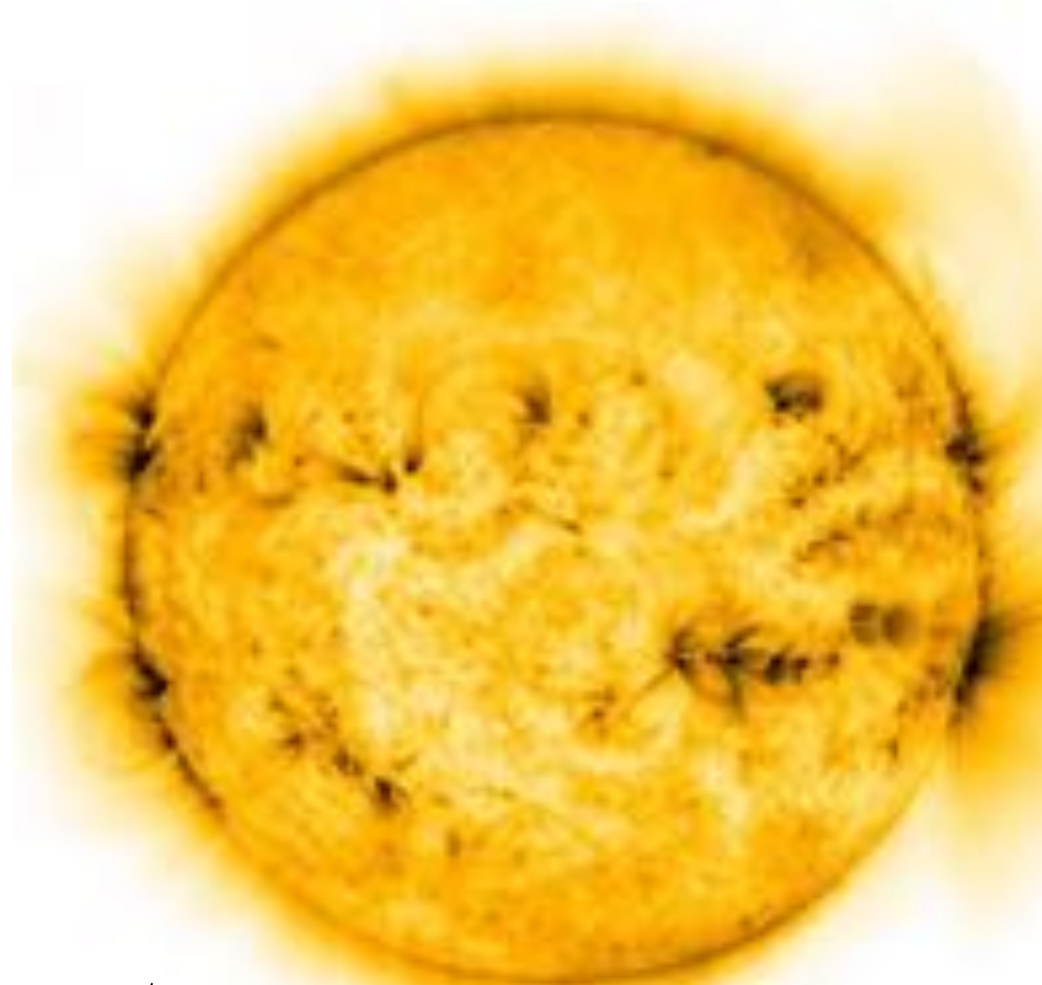


Solar-like magnetic cycles in 3D turbulent global models of stars

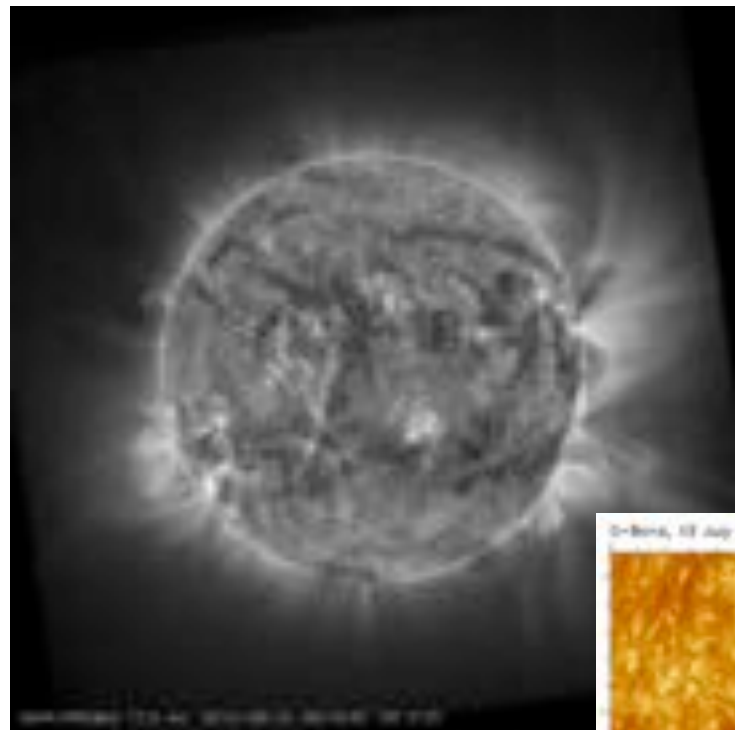
Antoine Strugarek

AIM/IRFU, CEA Saclay, France
Université de Montréal, Canada

*With P. Beaudoin, P. Charbonneau,
P. Smolarkiewicz, A.S. Brun,
J.D. do Nascimento Jr.*



The many scales of solar magnetism

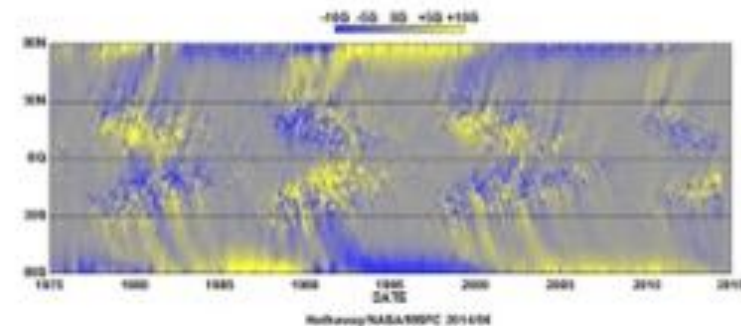


Sun

Size ~ 700 Mm

Rotation ~ month

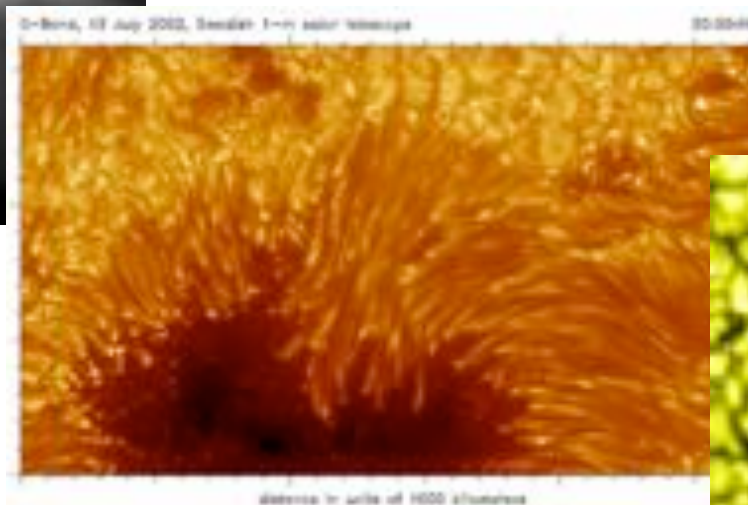
Cycle ~ 11 years



Granules

Size ~ 1 Mm

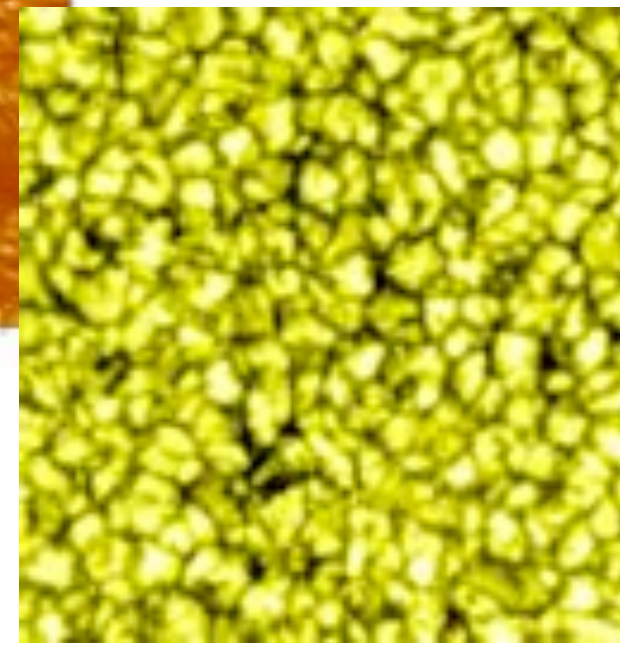
Life ~ 10 minutes



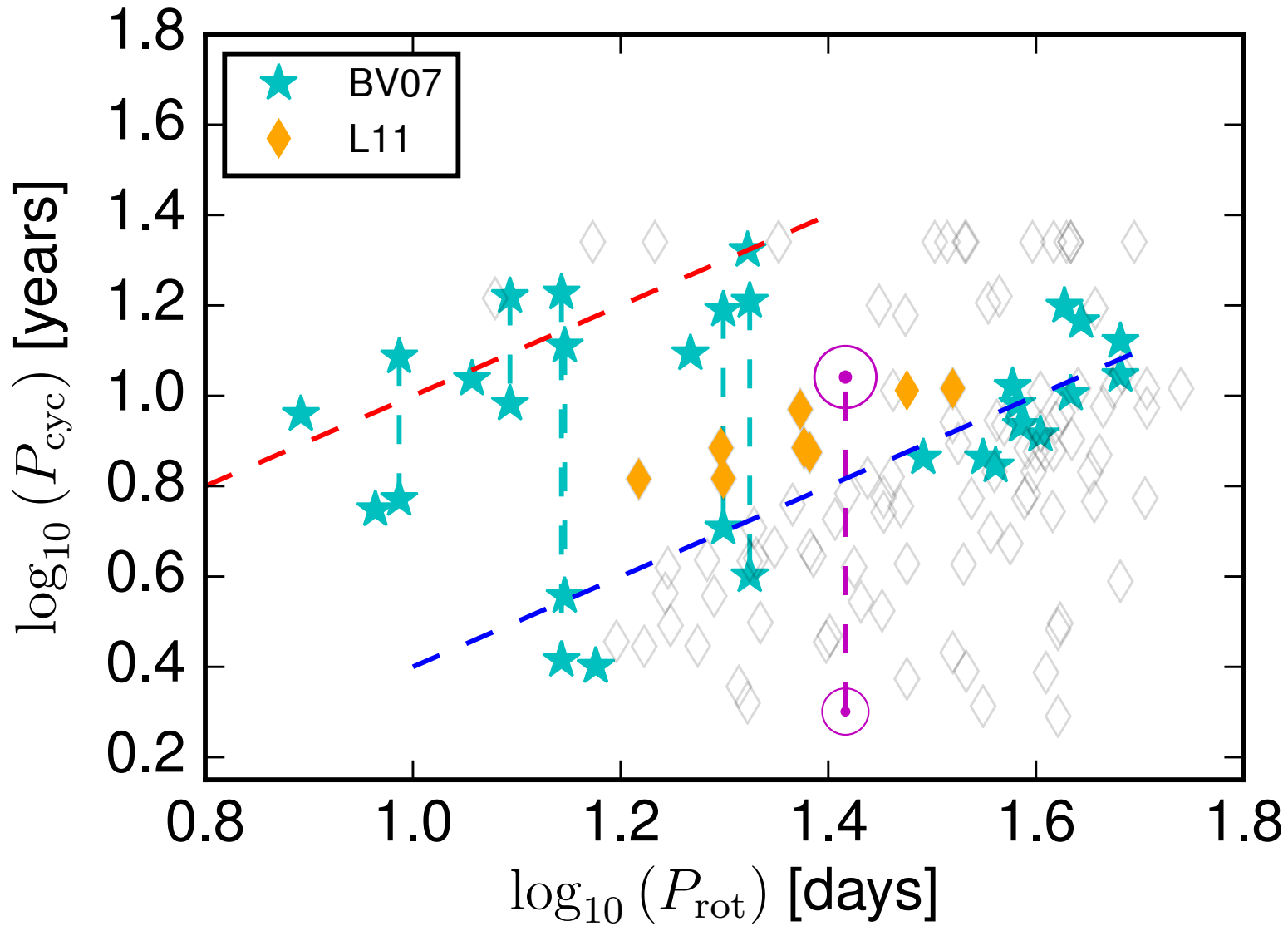
Spots

Size ~ 10 Mm

Life ~ days



The solar cycle in a stellar context

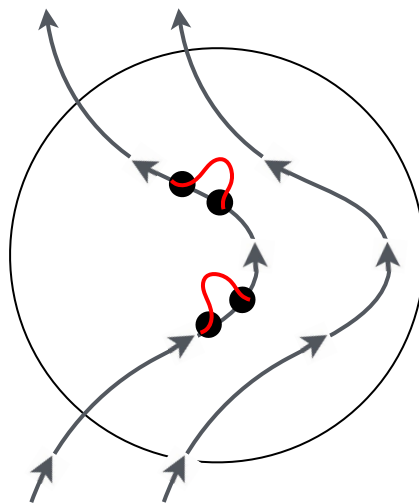
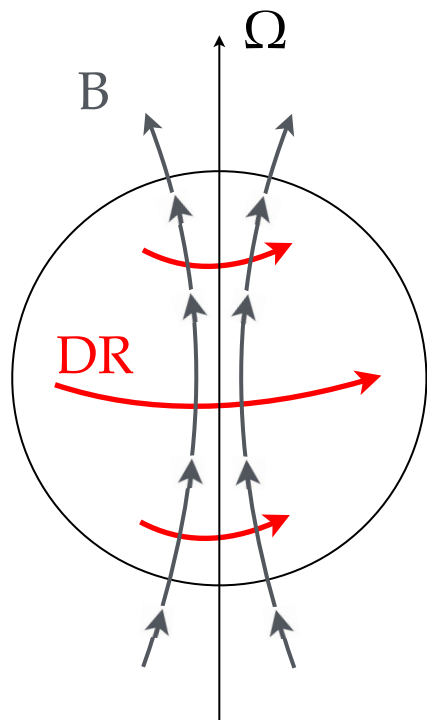


[Noyes et al. 1984; Bohm-Vitense 2007; Saar & Brandenburg 1999; Metcalfe+ 10,13,16; Do Nascimento+ 2015; Egeland+ 15;16]

Classical dynamo picture

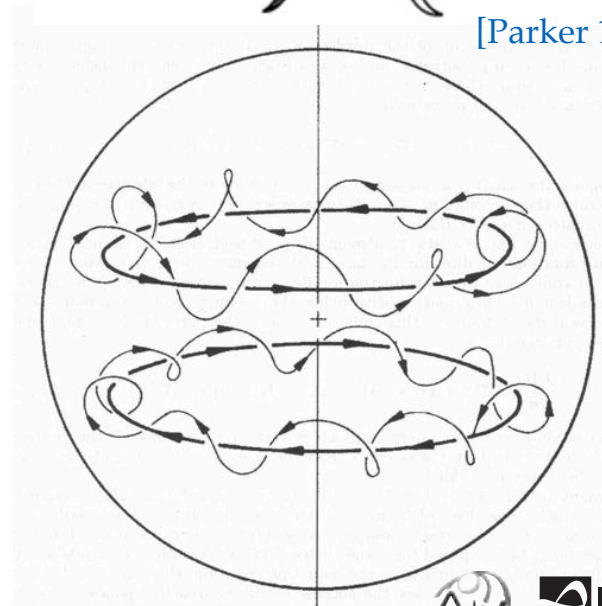
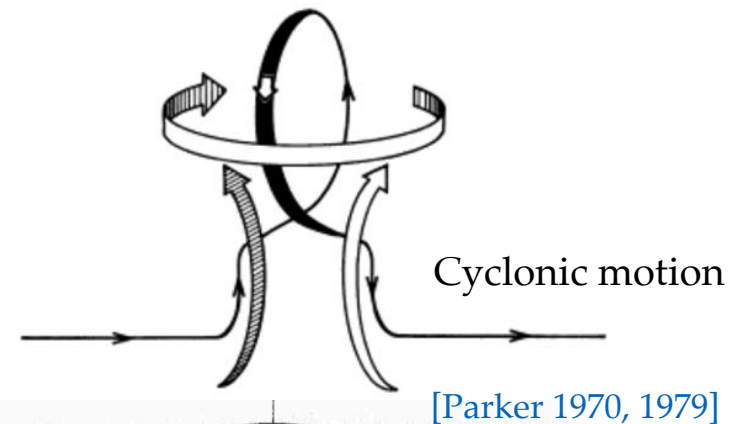
- Cowling's theorem: 3D axisymmetric flows cannot sustain a dynamo action

« Omega » effet: differential axisymmetric rotation easily convert poloidal field to toroidal field



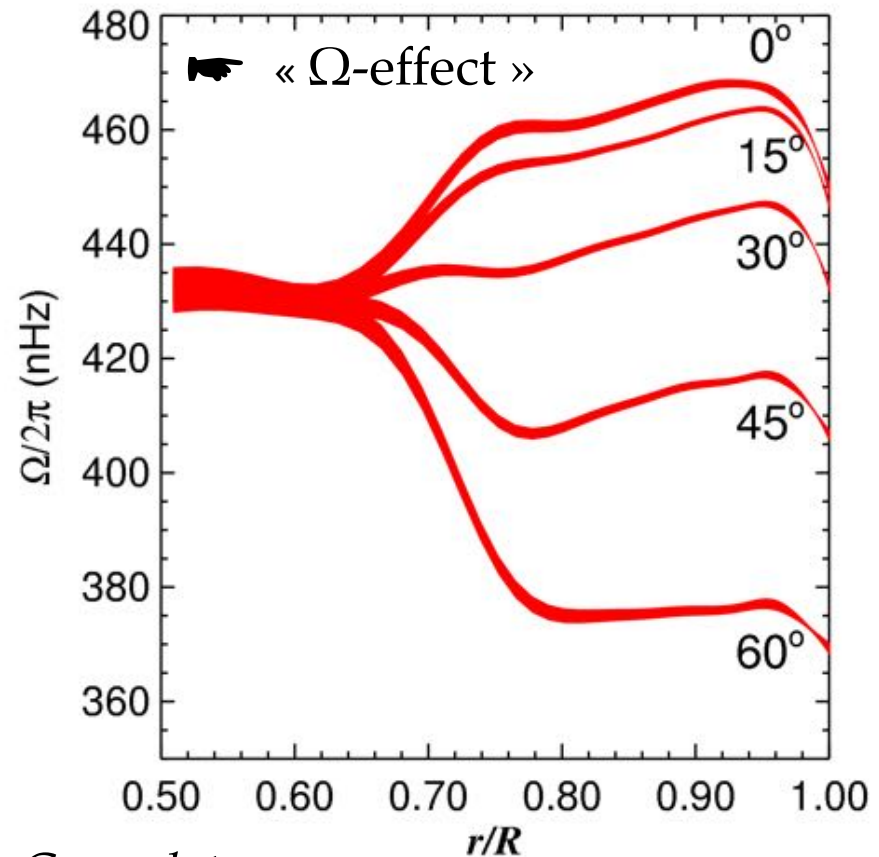
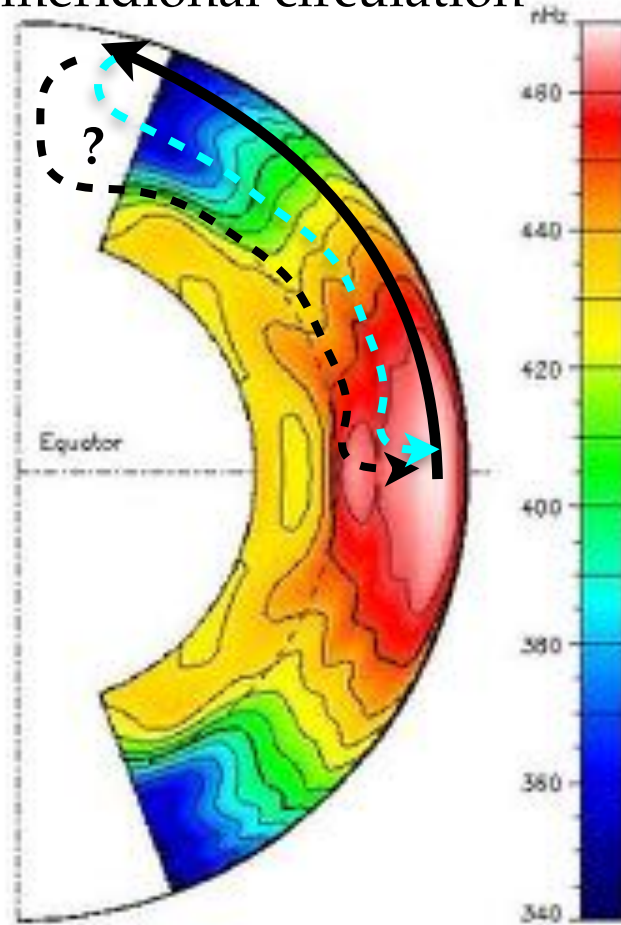
- Joy's and Hale's laws

Toroidal to poloidal conversion



Known ingredients of the solar dynamo

+ some meridional circulation

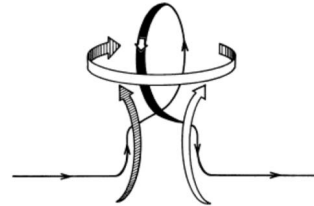


Gong data

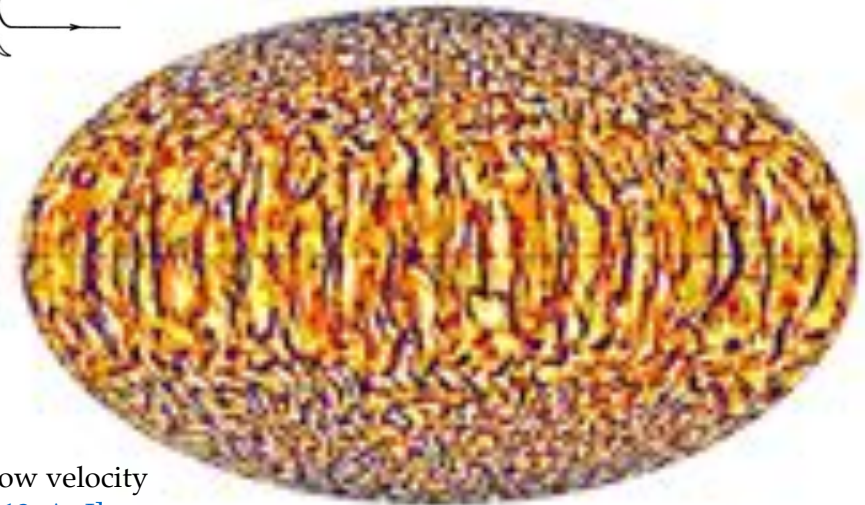
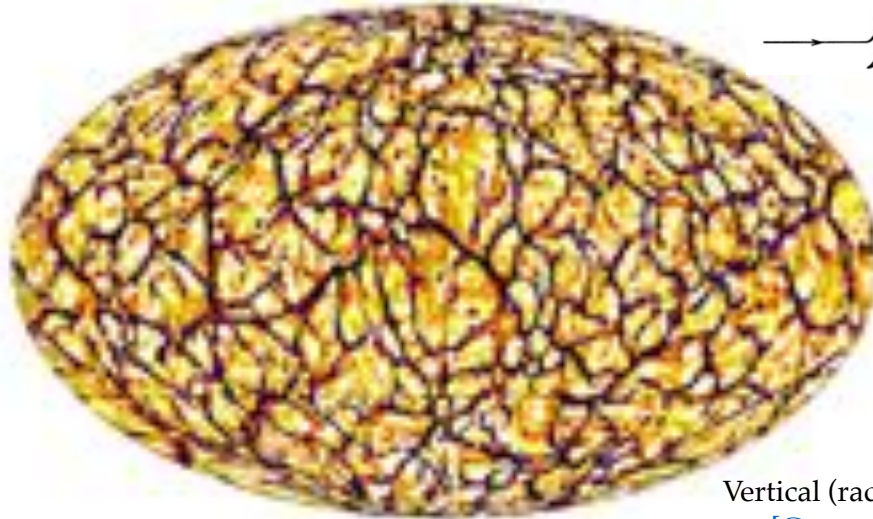
The solar differential rotation: we know the large-scale flow structure of the solar dynamo. It is powered by **Reynolds stresses**, arising from rotationally-induced anisotropy in turbulent transport of momentum and heat

Debated ingredients of the solar dynamo

No rotation



Rotation at solar rate

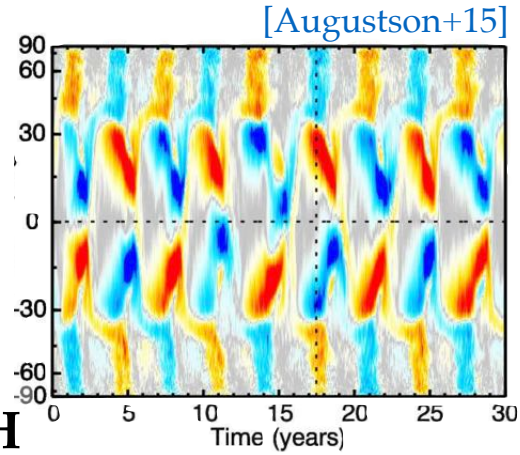
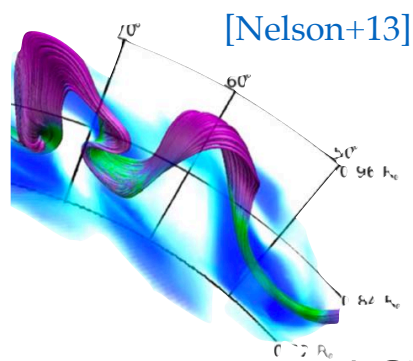
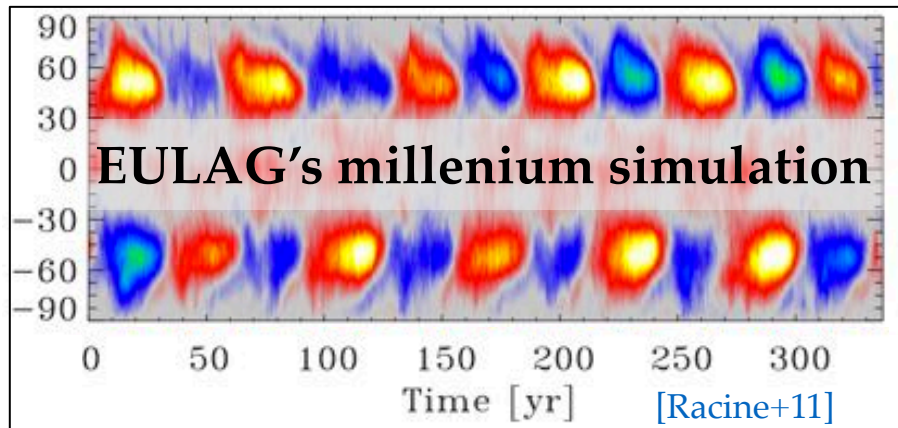


Vertical (radial) flow velocity
[Guerrero+ 2013, ApJ]

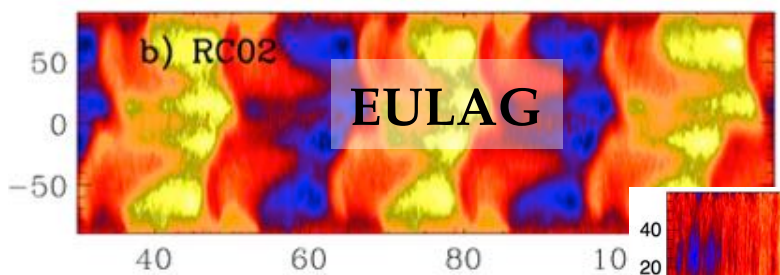


Turbulent anelastic convection under the influence of rotation is cyclonic and can *a priori* close the dynamo loop

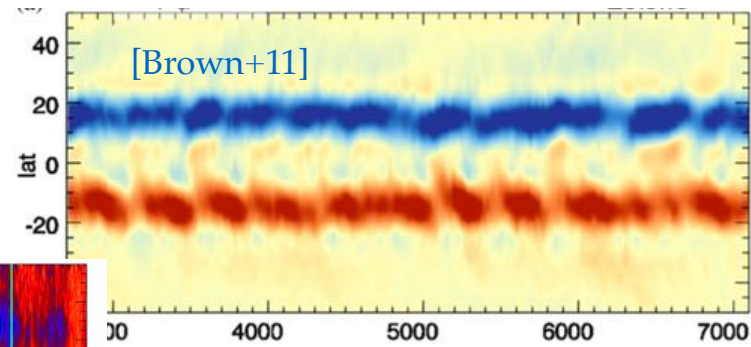
The zoo of 3D models...



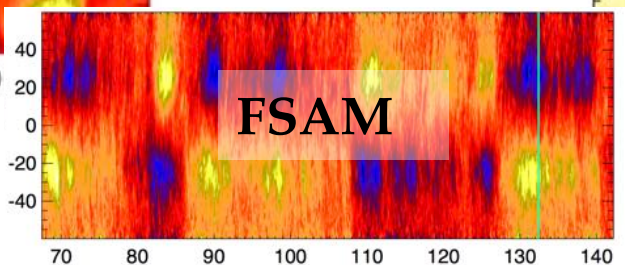
[Guerrero+16]



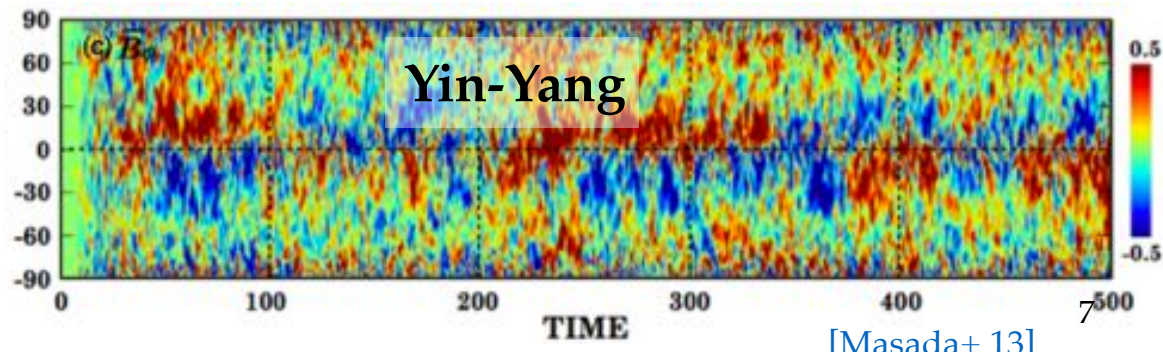
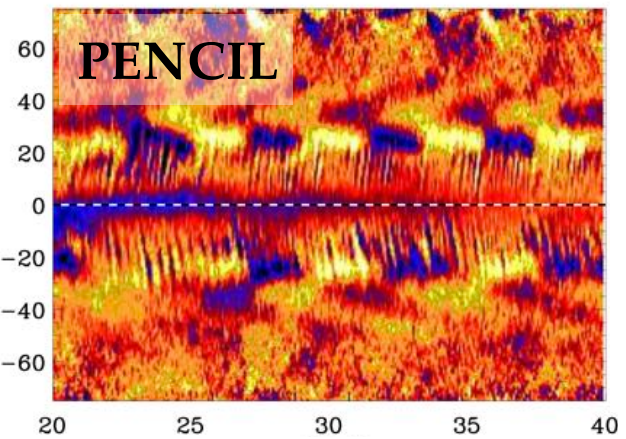
and much more...



[Fan+14]



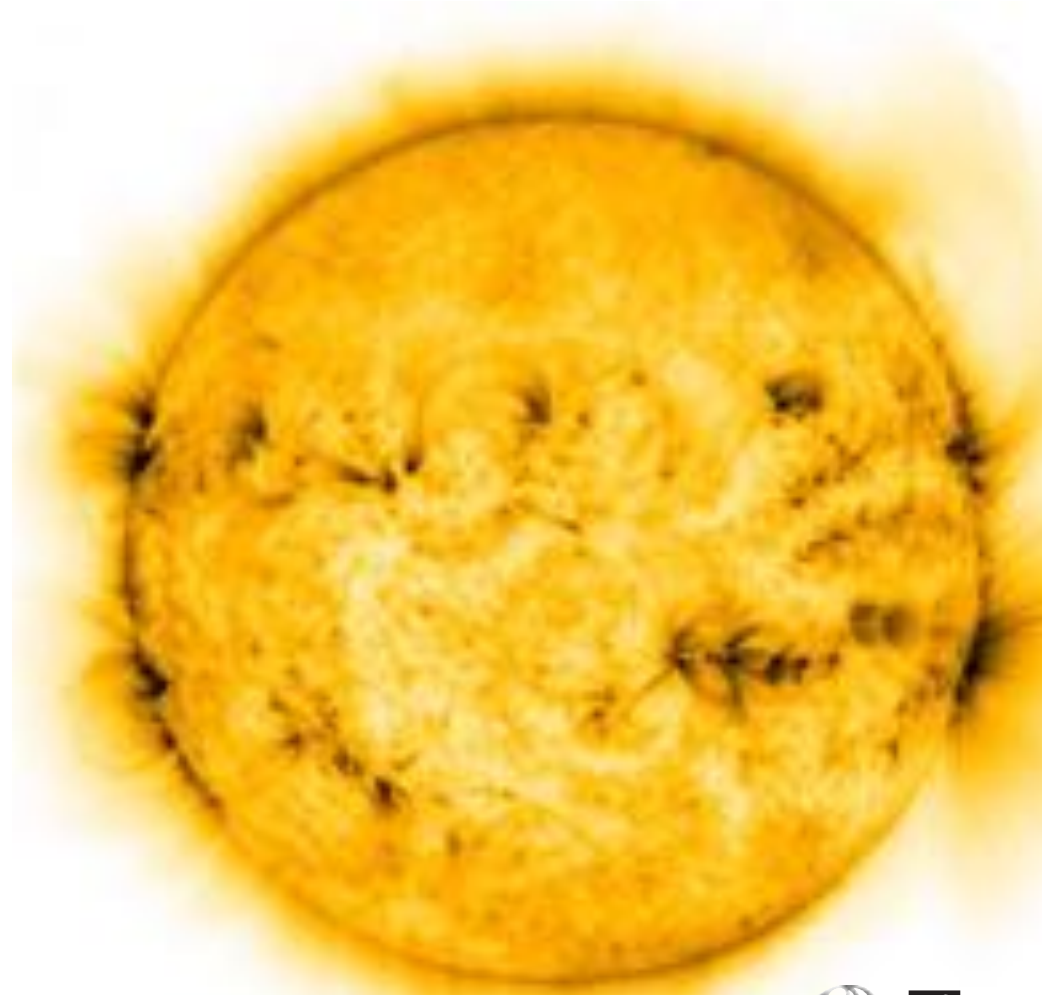
[Kapyla+12,Warnecke+14]



[Masada+13]

What sets the magnetic cycle periods in (solar-like) stars?

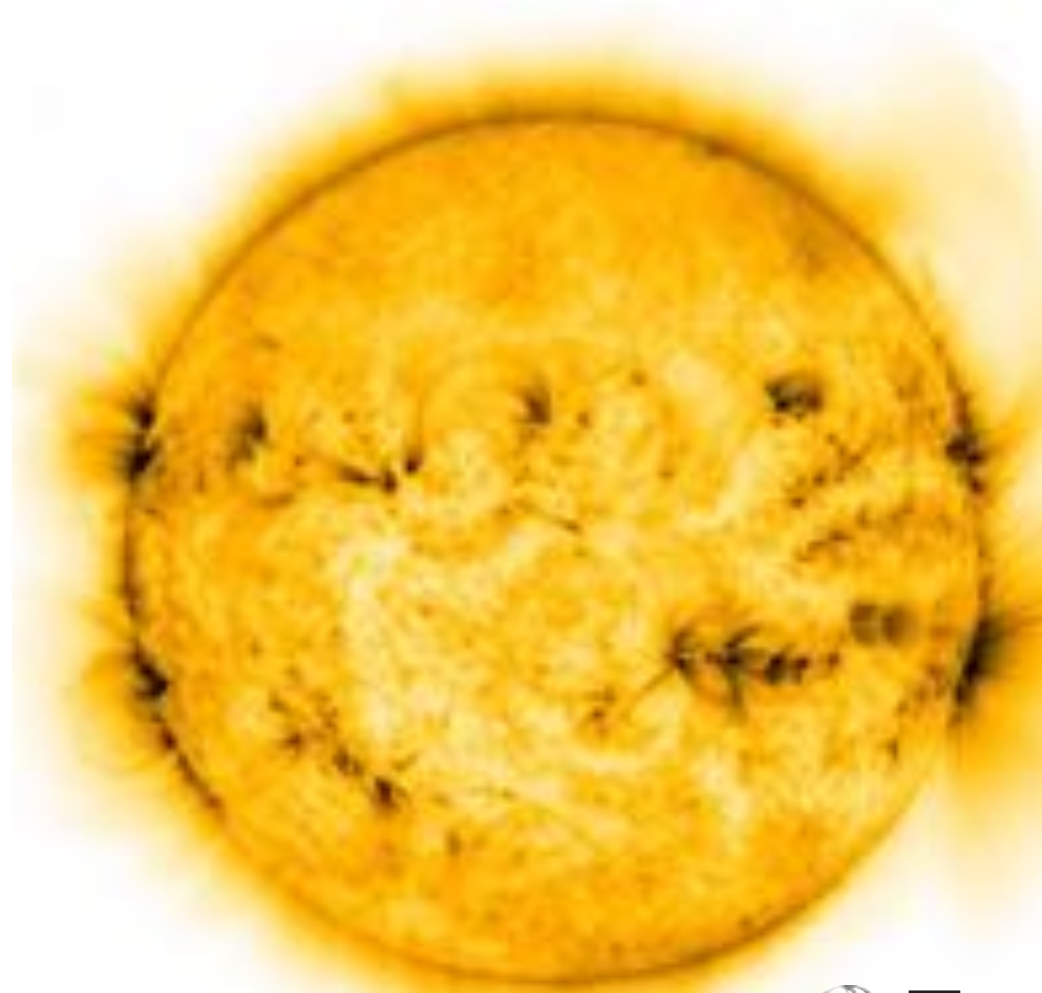
Strugarek+ 2017, submitted



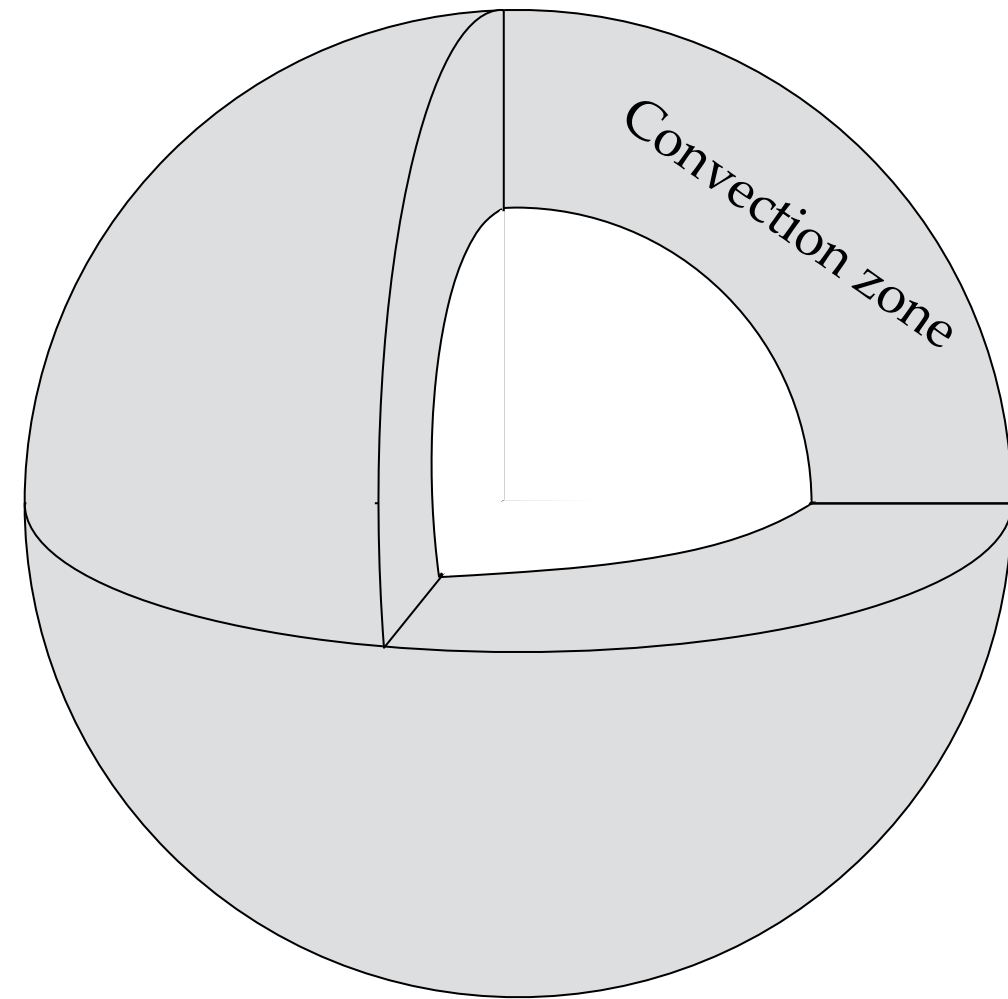
some global 3D models

What sets the magnetic cycle periods in ~~(solar-like) stars?~~

Strugarek+ 2017, submitted



Tool: the EULAG-MHD code

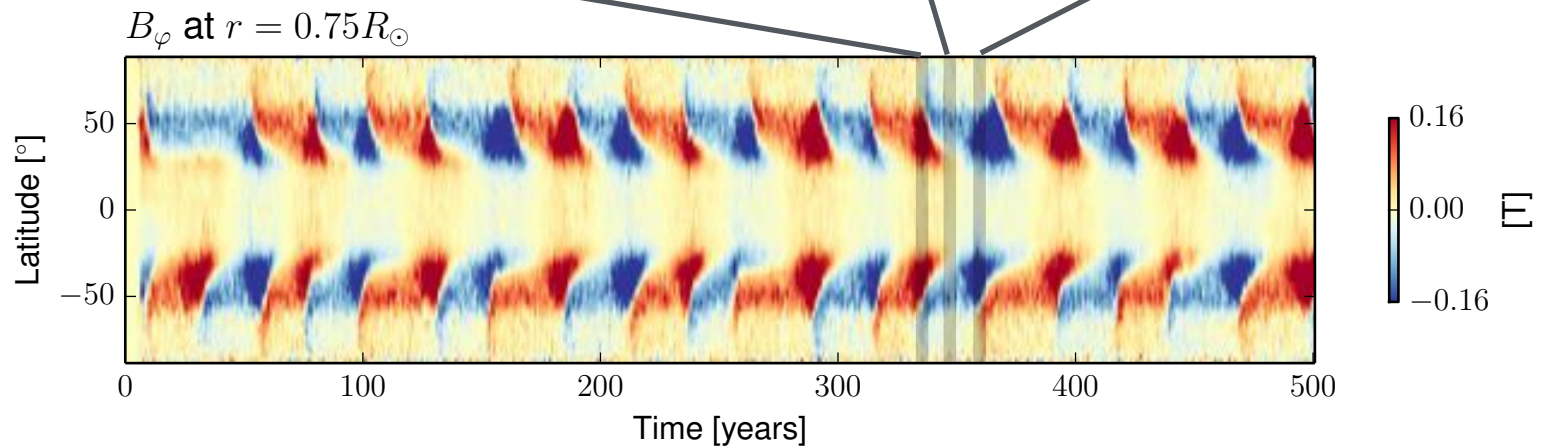
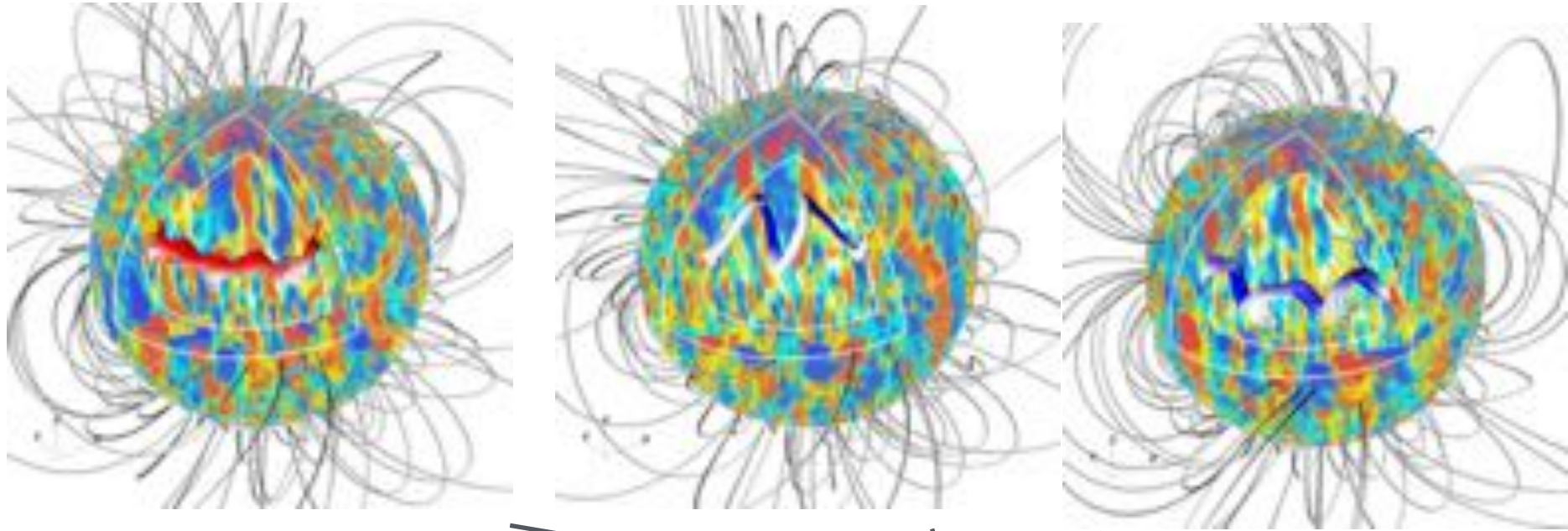


Core advection scheme:
MPDATA, a minimally
dissipative iterative upwind
NFT scheme; equivalent to a
dynamical, adaptive subgrid
model

Convective instability,
superadiabatic ambient profile
combined with Newtonian
cooling in energy equation

[Smolarkiewicz & Charbonneau 2013, JCP]

Prototype cyclic dynamo in a convective envelope

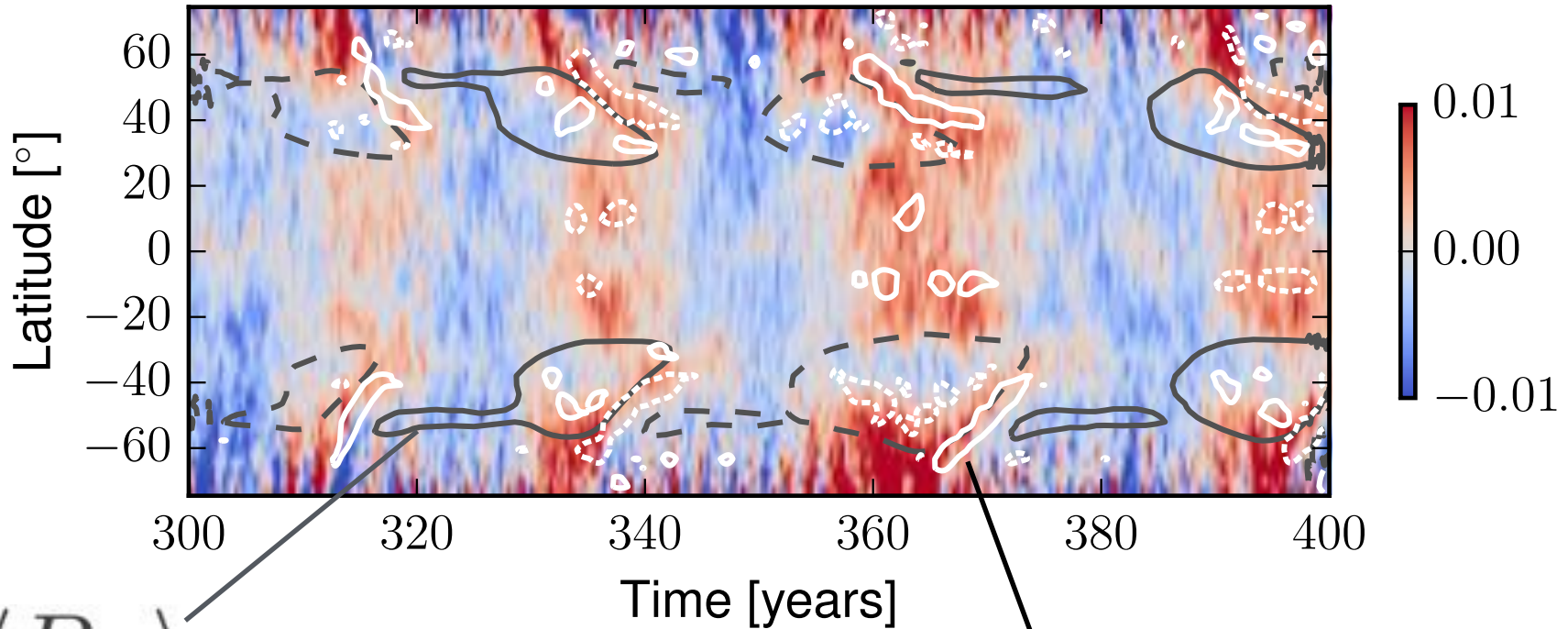


$R_o \sim 0.34$
 $N_p = 3.2$
 $\Delta S = 10^4 \text{ erg/K/g}$

No stable radiative zone

Perturbations of the differential rotation drive the dynamo

$$\delta\Omega = (\Omega - \langle\Omega\rangle_t) / \langle\Omega\rangle_t \text{ at } r = 0.75R_\odot$$

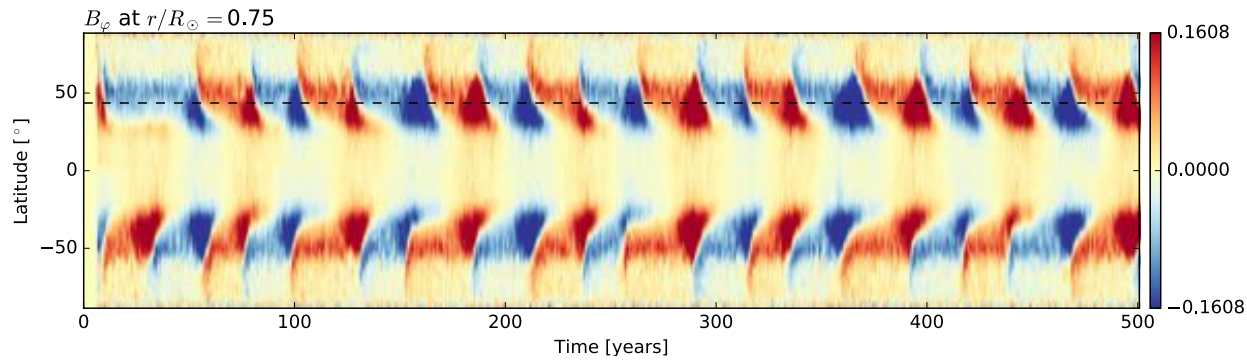


$\langle B_\varphi \rangle$

$$\partial_t \langle B_\varphi \rangle = \nabla \times ((\langle \mathbf{U}_\varphi \rangle \times \langle \mathbf{B}_{\text{pol}} \rangle)|_\varphi$$

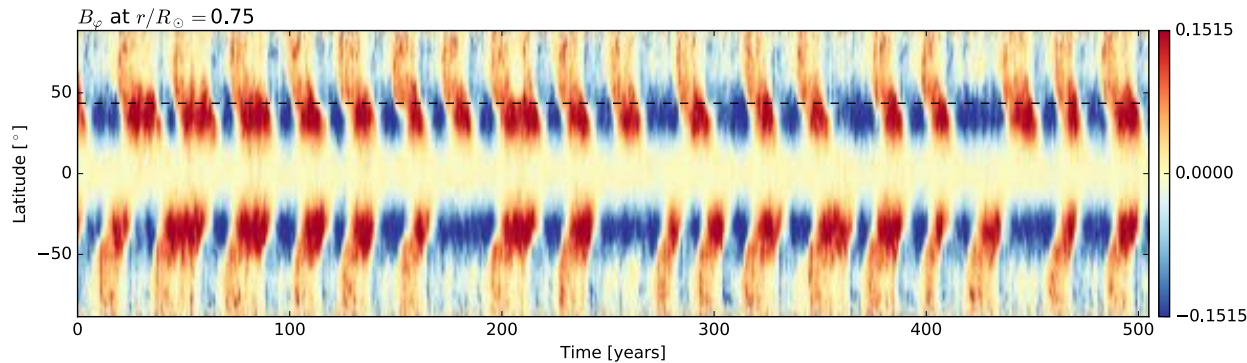
Systematic modulation of the cycle period

Ref.



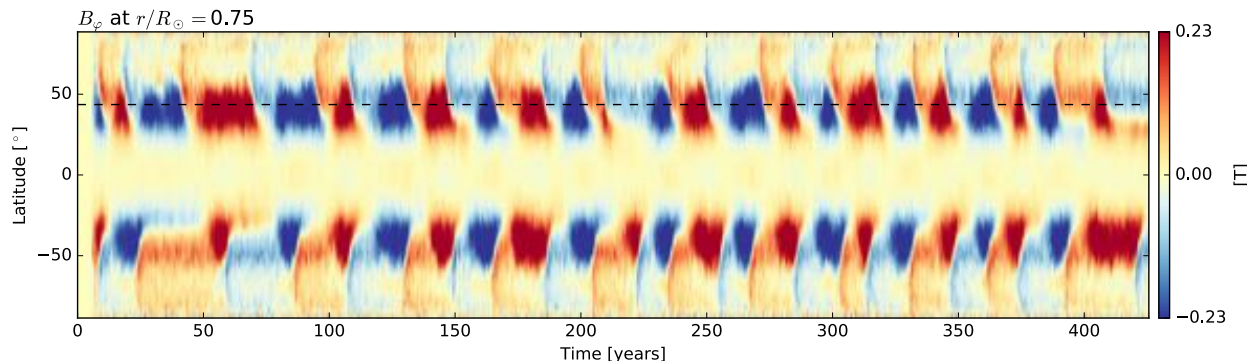
$P_{\text{cyc}} = 28 \text{ yrs}$

$\Omega/2$



$P_{\text{cyc}} = 13 \text{ yrs}$

Lum. $\times 2$



$P_{\text{cyc}} = 17 \text{ yrs}$

Cycle period is inversely proportional to the Rossby number

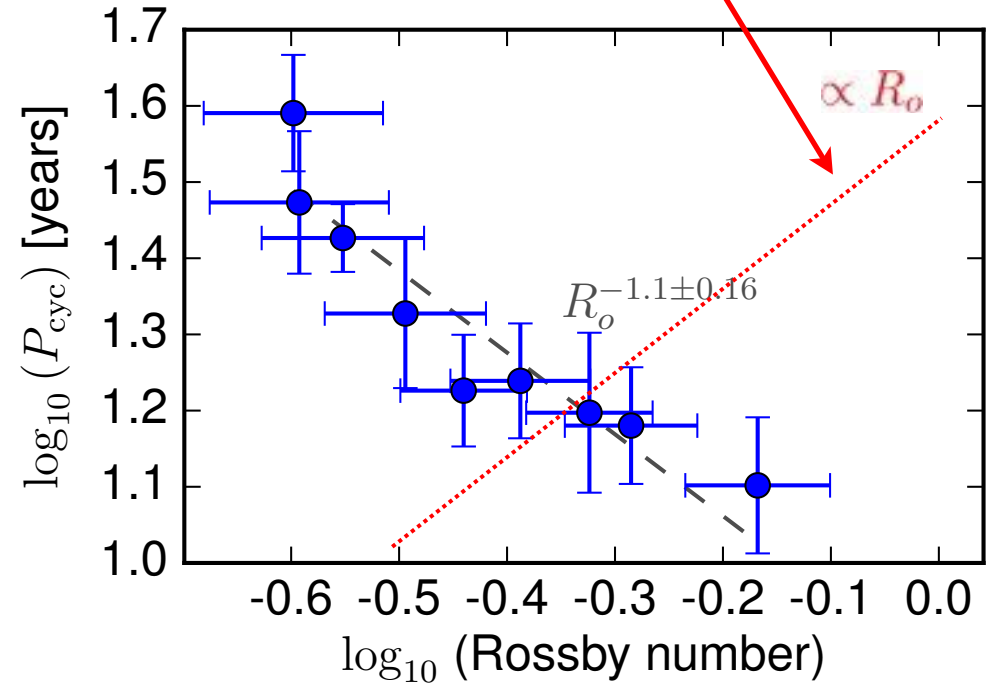
Basic linear $\alpha\Omega$ kinematic dynamo theory

Basic ingredients of stellar dynamos

- Differential rotation
- Cyclonic turbulence

'Go to' parameter is the **Rossby number**

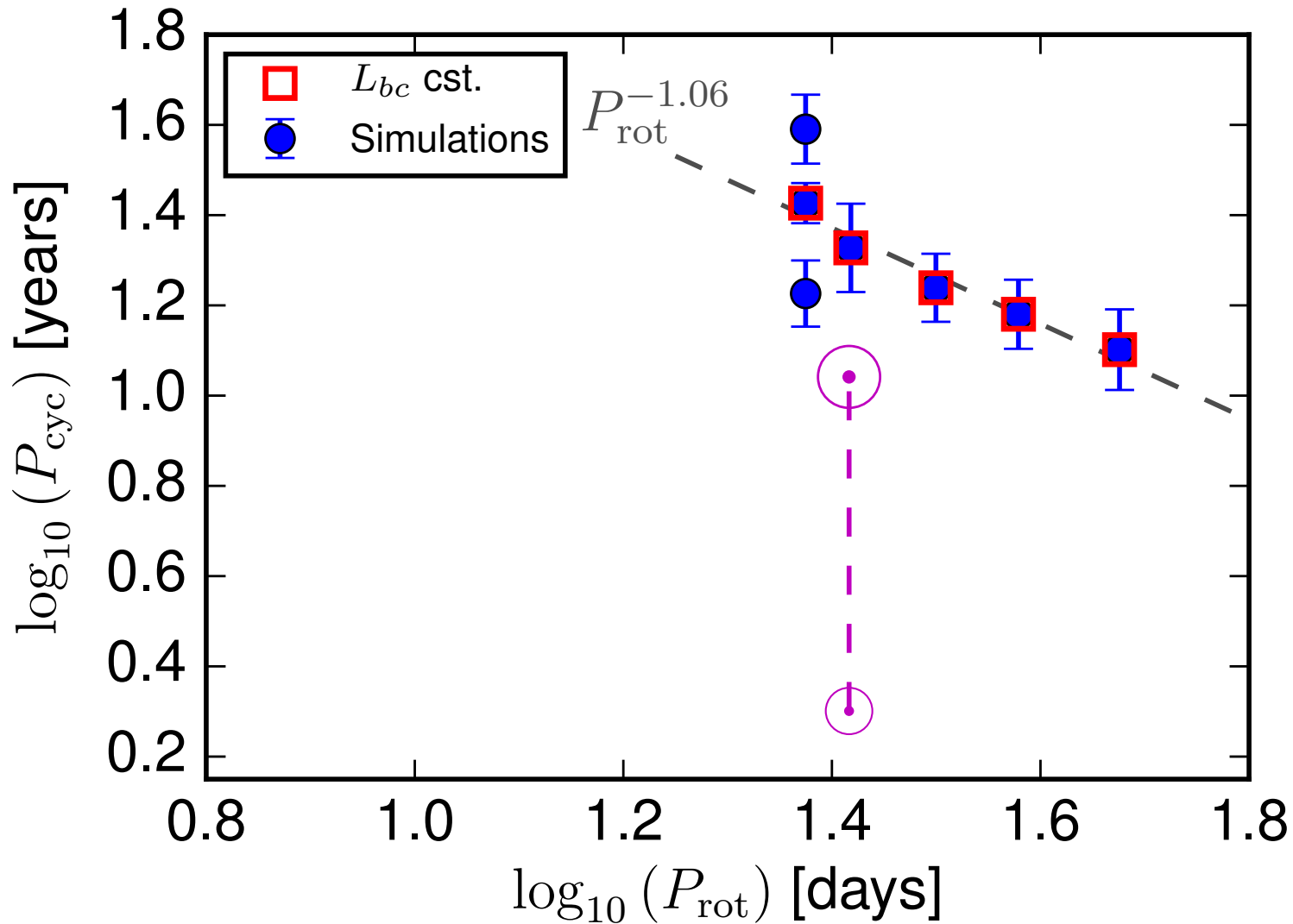
$$R_o = \frac{\text{NL Advection}}{\text{Coriolis}} \sim \frac{|\nabla \times \mathbf{U}|}{2\Omega_\star}$$



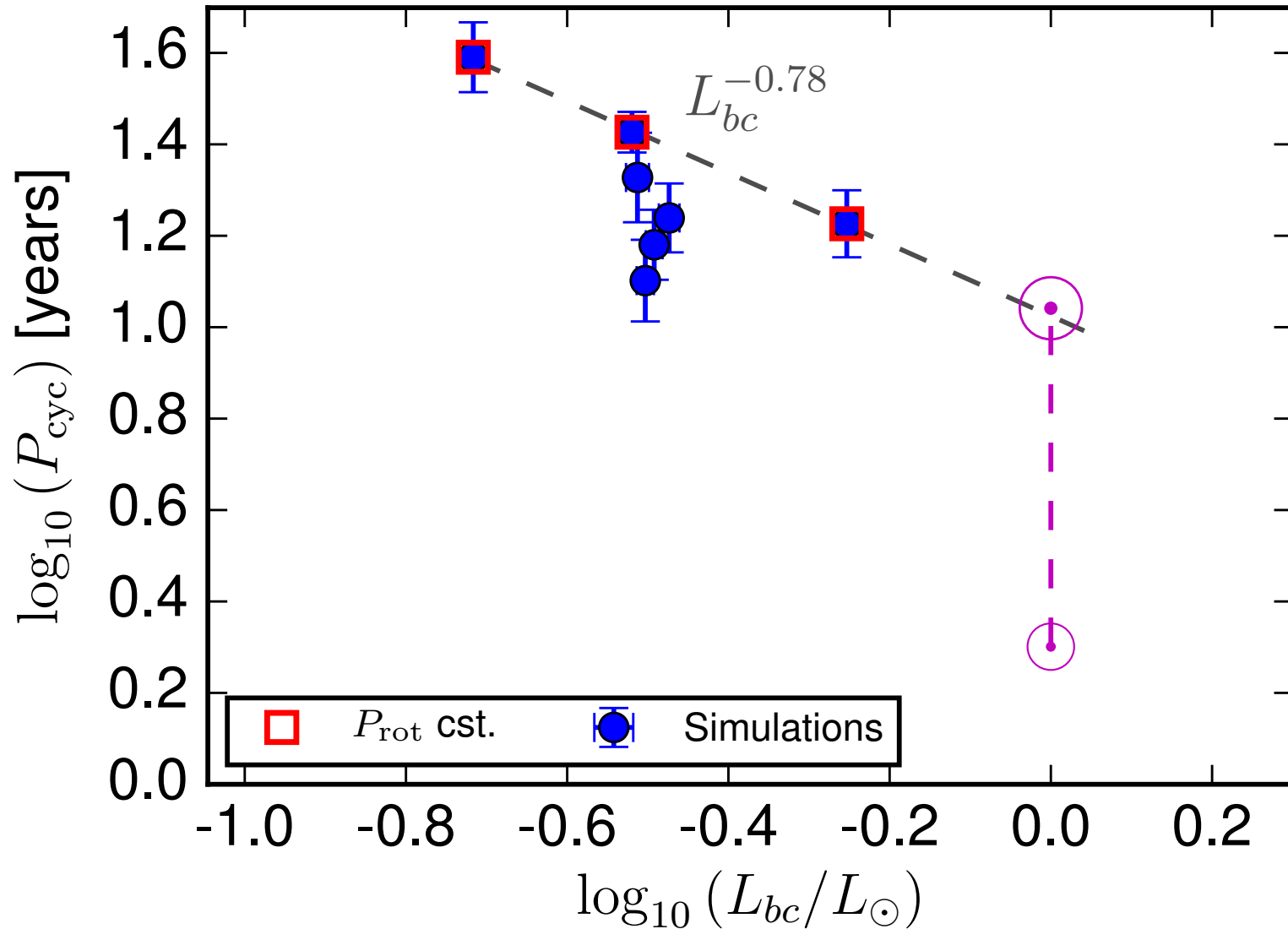
**Fundamentally non-linear convective dynamo:
not a classical dynamo wave**

How does this relate to the Sun?

Cycle period — Rotation period diagram



Cycle period — Luminosity diagram



Conclusions

Global, non-linear 3D turbulent simulations have been very useful in the past decade to refine our understanding of the dynamics of magnetized stellar convection zones

Such simulations produced a **large variety of solutions** over the past decade: **large-scale field self-organization, reversals, and magnetic cycles.**

New result: a non-linear dynamo producing a **stable cycles**, with a period varying systematically with luminosity and rotation period, **agreeing with the solar cycle period.** It suggests a new paradigm with the **cycle period proportional to the inverse of the Rossby number.**

All the simulations worldwide are today still very far from stellar turbulent regime...

Thank you for your attention

