non-thermal electron distribution

Non-thermal compton upscattering:

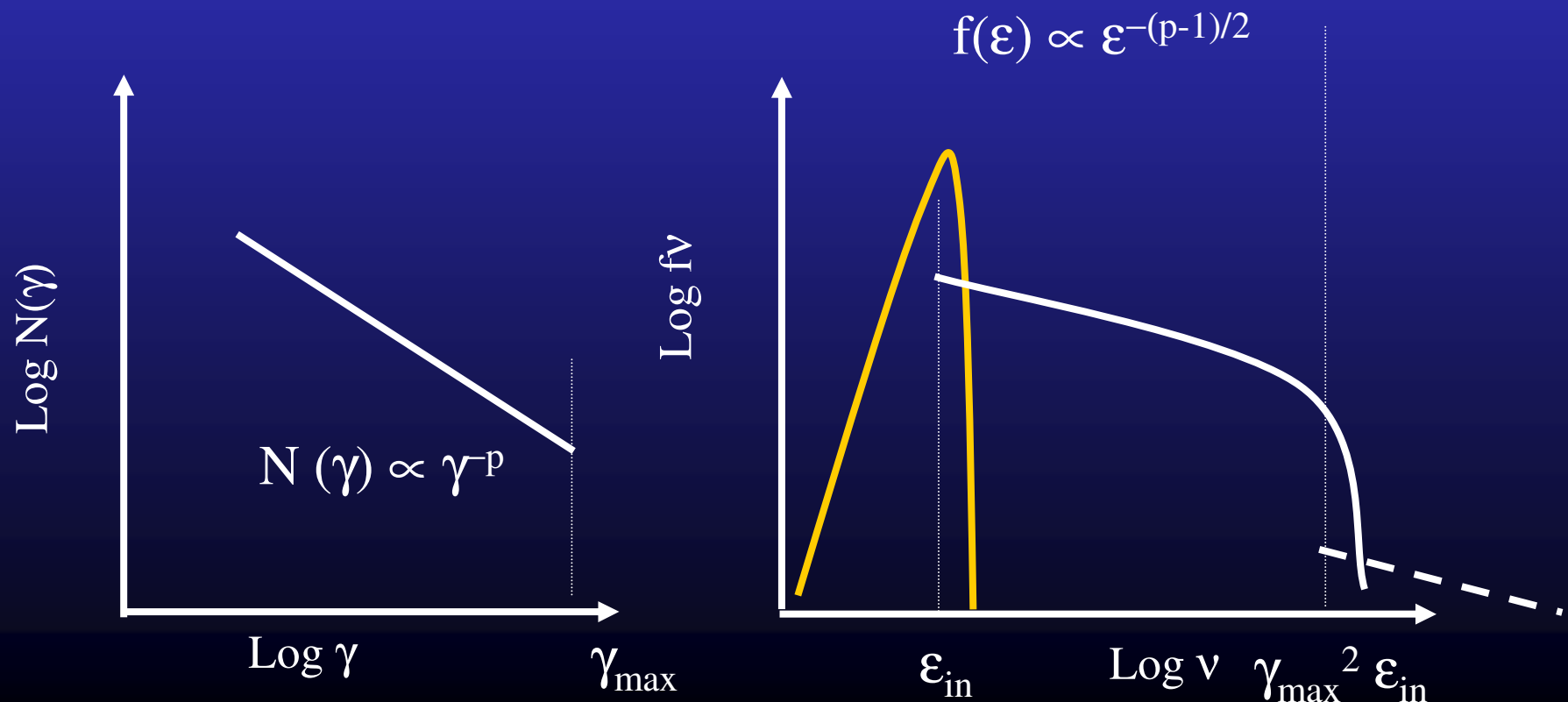
- If $\epsilon_{\text{in}} \ll \gamma$ then electron has most energy so loses it to photon
- Average over angle for isotropic electron and photon distribution.
- Output photons beamed into angle $1/\gamma$ from electrons
- Nonthermal $\epsilon_{\text{out}} \sim \gamma^2 \epsilon_{\text{in}}$
- Limit is $\epsilon_{\text{out}} < \gamma$



$$\epsilon_{\text{out}} \sim \frac{\epsilon_{\text{in}}(1 - \beta \cos \theta_{\text{ei}})}{1 - \beta \cos \theta_{\text{eo}}}$$

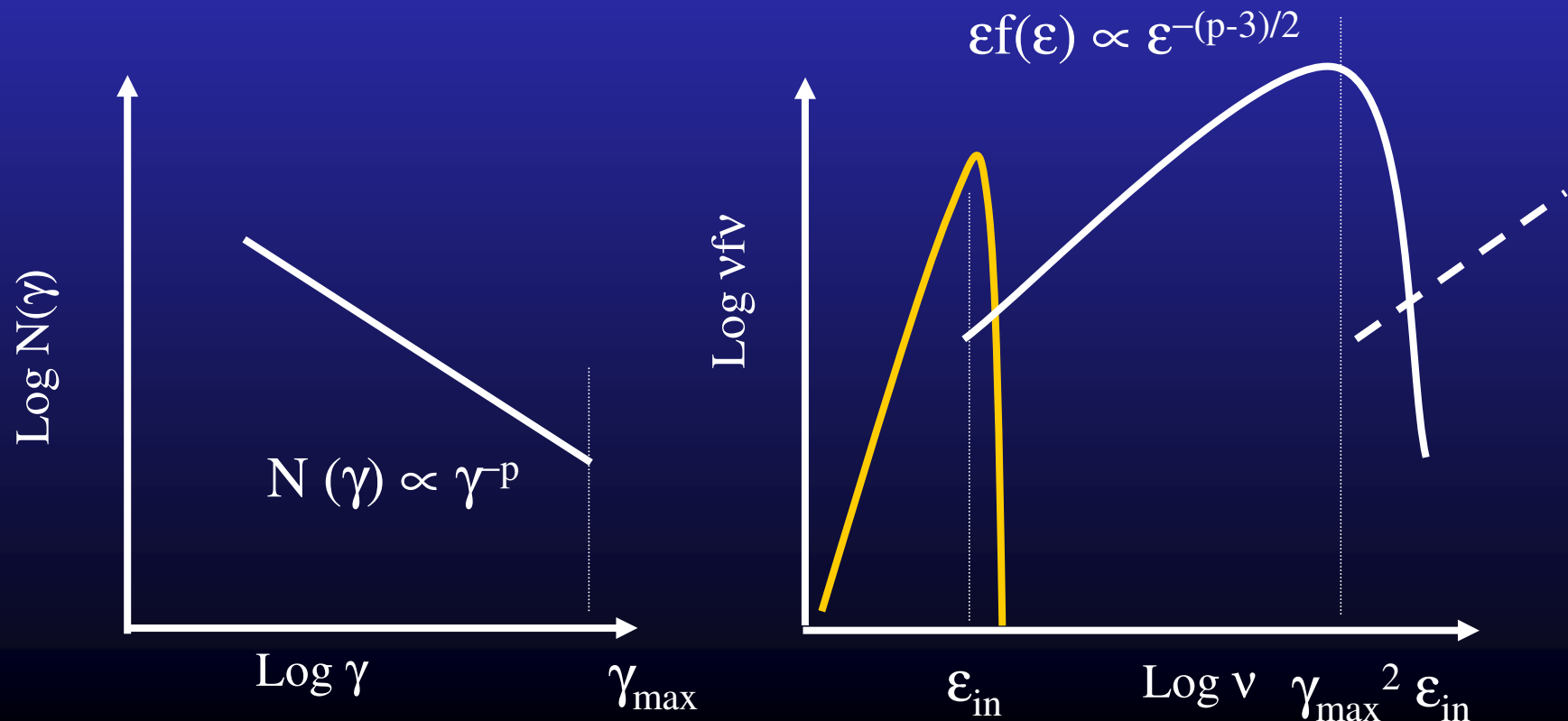
Optically thin nonthermal compton

- power law by single scattering of nonthermal electrons $N(\gamma) \propto \gamma^{-p}$
- index $\alpha = (p-1)/2$ ($p > 2$ so $\alpha > 0.5$ – monoenergetic injection)
- Starts a factor τ down from seed photons, extends to $\gamma_{\max}^2 \epsilon_{\text{in}}$

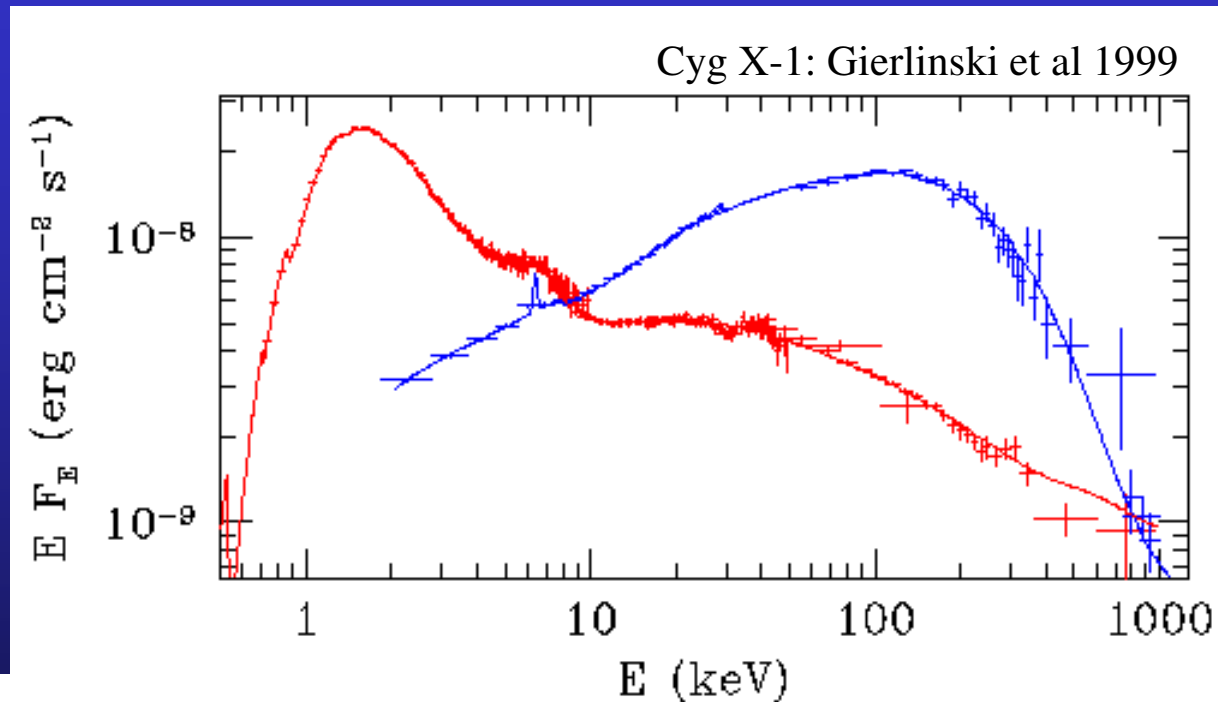


Optically thin nonthermal compton

- Again, can do by energy
- Lh in electron power, Ls in seed photons
- Y axis τ Ls to Lh, x axis from ϵ_{in} to $\gamma_{\text{max}}^2 \epsilon_{\text{in}}$



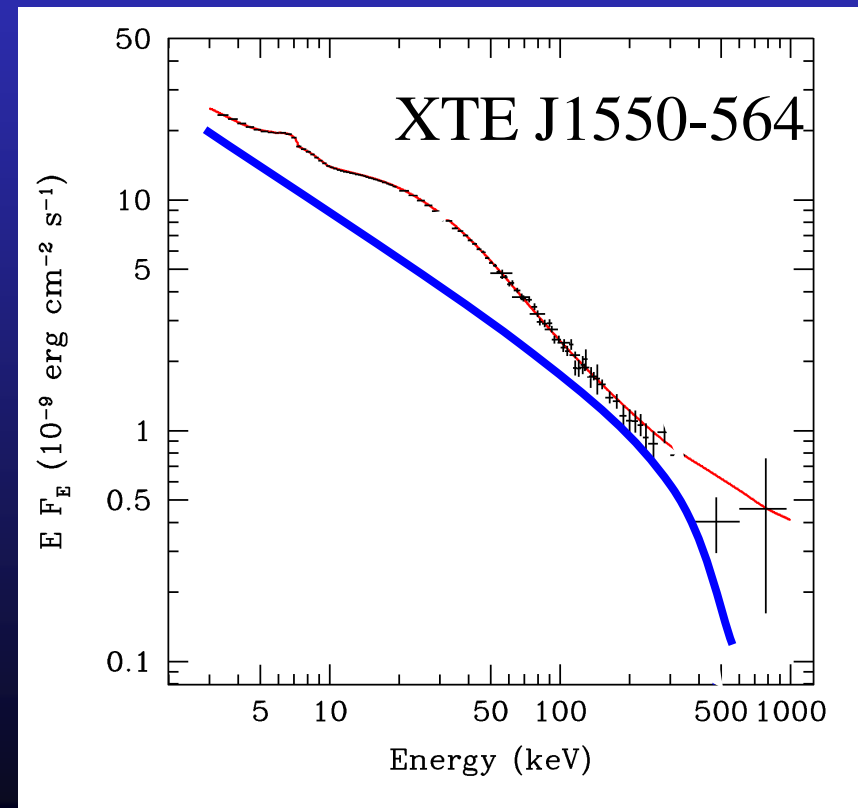
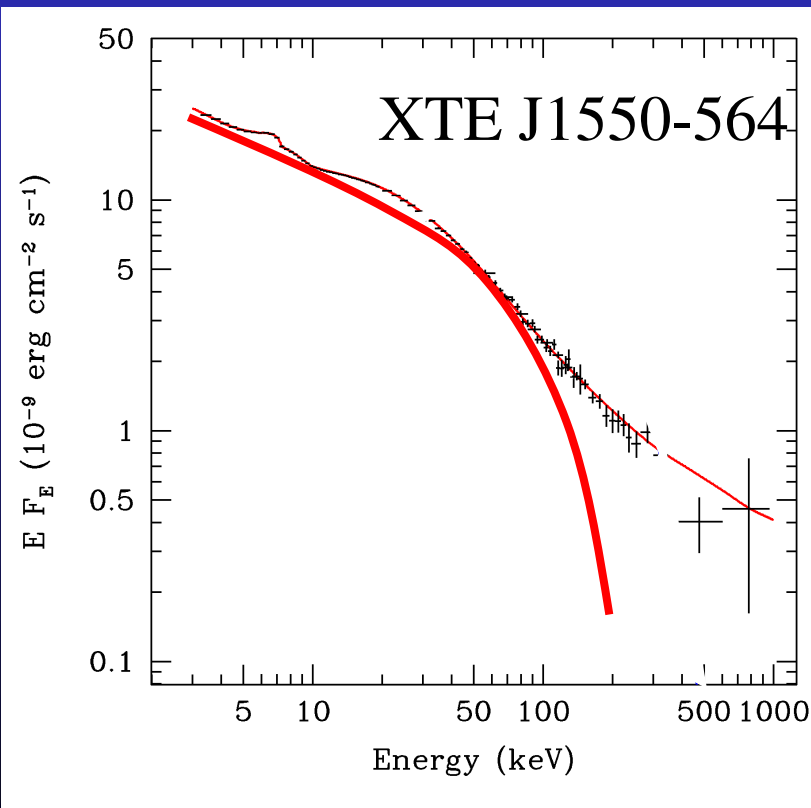
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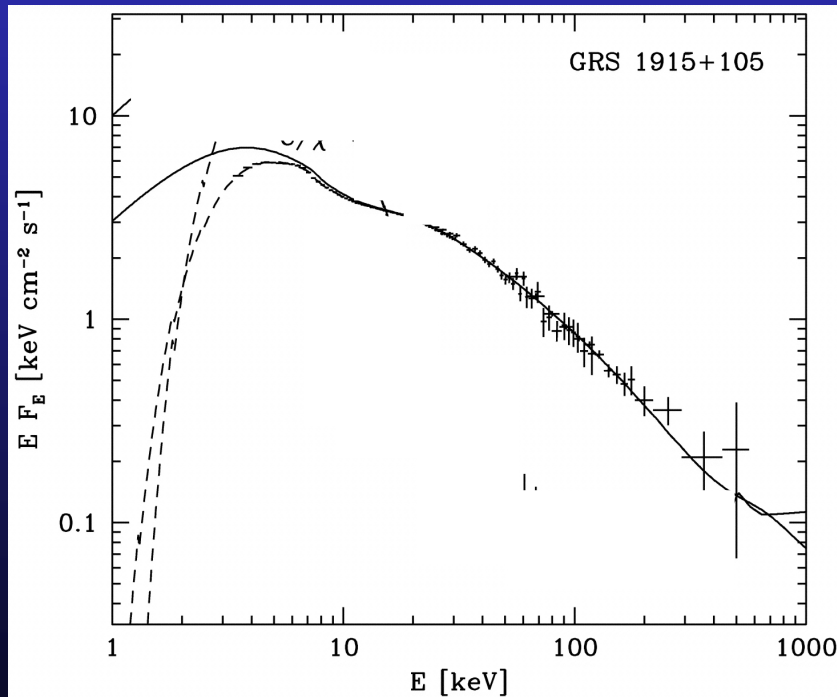
Hybrid plasma

- Very high states in GBH look like this
- NOT POWER LAW CONTINUUM Kubota & Makashima 2004
- thermal doesn't fit, nonthermal doesn't fit either as steep

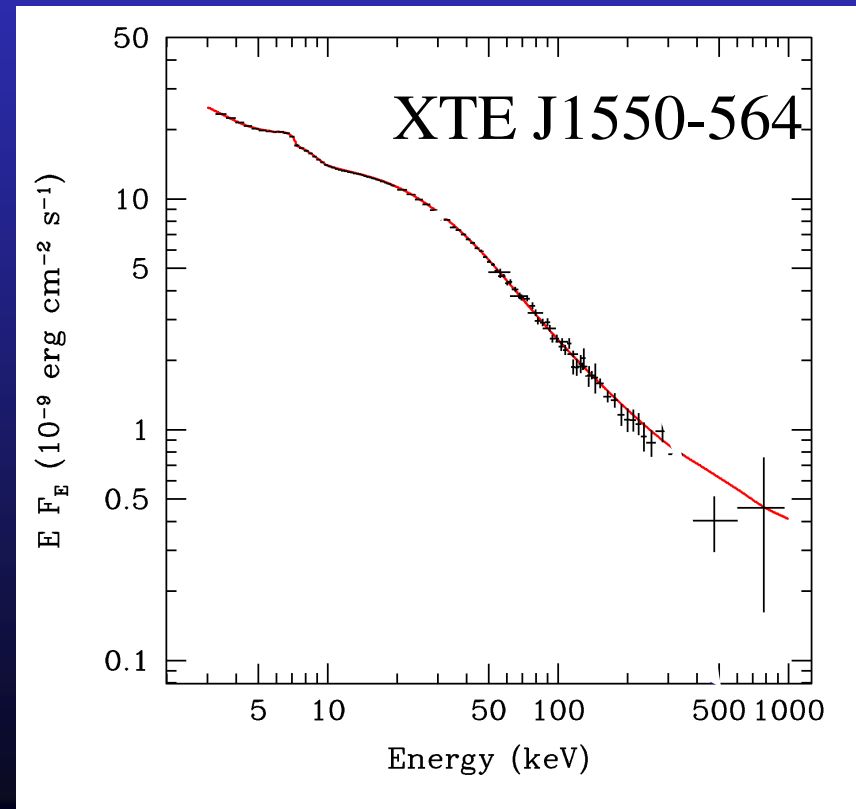


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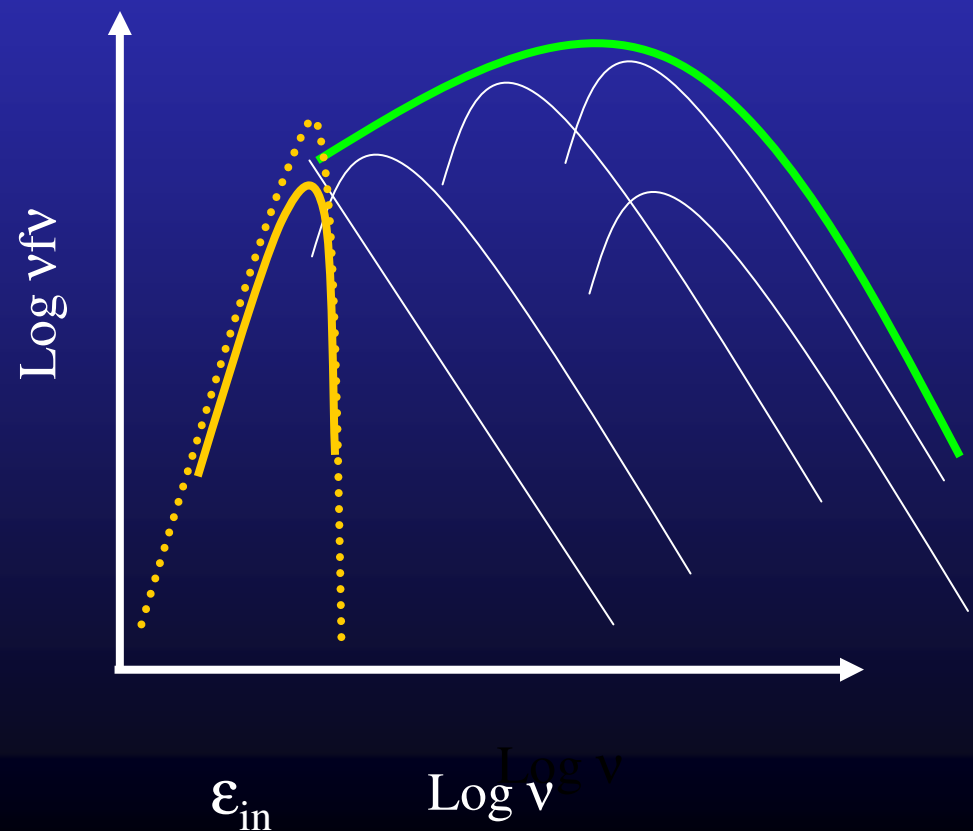
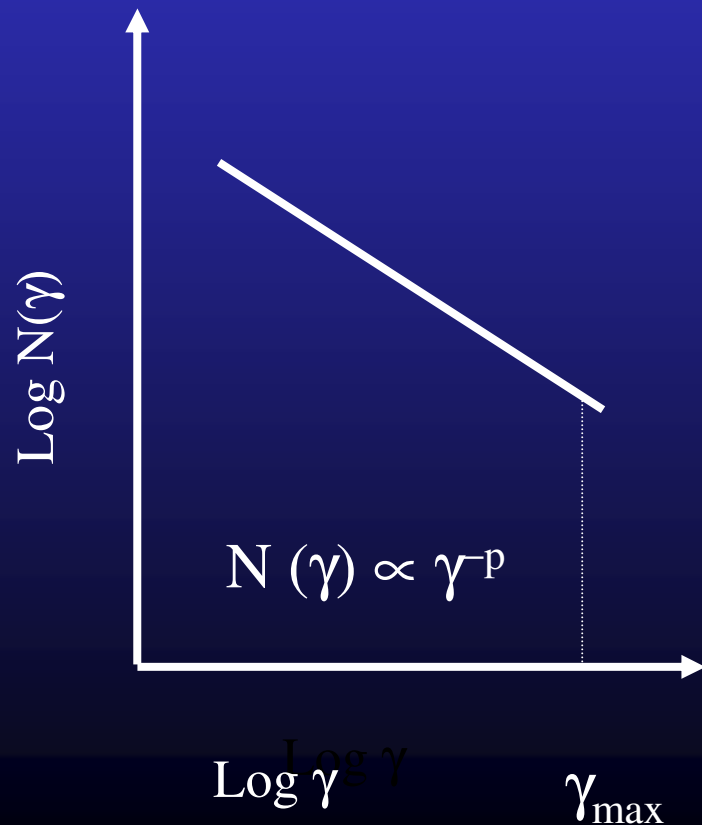
Zdziarski et al 2001



Gierlinski & Done 2002

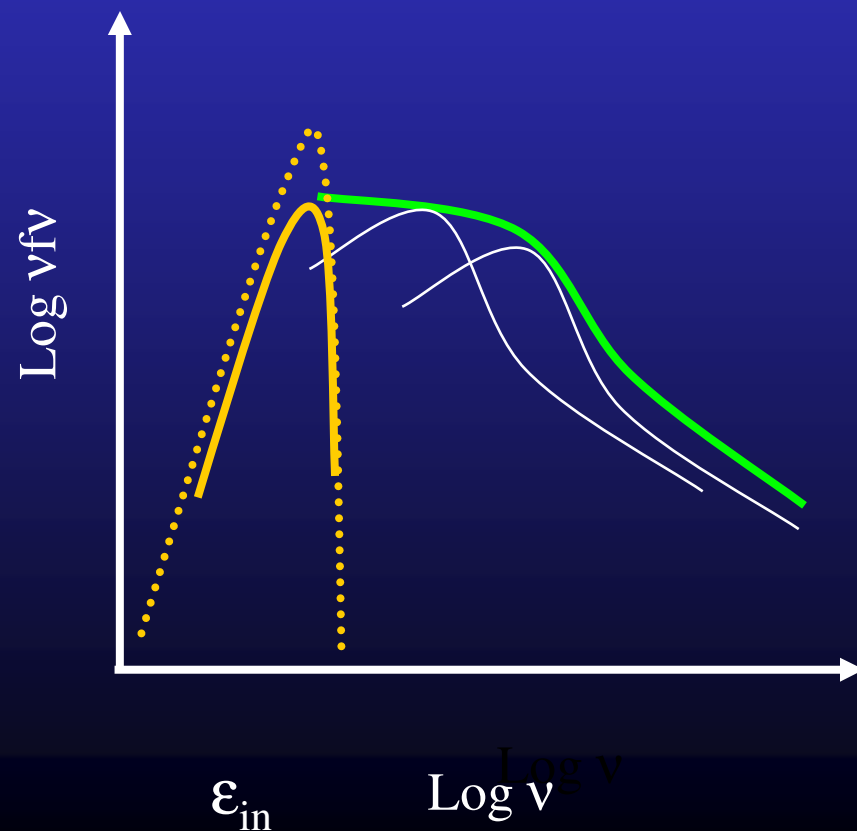
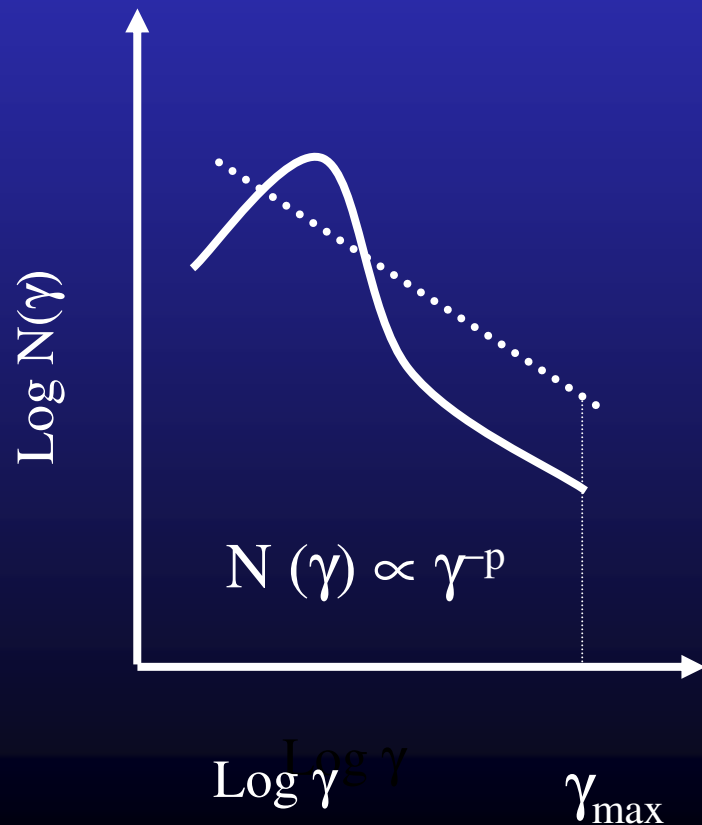
Optically thick nonthermal

- Multiple scattering $\tau > 1$ Ghisellini 1989
- If steep power law non-thermal electrons then $\langle \gamma \rangle \sim 1$ so get small energy boost each time – similar to thermal.
- But max energy is $\langle \gamma \rangle \sim 1$ ie mc^2 , 511 keV



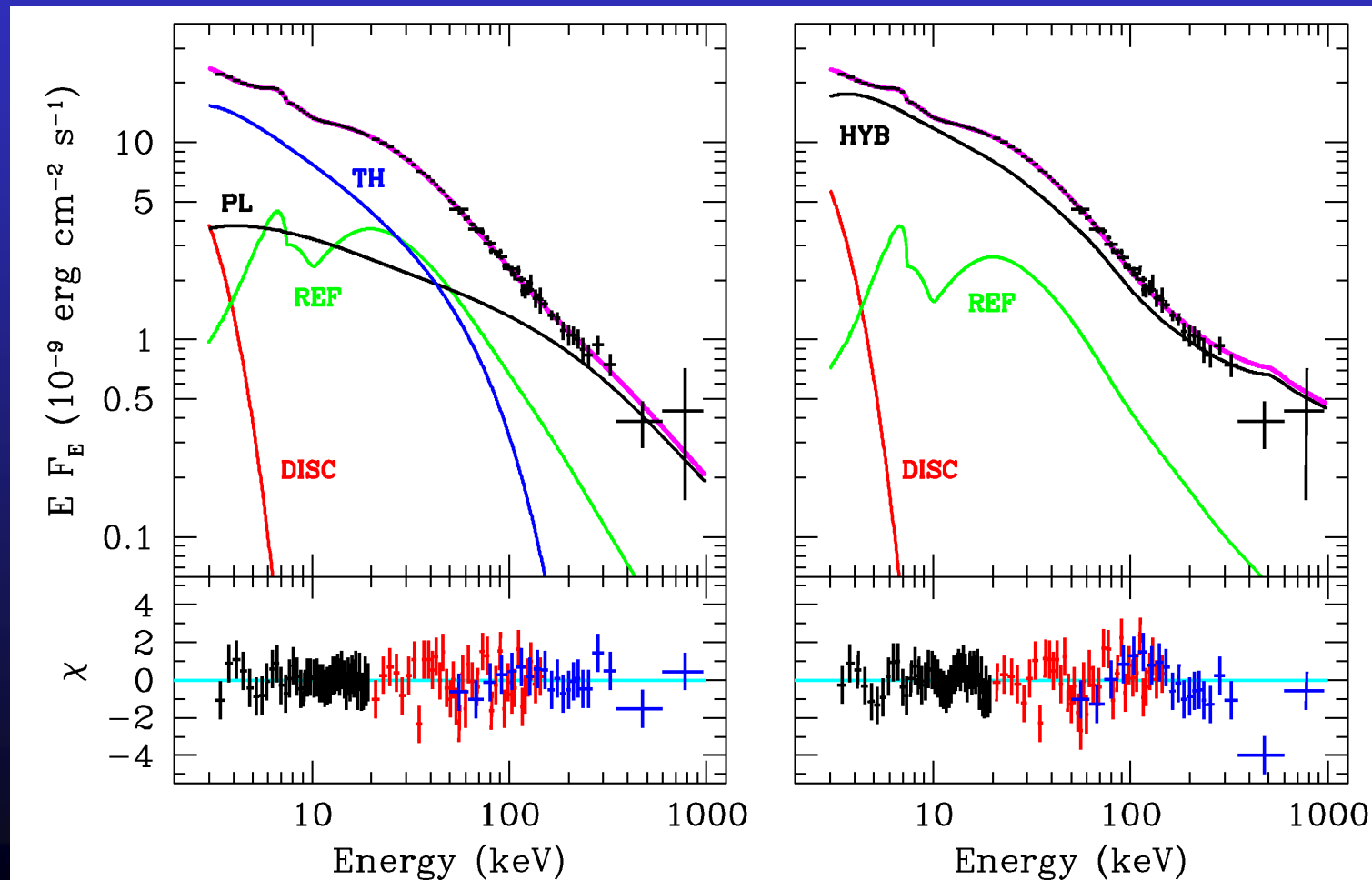
Hybrid plasma

- Optically thick nonthermal ? Contradiction?
- Multiple scattering $\tau > 1$ implies electron thermalise
- Coulomb collisions –between electrons. Most efficient at low γ
- Compton collisions – cooling γ^2 so most efficient at high γ



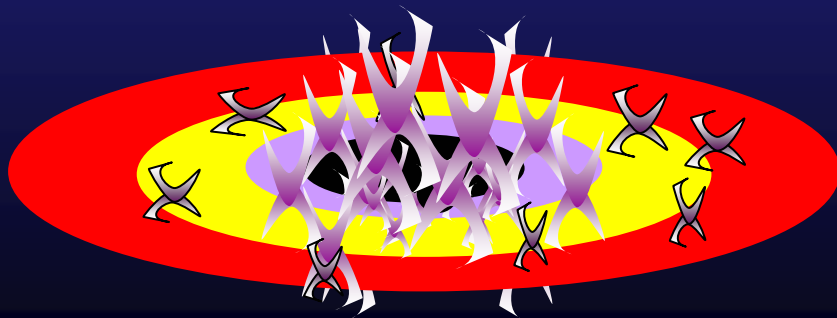
Very high state

Complex curvature – 2 electron dist, one thermal, one nonthermal ?
Or hybrid - single electron dist, low E thermal, high E nonthermal



Self consistent spectra: nonthermal

- nonthermal need shape of injected electrons as well as L_h and τ
- $Q(\gamma) \propto \gamma^{-s}$ between γ_{\min} and γ_{\max}
- Illuminate region with seed photons L_s
- Heating (inject) = cooling (coulomb, comp) \Rightarrow self consistent $N(\gamma)$ rate leaving $\dot{\gamma} =$ rate injected
- Where compton dominates $d\gamma/dt \propto \gamma^2$ integrate $N(\gamma) \propto \gamma^2 \int Q(\gamma) d\gamma$
- $= \gamma^2 [\gamma^{(s-1)} - \gamma_{\max}^{-(s-1)}] / (s-1)$ so can't be flatter than γ^2 hence spectrum can't be flatter than $\alpha=0.5$



- But could have separate thermal component plus hybrid!!

Conclusions

- Compton scattering – just photon and electrons!
- Incredible variety and subtle interplay
- Only approximately a power law
- low energy break (seed photons – disc or cyclo-sync)
- high energy break (mean electron energy)
- Need not be single thermal component – thermal plus nonthermal or hybrid