

Theory of CMB polarization and current status of polarization experiments

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Books:

- Cosmological Inflation and Large Scale Structure. Liddle & Lyth (CUP 2000).
- Cosmology. S Weinberg (Oxford Univ. Press 2008).
- **The Cosmic Microwave Bakcground.** Durrer (CUP 2008).
- **The primordial density perturbation.** Lyth & Liddle (CUP 2009)
- The Cosmic Microwave Background: from quantum fluctuations to the present Universe. Eds. Rubiño-Martin, Rebolo, Mediavilla (Cambridge Univ. Press 2010).

Papers (Polarization of the CMB):

- Ma & Bertschinger (1995), ApJ, 455, 7.
- Hu & Sugiyama (1995), Phys. Rev. D 51, 2599
- Seljak & Zaldarriaga (1996), ApJ, 469, 437.
- Zaldarriaga & Seljak (1997), Phys. Rev. D. 55, 1830.
- Kamionkowski, Kosowsky & Stebbins (1997), Phys. Rev. D 55, 7368.

Quantum fluctuations during inflation

- Any massless field experiences quantum fluctuations during inflation.
- Inflation stretches these to macroscopic scales.



• Two massless fields are guaranteed to exist during inflation:

$$d\ell^{2} = e^{2Ht} \left[(1+\zeta)\delta_{ij} + h_{ij} \right] dx^{i} dx^{j}$$

$$\uparrow \qquad \uparrow \qquad \uparrow$$
expansion scalar tensor
$$H(t) \approx const \quad isotropic \\ stretching \qquad stretching \ stretching$$

Quantum fluctuations during inflation

- Any massless field experiences quantum fluctuations during inflation.
- Inflation stretches these to macroscopic scales.
- Primordial power spectra:

inflation predicts





$$\langle h_{ij}^2 \rangle = \frac{2}{\pi^2} \frac{H^2}{M_{\rm pl}^2}$$

required to show that $|\dot{H}| \ll H^2$

Power spectra - Theory



Stokes parameters

The tip of the electric field vector E for a (monochromatic) electromagnetic wave propagating along a direction n traces out an elipse in a plane perpendicular to the direction of propagation.

$$\begin{cases} E_x = E_1 \cos(\omega t - \phi_1) \\ E_y = E_2 \cos(\omega t - \phi_2) \end{cases}$$
$$\begin{cases} E'_x = E_0 \cos(\beta) \cos(\omega t) \\ E'_y = -E_0 \sin(\beta) \sin(\omega t) \end{cases}$$



***** Stokes parameters are defined as:

$$I \equiv E_1^2 + E_2^2 = E_0^2$$

$$Q \equiv E_1^2 - E_2^2 = E_0^2 \cos(2\beta) \cos(2\chi)$$

$$U \equiv 2E_1 E_2 \cos(\phi_1 - \phi_2) = E_0^2 \cos(2\beta) \sin(2\chi)$$

$$V \equiv 2E_1 E_2 \sin(\phi_1 - \phi_2) = E_0^2 \sin(2\beta)$$

$$E_0 = \sqrt{I}$$
$$\sin(2\beta) = \frac{V}{I}$$
$$\tan(2\chi) = \frac{U}{Q}$$

$$I^2 = Q^2 + U^2 + V^2.$$

Stokes parameters

✤ In the case of quasi-monochromatic waves, we can also define Stokes parameters.

$$\epsilon_1(t) = E_1(t)e^{i\phi_1(t)}$$
$$\epsilon_2(t) = E_2(t)e^{i\phi_2(t)}$$

✤ A real device measures time-averaged quantities (energy):

$$<\epsilon_i\epsilon_j^*>=\frac{1}{T}\int_0^T dt\epsilon_i(t)\epsilon_j^*(t)$$

* In analogy, **Stokes parameters** for quasi-monochromatic waves are defined as:

$$I \equiv \langle \epsilon_1 \epsilon_1^* \rangle + \langle \epsilon_2 \epsilon_2^* \rangle$$

$$Q \equiv \langle \epsilon_1 \epsilon_1^* \rangle - \langle \epsilon_2 \epsilon_2^* \rangle$$

$$U \equiv \langle \epsilon_1 \epsilon_2^* \rangle + \langle \epsilon_2 \epsilon_1^* \rangle$$

$$V \equiv \frac{1}{i} (\langle \epsilon_1 \epsilon_2^* \rangle - \langle \epsilon_2 \epsilon_1^* \rangle)$$

$$I^2 \ge Q^2 + U^2 + V^2.$$

Stokes parameters

* Linear polarization is described by Stokes Q and U parameters.

 \diamond Q measures the different of intensities in the two axes x and y, while U measures the difference of intensities in a coordinate system at 45°.

* Not all Stokes parameters are rotationally invariant. Under a rotation of ψ degrees of the coordinate system, we have

I' = I $Q' = Q\cos(2\psi) - U\sin(2\psi)$ V' = V $U' = U\cos(2\psi) + Q\sin(2\psi)$

or in a more compact form

$$Q' \pm iU' = e^{\pm 2i\psi}(Q \pm iU)$$

♦ Hence, (Q±iU) transforms like a spin-2 variable under rotations.

Spin weighted spherical harmonics

- Spin-s spherical harmonics.
- Under rotations, they transform as: ${}_{s}Y_{\ell m} \rightarrow e^{\pm si\psi}{}_{s}Y_{\ell m}(\hat{n})$
- Orthogonality and completeness

$$\int d\hat{\mathbf{n}}_{s} Y_{\ell m}^{*}(\hat{\mathbf{n}})_{s} Y_{\ell m}(\hat{\mathbf{n}}) = \delta_{\ell \ell'} \delta_{m m'}$$
$$\sum_{\ell m} {}_{s} Y_{\ell m}^{*}(\hat{\mathbf{n}})_{s} Y_{\ell m}(\hat{\mathbf{n}}') = \delta(\phi - \phi') \delta(\cos \theta - \cos \theta')$$

Relation to Wigner rotation matrices:

$${}_{s}Y_{\ell m}(\theta,\phi) = (-1)^{m} \sqrt{\frac{2\ell+1}{4\pi}} e^{-is\psi} D_{-m,s}^{\ell}(\phi,\theta,-\psi)$$

Statistical representation

♦All-sky decomposition:

$$(Q \pm iU)(\hat{n}) = \sum_{\ell=2}^{\infty} \sum_{m=-\ell}^{+\ell} a_{\ell m}^{\pm 2} Y_{\ell m}(\hat{n}) = \sum_{\ell=2}^{\infty} \sum_{m=-\ell}^{+\ell} (a_{E,\ell m} \pm ia_{B,\ell m}) Y_{\ell m}(\hat{n})$$

• Here, $a_{lm}^{\pm 2}$ is a decomposition into positive and negative helicity. The helicity basis

$$e^{\pm} = \frac{1}{\sqrt{2}} (e_{\theta} \pm i e_{\phi})$$

◆ In the last equality we have defined E- and B-modes:

$$a_{E,\ell m} = \frac{1}{2} (a_{\ell m}^{+2} + a_{\ell m}^{-2}) \qquad a_{B,\ell m} = \frac{-i}{2} (a_{\ell m}^{+2} - a_{\ell m}^{-2})$$

♦ Under parity transformations $(n \rightarrow -n)$, the E-modes remain invariant, while B-modes change sign.

The polarization of the CMB anisotropies

Four parity-independent power spectra can be formed:

$$C_{TT} = \frac{1}{2l+1} \sum_{m} \left\langle a_{T,lm}^* a_{T,lm} \right\rangle \qquad C_{BB} = \frac{1}{2l+1} \sum_{m} \left\langle a_{B,lm}^* a_{B,lm} \right\rangle$$
$$C_{EE} = \frac{1}{2l+1} \sum_{m} \left\langle a_{E,lm}^* a_{E,lm} \right\rangle \qquad C_{TE} = \frac{1}{2l+1} \sum_{m} \left\langle a_{T,lm}^* a_{E,lm} \right\rangle$$

Physics of generation of the Polarization. Different sources of anisotropies generate different types of modes:

	Scalar (density perturbations)	Tensor (gravitational waves)
E-modes	Yes	Yes
B-modes	No	Yes

B-modes probe the existence of primordial gravitational waves.

E and B modes

A plane wave moving from top to bottom. The direction of the polarization vector defines if they are E or B modes.

- Full-sky polarization maps can be decomposed into two components usually called E-modes (analog of the gradient component) and B-modes (analog of the curl component) (see Kamionkowski et al. 1997; Seljak & Zaldarriaga 1997).
- These modes are <u>independent on the coordinate system</u>, and are related to the Q and U Stokes parameters by a non-local transformation.



(A pure E-mode turns into pure B-mode if we turn all polarization vectors by 45°).

E and B modes

E-mode Polarization



(Kamionkowski & Kovetz 2016)

Thomson scattering

✤Differential cross-section gives:

$$\begin{pmatrix} E_1 \\ E_2 \end{pmatrix} = -\frac{r_c}{R} \begin{pmatrix} 1 & 0 \\ 0 & \cos \theta \end{pmatrix} \begin{pmatrix} E'_1 \\ E'_2 \end{pmatrix}$$

Defining the y-axes of the incoming and outgoing coordinate systems to be in the scattering plane, the Stokes parameters of the outgoing beam, defined with respect to the x-axis, we have:

$$I = \frac{3\sigma_T}{8\pi R^2} I'(1 + \cos^2(\beta)) \qquad Q = \frac{3\sigma_T}{8\pi R^2} I' \sin^2(\beta) \qquad U = V = 0$$

For unpolarized light, linear polarization is generated, perpendicular to scattering plane (Q>0).

• The net polarization produced by the scattering of an incoming, unpolarized ratiation field of intensity $I'(\theta, \phi)$ is determined by integrating over all incoming directions.

$$I(\hat{z}) = \frac{3\sigma_T}{8\pi R^2} \int d\Omega I'(\theta,\phi)(1+\cos^2(\theta))$$

$$Q(\hat{z}) - iU(\hat{z}) = \frac{3\sigma_T}{8\pi R^2} \int d\Omega \sin^2(\theta) e^{i2\phi} I'(\theta,\phi)$$
Only a_{2m} components components contribute.

* <u>A net polarization is generated if there is a quadrupole anisotropy in the radiation field</u>.



Polarization: scalar perturbations

◆Breakdown of tight-coupling leads to a quadrupole anisotropy.

✤ For scalar perturbations, the polarization signal arises from the gradient of the peculiar velocity of the photon fluid (e.g. Zaldarriaga & Harari 1995).

Gradient of the velocity is along the direction of the wavevector, so the polarization is purely E-mode:

$$\Delta_E \approx -0.17(1-\mu^2)\Delta\eta_{dec}kv_{\gamma}(\eta_{dec})$$

Velocity is 90° out of phase with respect to temperature – turning points of oscillator are zero points of velocity:

$$\Delta_T \propto \cos(kr_s) \qquad v_{\gamma} \propto \sin(kr_s)$$

✤ Polarization peaks are at troughs of temperature peaks.

Power spectra - Theory



Planck Collaboration XIII (2016)





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TE Polarization and acoustic peaks

Cross-correlation of temperature and polarization

 $\Delta_T \Delta_E \propto \cos(kr_s) \sin(kr_s) \propto \sin(2kr_s)$

- ✤ TE spectrum "oscillates" at twice the frequency
- ✤ TE correlation is radial or tangential around hot spots.

✤ Large scales: anticorrelation peak around l=150, a distinctive signature of primordial adiabatic fluctuations (Peiris et al. 2003).

Power spectra - Theory





How did the Universe became neutral? Sketch of the Ionization History



Reionization

Optical depth to Thomson scattering to reionization

$$\begin{aligned} \tau(z) &= \int d\eta n_e \sigma_T a = \int d\ln a \frac{n_e \sigma_T}{H(a)} \propto (\Omega_b h^2) (\Omega_m h^2)^{-1/2} (1+z)^{3/2} \\ &= \left(\frac{\Omega_b h^2}{0.02}\right) \left(\frac{\Omega_m h^2}{0.15}\right)^{-1/2} \left(\frac{1+z}{61}\right)^{3/2} \end{aligned}$$

CMB re-scatters off re-ionized gas.
Generation of new anisotropies at large scales
(Doppler) and absorption at small scales:

$$\Delta_T \to \Delta_T e^{-\tau} \quad \Delta_E \to \Delta_E \tau$$

$$C_{\ell}^{TE} \propto \tau e^{-\tau} \qquad C_{\ell}^{EE} \propto \tau^2$$

* Effect peaks at horizon scale at recombination ($l\approx 2-3$). If the optical depth is very large, primordial anisotropies are erased.





✤ Planck Collaboration XLVII (2016).

* $\tau = 0.058 \pm 0.012$ (assuming instantaneous reionization).

✤ Redshift of reionization is model dependent: $z_{re} \sim 8.5$. Complementary to 21cm studies.

Needed to break degeneracies with other parameters (r).



Power spectra - Theory



Gravitational lensing as seen by Planck





(Slide from A. Lewis, https://indico.in2p3.fr/event/14661/timetable/#all)



Duncan Hanson



Power spectra - Theory



Polarization and tensor modes: Gravitational waves

Gravitational waves are a natural consequence of inflationary models (Grishchuk 1974; Rubakov et al. 1982; Starobinsky 1982, 1983; Abbott & Wise 1984).

- ♦ GW created as vacuum fluctuations (exactly as density perturbations).
 - Evolution at large scales. Similar to temperature fluctuations. Flat power at large scales.
 - ► Evolution at small scales. After re-entering the horizon, fluctuations evolve like radiation (a⁻⁴), so their ratio keeps constant. $\Omega_{GW} \sim \Omega_r (H/m_{pl})^2 \sim 10^{-4} V/m_p^4$. → GW oscillate and decay at horizon crossing.

♦ Gravitational waves produce a quadrupolar distortion in the temperature of the CMB.

✤ B-mode polarization is produced, because the symmetry of a plane wave is broken by the transverse nature of gravity wave polarization.

$$C_{El}^{(T)} = (4\pi)^2 \int k^2 \, dk \, P_h(k) \left| \int d\tau \, g(\tau) \Psi(k,\tau) \left[-j_l(x) + j_l''(x) + \frac{2j_l(x)}{x^2} + \frac{4j_l'(x)}{x} \right] \right|^2,$$

$$C_{Bl}^{(T)} = (4\pi)^2 \int k^2 \, dk \, P_h(k) \left| \int d\tau \, g(\tau) \Psi(k,\tau) \left[2j_l'(x) + \frac{4j_l}{x} \right] \right|^2, \quad \text{(Seljak & Zaldarriaga 1997)}$$

***** E and B modes have similar amplitude.

Again, polarization is only generated at last scattering surface (or reionization).

Power spectra - Theory



Power spectra - Theory



What would a detection of GW tell us?

- It would provide strong evidence that inflation happened!
- The amplitude of the power spectrum is a (model-independent) measurement of the energy scale of inflation.

$$P_{tensor} = \frac{8}{m_{Pl}^2} \left(\frac{H}{2\pi}\right)^2 \propto E_{inf}^4$$

• Defining the tensor-to-scalar ratio (r) at a certain scale k_0 (typically 0.001 Mpc⁻¹), we have

$$r = \frac{P_{tensor}(k_0)}{P_{scalar}(k_0)} = 0.008 \left(\frac{E_{inf}}{10^{16} GeV}\right)^4$$

• Values of **r** of the order of 0.01 or larger would imply that inflation occurred at the GUT scale.

• These scales are 12 orders of magnitude larger than those achievable at LHC!

Primordial gravitational waves and B-modes



 \succ r=0.1 corresponds to an energy scale of inflation around 2x10¹⁶ GeV.

CMB polarization experiments. Present and future

Planck Collaboration XIII (2016)





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PLANCK 2015. Implications on inflation



(Planck Collaboration XX, 2016)



Joint analysis of BICEP2/Keck and PLANCK



- r=0.048 +-0.035 → r<0.12 at 95% C.L.
- 5.1 sigma detection of **dust emission**→ foregrounds!
- Other lines: **BICEP** alone, **Keck** alone.
- Other results: 7 sigma detection of lensing B modes.

BICEP2 Keck and Planck Collaborations (2015), PRL 114, 101301.



State of EE, BB – 2017



CMB Stage 3 experiments



(Slide from J. Carlstrom. Florence 2017. https://indico.in2p3.fr/event/14661/timetable)

Photo credit Cynthia Chiang

CMB experiments at European sites

CMB polarization experiments:

- QUIJOTE **
- GROUNDBIRD
- LSPE-STRIP
- Interferometer with optical correlator
- CMB spectrometers:
- KISS
- IAC spectrometer

Teide Observatory (Tenerife)





(** = in operation)

(J.A. Rubiño. https://indico.in2p3.fr/event/14661/timetable)

Teide Observatory (Tenerife)

Same sky area (>20% sky, North Hemisphere) 10 frequencies from 10 to 240 GHz Redundancy, cross-correlation

QUIJOTE

6 frequencies in 10-40 GHz range Large scale survey, deep fields



LSPE/SWIPE 140-220-240GHz

1st Stage

2nd Stag

Pulse Tube Cooler

LSPE horns & bolo holders (INFN-RM

lanes (INFN-RM1)

LSPE/STRIP 43 + 90 GHz channels Large scale surveys, deep fields

60

(J.A. Rubiño. <u>https://indico.in2p3.fr/event/14661/timetable</u>

Moore's law for detectors



Figure 2. Plot illustrating the evolution of the raw sensitivity of CMB experiments, which scales as the total number of bolometers. Ground-based CMB experiments are classified into Stages with Stage II experiments having O(1000) detectors, Stage III experiments having O(10,000) detectors, and a Stage IV experiment (such as CMB-S4) having O(100,000) detectors. Figure from Snowmass CF5 Neutrino planning document.

CMB-S4 Science Book – arXiv:1610.02743



A European "whitepaper" (in preparation)

- Introduction
- The Scientific Questions
 - Neutrino Sector, Dark Sector, Inflation, ...

E-CMB/A European coordination for Cosmic Microwave Background Science

- The Requirements to answer these questions
 - What do we need to do?
- The Community
- The State of the Art Today
 - Planck, the S3 experiments, European experiments, ...
- The Scientific Landscape for the Coming Years
 - S4?, LiteBIRD?, others?
- Near Term Roadmap
- Mid Term Roadmap
- Long Term Roadmap

http://wiki.e-cmb.org

CORE The Cosmic Origins Explorer A proposal in response to the ESA call for a Medium-Size space mission for launch in 2029-2030 ٠ ٠ 10^{4} 10^{3} 10² 10⁻³ Lead Proposer: Jacques Delabrouille 10⁻⁵ Co-Leads: Paolo de Bernardis 10-6 François R. Bouchet For ultimate CMB polarisation maps

Submitted to M5 ESA call, but not accepted.

Science case:

- Inflation
- Gravitational lensing (neutrino masses < 44meV).
- DE (FoM increased x10 wrt EUCLID)
- Neff with error < 0.04
- Galaxy clusters.

PIXIE: Primordial Inflation Explorer

- 400 spectral channel in the frequency range 30 GHz and 6THz (Δv ~ 15GHz)
- about 1000 (!!!) times more sensitive than COBE/FIRAS
- B-mode polarization from inflation (r ≈ 10⁻³)
- , improved limits on µ and y

was proposed 2011 as NASA EX mission (i.e. cost ~ 200 M\$)

Kogut et al, JCAP, 2011, arXiv:1105.2044

(Slide from J. Chluba)

LiteBIRD

Lite (Light) Satellite for the Studies of B-mode Polarization and Inflation from Cosmic Background Radiation Detection – Japanese PI: Masashi Hazumi, US PI: Adrian Lee

Conclusions

• A very significant fraction of all the information in cosmology over the last 20 years has come from the study of the CMB anisotropies.

- Still a wealth of information encoded in the polarization of the CMB.
 - Inflation: origin of primordial perturbations. But not only this!
 - Light relics from early universe (Neff)
 - Neutrino: setting the mass scale and testing the 3-neutrino paradigm
 - Reionization: complementary way to 21cm studies.
 - Primordial magnetic fields, Cosmic strings.
 - CMB lensing: mapping all mass in the universe. \rightarrow X-correlation studies.
 - Dark matter, dark energy
 - Unknowns: CMB anomalies at low multipoles, tensions between high & low z universe (H₀, sigma8), lensing, ...