At z=1000 the Universe has cooled down to 3000 K. Hydrogen becomes neutral ("Recombination").

At z < 40 the first "PopIII" star (clusters)/small galaxies form.

## At 6-15 these gradually photooniz heheito en in the Gradually

At z<6 galaxies form most of their stars and grow by merging.

At z<1 massive galaxy clusters are assembled.









## Lecture #1

Cosmic Reionization

Andrea Ferrara Scuola Normale Superiore, Pisa, Italy

### "Historical" material

- Barkana, R. & Loeb, A. 2001, Phys. Rep., 349, 125
- Ciardi, B. & Ferrara, A. 2006, SSRv, 116, 625 (updated: Apr 2008)

## **Recent material**

- Ferrara, A. 2008, Saas-Fee Advanced Courses, 36. p. 161-258
- Choudhury, T. 2009, Current Science 97, 841
- Meiksin, A. 2009, Rev. Mod. Phys., 81:1405
- Ferrara, A. & Pandolfi, S. 2014, Varenna School arXiv1409.4946

#### **COSMOLOGICAL I-FRONTS PROPAGATION**

.

#### Single source

Physical coordinates 
$$\bar{n}_{H}\left(\frac{dV_{p}}{dt} - 3HV_{p}\right) = \frac{dN_{\gamma}}{dt} - \alpha_{B}\left\langle n_{H}^{2}\right\rangle V_{p}$$
.  
 $C = \left\langle n_{H}^{2}\right\rangle / \bar{n}_{H}^{2}$ .

Comoving coordinates

$$\frac{dV}{dt} = \frac{1}{\bar{n}_H^0} \frac{dN_\gamma}{dt} - \alpha_B \frac{C}{a^3} \bar{n}_H^0 V$$

$$V(t) = \int_{t_i}^t \frac{1}{\bar{n}_H^0} \frac{dN\gamma}{dt'} e^{F(t',t)} dt'$$
,

where

$$F(t',t) = -\alpha_B \bar{n}_H^0 \int_{t'}^t \frac{C(t'')}{a^3(t'')} dt''$$
.

#### **COSMOLOGICAL I-FRONTS PROPAGATION**

Statistical approach

volume filling factor  $Q_{\rm HII} = V_{\rm HII} / V$ 

$$\frac{n\gamma}{\bar{n}_b} = N_{\rm ion} F_{\rm col} \qquad \qquad N_{\rm ion} \equiv N_\gamma \, f_{\rm star} \, f_{\rm esc}$$

$$\frac{dQ_{\rm H~II}}{dt} = \frac{N_{\rm ion}}{0.76} \frac{dF_{\rm col}}{dt} - \alpha_B \frac{C}{a^3} \bar{n}_H^0 Q_{\rm H~II} ,$$

$$Q_{\rm H~II}(t) = \int_0^t \frac{N_{\rm ion}}{0.76} \frac{dF_{\rm col}}{dt'} e^{F(t',t)} dt'$$
,

#### "HELLO WORLD!" REIONIZATION MODEL



#### **COSMOLOGICAL RADIATIVE TRANSFER**

$$J_{\nu} = J(t, \mathbf{x}, \mathbf{\omega}, \mathbf{v})$$
$$\dot{J}_{\nu} \equiv \frac{\partial J_{\nu}}{\partial t} - H(t)\nu \frac{\partial J_{\nu}}{\partial \nu} = -3H(t)J_{\nu} - c\kappa_{\nu}J_{\nu} + \frac{c}{4\pi}\epsilon_{\nu}$$

redshifting dilution absorption emission

Formal solution 
$$J_{\nu}(t) = \frac{c}{4\pi} \int_{0}^{t} \mathrm{d}t' \epsilon_{\nu'}(t') \frac{a^{3}(t')}{a^{3}(t)} e^{-\tau(t,t',\nu)}$$
  $\tau \equiv c \int_{t'}^{t} \mathrm{d}t'' \kappa_{\nu''}(t'') \frac{\tau''}{a^{3}(t)} e^{-\tau(t,t',\nu)}$   
 $\nu'^{(\prime\prime)} = \nu \frac{a(t)}{a(t'^{(\prime\prime)})}$ 

 $\kappa_{\nu} \gg H/c$  (Local approximation)

 $J_{\nu}(t) \approx \frac{\epsilon_{\nu}(t)}{4\pi\kappa_{\nu}(t)}$ 

#### NUMERICAL SOLUTION TECHNIQUES

- Ray Tracing/Long characteristics Abel, Norman & Madau 1999; Razoumov & Scott 1999; Sokasian, Abel & Hernquist 2001; Razoumov etal 2002
- Ray Tracing/Short characteristics Umemura etal 1999; Rijkhorst etal 2005
- Flux-Eddington tensor Gnedin & Abel 2001
- Flux-limited diffusion *Turner & Stone 2001; Whitehouse & Bate 2004*
- Fourier transforms Cen 2002
- Unstructured grids Ritzerveld etal 2004
- Statistical (MC) methods Ciardi etal 2001; Maselli, Ferrara & Ciardi 2003

#### TSU<sup>3</sup> CODE BENCHMARK

## www.mpa-garching.mpg.de/tsu3/

Stromgren sphere





Cosmological field













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# **Reionization completed**

## **Reionization Topology**



## Gunn and Peterson (1965)

## NOTES

#### ON THE DENSITY OF NEUTRAL HYDROGEN IN INTERGALACTIC SPACE

Recent spectroscopic observations by Schmidt (1965) of the quasi-stellar source 3C 9, which is reported by him to have a redshift of 2.01, and for which Lyman-a is in the visible spectrum, make possible the determination of a new very low value for the density of neutral hydrogen in intergalactic space. It is observed that the continuum of the source continues (though perhaps somewhat weakened) to the blue of Ly-a; the line as seen on the plates has some structure but no obvious asymmetry. Consider, however, the fate of photons emitted to the blue of Ly-a. As we move away from the source along the line of sight, the source becomes redshifted to observers locally at rest in the expansion, and for one such observer, the frequency of any such photon coincides with the rest frequency of Ly-a in his frame and can be scattered by neutral hydrogen in his vicinity. The calculation of the size of the effect is very easily performed as follows:

#### **BASIC FORMULAE**

Historical formula  

$$\begin{split} p &= \int_0^{z_0} dp = \int_0^{z_0} n \left[ t(z) \right] \sigma \left[ \nu(1+z) \right] \frac{dl}{dz} dz. \\ \sigma(\nu) &= \frac{\pi e^2}{m c} f g(\nu - \nu_a), \\ \tau_{\rm GP} &= \frac{\pi e^2}{m_e c} f_\alpha \lambda_\alpha H^{-1}(z) n_{\rm HI} \end{split}$$

Modern formula

$$\tau_{\rm GP}(z) = 4.9 \times 10^5 \left(\frac{\Omega_m h^2}{0.13}\right)^{-1/2} \left(\frac{\Omega_b h^2}{0.02}\right) \left(\frac{1+z}{7}\right)^{3/2} \left(\frac{n_{\rm HI}}{n_{\rm H}}\right)$$

A neutral fraction  $x_{HI} \approx 10^{-4}$  gives rise to complete GP absorption 22



Lyman Forest Absorption

Patchy Absorption

Black Gunn-Peterson trough

#### Fan 2006

#### **GUNN-PETERSON EFFECT**



#### SOURCE LIST

• Stars: Pop II and/or (massive) Pop III

In what proportion ?  $(4, 30, 100) \times 10^3$  phot/baryon into stars

• Quasars

Too rare, too late; key sources for HeII reionization

• Supernova explosions

Filling factor too small; Compton-y limited

• Dark Matter: decays/annihilations

*Light particles (LDM, sterile neutrinos) can produce a*  $\tau_e < 0.01$  *Heavy particles (neutralinos, gravitinos) totally negligible* 

• Mini-quasars

Limited by unresolved SXRB Only 3 phot/baryon in IGM in 10 Salpeter times

• Structure formation

Important for HeII reionization, bremsstrahlung has  $f_{esc} \approx 1!$ 

#### CMB

## Reionization affects CMB in three ways:

- 1. Damping of primary anisotropies on all scales
- 2. Small scale secondary anisotropies (patchy reionization)
- 3. Large scale polarization signal

#### ELECTRON SCATTERING OPTICAL DEPTH

$$\tau_e(z_{\rm rei}) = \int_0^{z_{\rm rei}} n_e \sigma_T (1+z)^{-1} \left[ c/H(z) \right] dz$$

$$\tau_e(z_{\rm rei}) \approx \left(\frac{c \,\sigma_T}{H_0}\right) \left(\frac{2\Omega_b}{3\Omega_m^{1/2}}\right) \left[\frac{\rho_{\rm cr}(1-Y)(1+y)}{m_H}\right] (1+z_{\rm rei})^{3/2} \approx (0.0521) \left[\frac{(1+z_{\rm rei})}{8}\right]^{3/2}$$





#### **REIONIZATION TESTS**

#### Planck Collaboration 15

#### PLANCK POLARIZATION DATA



#### EXPERIMENTAL CONSTRAINTS

- Lyα Gunn-Peterson opacity
- Electron scattering optical depth
- Lyβ Gunn-Peterson opacity
- UV Background intensity
- Redshift evolution of Lyman Limit Systems
- IGM Temperature evolution
- IGM Metallicity
- Cosmic star formation history
- High-z galaxy counts
- Near Infrared Background

#### **CONSTRAINING REIONIZATION**



#### **IONIZING PHOTON BUDGET**



#### **CONSTRAINING REIONIZATION**



#### **IMPACT ON PARAMETERS**

Principal components

$$x_e(z) = x_e^f(z) + \sum_{\mu} m_{\mu} S_{\mu}(z),$$

$$m_{\mu} = \frac{1}{z_{max} - z_{min}} \int_{z_{min}}^{z_{max}} dz \ S_{\mu}(z) \delta x_{e}(z)$$
PC amplitudes

#### **IMPACT ON PARAMETERS**

## Principal Component + MCMC Analysis

Parameter	WMAP7	WMAP7 + PC	WMAP7 + ASTRO
$\Omega_m$	$0.266\pm0.029$	$0.243 \pm 0.032$	$0.273 \pm 0.027$
$\Omega_b h^2$	$0.02258^{+0.00057}_{-0.00056}$	$0.02321 \pm 0.00076$	$0.02183 \pm 0.00054$
h	$0.710 \pm 0.025$	$0.735 \pm 0.033$	$0.698 \pm 0.023$
$n_s$	$0.963 \pm 0.014$	$0.994 \pm 0.023$	$0.958 \pm 0.013$
$\sigma_8$	$0.801 \pm 0.030$		$0.794 \pm 0.027$
$ au_e$	$0.088 \pm 0.015$	$0.093 \pm 0.010$	$0.080 \pm 0.012$
$z_r^*$	$10.5\pm1.2$		$6.7\pm0.6$

## Lecture #2

HI 21 cm line intensity mapping

#### DRAWBACKS

- Lya line powerful probe of reionization but the GP opacity is enormous
- CMB probes only provide integrated measurements of the electron scattering optical depth, i.e. no sensitivity to specific redshift

Spin-flip (hyperfine) transition of neutral hydrogen [due to electron-proton magnetic interactions]

#### LINE RADIATIVE TRANSFER



$$\frac{dI_{v}}{d\ell} = \frac{\phi(v)hv}{4\pi} \left[ n_{1}A_{10} - (n_{0}B_{01} - n_{1}B_{10})I_{v} \right]$$

- $I_{v:}$  specific line intensity
- $\phi(v)$ : line profile
- $A_{ij}, B_{ij}$ : Einstein coefficients

Line frequency  $v_{21}$ =1420.4057 MHz or  $\lambda_{21}$ =21.1061 cm

#### LINE RADIATIVE TRANSFER

$$\left(\frac{n_1}{n_0}\right) = \left(\frac{g_1}{g_0}\right) \exp\left\{\frac{-T_*}{T_S}\right\}$$

- $g_l/g_0 = 3$  (spin degeneracy factors)
- $T_* = E_{10}/k_B = 68 \text{ mK}$
- $T_S$ : spin temperature

Usually  $T_* \ll T_S$ ,  $T_\gamma$  hence  $n_1 = 3n_0$ [stimulated emission is important]

#### BRIGHTNESS TEMPERATURE

Effective temperature required by a black body radiator such that

$$I_{v} = B_{v}(T_{b})$$

At radio-frequencies, we work in the Raleigh-Jeans approximation. Hence  $T_b(v) \approx I_v c^2/2k_B \dot{v}^2$ 

The RT equation can be casted in terms of the *brightness temperature* 

$$T'_{b}(\mathbf{v}) = T_{S}(1 - e^{-\tau_{v}}) + T'_{R}(\mathbf{v})e^{-\tau_{v}}$$

- $T_b(v) = T'_b(v)/(l+z)$  is the *observed* brightness temperature
- $T'_{b}(v)$  is the brightness temperature in the cloud framework
- $T'_{R}(v)$  is the brightness of the background radiation field along the l.o.s.

LINE OPTICAL DEPTH

$$\tau_{\rm v} \equiv \int ds \, \alpha_{\rm v}$$

The absorption coefficient depends on the Einstein coefficients

$$\alpha = \phi(v) \frac{hv}{4\pi} (n_0 B_{01} - n_1 B_{10})$$

Derivation similar to GP opacity. Use  $\phi(v) \approx (\Delta v)^{-1}$ 

$$\tau_{10} = \frac{3}{32\pi} \frac{hc^3 A_{10}}{k_B T_S v_{10}^2} \frac{x_{\text{HI}} n_{\text{H}}}{(1+z) (dv_{\parallel}/dr_{\parallel})}$$
$$\approx 0.0092 (1+\delta) (1+z)^{3/2} \frac{x_{\text{HI}}}{T_S} \left[ \frac{H(z)/(1+z)}{dv_{\parallel}/dr_{\parallel}} \right]$$

#### **OBSERVED SIGNAL**

We observe the *contrast*  $T_{b}$ - $T_{R}$  between cloud and background, i.e. CMB Small optical depth limit,  $\tau_v \ll 1$ 

$$T_b(\mathbf{v}) \approx \frac{T_S - T_{\gamma}(z)}{1+z} \tau_{\mathbf{v}_0}$$
  
$$\approx 9 x_{\mathrm{HI}}(1+\delta) (1+z)^{1/2} \left[1 - \frac{T_{\gamma}(z)}{T_S}\right] \left[\frac{H(z)/(1+z)}{dv_{\parallel}/dr_{\parallel}}\right] \mathrm{mK}$$

### Note that

- If T<sub>S</sub> > T<sub>γ</sub> the signal appears in emission
  If T<sub>S</sub> < T<sub>γ</sub> the signal appears in absorption
- In emission the signal saturates; in absorption it can become arbitrarily large •

#### SPIN TEMPERATURE

### **Determined by**

- Interactions with CMB photons
- Particle collisions
- Scattering of UV photons

[drive  $T_S = T_{\gamma}$ ] [drive  $T_S$  away from  $T_{\gamma}$ ] [drive  $T_S$  away from  $T_{\gamma}$ ]

#### **Detailed balance**

#### SPIN TEMPERATURE

In the Rayleigh-Jeans regime the detailed balance eq. reads

$$T_{S}^{-1} = \frac{T_{\gamma}^{-1} + x_{c}T_{K}^{-1} + x_{\alpha}T_{c}^{-1}}{1 + x_{c} + x_{\alpha}},$$

where, by definition,

Most often,  $T_c \approx T_K$  in which case

$$1 - \frac{T_{\gamma}}{T_S} = \frac{x_c + x_{\alpha}}{1 + x_c + x_{\alpha}} \left( 1 - \frac{T_{\gamma}}{T_K} \right)$$

#### COUPLINGS

### **Collisional coupling**

$$x_c^i \equiv \frac{C_{10}^i}{A_{10}} \frac{T_\star}{T_\gamma} = \frac{n_i \kappa_{10}^i}{A_{10}} \frac{T_\star}{T_\gamma} \qquad i = \text{hydrogen atoms, electrons}$$

Critical overdensity at which  $x_c = 1$  for H-H collisions  $1 + \delta_{coll} = 0.99 \left[\frac{\kappa_{10}(88 \text{ K})}{\kappa_{10}(T_K)}\right] \left(\frac{0.023}{\Omega_b h^2}\right) \left(\frac{70}{1+z}\right)^2$ 

At z < 70,  $x_c$  becomes very small and hence  $T_S \approx T_{\gamma}$ 

By  $z \approx 30$  the IGM would become invisible

#### COUPLINGS

### UV coupling [Wouthuysen-Field effect]



Hyperfine splittings of the 1S and 2P levels. The solid lines label transitions that mix the ground state hyperfine levels, while the dashed lines label complementary allowed transitions that do not participate in mixing.

$$x_{\alpha} = \frac{4P_{\alpha}}{27A_{10}} \frac{T_{\star}}{T_{\gamma}}$$

$$P_{\alpha} = 4\pi\sigma_0 \int d\mathbf{v} J_{\mathbf{v}}(\mathbf{v})\phi_{\alpha}(\mathbf{v})$$

#### POWER SPECTRUM

Define the fractional perturbation to the brightness temperature

$$\delta_{21}(\mathbf{x}) \equiv [T_b(\mathbf{x}) - \bar{T}_b] / \bar{T}_b$$
 (zero mean field)

Perform its Fourier transform:  $\tilde{\delta}_{21}(\mathbf{k})$ .

The 21cm power spectrum,  $P_{21}(\mathbf{k})$  is defined by

$$\left< \tilde{\delta}_{21}(\mathbf{k}_1) \, \tilde{\delta}_{21}(\mathbf{k}_2) \right> \equiv (2\pi)^3 \delta_D(\mathbf{k}_1 - \mathbf{k}_2) P_{21}(\mathbf{k}_1)$$
kinetic temperature Dirac-delta
Dimensionless version  $\Delta^2(\mathbf{k}) = (k^3/2\pi^2) P(\mathbf{k})$ 

#### **GLOBAL HISTORY (NO HEATING)**



IGM temperature evolution including only adiabatic cooling and Compton heating. The spin temperature includes only collisional coupling.

Corresponding differential brightness temperature against the CMB

#### **GLOBAL SIGNAL: ADD REIONIZATION**



SIMULATED SIGNAL

## Brightness Temperature Evolution



#### SIMULATED POWER SPECTRUM



#### HEATING PROCESSES

- X-ray heating from astrophysical sources
- Lya heating
- Dark matter annihilation/decay heating
- Shock heating

#### IGM THERMAL HISTORY

#### Valdes & AF 09; Mapelli+10; Evoli+12

#### DARK MATTER HEATING



Evoli, Mesinger & AF+14

Dark matter annihilations

**IONIZATION AND HEATING** 

## **IONIZATION EQUATION**

$$\frac{dx_e}{dz} = \frac{dt}{dz} \left[ \Gamma_{\text{ion}} - \alpha_{\text{B}} C x_e^2 n_b f_{\text{H}} \right] ,$$

$$\frac{dT_K}{dz} = \frac{2T_K}{1+z} + \frac{2T_K}{3n_b} \frac{dn_b}{dz} - \frac{T_K}{1+x_e} \frac{dx_e}{dz} + \frac{2}{3k_B(1+f_{He}+x_e)} \frac{dt}{dz} \sum_{p} \epsilon_p$$
ENERGY EQUATION

#### DARK MATTER HEATING

**STRUCTURE** 

FORMATION BOOST

$$\underset{\text{RATE}}{\text{HEATING}} \qquad \mathcal{E}_{\chi} = \frac{1}{n_b} \frac{dE}{dtdV}(z) = (1+z)^3 \frac{\Omega_{\chi}^2}{\Omega_b} \rho_{c,0} [1+B(z)] m_p c^2 \frac{\langle \sigma v \rangle}{m_{\chi}}$$

$$B(z) = rac{b_h}{(1+z)^\delta} ext{erfc} \left(rac{1+z}{1+z_h}
ight)$$

Average DM density enhancement from collapsed structures

MINIMUM HALO  
MASS  
$$\begin{array}{c|c} \hline M_{h,min} \ [M_{\odot}] & b_h & z_h & \delta \\ \hline \hline M_{h,min} \ [M_{\odot}] & 1.6 \times 10^5 & 19.5 & 1.54 \\ \hline 10^{-3} & 1.6 \times 10^5 & 19.0 & 1.52 \\ \hline 10^{-6} & 6.0 \times 10^5 & 19.0 & 1.52 \\ \hline 10^{-9} & 2.3 \times 10^6 & 18.6 & 1.48 \end{array}$$

#### FIDUCIAL CDM CANDIDATE

Light WIMP particle:  $m_X = 10 \text{ GeV}$ Annihilating into  $\mu^+\mu^-$ Annihilation cross-section  $\langle \sigma v \rangle \leq 4.3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$ 

EXPLAINS

- Signal from Galactic Center
- Low-energy signals from direct detections
- Cross-section compatible with combined Planck, WMAP9, ACT, SPT data

#### CMB CONSTRAINTS



#### GLOBAL SIGNAL

Transition from DM to astrophysical source heating



#### POWER SPECTRUM



#### SUMMARY OF DM HEATING EFFECTS

- Depressed second (heating) peak of the power spectrum
- The second peak occurs while the signal is in *emission*
- Such feature *cannot* be produced by astrophysics
- If DM dominates heating,  $\delta T_b = 0$  before X-ray sources appear
- A null detection at very high-z would indicate DM *pre-heating*

## More reionization tests

#### **QSO HII REGIONS**

$$\langle x_{\rm HI} \rangle = 1.0$$
  $\langle x_{\rm HI} \rangle = 0.1$   $\langle x_{\rm HI} \rangle = 2.3 \times 10^{-4}$ 



$$R_d \approx \left(\frac{3\dot{N}_{\gamma}t_Q}{4\pi n_{\rm H}x_{\rm HI}}\right)^{1/3}$$

6.2

6.

#### **QSO HII REGIONS**



#### GAP STATISTICS



#### GAP STATISTICS



#### GAPS IN GRB AFTERGLOWS



#### FOUR BASIC FACTS

- \* Reionization started by metal-free stars @ z=20; 90% complete @ z=8
- $\therefore$  Early Reionization (z > 7) not in contrast with any QSOAL test (GP, Gaps, HII regions)
- $f_{\gamma}$  ≥ 80% of the ionizing power at *z* ≥ 7 from halos of M < 10<sup>9</sup> M<sub>☉</sub>
- Bulk of reionization sources not observed yet. Need JWST.