

*Low-Frequency Solar p Modes:
Observations Obtained from
m-Averaged Spectra*

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m-averaged spectrum:

average the $(2l+1)$ m-components of an oscillation multiplet (n, l)

> Rotational and structural effects: degeneracy lift of mode frequency into $(2l+1)$ m-multiplets.

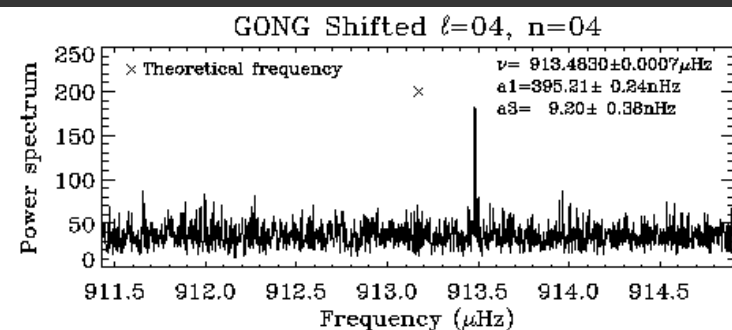
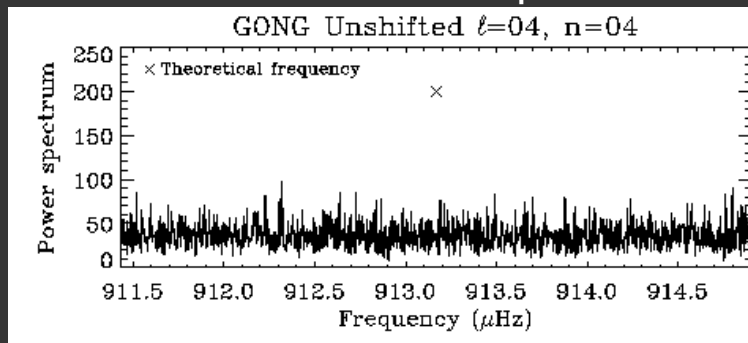
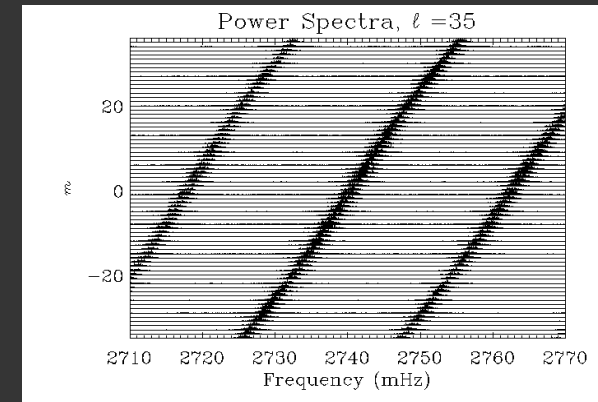
> The shifts (a-coefficients) are determined as we are searching for the low-frequency modes.

$$\nu_{n,l,m} = \nu_{n,l} + \sum_{k=1}^{k_{\max}} a_k(n,l) P_k^{(l)}(m)$$

> Several way to find the best estimates of the a-coefficients:

- *minimum likelihood*,
- *narrowest peak in the m-averaged spectrum*,
- *smallest entropy*.

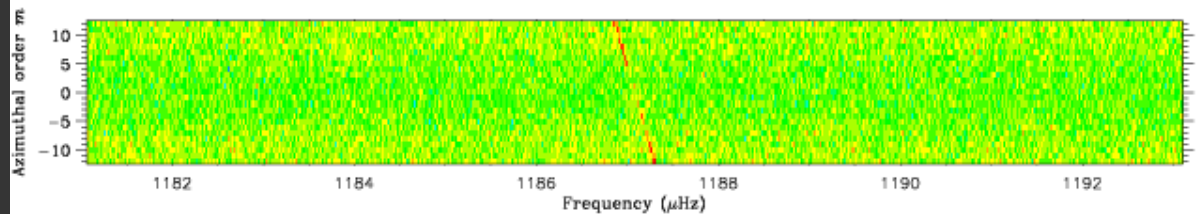
> Considerably improves SNR even when the m-components have too low SNR to be measured in the individual-m spectra.



m-averaged spectrum technique

$l = 12, n = 4$ mode at $\sim 1187 \mu\text{Hz}$

m-v diagram



m-averaged spectrum

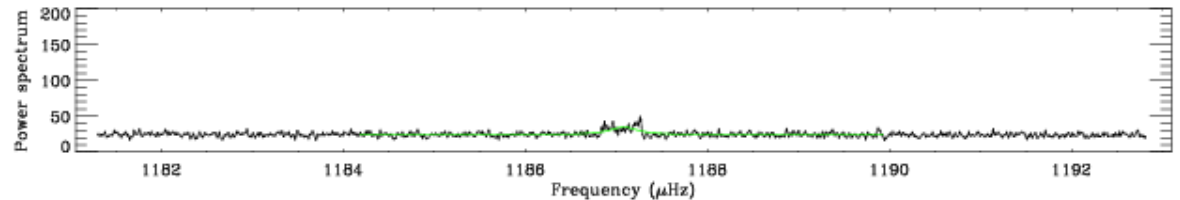
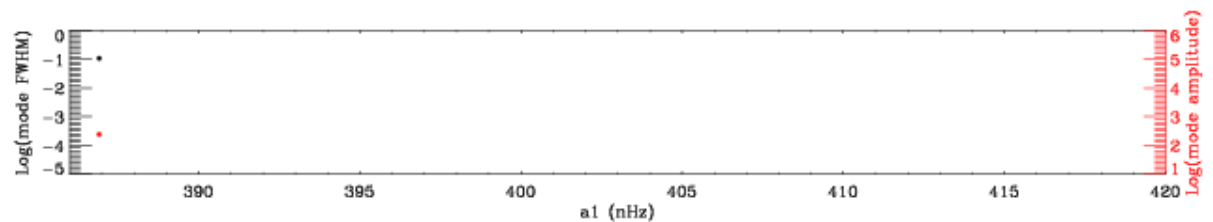
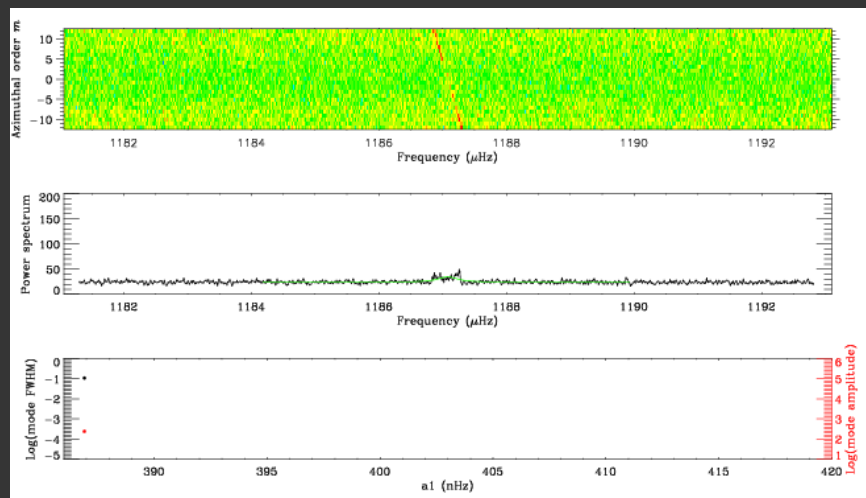


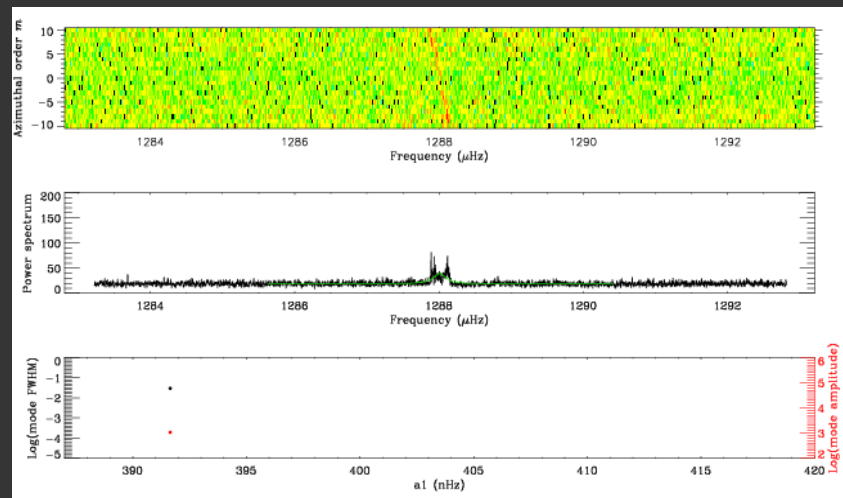
Figure-of-merit (a1)



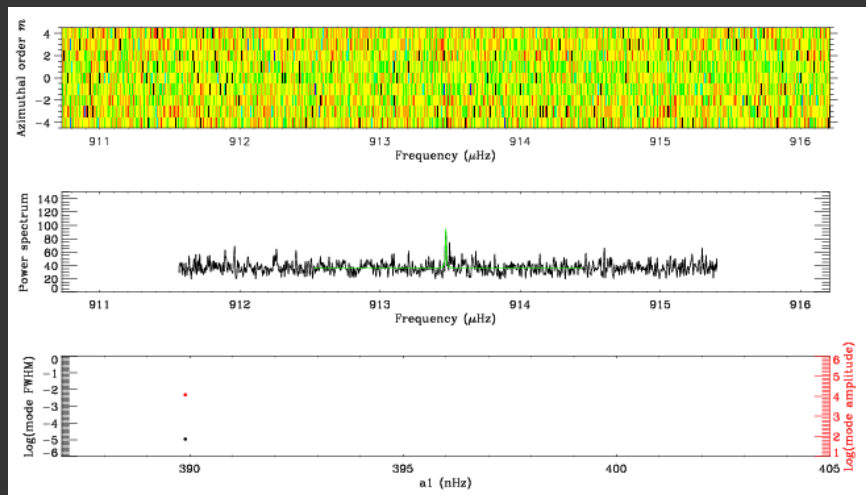
$l = 12, n = 4$ mode at $\sim 1187 \mu\text{Hz}$



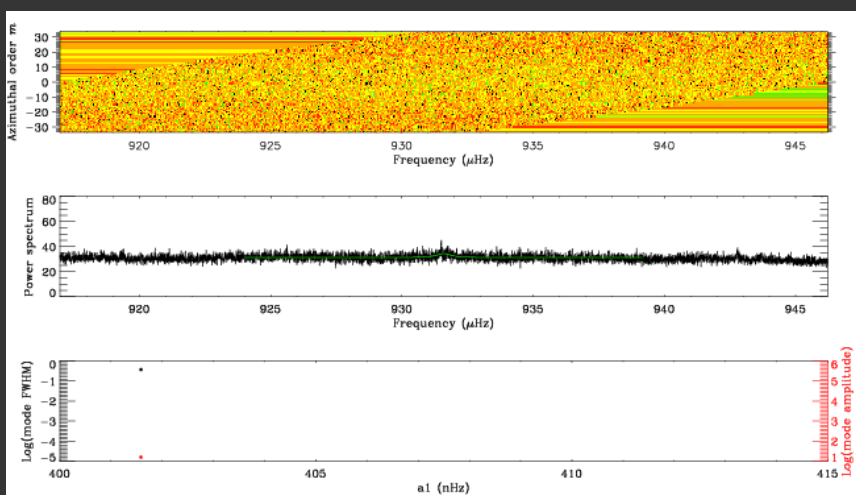
$l = 10, n = 5$ mode at $\sim 1288 \mu\text{Hz}$



$l = 4, n = 4$ mode at $\sim 913.5 \mu\text{Hz}$

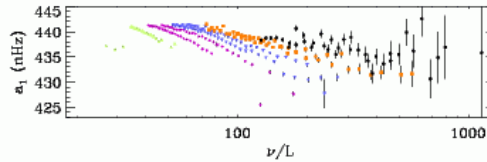
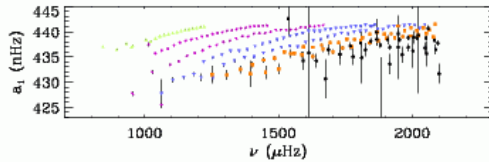


$l = 33, n = 1$ mode at $\sim 931 \mu\text{Hz}$

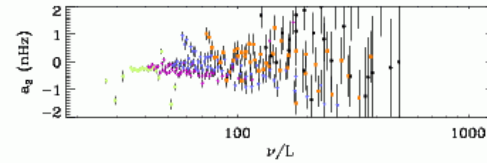
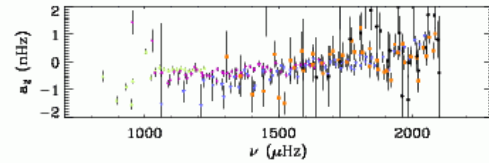


3960 days of GONG data

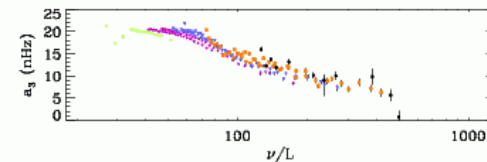
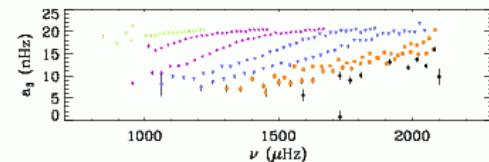
a1



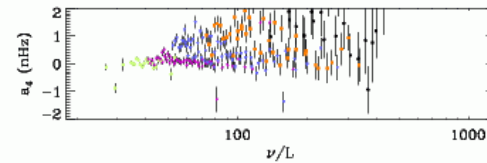
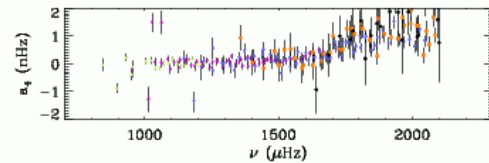
a2



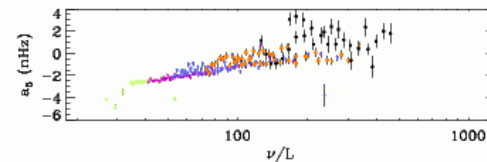
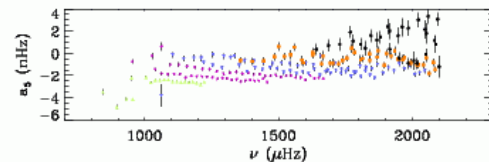
a3



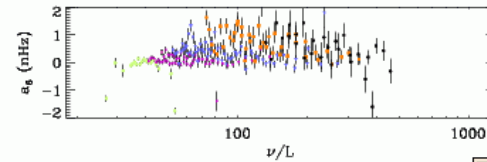
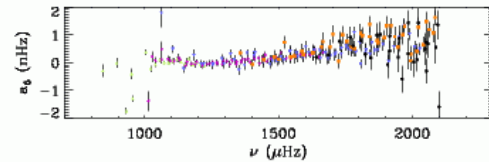
a4



a5



a6



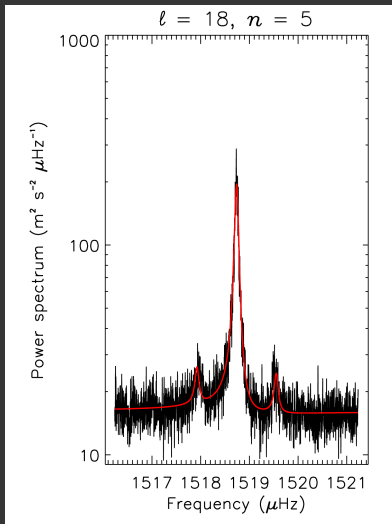
Frequency (ν)

$\nu / \sqrt{l(l+1)}$

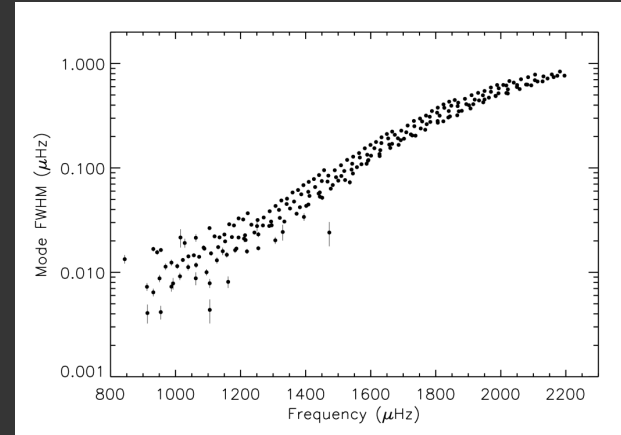
Six first a -coefficients estimated using the m -averaged spectrum technique of the low-frequency p modes ($1 \leq l \leq 35$)

3960 days of GONG data

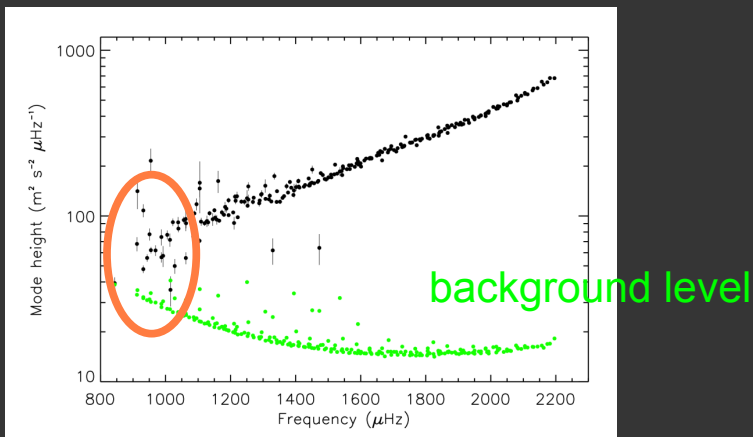
Fitted mode parameters



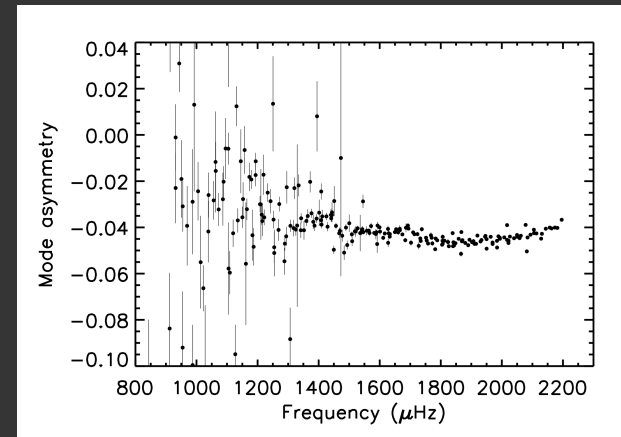
Mode linewidths (FWHMs)



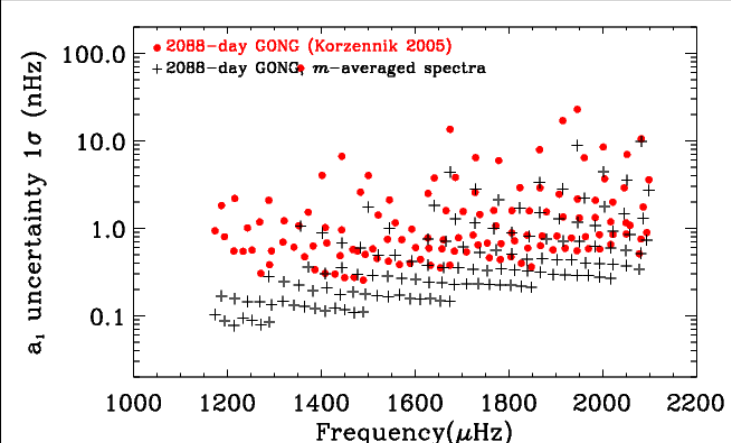
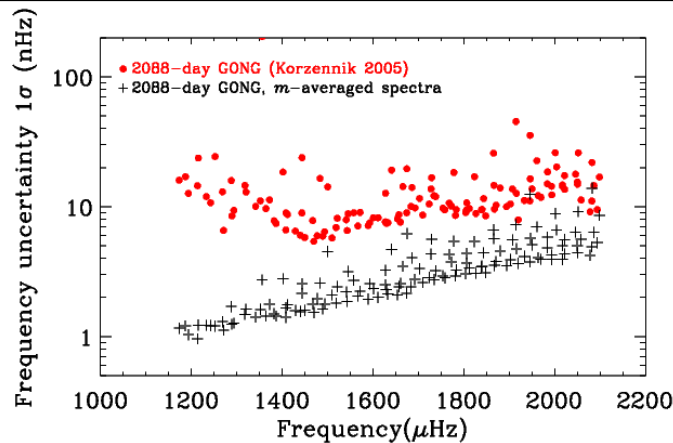
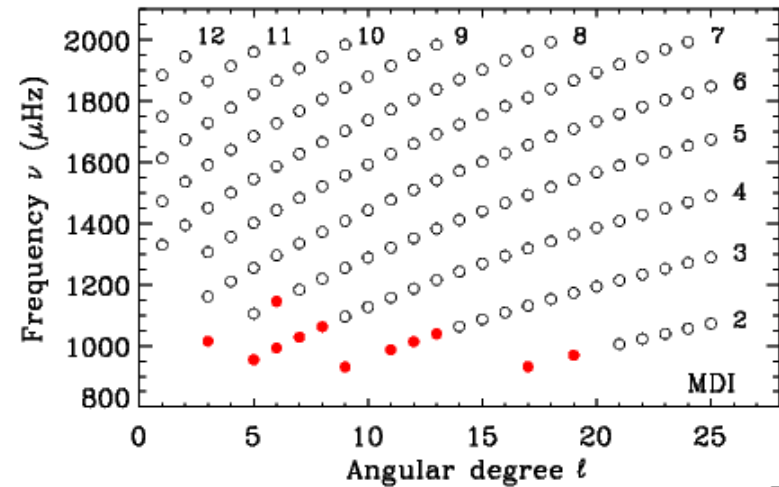
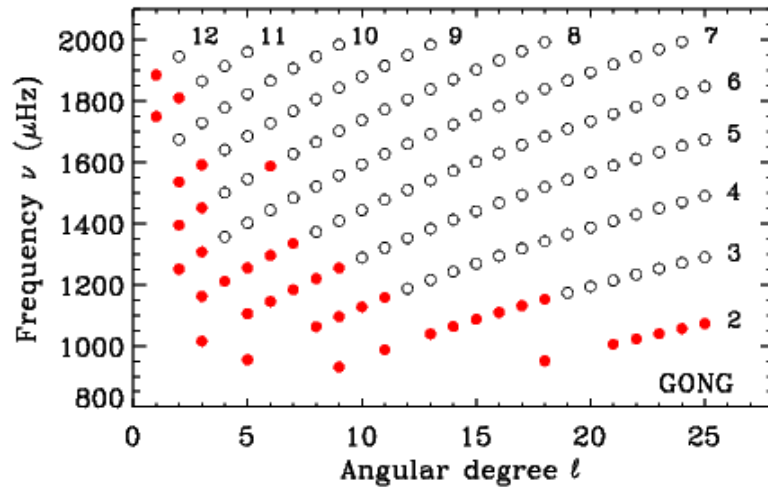
Mode amplitudes



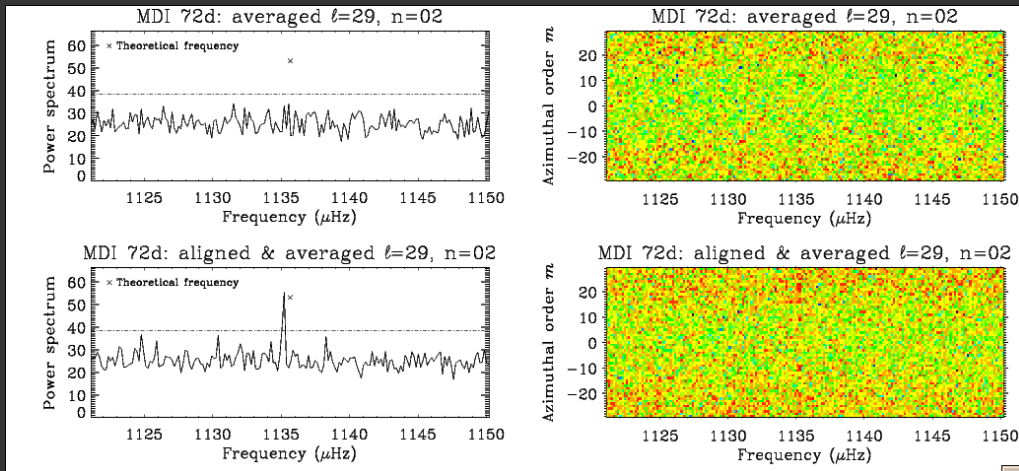
Mode asymmetries



2088-day: comparison with other measurement (Korzennik 2005)

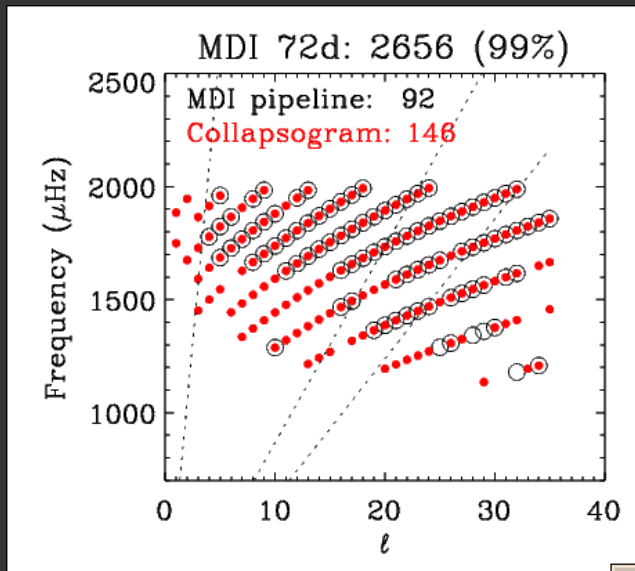


MDI 72-day & GONG 108-day time series

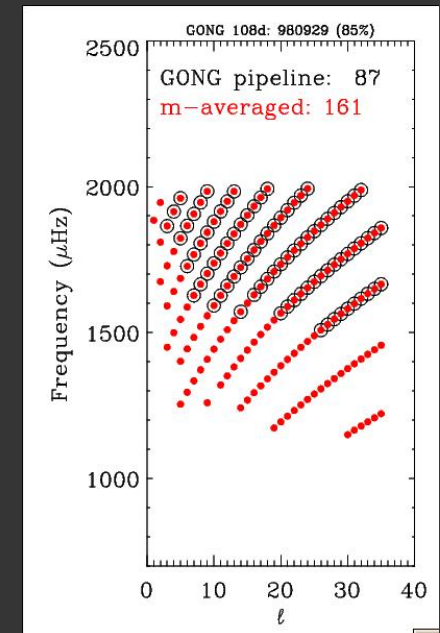


Example of a m -averaged spectrum with 72 days of MDI observations

MDI 72-day time series



GONG 108-day time series



Conclusions

- > New method to measure and fit the low-frequency modes in spatially-resolved data
- > **Lower frequency** where classic peak-fitting methods fail because low SNR
- > **Better precision** of the fitted modes
- > Rotation/Structure: deeper and better resolution throughout the Sun