

# Rotational periods and evolutionary models for subgiant stars

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## **Angular Momentum of Cool Stars:**

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- ✓ Subgiant sample and time series analysis
- ✓ Evolutionary models and rotational periods
- ✓ Results
- ✓ Conclusions

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**Astronomy  
&  
Astrophysics**

LETTER TO THE EDITOR

**Rotational periods and evolutionary models for subgiant stars  
observed by CoRoT<sup>★,★★</sup>**

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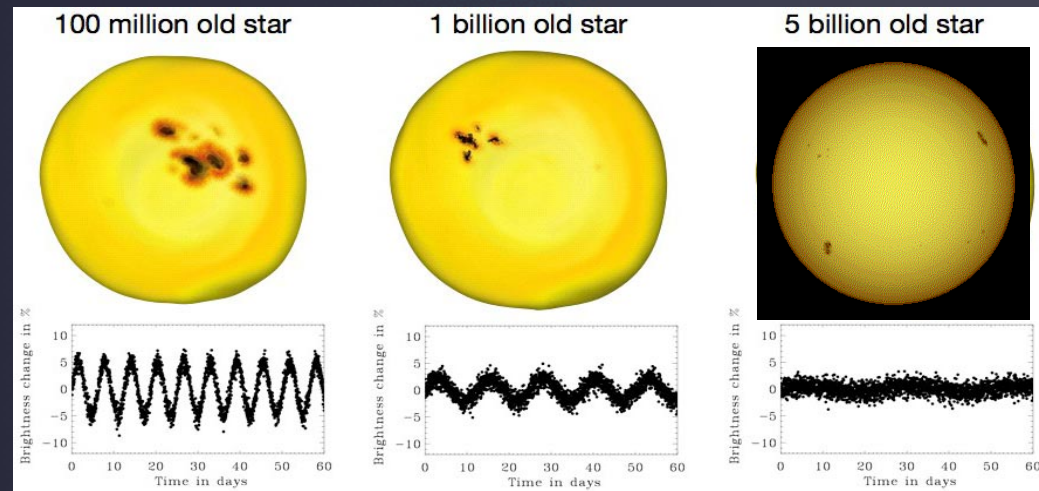
Received 11 June 2012 / Accepted 23 October 2012

# Rotation

- Fundamental stellar property
- Intimately related
  - generation of magnetic field and magnetic activity
  - Loss of mass
  - Interior structure, mixing, chemical evolution...

## Challenger task

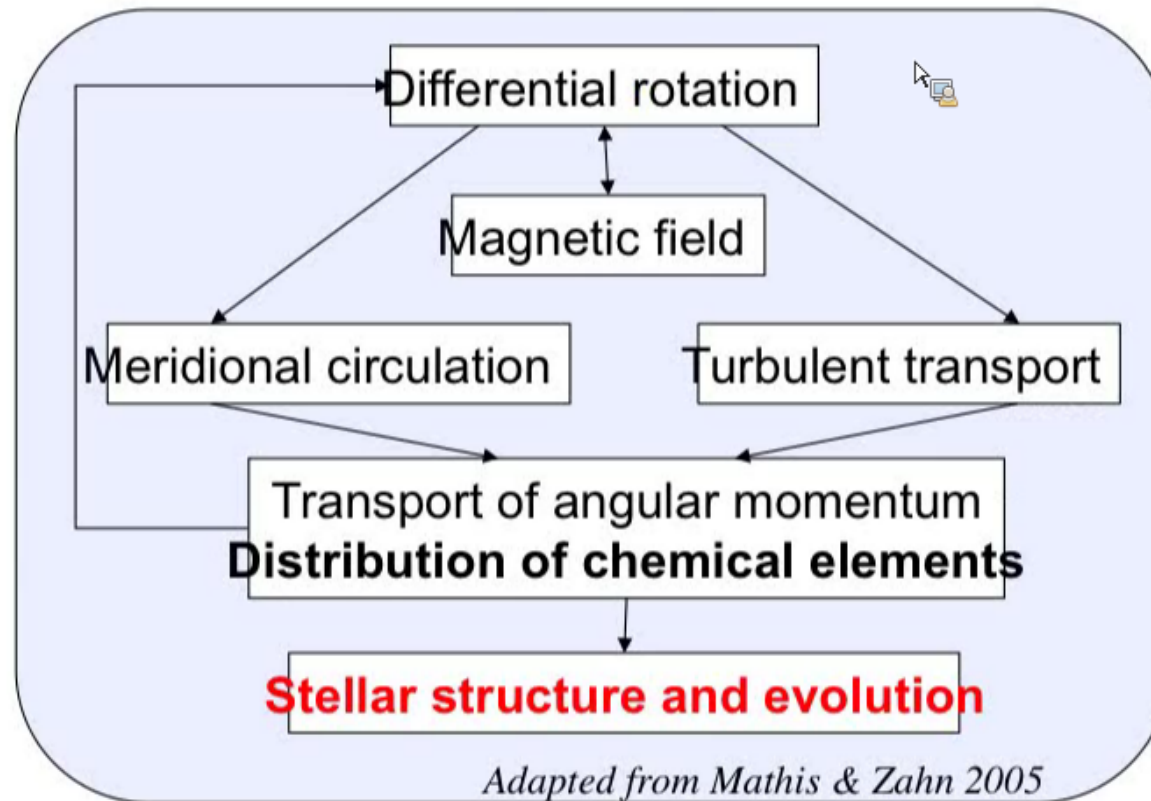
### Measuring the spin rates for old stars



KEPLER / Søren Meibon, ApJL 733 L9. 2011

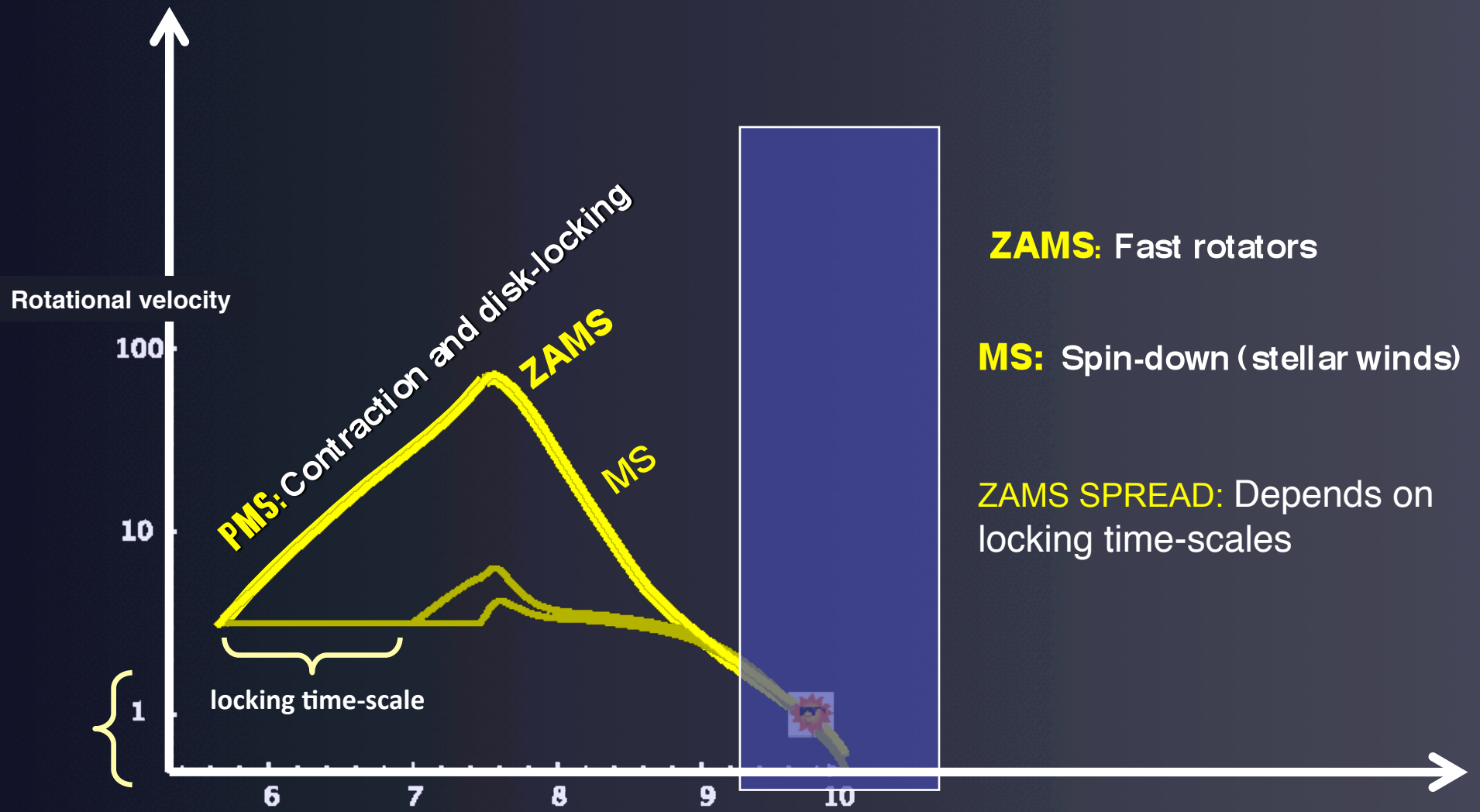


# Rotation and stellar evolution



Complex role in our understanding of stellar structure and evolution





**ZAMS:** Fast rotators

**MS:** Spin-down (stellar winds)

**ZAMS SPREAD:** Depends on locking time-scales

Long Periods  
(Prot)

Time in log (age)

**CoRot** and KEPLER Contribution

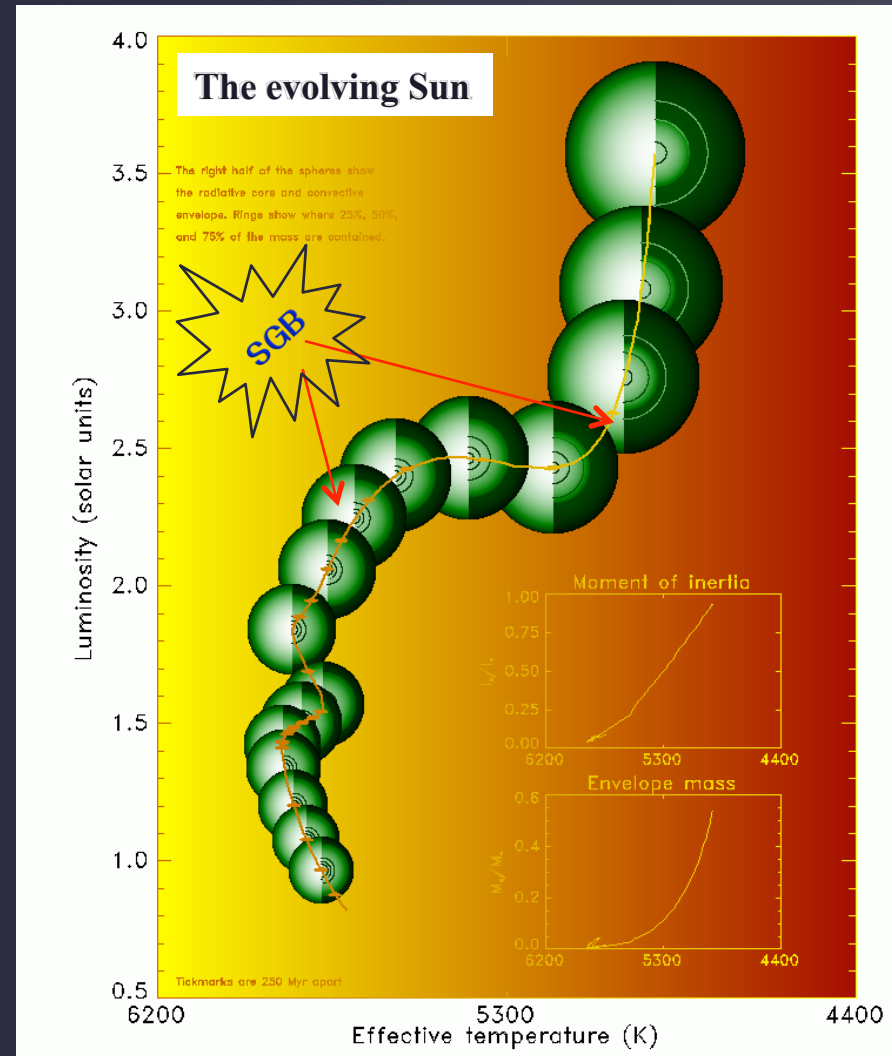
Long Rot Periods

low  $V_{\text{sin}i}$



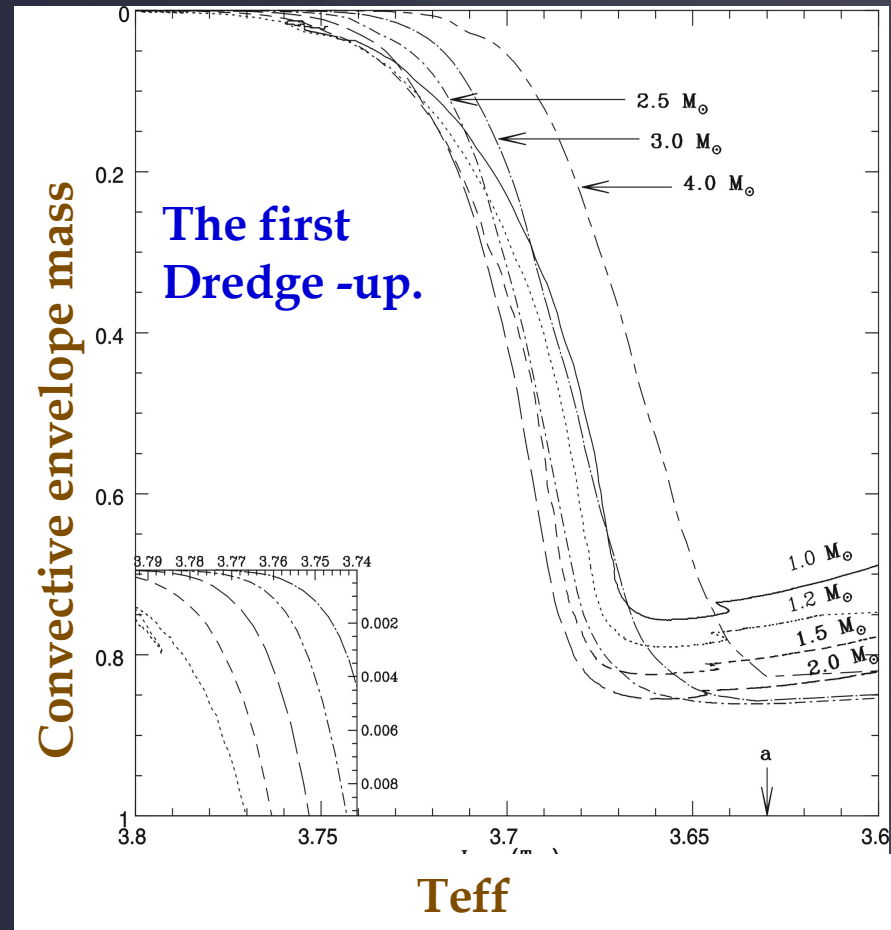
# Why subgiants...

- ✓ A known rare class of objects
- ✓ Dating purpose
- ✓ Associated with rotation periods ( $P_{rot}$ )  $\rightarrow$  stellar gyrochronology
- ✓ Small range of masses
- ✓ F-type subgiants are important for studying solar-like oscillations



# Why subgiants...

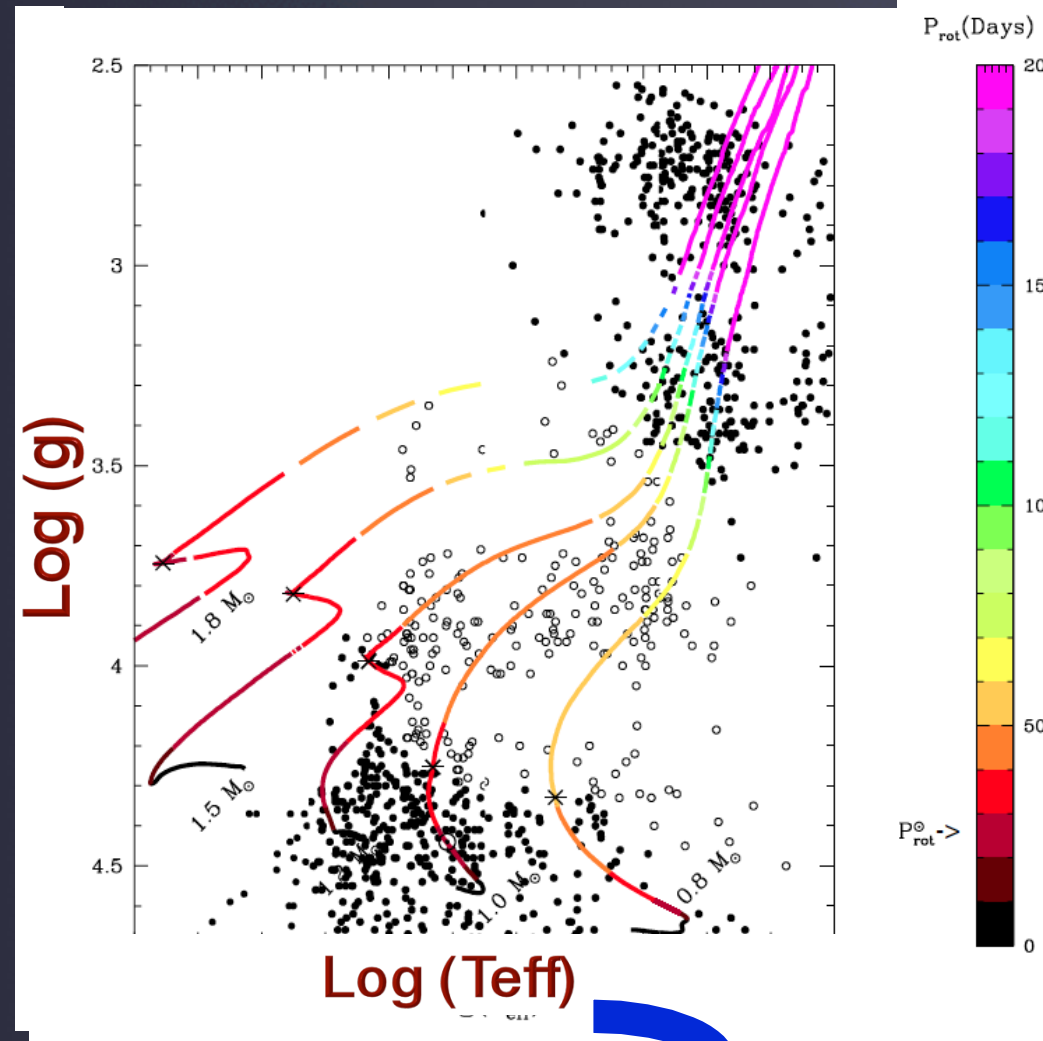
- ✓ Subgiant branch: their surface convection zone becomes deeper.
- ✓ The matter that resided below the surface convection zone at the MS is then exposed.
- ✓ The Prot of subgiant stars could constrain the interior angular momentum distribution and mixing in low-mass stars.





# CoRoT Subgiant stars

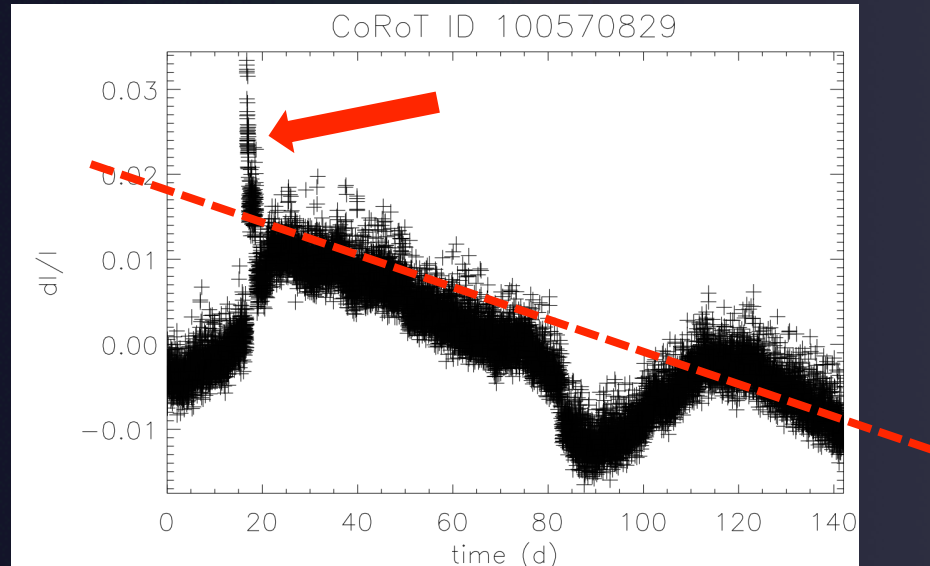
- 196 subgiants classified as subgiants by Gazzano et al. (2010)
- CoRoT Exo-dat (Deleuil et al. 2006; 2009; Meunier et al. 2007)
- Public data level 2 (N2) delivered by the CoRoT pipeline after nominal corrections (Samadi et al. 2006).
- Teff, logg, [M/H], vsini from Matisse (Recio-Blanco et al. 2006)



Infrared JHK 2MASS band  
 $c_1, c_2, c_3$  e  $c_4$  (Catelan et al. 2011)

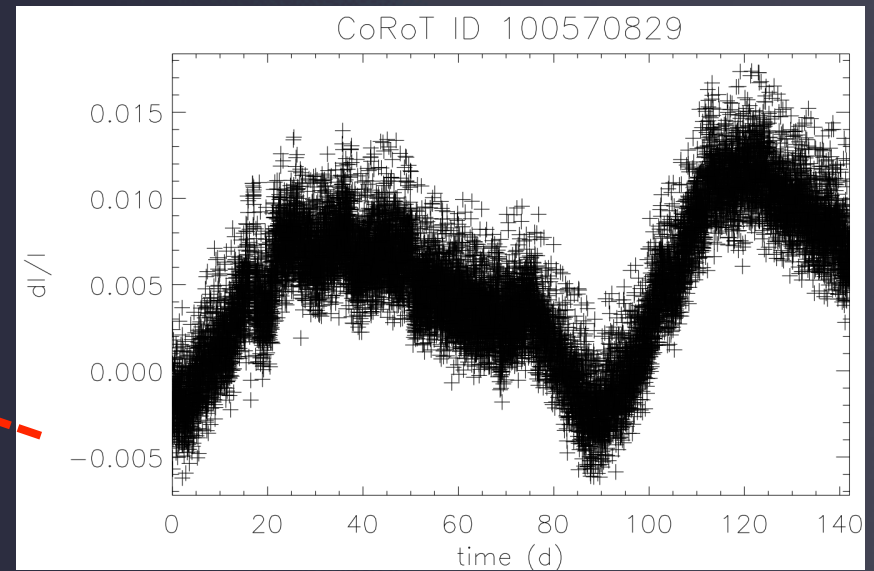
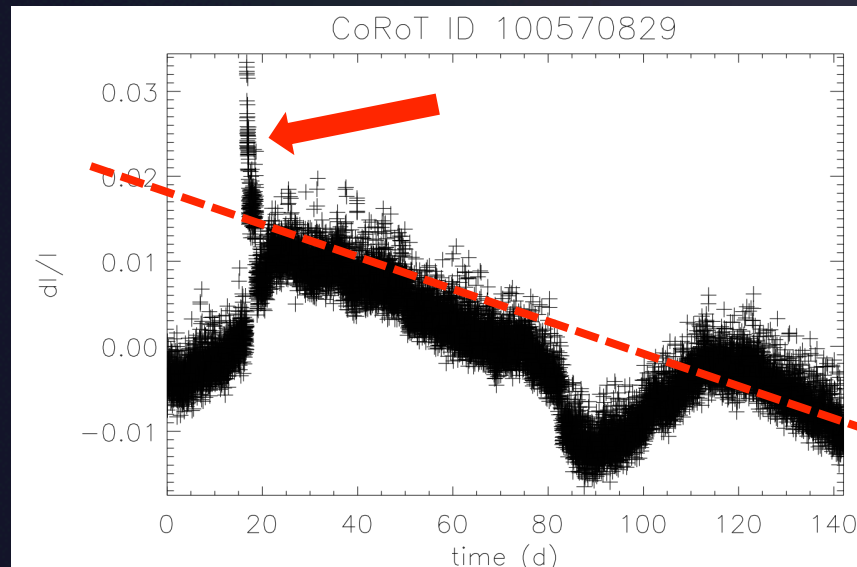
# Time series analysis

## Light Curve correction



**CoRoT ID 100570829**

# CoRoT ID 100570829

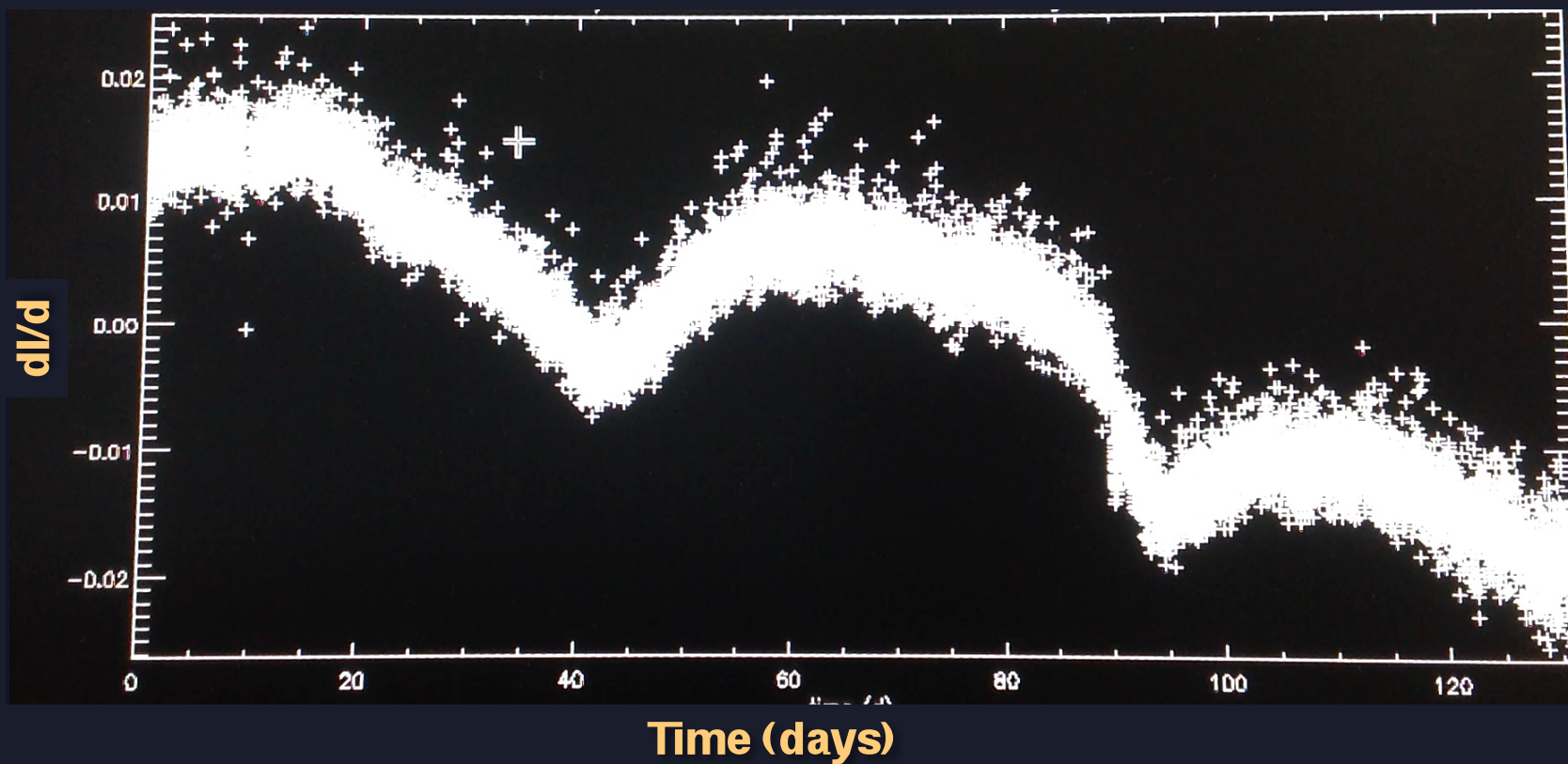


**Prot = 84.2 days**



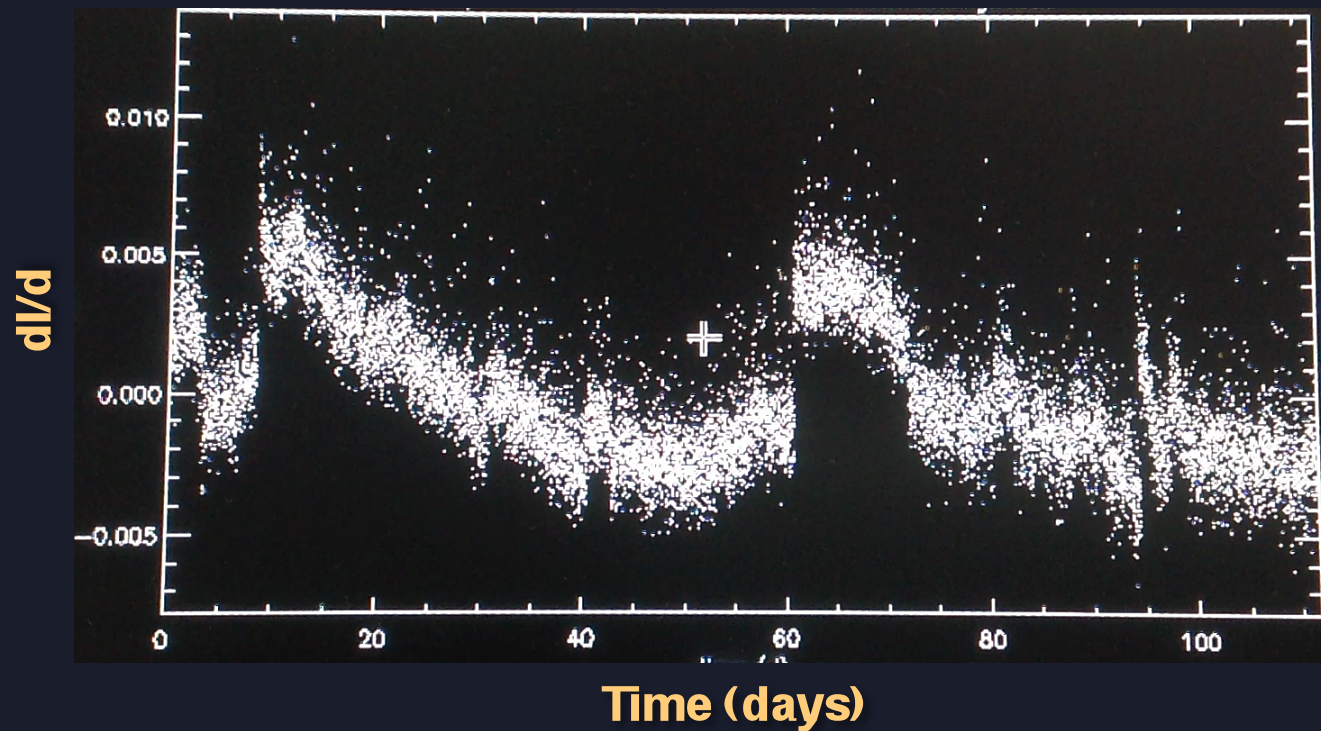
# DETREND CORRECTION

CoRoT ID 0102636100



# Discontinuity + DETREND CORRECTION

CoRoT ID 030004247



# Time series analysis

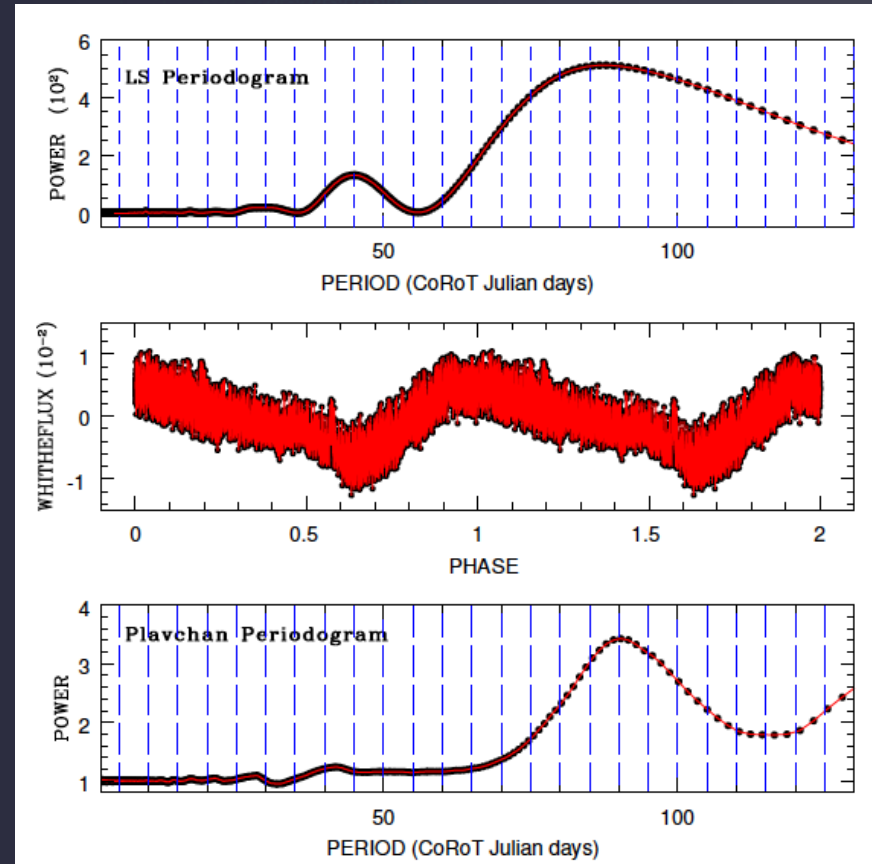
CoRoT ID 0102636100

- ✓ Lomb-Scargle
- ✓ Plavchan Periodogram
- ✓ Wavelete
- ✓ Phase Diagram
- ✓ Prot = 74 d

Quality

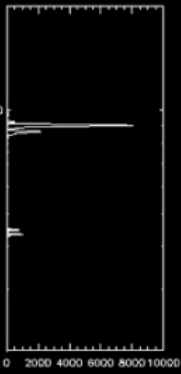
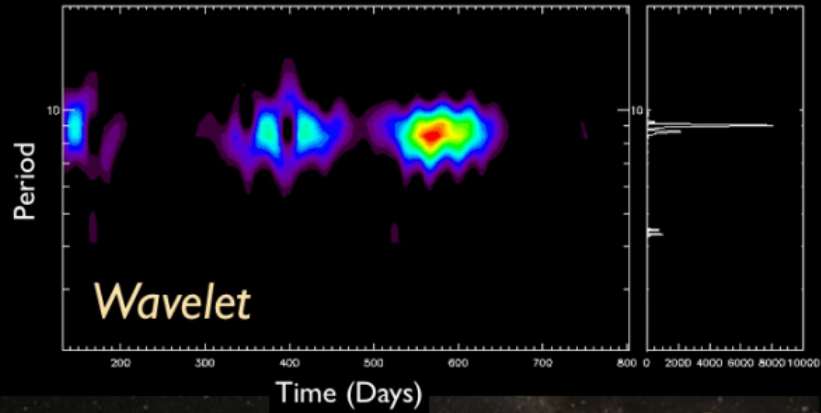
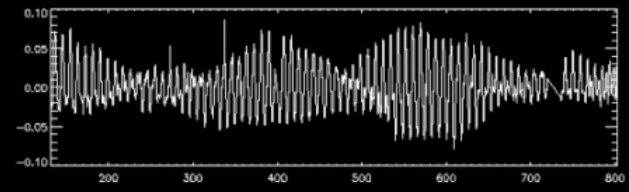
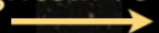
-FAP (False Alarm Probability)  $< 10^{-6}$

- Prot error  $\sigma$  Prot = 0,2865 FWHM





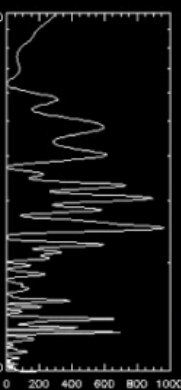
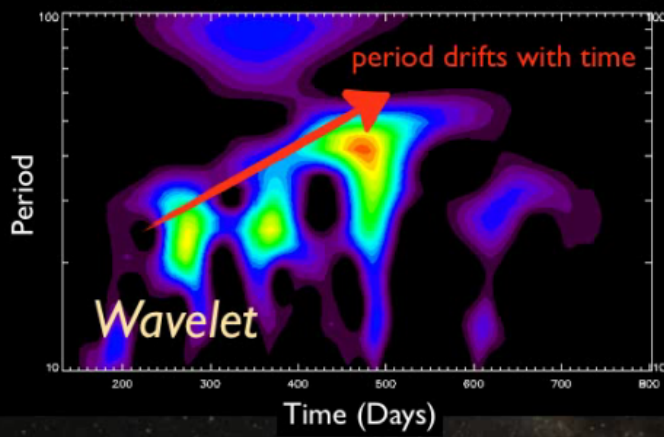
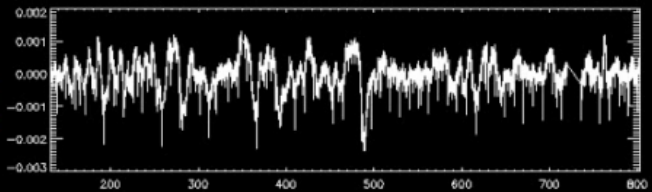
Lightcurve



Periodogram



Lightcurve



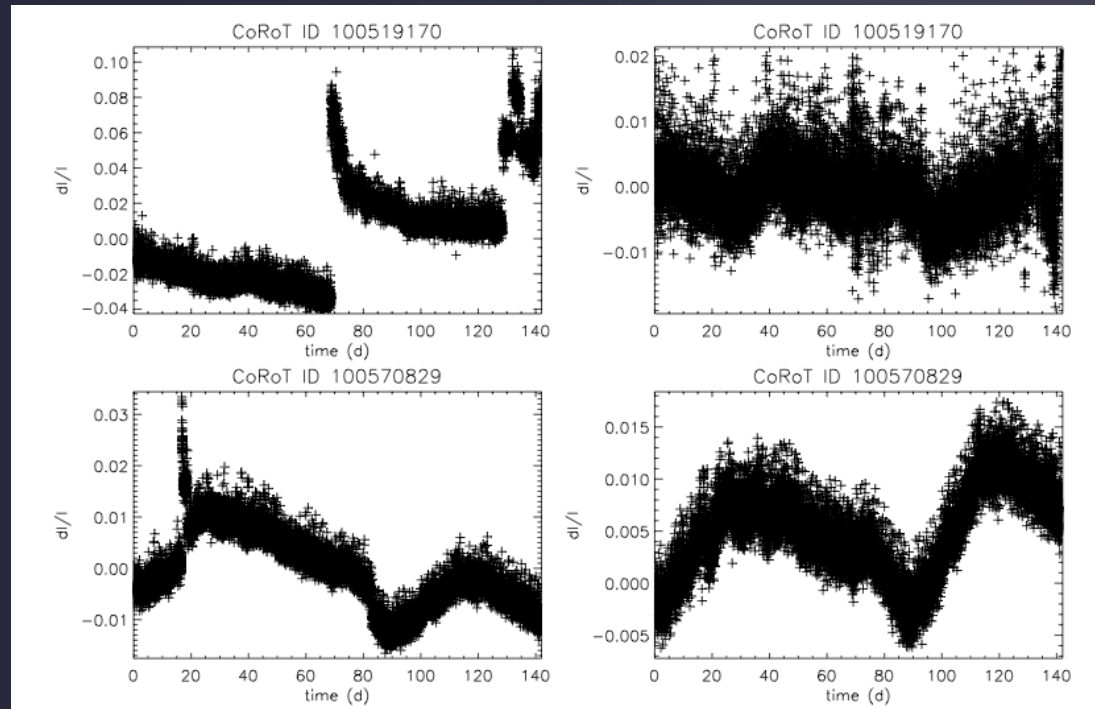
Periodogram



Lucianne Walkowicz (2012)

✓ Plot of selected light curves **before** and **after** the removal of the discontinuities and / or long-term trends

✓ The subgiant sample and their rotational periods



CoRoT ID	RA (deg)	Dec (deg)	$(J - H)_{C_3}$ (mag)	$P_{\text{rot}}$ (LS) (days)	Error (days)	FAP	$FWHM$ (days)	$P_{\text{rot}}$ (Plavchan) (days)
100519170	290.743009	1.406339	0.33446	74.3	27.2	$<10^{-6}$	95	73.2
100543054	290.778772	1.326228	0.43519	63.9	10.0	$<10^{-6}$	35	65.6
100570829	290.820823	1.19351	0.31981	84.2	15.8	$<10^{-6}$	55	87.5
100603128	290.869237	1.430996	0.44692	72	10.0	$<10^{-6}$	35	62.9
100686488	290.994464	0.948138	0.44898	66.7	8.6	$<10^{-6}$	30	69.0
100698726	291.015259	1.174825	0.24425	17.1	2.3	$<10^{-6}$	8	16.9

# Brief description of the physics adopted for the transport of internal angular momentum

- ✓ Physics adopted for the transport of internal angular momentum for the present modeling used the same approach as Pinsonneault et al. (1989) after updating the treatment of the instabilities relevant to the transport of angular momentum according to Zahn (1992) and Talon & Zahn (1997).
- ✓ Initial conditions: The rotational properties are influenced by the pre-main-sequence phase. Kawaler (1987) determined the initial angular momentum for the Sun as  $J_0 = 1.63 \times 10^{50} \text{ g cm}^2 \text{ s}^{-1}$ .
- ✓ Angular momentum loss: Kawaler (1988) described the angular momentum loss for stars with an outer convective envelope as

$$\frac{dJ}{dt} = -K\Omega^{1+4N/3} \left(\frac{R}{R_\odot}\right)^{2-N} \left(\frac{M}{M_\odot}\right)^{-N/3},$$

with  $\Omega$  the angular velocity and  $K$  a constant that combines scale factors for the wind velocity and magnetic field strength. This is adjusted to give the solar surface rotation velocity at the solar age.  $N$  denotes the wind index and is a measure of the magnetic geometry.  $N = 3/2$  for the Sun. The mass loss dependence rate is very weak, and we assumed the rate  $\dot{M}$  to be  $10^{-14} M_\odot \text{ yr}^{-1}$ .

The transport of angular momentum is governed by an advection/diffusion equation:

$$\frac{\partial}{\partial t} [\rho r^2 \Omega] = \frac{1}{5r^2} \frac{\partial}{\partial r} [\rho r^4 \Omega U_r] + \frac{1}{r^2} \frac{\partial}{\partial r} \left[ \rho \nu_v r^4 \frac{\partial \Omega}{\partial r} \right], \quad (\text{A.4})$$

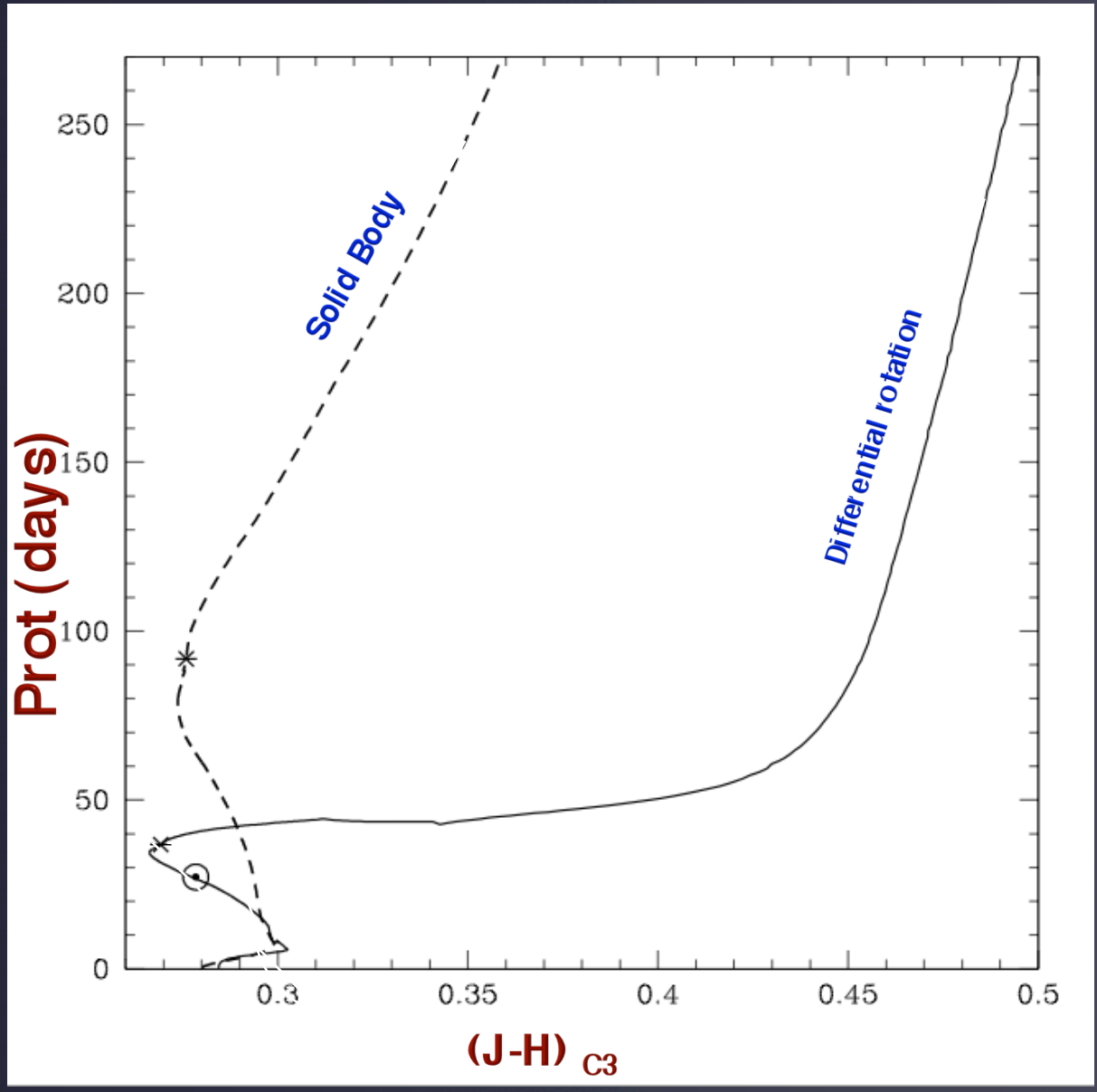
with  $\Omega$  the angular velocity and  $\nu_v$  the vertical turbulent viscosity. We use the prescription given by Talon & Zahn (1997):

$$\nu_v = D_v = \frac{8Ri_c}{5} \frac{(rd\Omega/dr)^2}{N_T^2/(\kappa + D_h)}, \quad (\text{A.5})$$

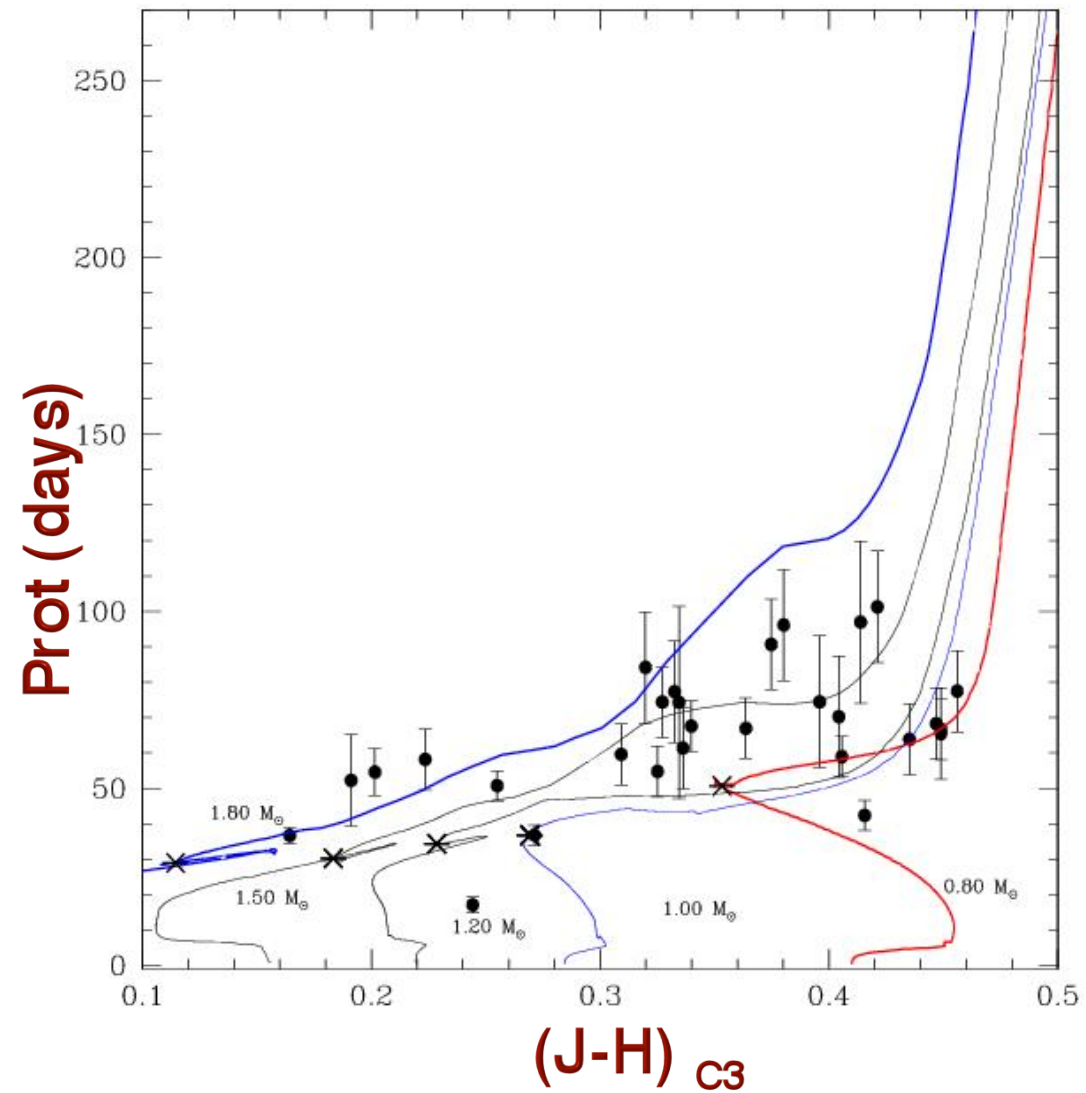
taking into account the homogenizing effect of the horizontal diffusion ( $D_h$ ) on the restoring force caused by the gradient of molecular weight.  $N_T^2 = \frac{g\delta}{H_p} (\nabla_{\text{ad}} - \nabla)$  is the Brunt-Väisälä frequency,  $\kappa$  the radiative diffusivity, and  $Ri_c \sim 1/4$  is the critical Richardson number (see Talon et al. 1997). The horizontal shear is sustained by the advection of momentum:

$$D_h = \frac{rU_r}{C_h} \left[ \frac{1}{3} \frac{d \ln \rho r^2 U_r}{d \ln r} - \frac{1}{2} \frac{d \ln \rho r^2 \Omega}{d \ln r} \right]. \quad (\text{A.6})$$

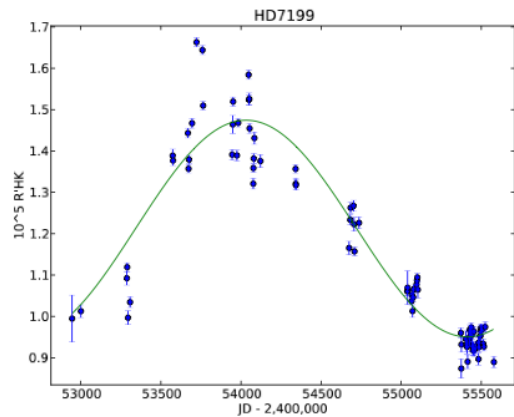




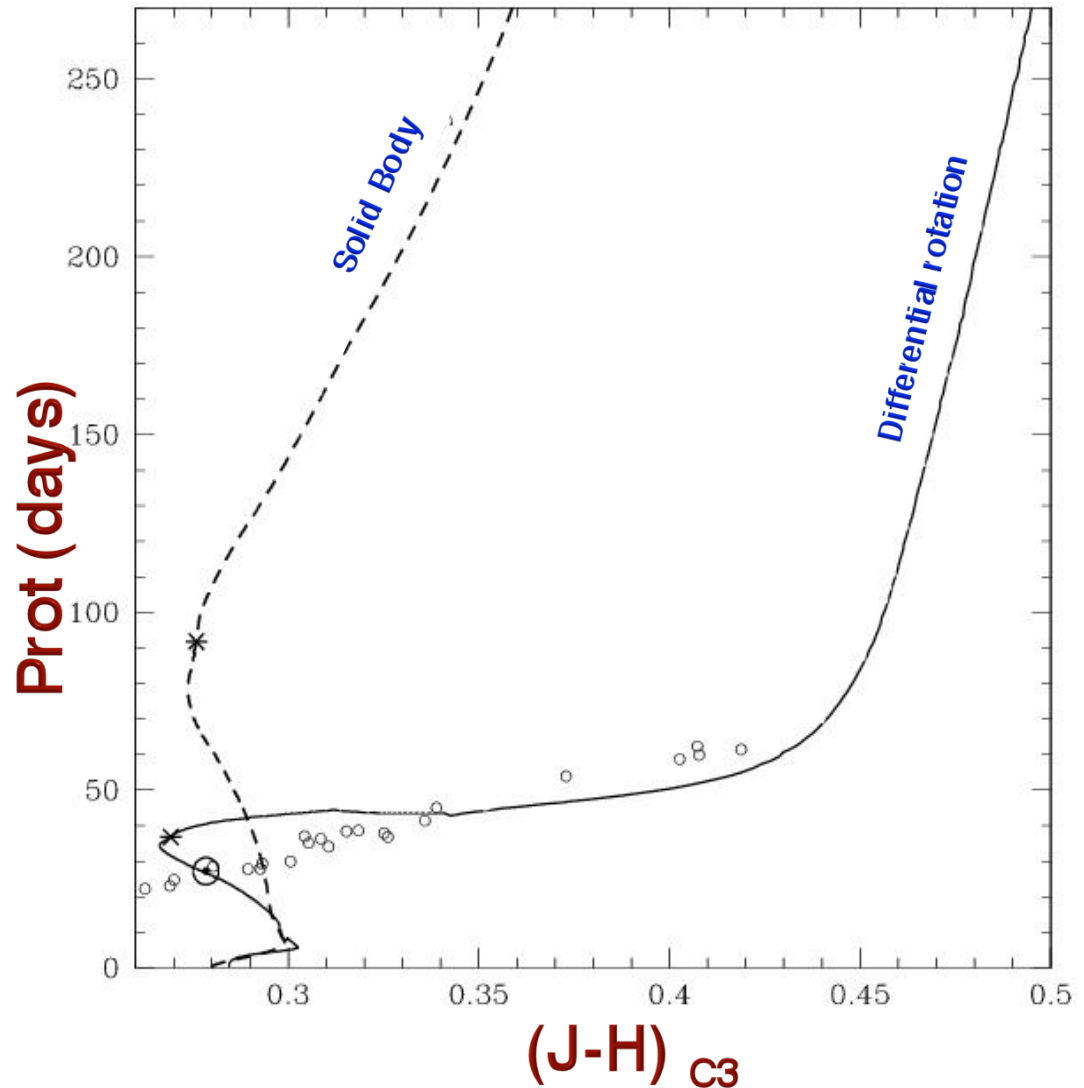
# Rotational Periods from CoRoT



**Prot agree well with the range  
of periods determined from  
the activity modulation  
studies of subgiants of 1  
Solar mass**



**high-precision Ca II  
H&K chromospheric  
activity measurements  
+  
Mount Wilson S index**



**Model Validation: Periods from Lovis et al (2011) !!!**

## Conclusions

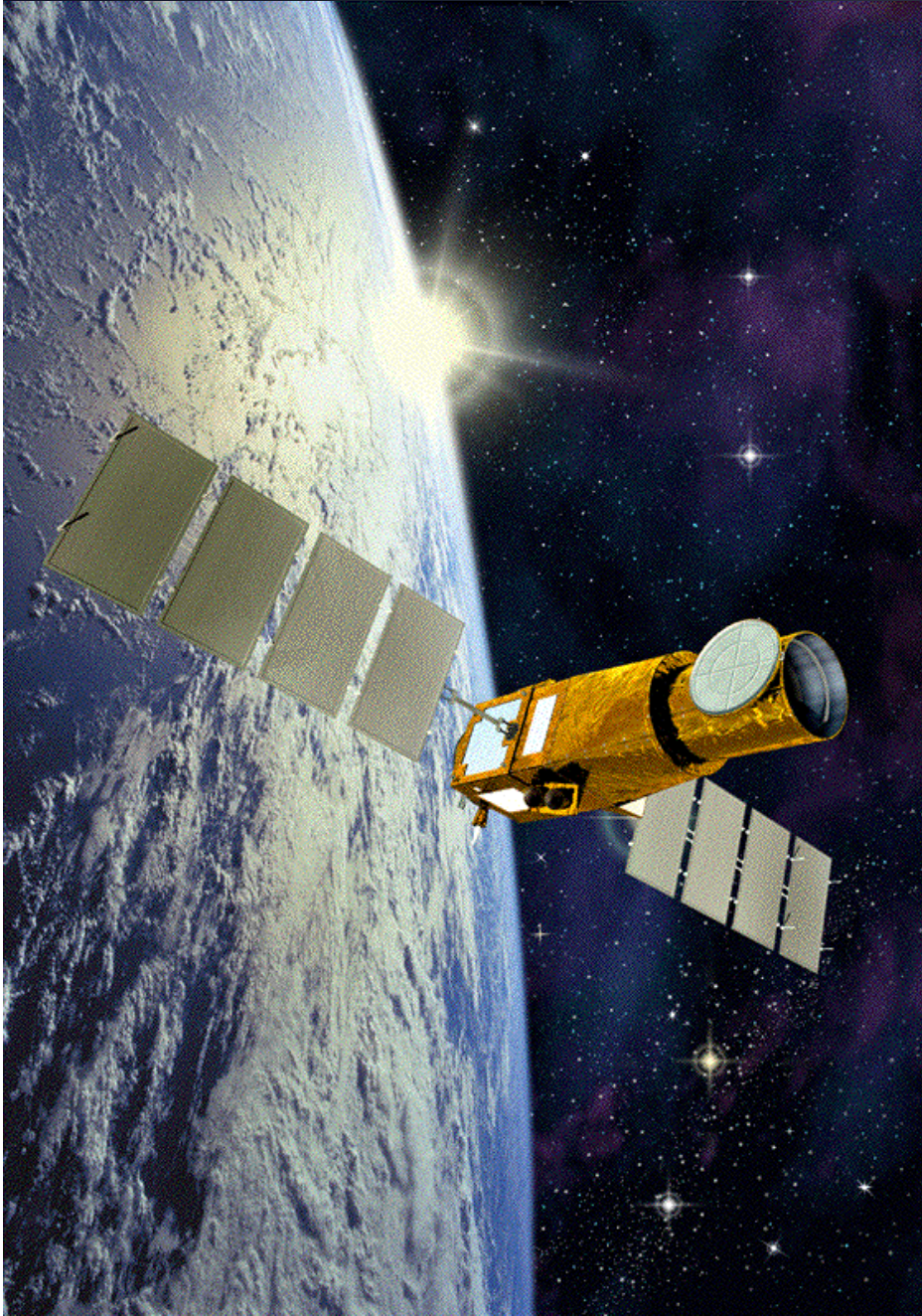
- Prot determined for subgiants observed by CoRoT
- These Prot + evolutionary models helped us to more tightly constrain the angular momentum evolution for evolved stars  $\Leftrightarrow$  seismology
- Prot ranging from 30 to 100 d in the range from 0.8 to 1.8 solar masses
- The Prot range for subgiants reinforces the scene of a differential rotation in depth or a fast-core rotating ~~(solid body)~~
- This result also agrees with the findings by Mosser et al. (2012), who observed that rotational splittings and core rotation significantly slows down during the RGB.

**Rotation periods for sun-like KEPLER SUBGIANTS: KIC11395018, KIC10920273 (do Nascimento, Garcia, Manthur, Pinsonneault, Chaplin et al. (2013, In preparation))**



# Things still to do...

- Hints for a dynamo theory in a slowly rotating domain and depth convective zone...
- Mixed models and the core rotation in subgiants
- Better constraint the strong structural evolution in subgiants: core contraction + envelope expansion
- What about the lifetime of spots for subgiants



**It is just the  
beginning for  
rotation of solar  
type stars**

**Thank you!**