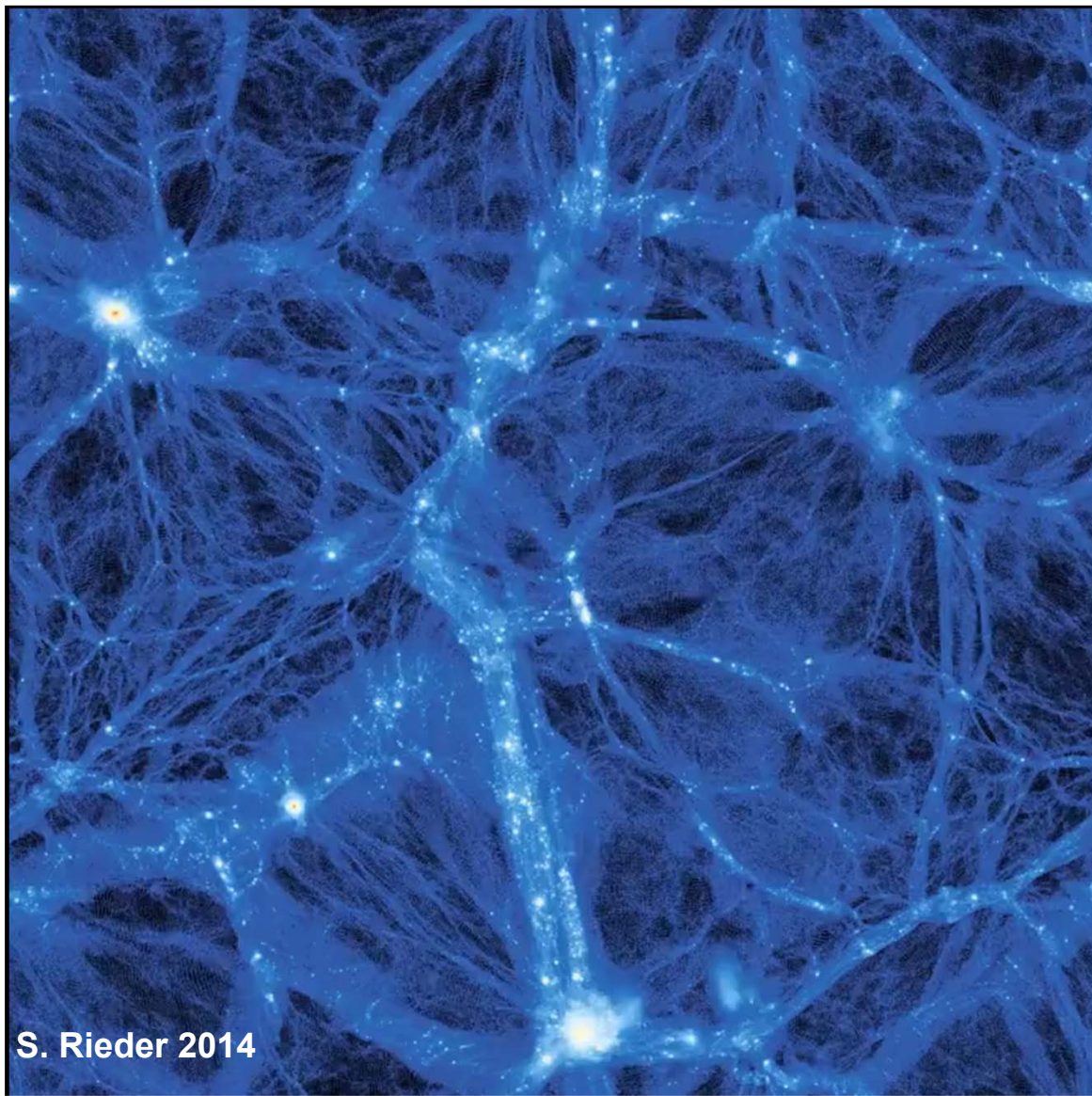


A visualization of the cosmic web, showing a complex network of orange and yellow filaments and nodes against a dark blue background. The nodes are bright points of light, and the filaments are thin, glowing lines connecting them. The overall structure is a dense, interconnected web.

the Cosmic Web:

Structure & Dynamics

Rien van de Weijgaert,
Canary Islands Cosmology School, Fuerteventura, Sept. 2017



on scales of ~ 0.1 -500
millions of lightyears

complex weblike pattern

in which
matter, gas & galaxies
are organized in

- ▣ compact clusters,
 - ▣ elongated filaments
 - ▣ flattened walls
- around
- ▣ cosmic voids

Cosmic Web



Complex Patterns in the Cosmos: Cosmic Web

MMF/Nexus+ tracing of filaments

**inherent multiscale
character of filamentary web**

Hidding, Cautun, vdW et al. 2018

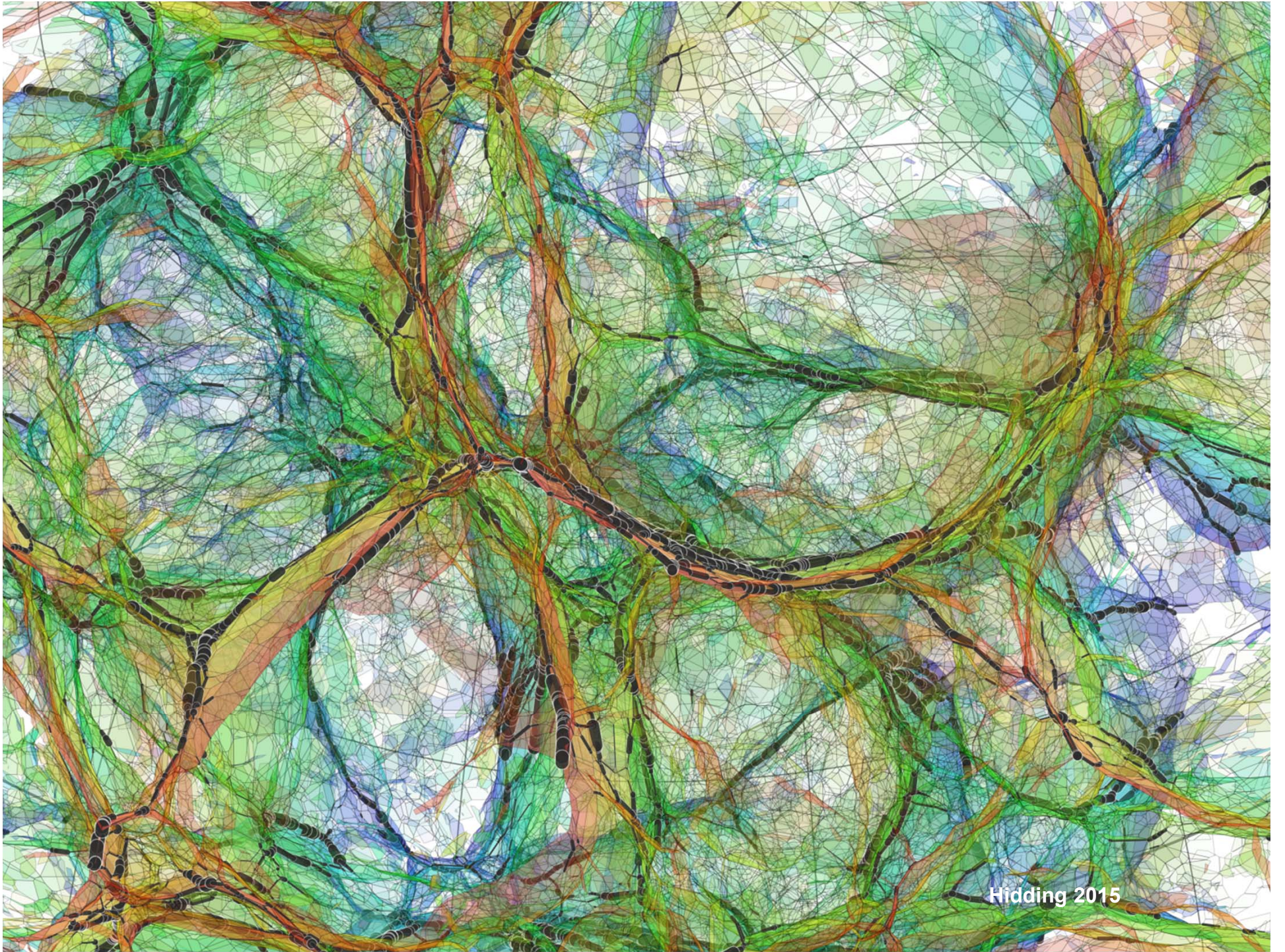
Complex macroscopic patterns in nature arise from the action of basic, often even simple, physical forces and processes. In many physical systems, the spatial organization of matter is one of the most readily observable manifestations of the nonlinear collective actions forming and moulding them.

The richly structured morphologies are a rich source of information on the physical forces at work and the conditions under which the systems evolved. In many branches of science the study of geometric patterns has therefore developed into a major industry for exploring and uncovering the underlying physics

Balbus & Hawley 1998

Cosmic Web

Setting the Scene



Hidding 2015

A million galaxies

Shane-Wirtanen map:

On the basis of the Shane-Wirtanen counts,

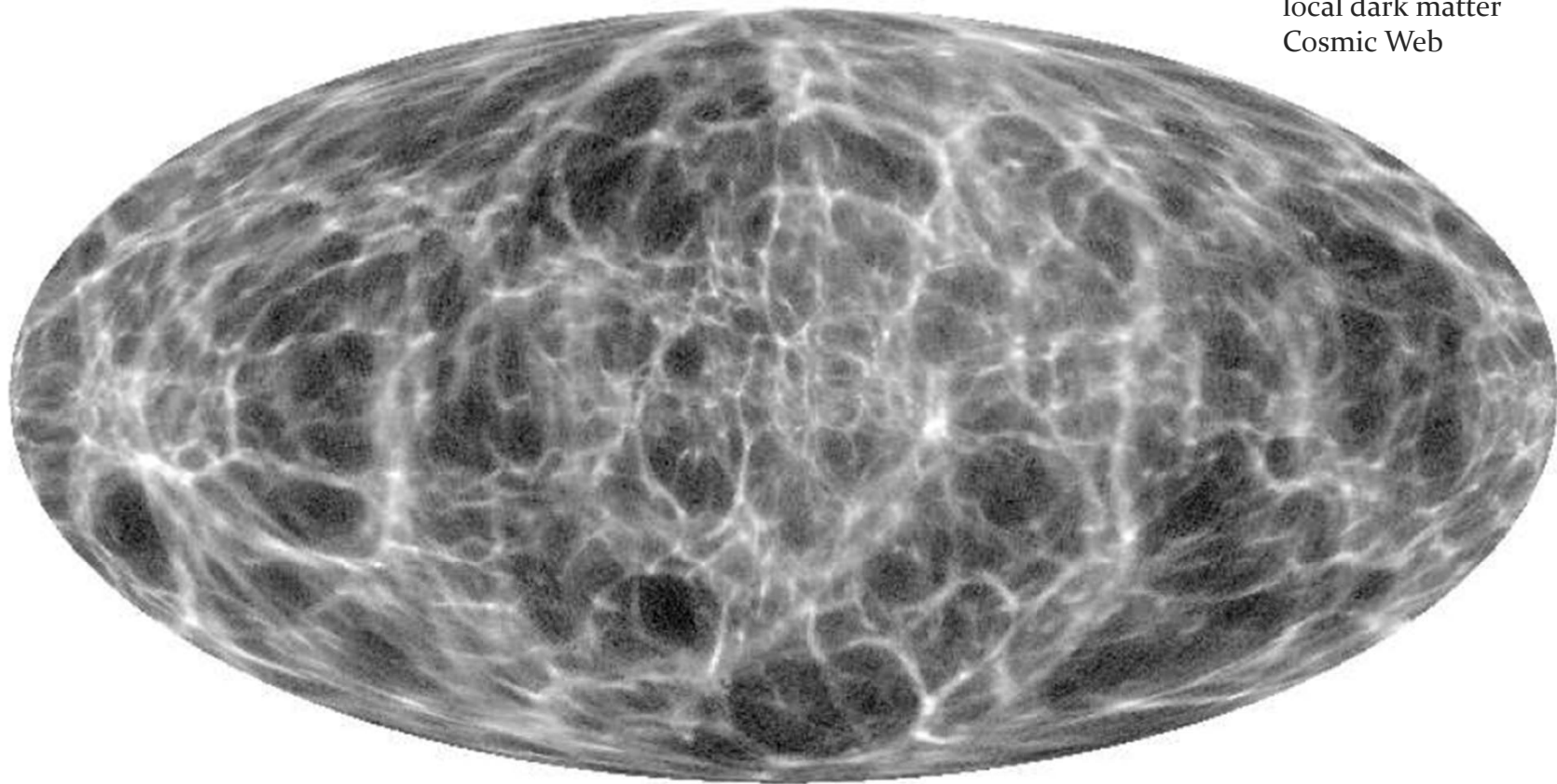
P.J.E. Peebles produced a map of the sky distribution of 1 million galaxies on the sky:

- Clearly visible are clusters
- hint of filamentary LSS features, embedding clusters

local Cosmic Web: z MRS

most detailed reconstruction
of the

local dark matter
Cosmic Web



1.0  6.0

Courtesy: Francisco Kitaura

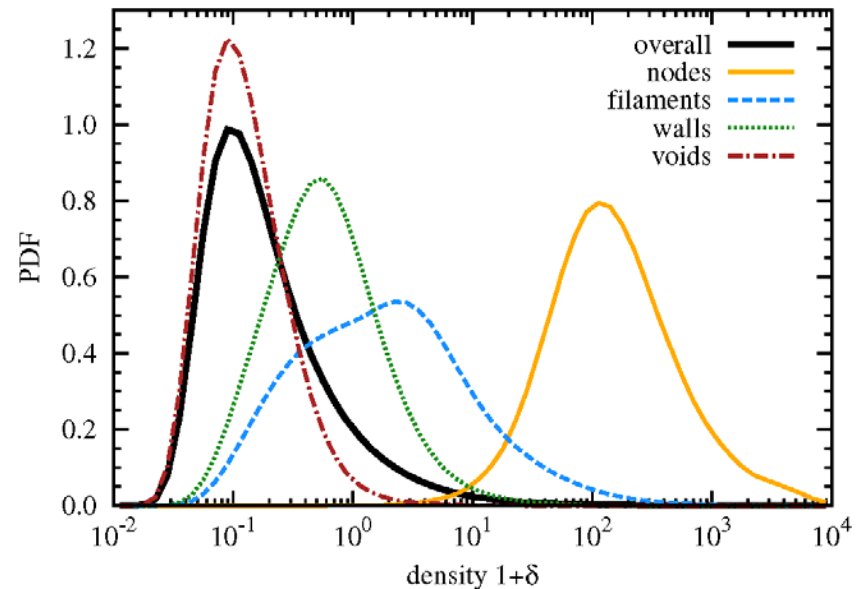
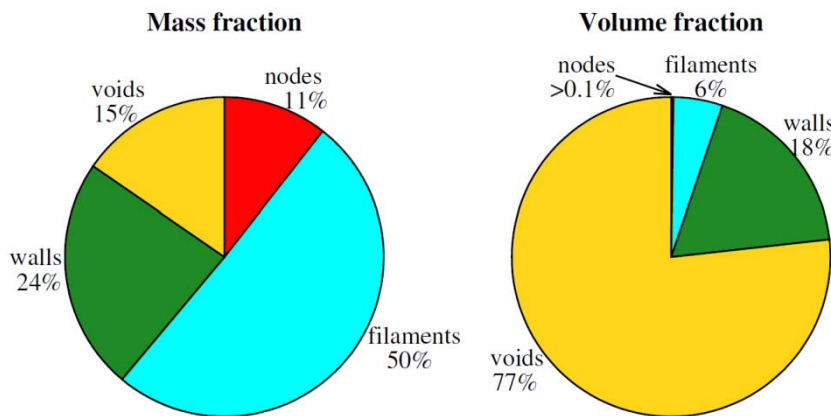
Cosmic Web:

Density-Morphology Connection

Mass & Volume content
Web morphologies



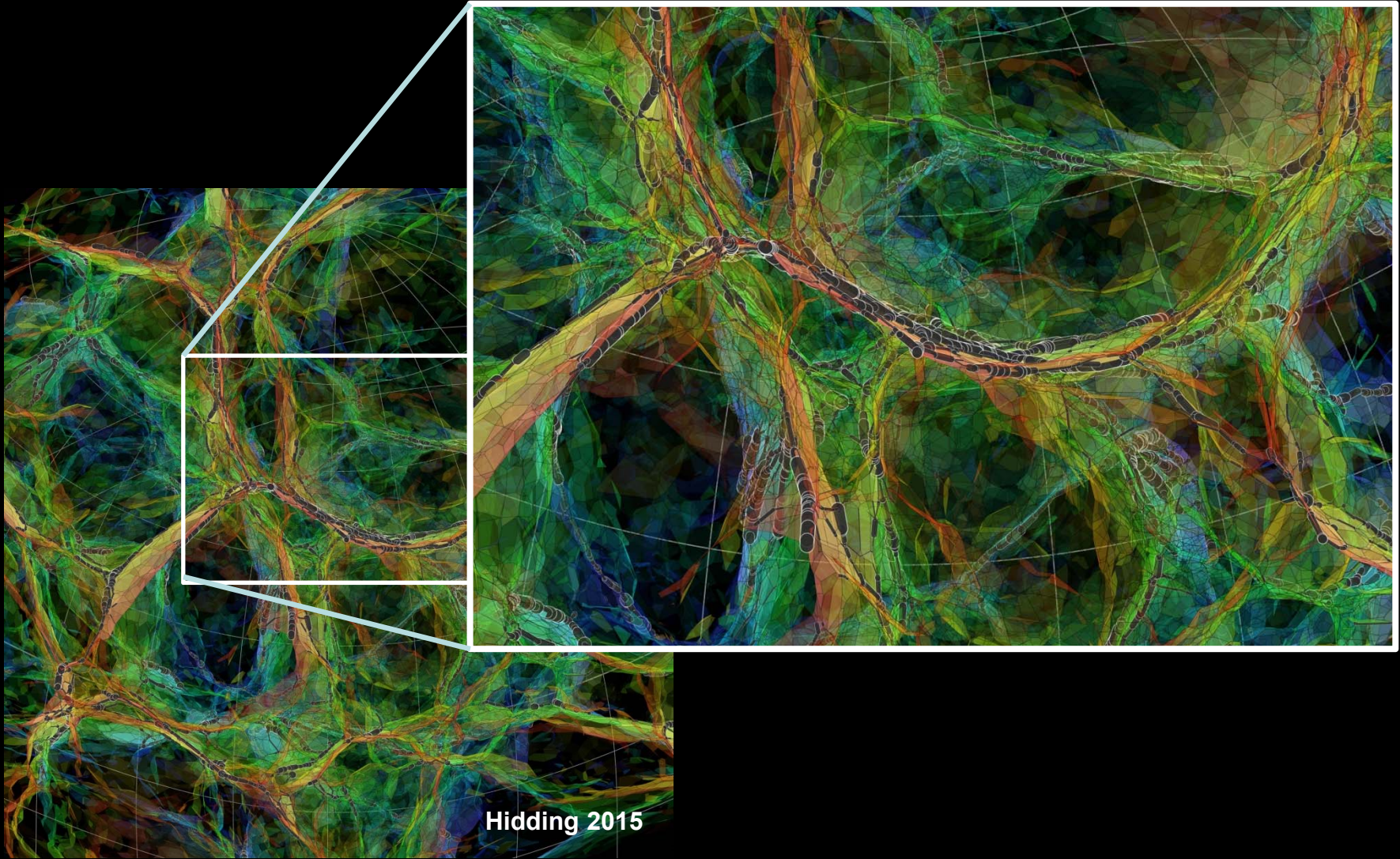
Density distribution
Individual morphologies

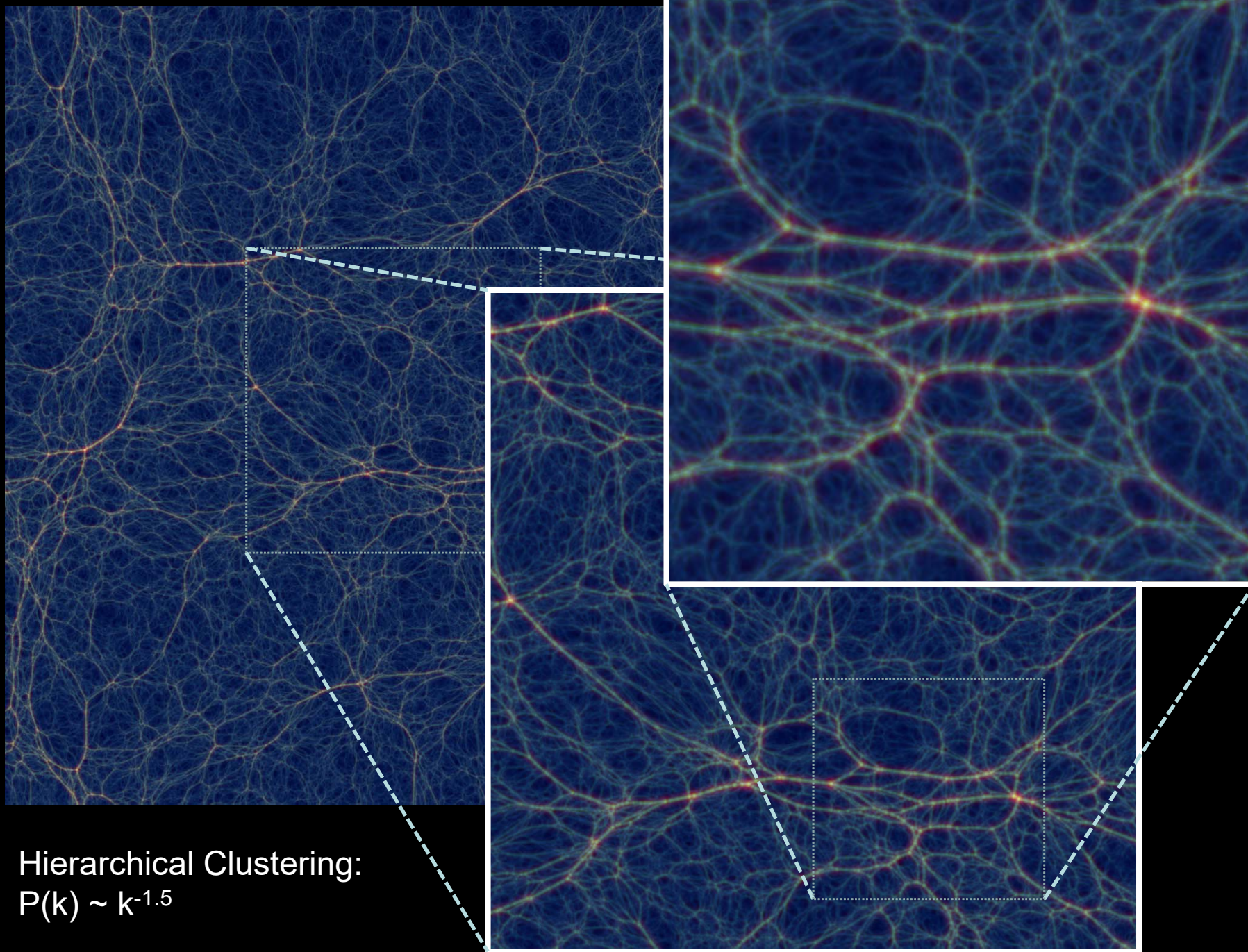


Cosmic Web Characteristics

- **anisotropic structure:**
 - filaments dominant structural feature - elongated
 - sheets/walls - flattened
- **multiscale nature**
 - structure on wide range of scales
 - structures have wide range of densities
- **overdense-underdense asymmetry**
 - voids: underdense, large & roundish
 - filaments & walls: overdense, flattened/elongated
 - clusters: dense, massive & compact nodes
- **complex spatial connectivity**
 - all structural features connected in a complex, multiscale weblike network

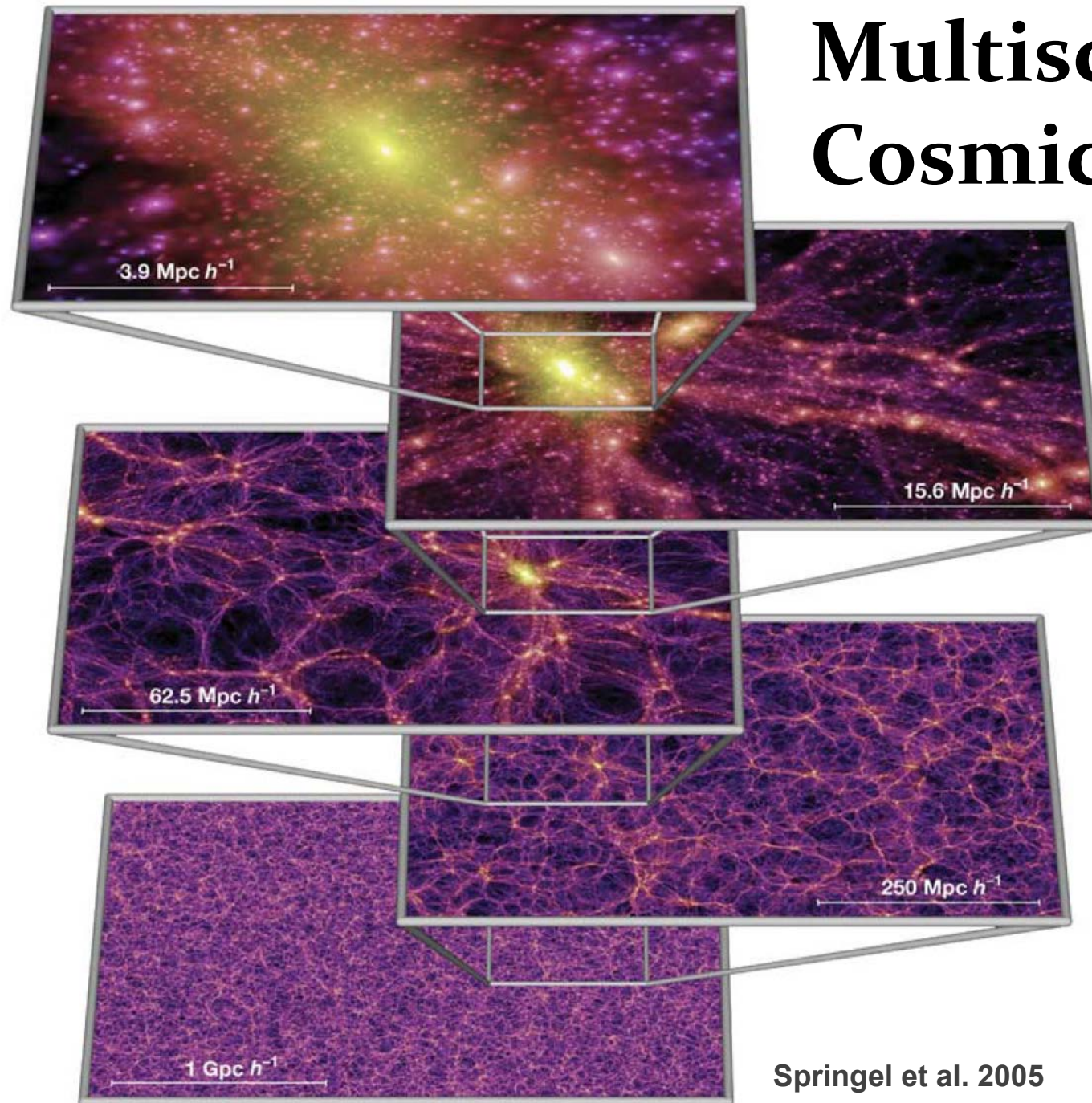
Pisces-Perseus Supercluster





Hierarchical Clustering:
 $P(k) \sim k^{-1.5}$

Multiscale Cosmic Web

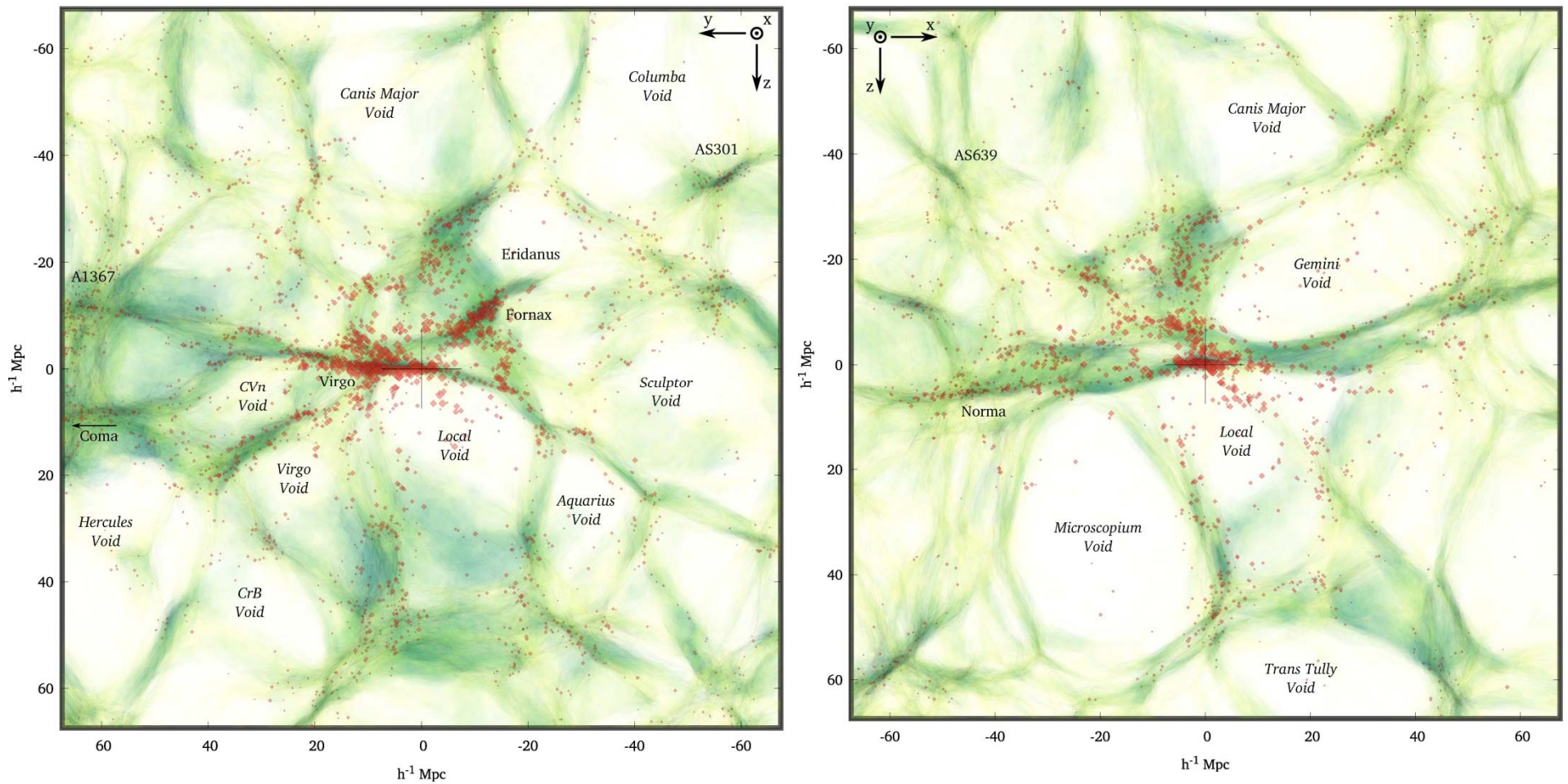


Springel et al. 2005

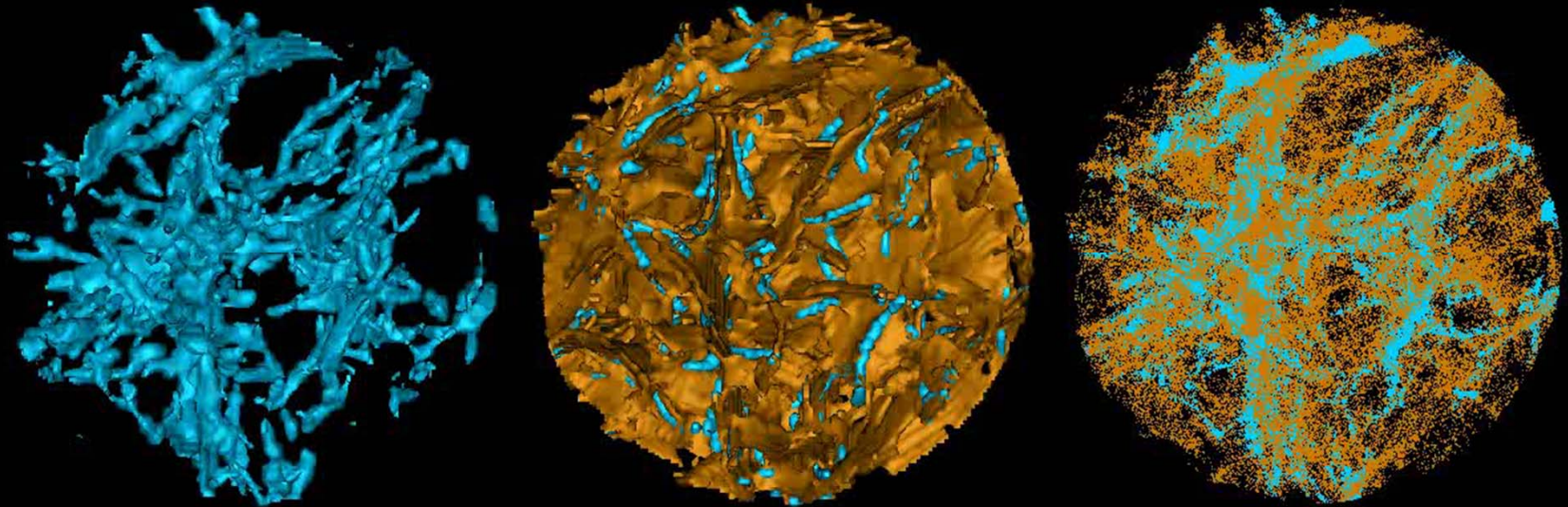
Void Population Local Universe

mean KIGEN-adhesion reconstruction (2MRS)

Hidding, Kitaura, vdW & Hess 2016/2017



Cosmic Web: Connectivity



MMF/Nexus
Cautun et al. 2013, 2014

Stochastic Spatial Pattern

- Clusters,
 - Filaments &
 - Walls
- around
- Voids

in which matter & galaxies

have agglomerated

through gravity

The Cosmic Web

Physical Significance:

- **Manifestation mildly nonlinear clustering:**
**Transition stage between linear phase
and fully collapsed/virialized objects**
- **Weblike configurations contain
cosmological information:**
eg. Void shapes & Alignments
- **Cosmic environment within which to understand
the formation of galaxies.**

Cosmic Web

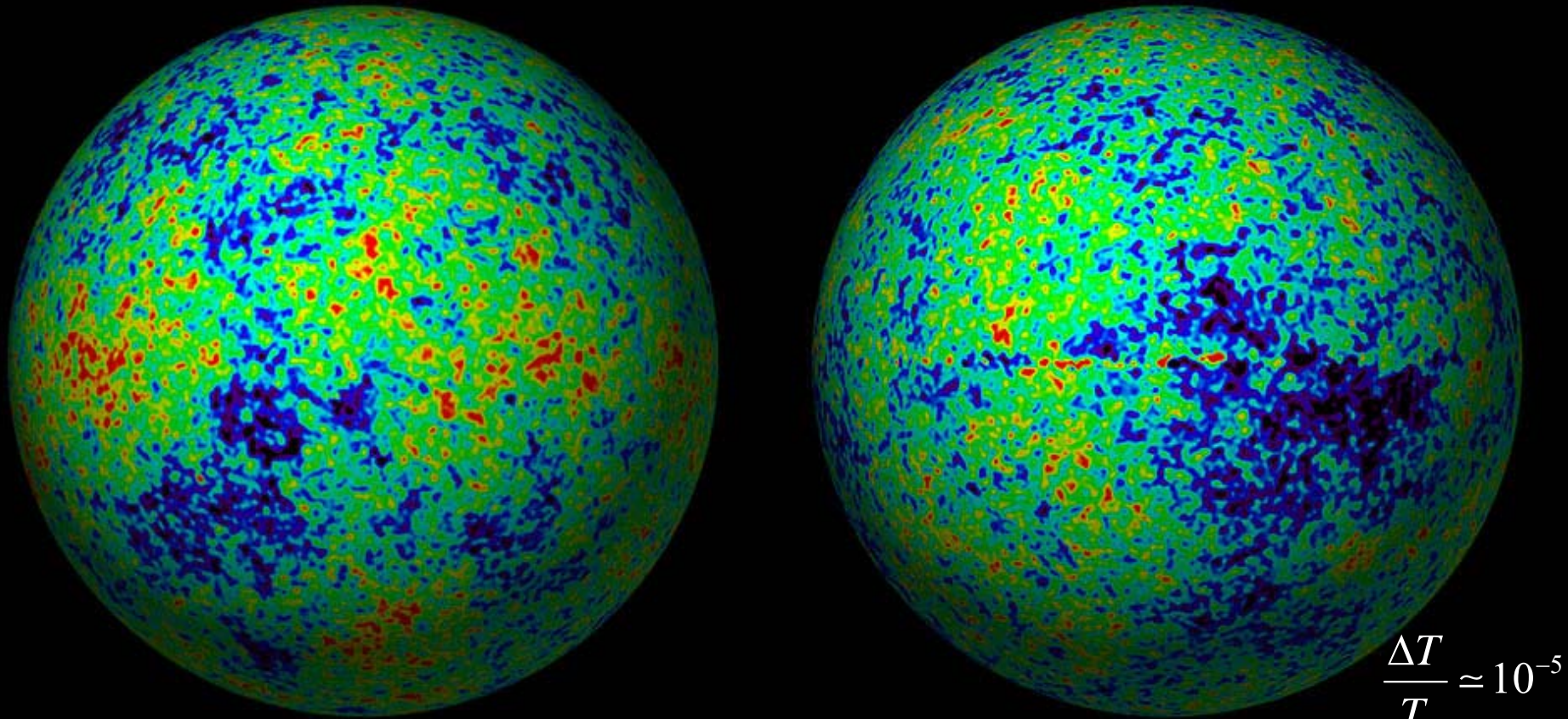
**Dynamics & Formation:
Program**

Cosmic Web – Formation, Evolution, Dynamics

- **the Mechanism** - **Gravitational Instability**
- **Anisotropic Collapse** - **Formation of filaments and walls**
- **Weaving the Web** - **Connection Clusters, Filaments and Walls**
- **Hierarchical Formation** - **from small to the Megaparsec Cosmic Web**
- **Anisotropy & Hierarchy** - **the Adhesion formalism**
- **Phase Space** - **Multistream structure**
 - **Caustics & Catastrophes**
 - **Skeleton of the Cosmic Web**
- **Voids** - **Void Hierarchy**
 - **the evolving soapsud**

**Cosmic
Structure Formation:
Gravitational
Instability**

Primordial Universe

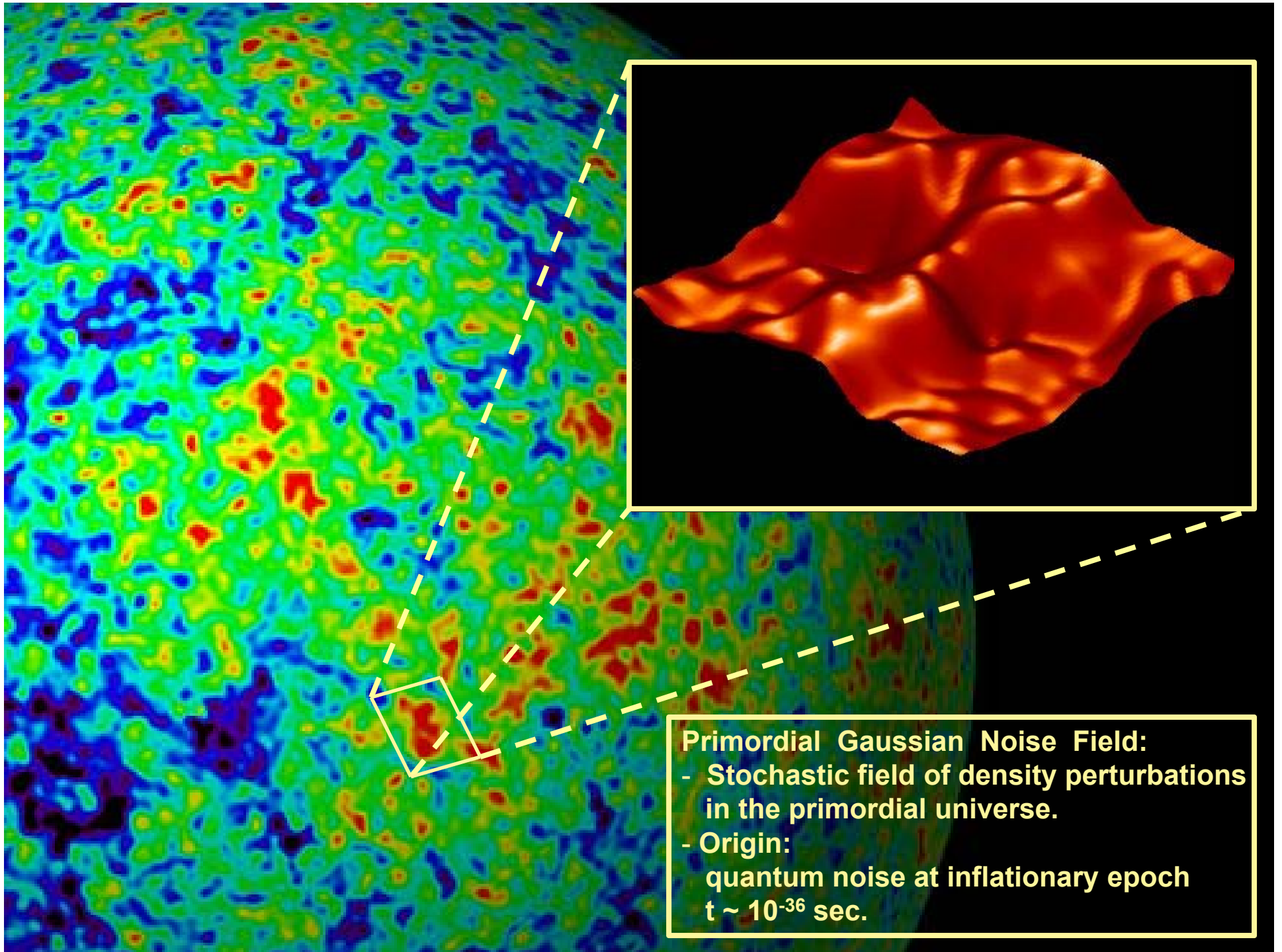


$$\frac{\Delta T}{T} \simeq 10^{-5}$$

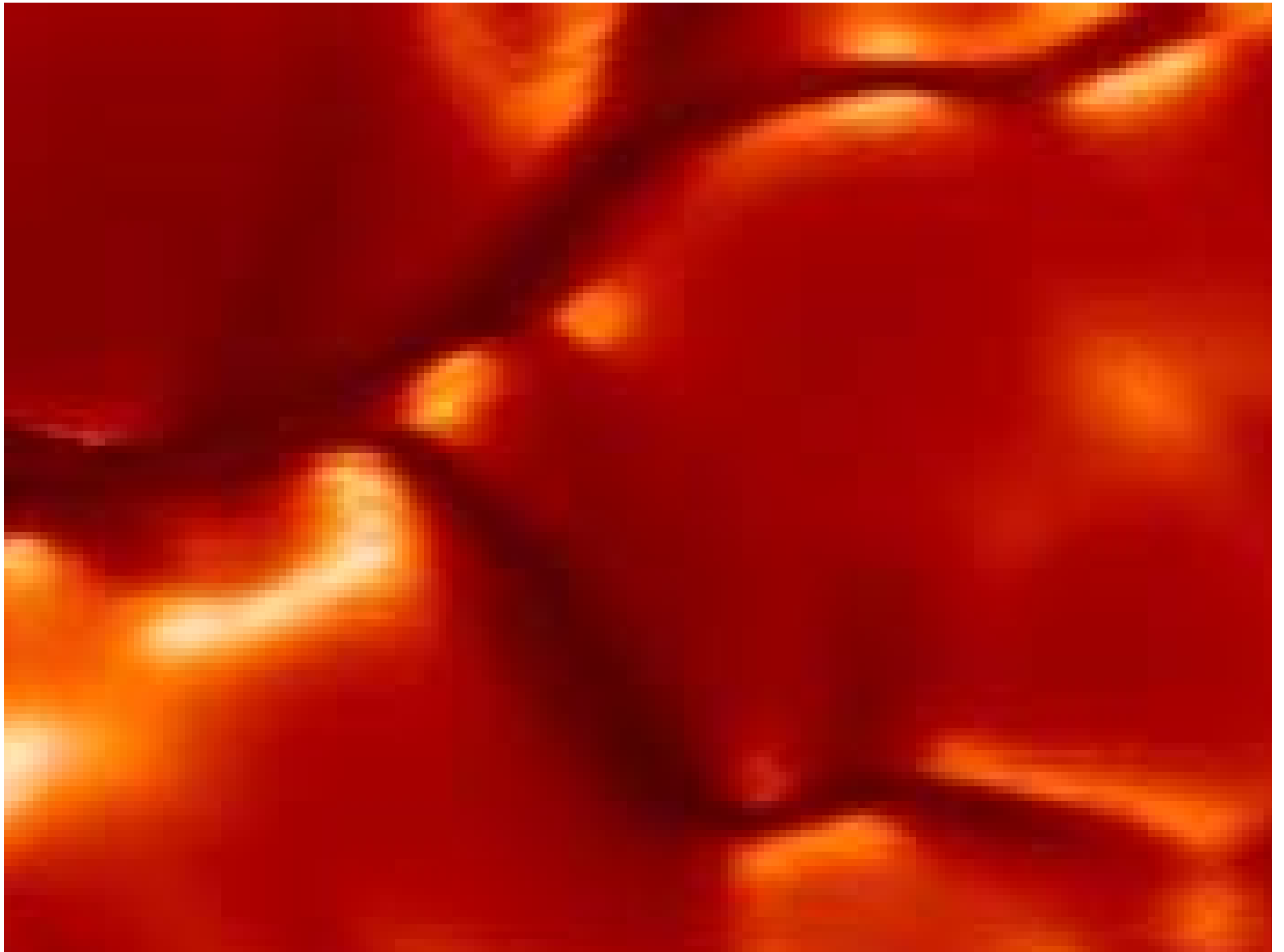
global representation cosmic surface last scattering: the world inside out

Temperature Map CMB radiation:

Tiny variations in primordial temperature, reflecting tiny inhomogeneities in energy density of $\sim 10^{-5}$ K at recombination epoch, 379,000 yrs after Big Bang



Primordial Gaussian Noise Field:
- Stochastic field of density perturbations in the primordial universe.
- Origin: quantum noise at inflationary epoch $t \sim 10^{-36}$ sec.



Density Perturbation Field:

$$\delta(\vec{x}, t) = \frac{\rho(x, t) - \rho_u(t)}{\rho_u(t)}$$

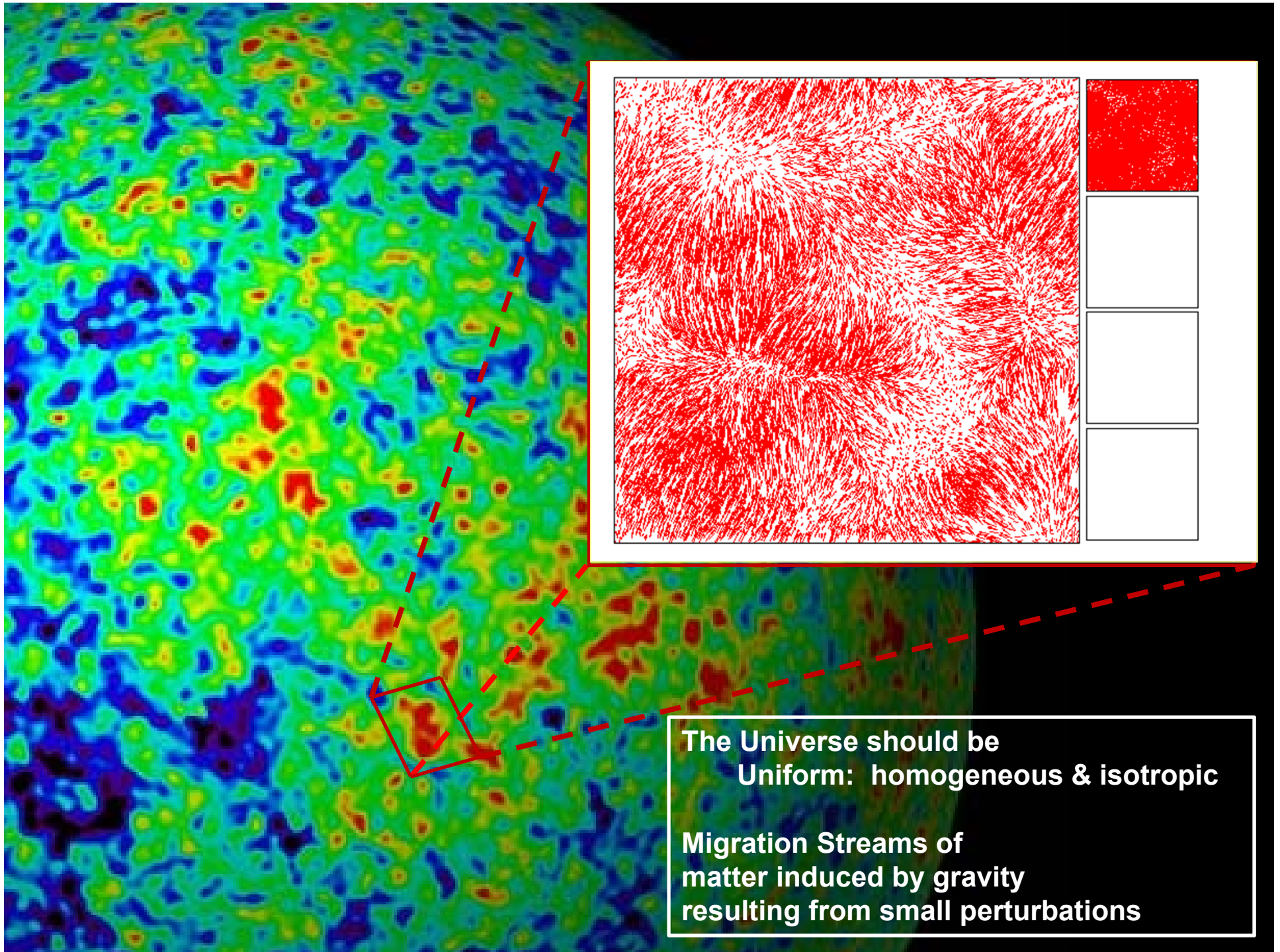
The background of the slide is a Cosmic Microwave Background (CMB) fluctuation map, showing a complex pattern of red and orange tones with subtle variations in intensity, representing temperature fluctuations in the early universe.

Gravity Perturbations



Gravity Perturbations

$$\mathbf{g}(\mathbf{r}, t) = -\frac{1}{a} \nabla \phi = \frac{3\Omega H^2}{8\pi} \int d\mathbf{x}' \delta(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3}$$



The Universe should be
Uniform: homogeneous & isotropic

Migration Streams of
matter induced by gravity
resulting from small perturbations

Cosmic Structure Formation

(Energy) Density Perturbations



Gravity Perturbations



(Cosmic) Flows of (Energy) & Matter:

☐ towards high density regions:

- assemble more and more matter
- their expansion comes to a halt
- turn around and collapse

☐ evacuating void regions

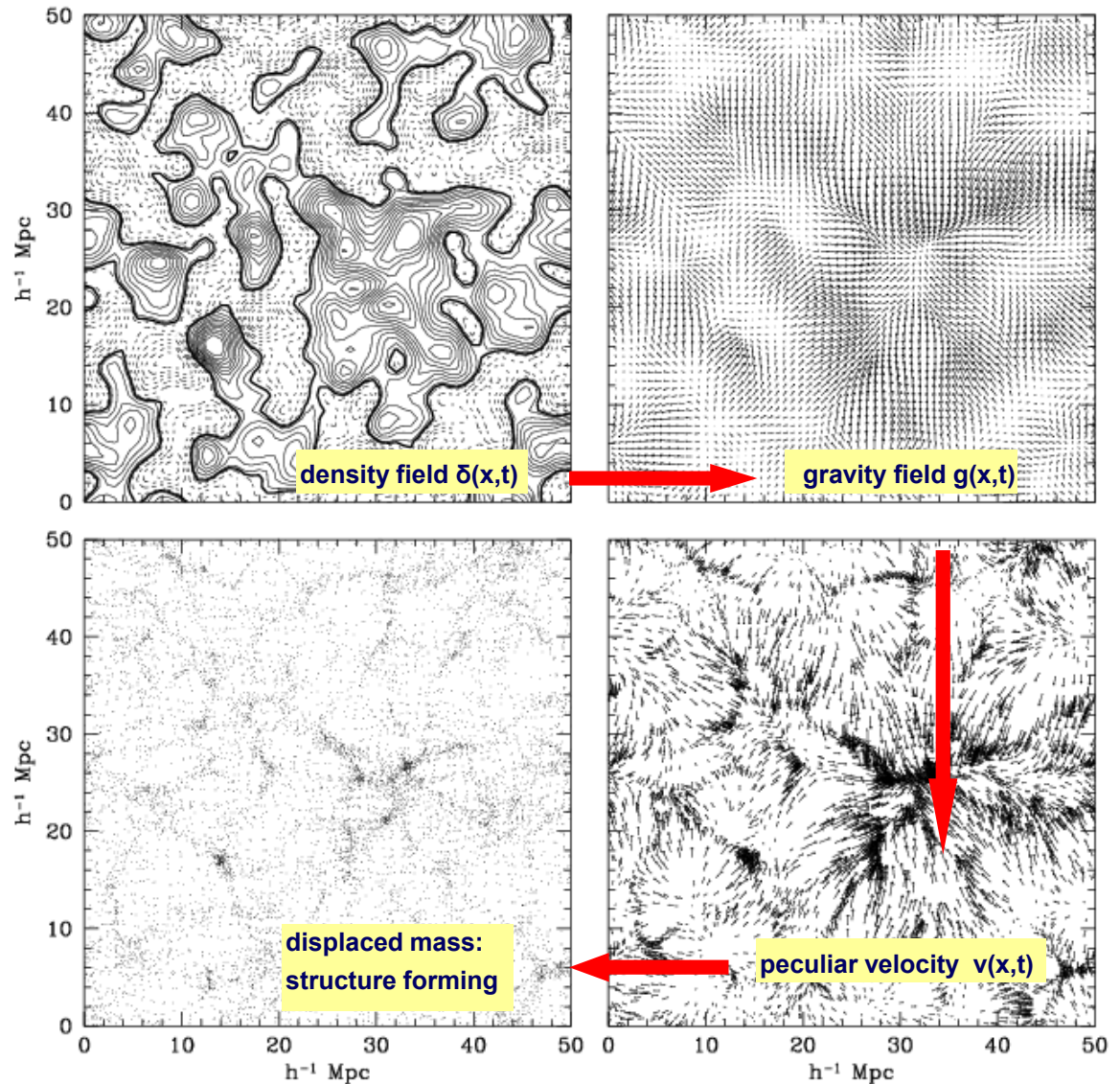
- low-density regions expand
- matter moves out of region
- turn into prominent empty voids



Emergence of cosmic structures

☐ Computer Simulations

- succesfull confrontation with observational reality



Cosmic Structure Formation

Millennium
Simulation:
LCDM

31.25 Mpc/h



Dark Matter,
(~ 5.5x more than
baryonic matter)



**without: not enough time
to form structure in the
Universe in 13.8 Gyrs**

**(cosmic web, clusters,
galaxies, stars, ...)**

(courtesy:
Virgo/V. Springel).

Cosmic Structure Formation

Millennium
Simulation:
LCDM

31.25 Mpc/h



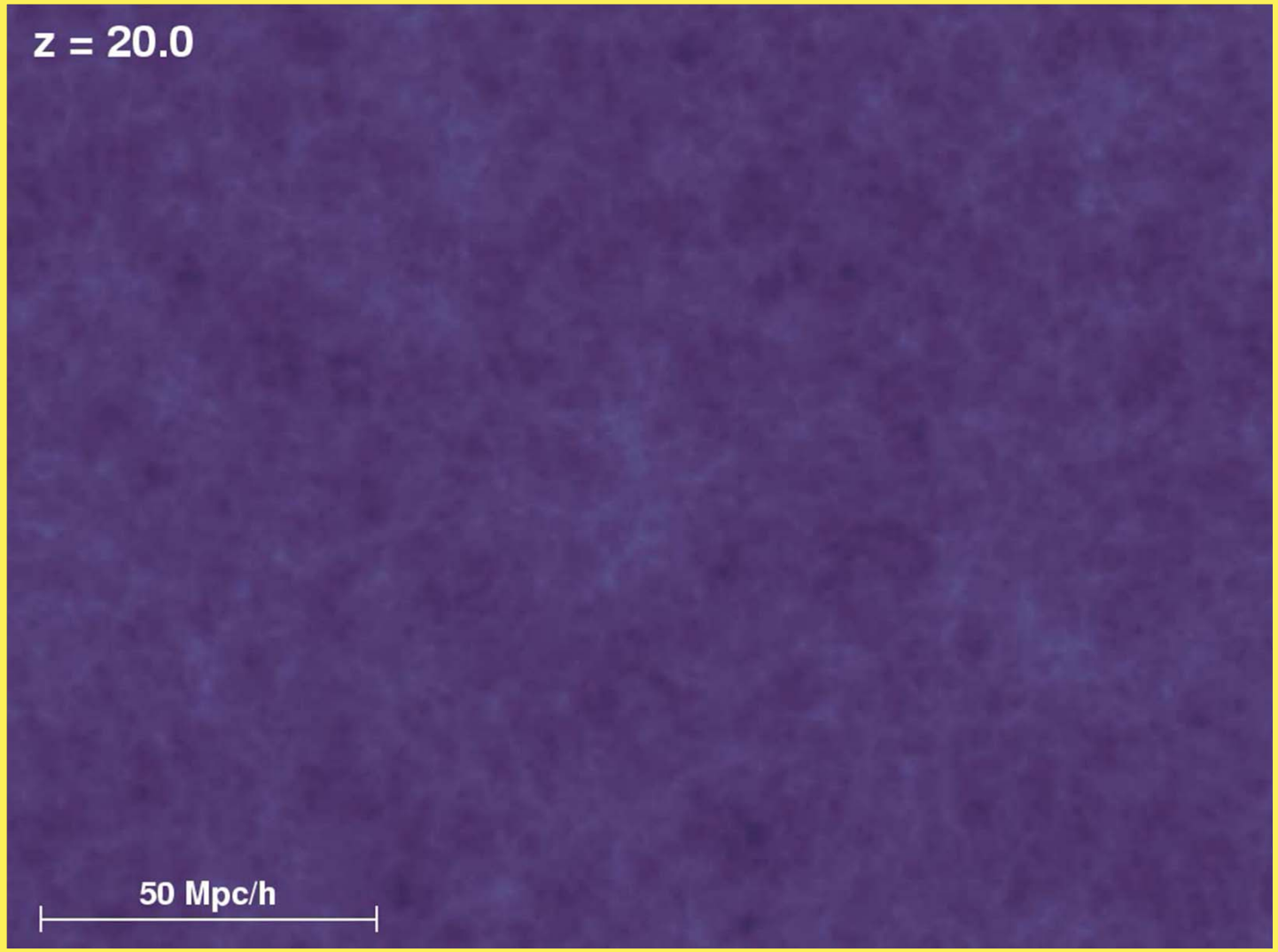
(courtesy:
Virgo/V. Springel).

Cosmic Structure Formation

**Formation
Cosmic Web:
simulation
sequence
(cold)
dark matter**

(courtesy:
Virgo/V. Springel).

$z = 20.0$



50 Mpc/h

Dynamical Evolution Cosmic Web

- hierarchical structure formation
- anisotropic collapse
- establishing the connectivity
- void formation:
 - asymmetry
 - overdense vs. underdense

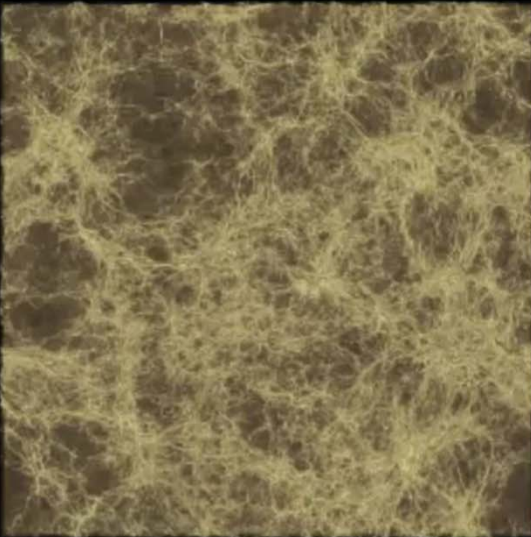
the Cosmic Web:

**evolution of
walls & filaments**

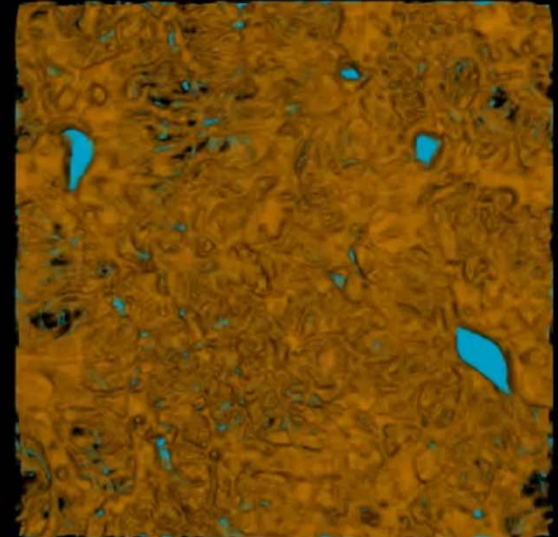
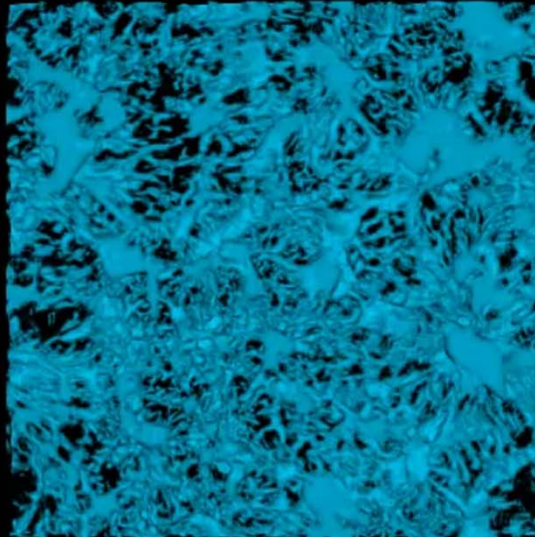
NEXUS/MMF

Evolution Cosmic Web

$t = 0.56$ Gyrs



$z = 8.70$

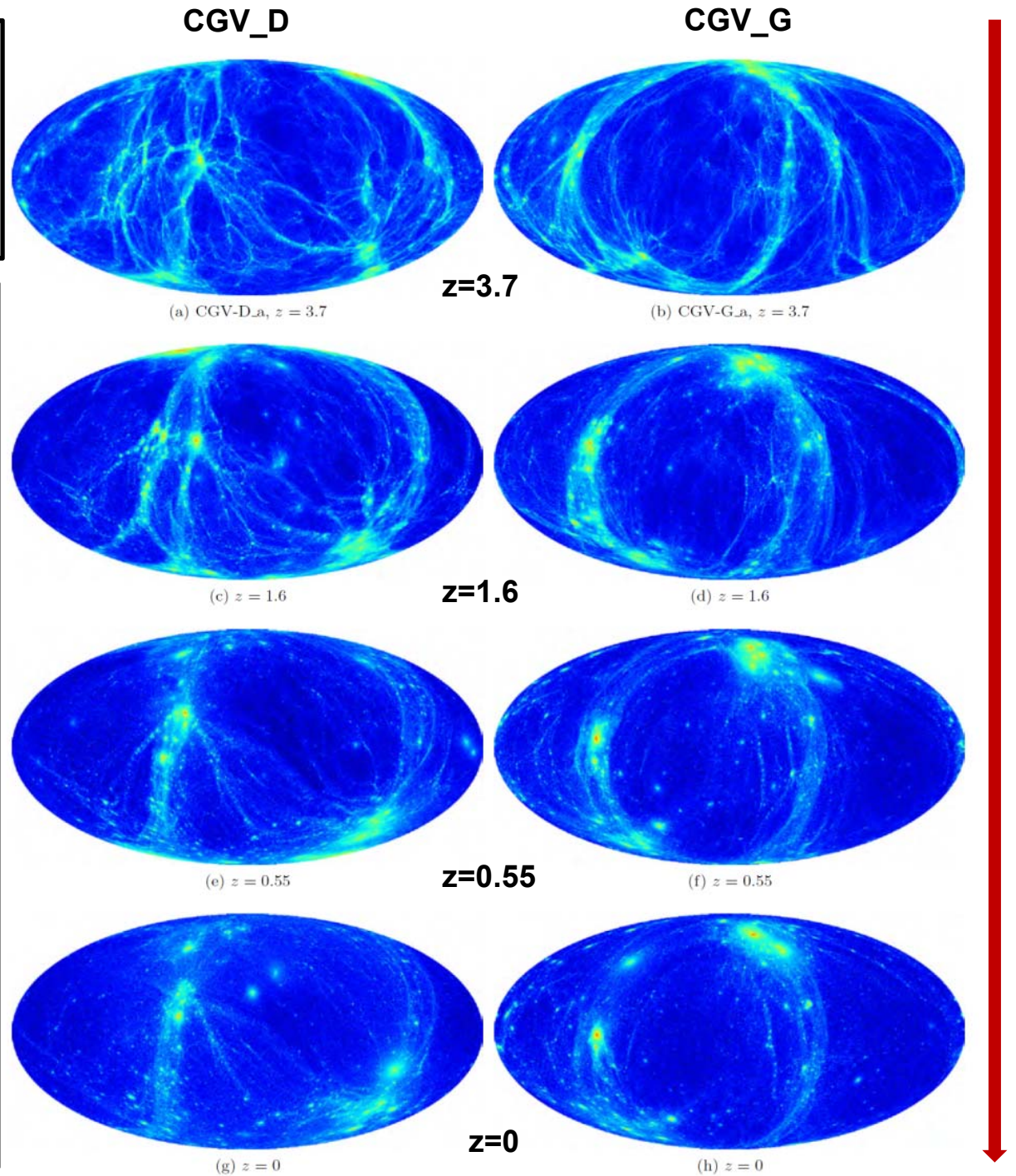


CGV:

on walls & filaments

- Mollweide sky projection matter distribution around CGV halos
- CGV halos embedded in walls
- Walls dominate void infrastructure
- substantial fraction in filaments (embedded in walls)
- active dynamical evolution of wall-filament goes along with active void galaxy halo evolution

Rieder et al. 2013



CGV:

on walls & filaments

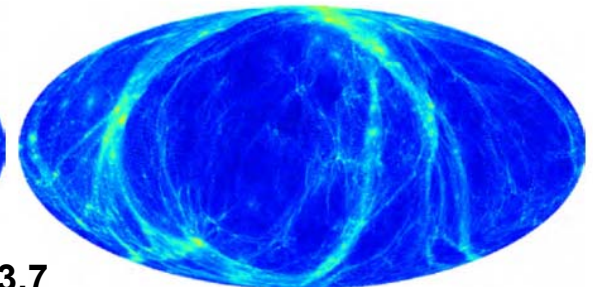
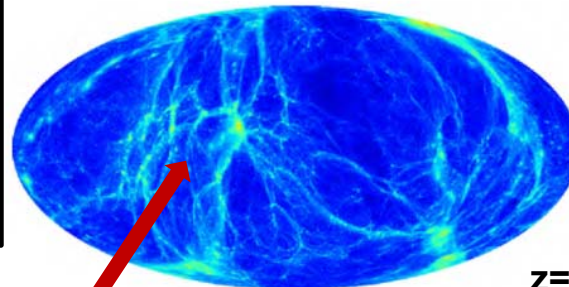
- Mollweide sky projection matter distribution around CGV halos
- CGV halos embedded in walls
- Walls dominate void infrastructure
- substantial fraction in filaments (embedded in walls)
- active dynamical evolution of wall-filament goes along with active void galaxy halo evolution

merging system of
Intravoid walls

Rieder et al. 2013

CGV_D

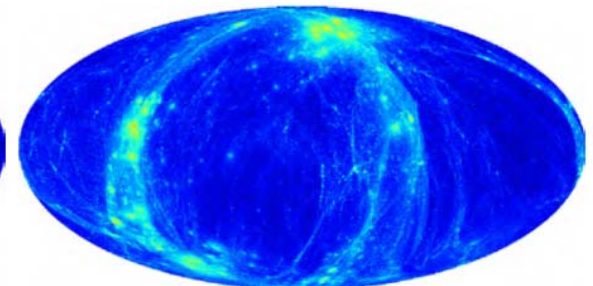
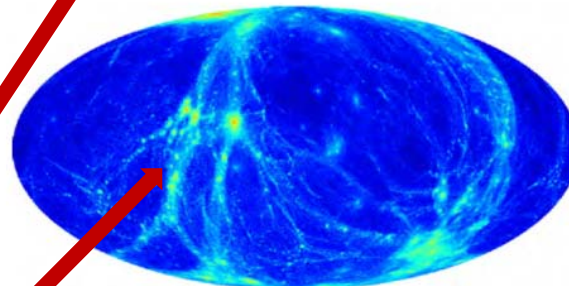
CGV_G



(a) CGV-D.a, $z = 3.7$

(b) CGV-G.a, $z = 3.7$

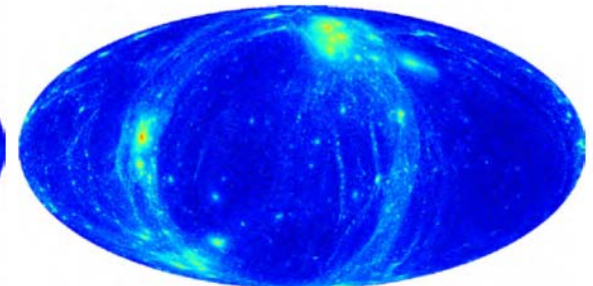
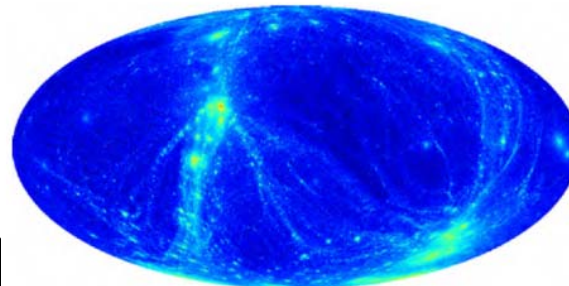
$z=3.7$



(c) $z = 1.6$

(d) $z = 1.6$

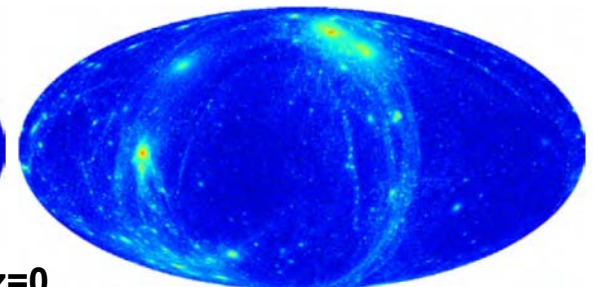
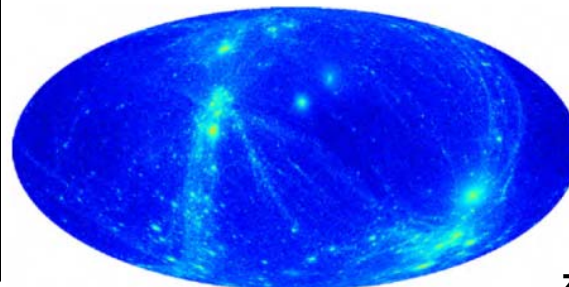
$z=1.6$



(e) $z = 0.55$

(f) $z = 0.55$

$z=0.55$



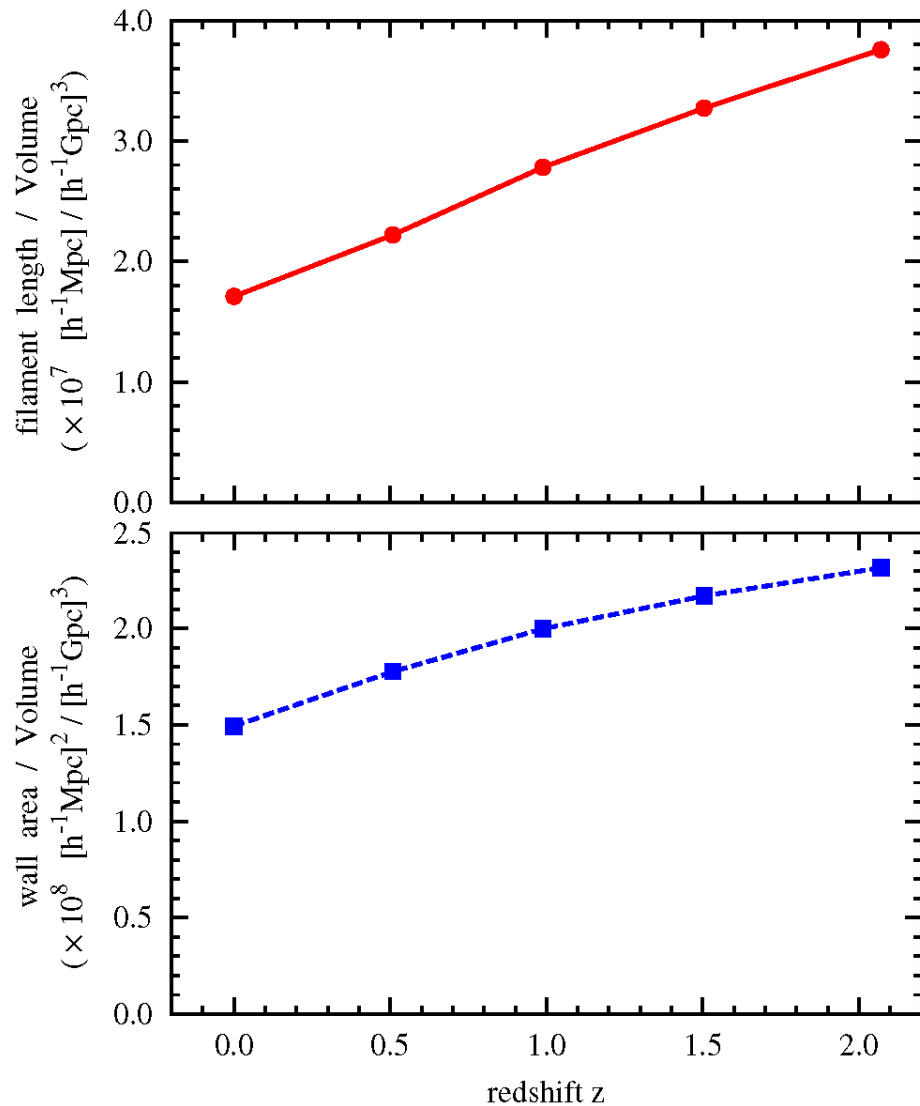
(g) $z = 0$

(h) $z = 0$

$z=0$



Evolving Filament & Wall Network

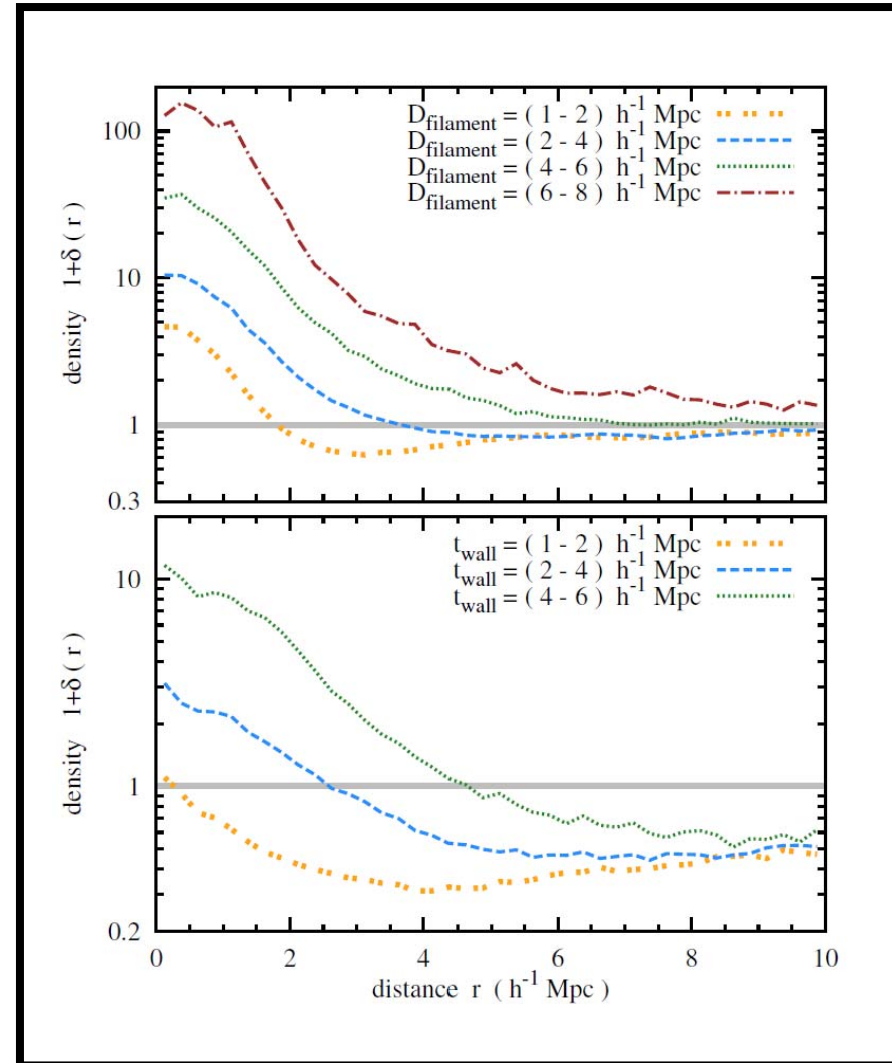
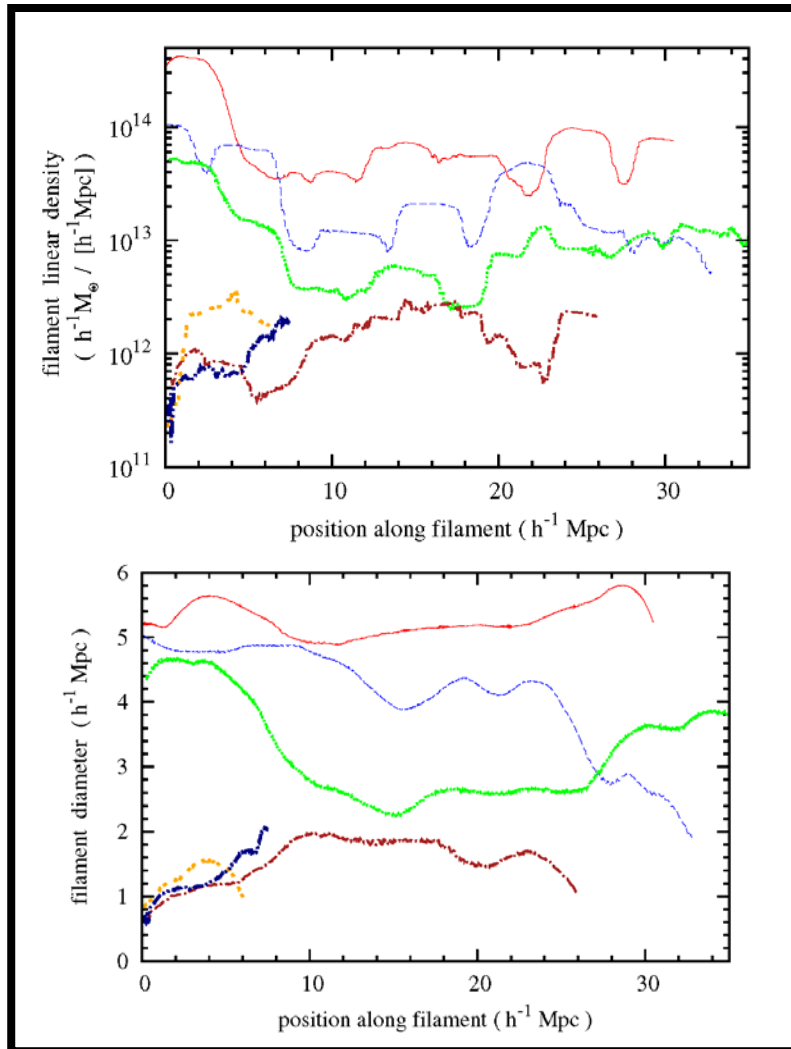


Total length of filament network :
decreasing as a function of time

Total surface area of wall network :
decreasing as a function of time

Walls & Filaments

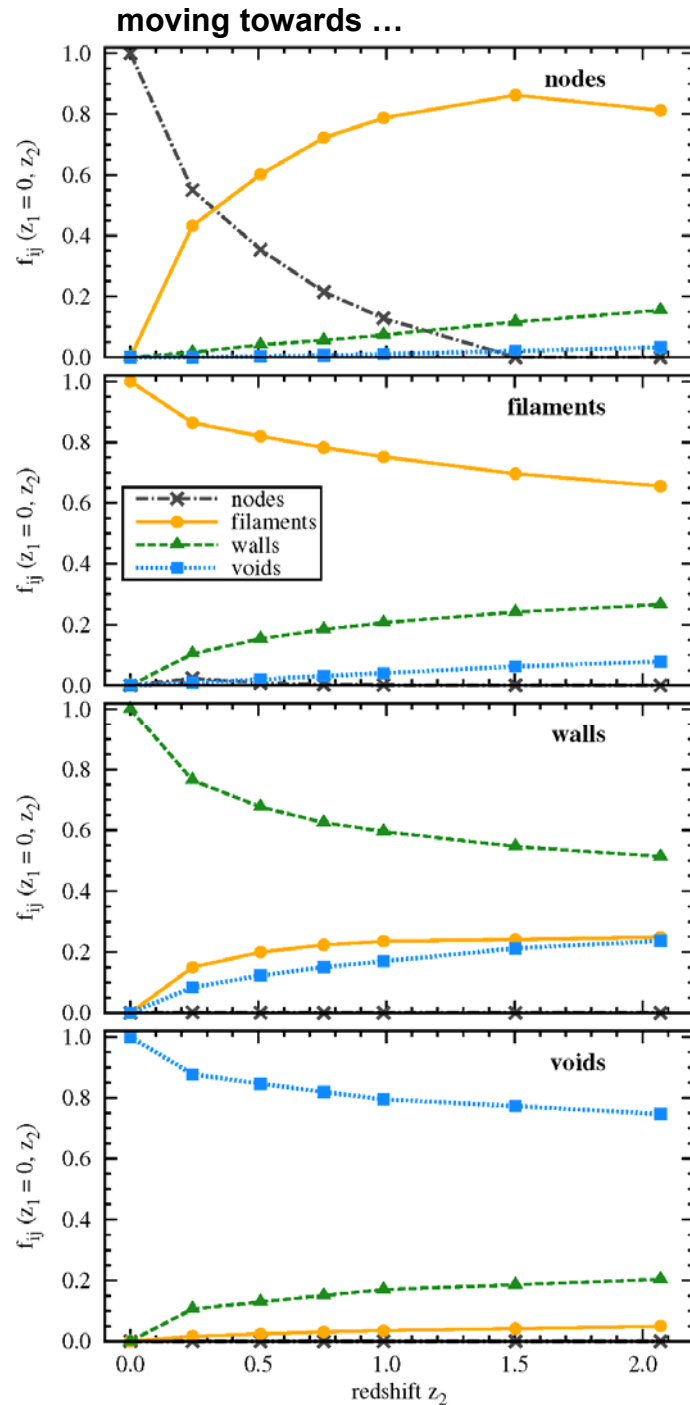
Internal Diameter & Density Profiles



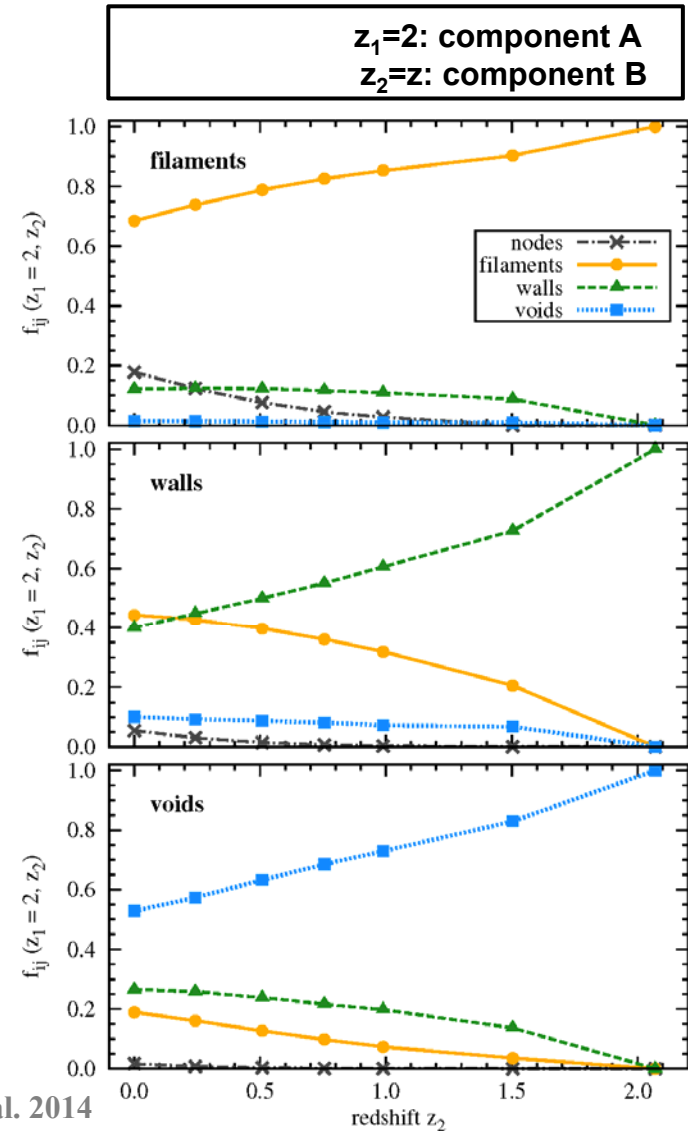
Cosmic Web:

Evolutionary Trends

Web Migration

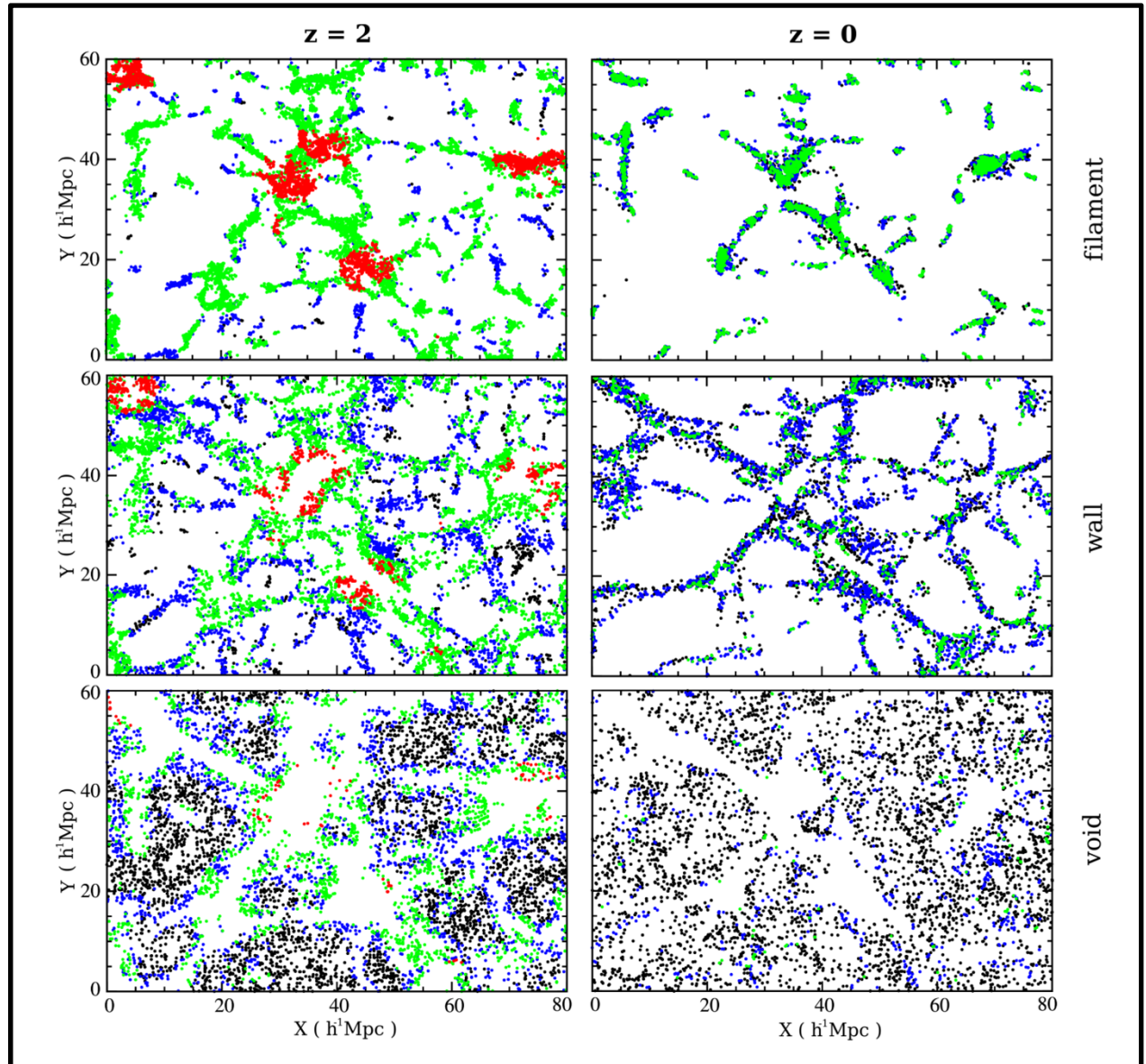
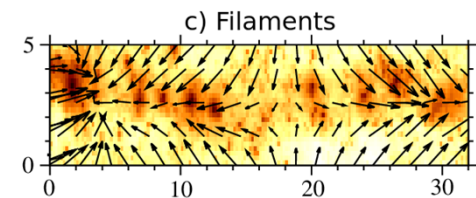
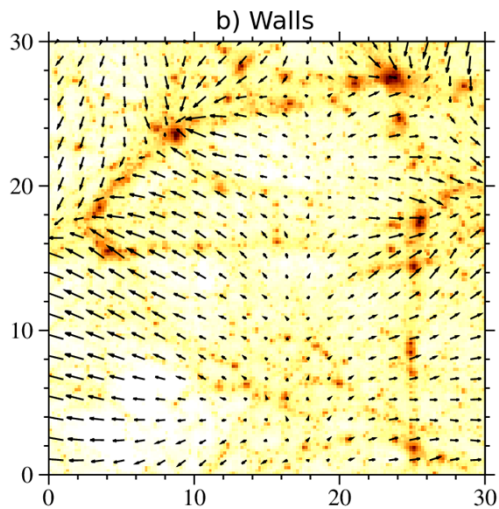
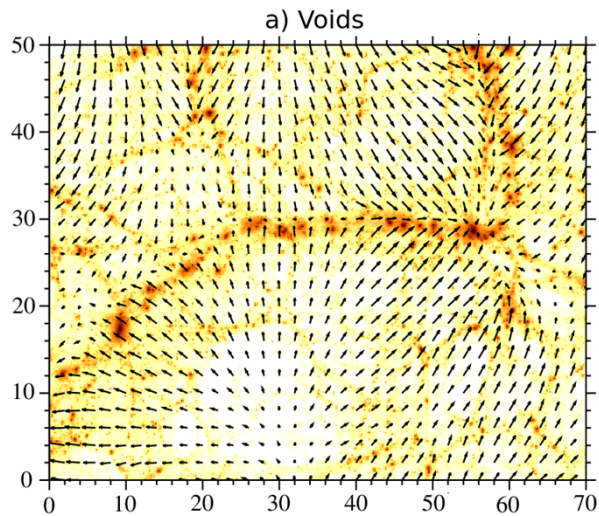


$z_1=0$: component B
 $z_2=z$: component A

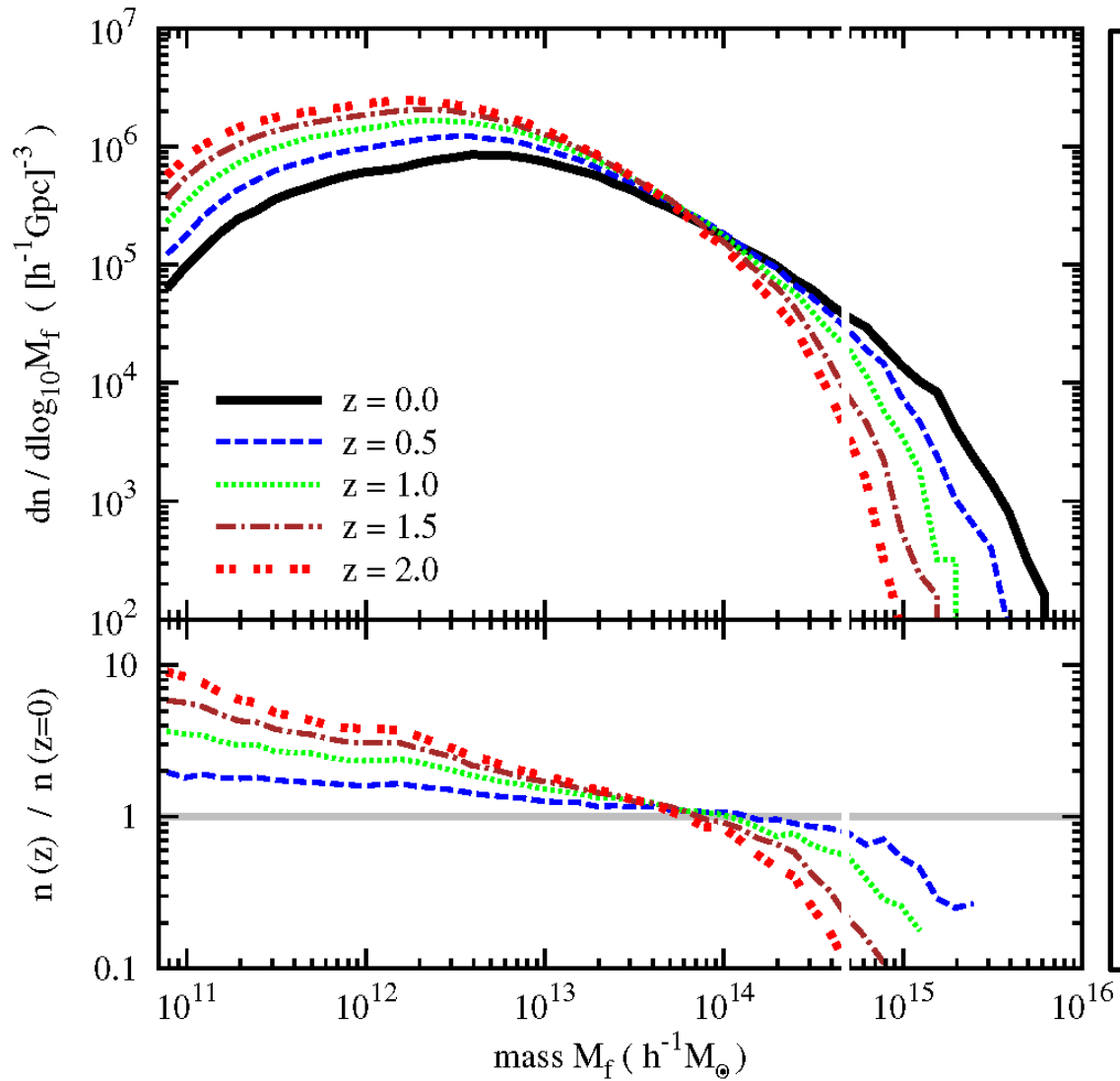


moving out of ...

Web Mass Emigration



Evolving Filament Population



Filament Mass Function:

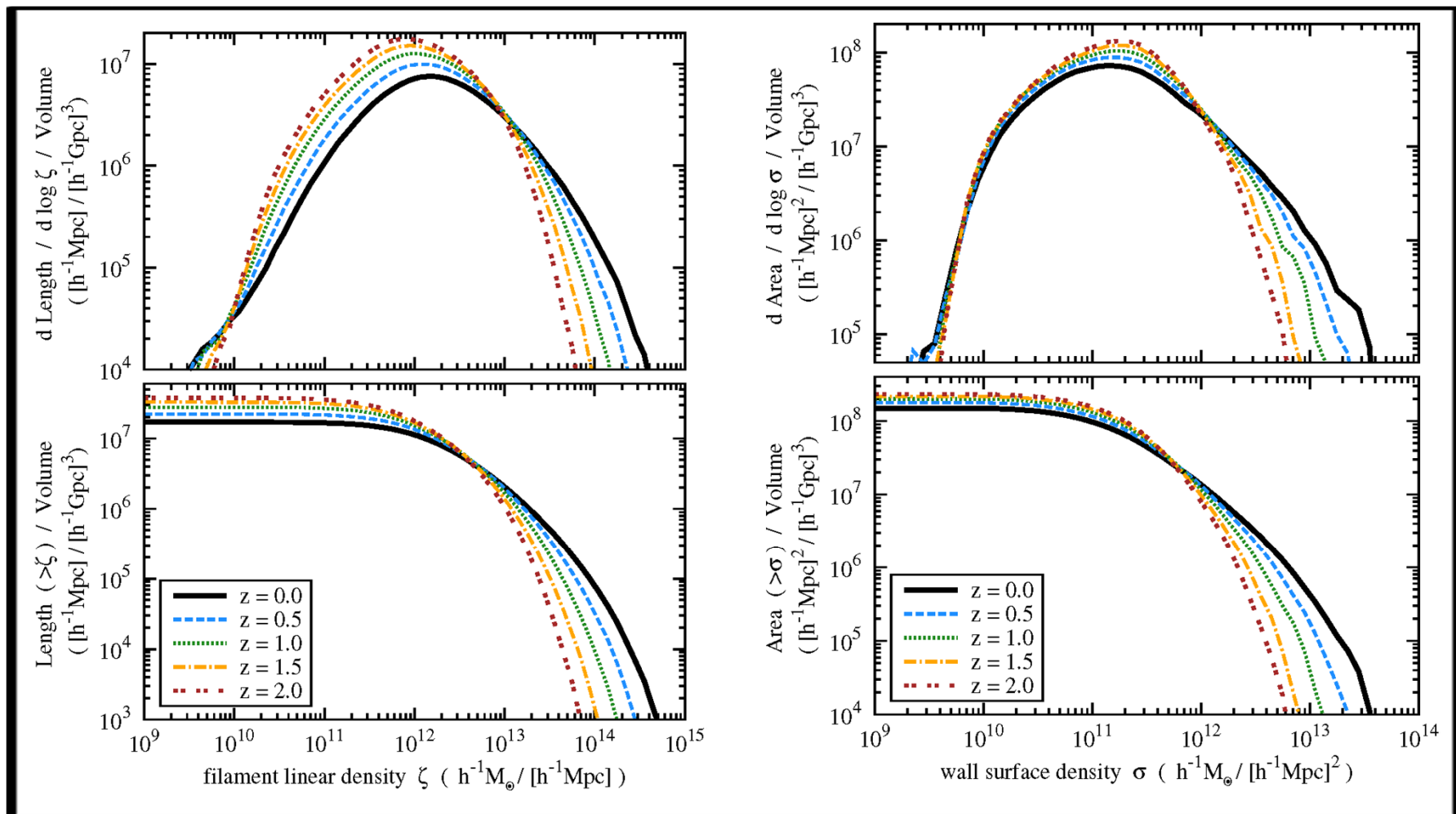
- shifting from small to large mass filaments
- reflection hierarchical evolution filament population

Evolving Filament & Wall Densities

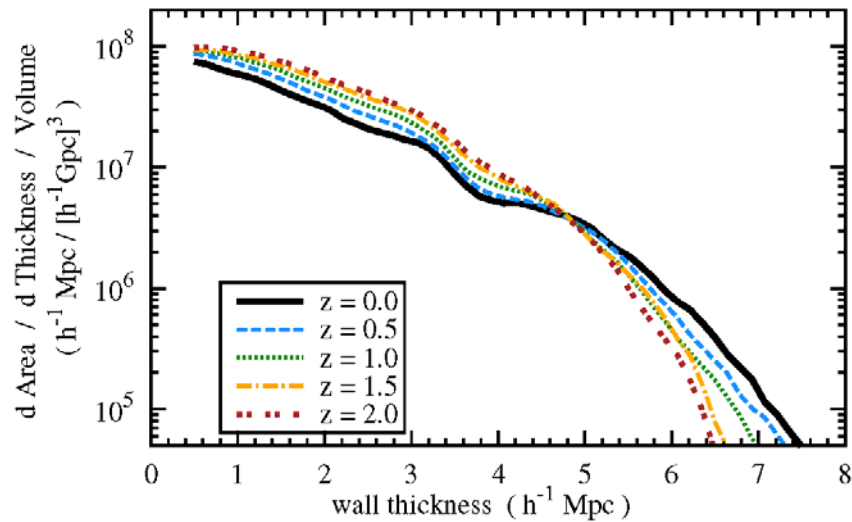
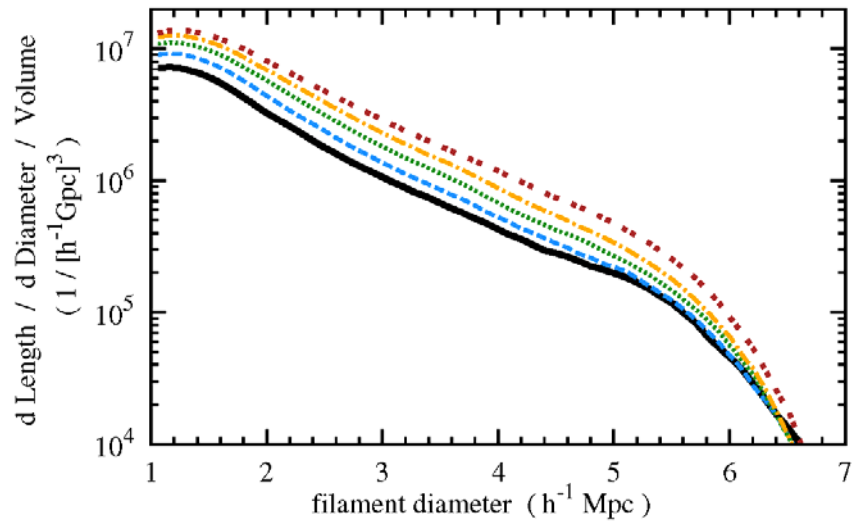
Filament population: evolves continuously towards more dense filaments

Wall population: tenuous walls do not evolve into more dense walls

Cautun et al. 2014



Evolving Filament & Wall Diameters



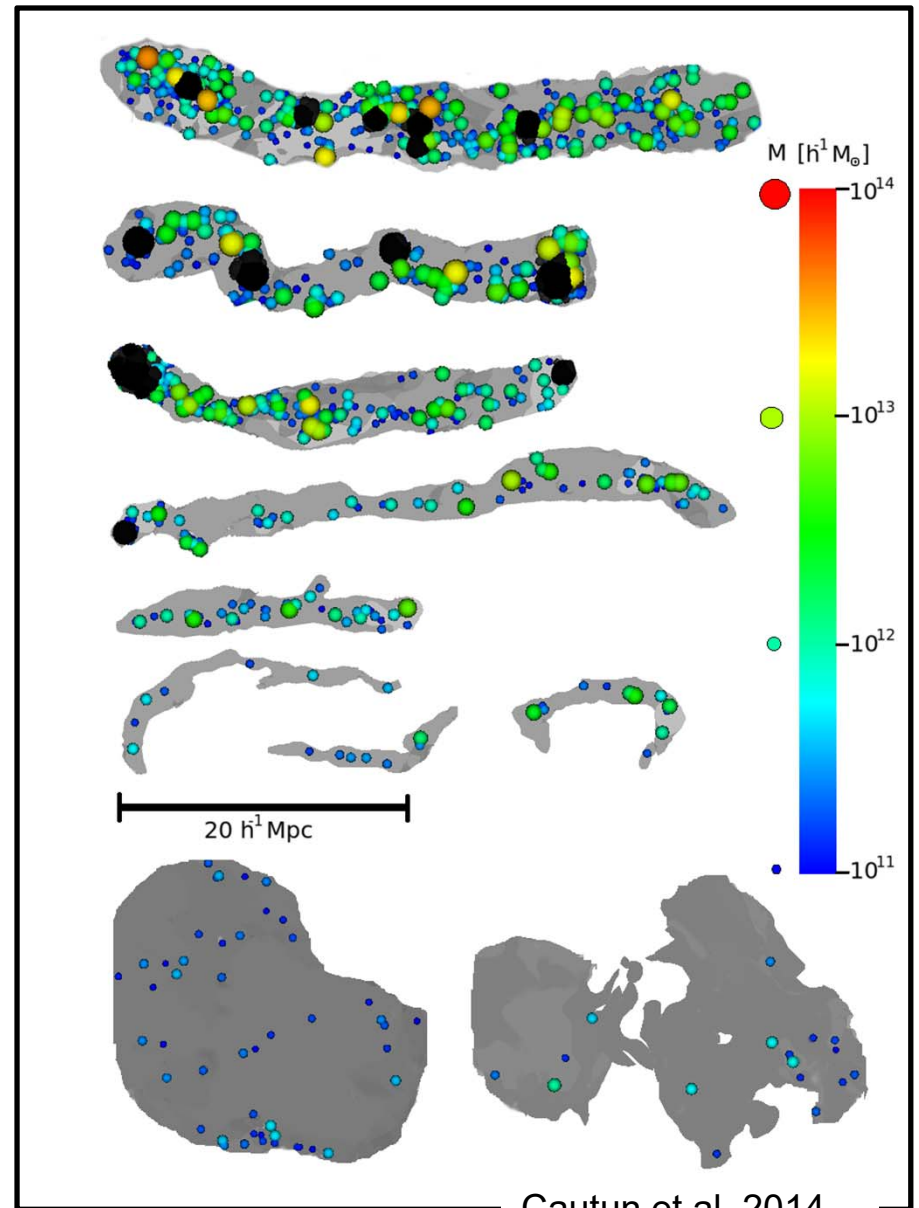
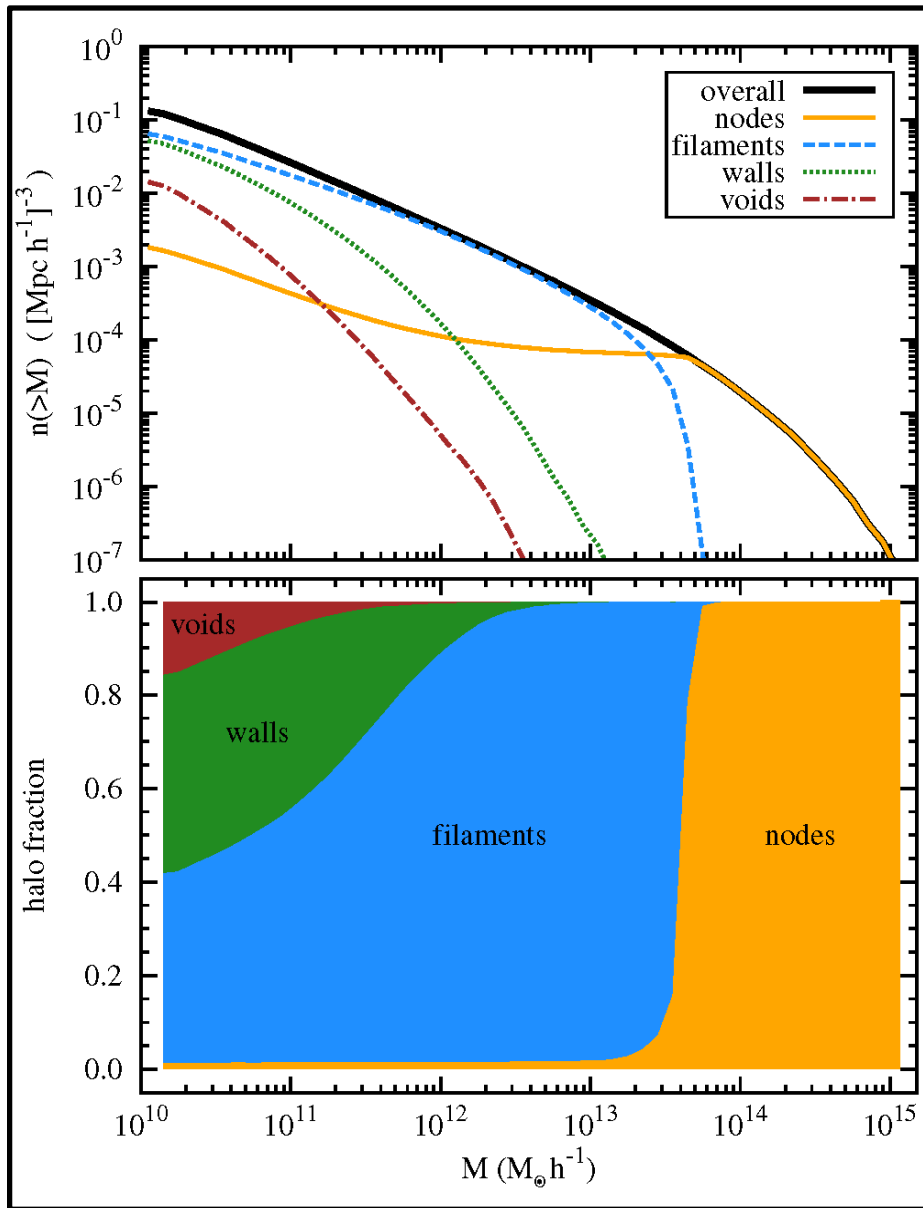
Filament population:
increasing diameter

Wall population:
increasing thickness for denser walls
decrease of tenuous walls

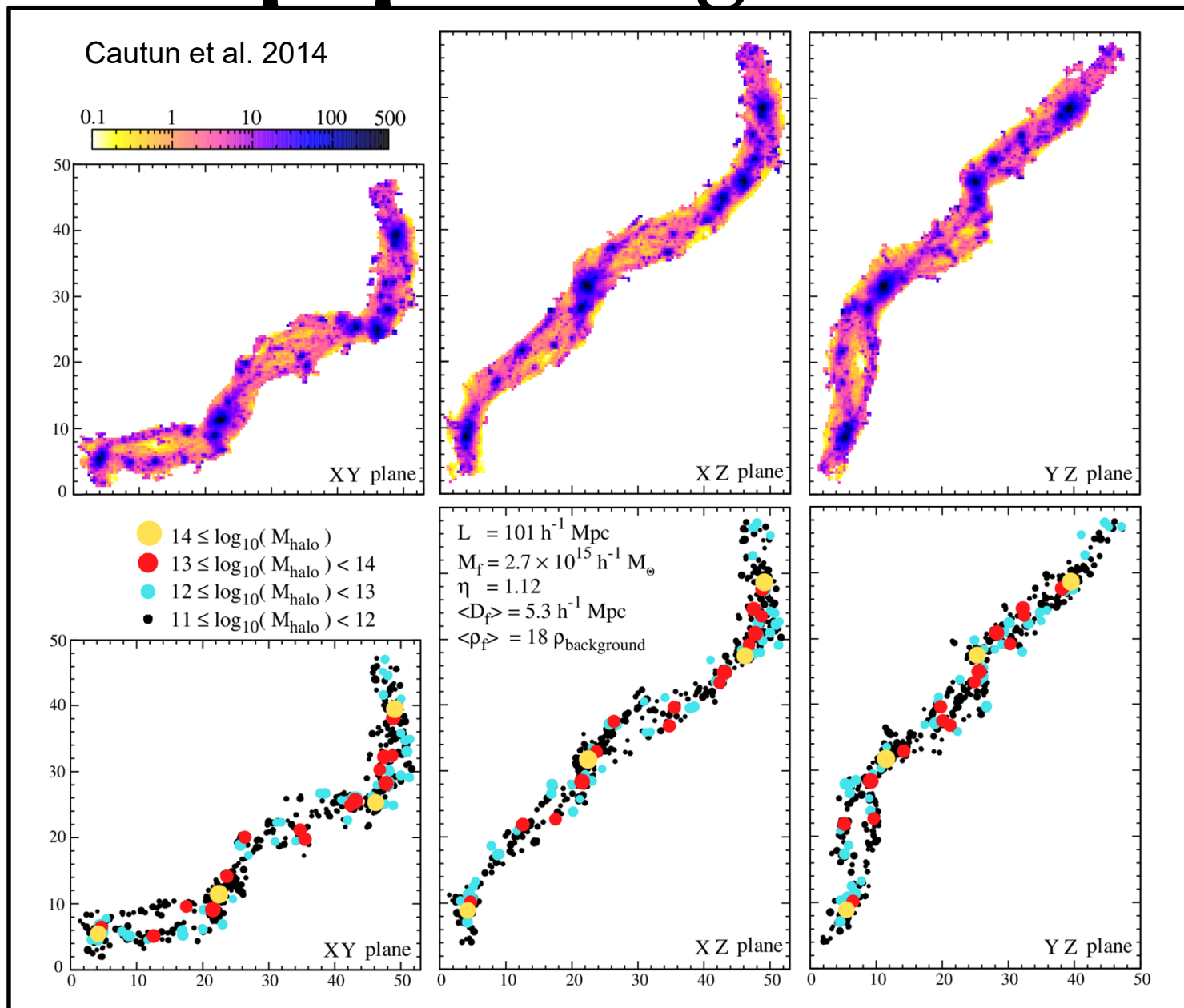
Cosmic Web:

Halo Distribution

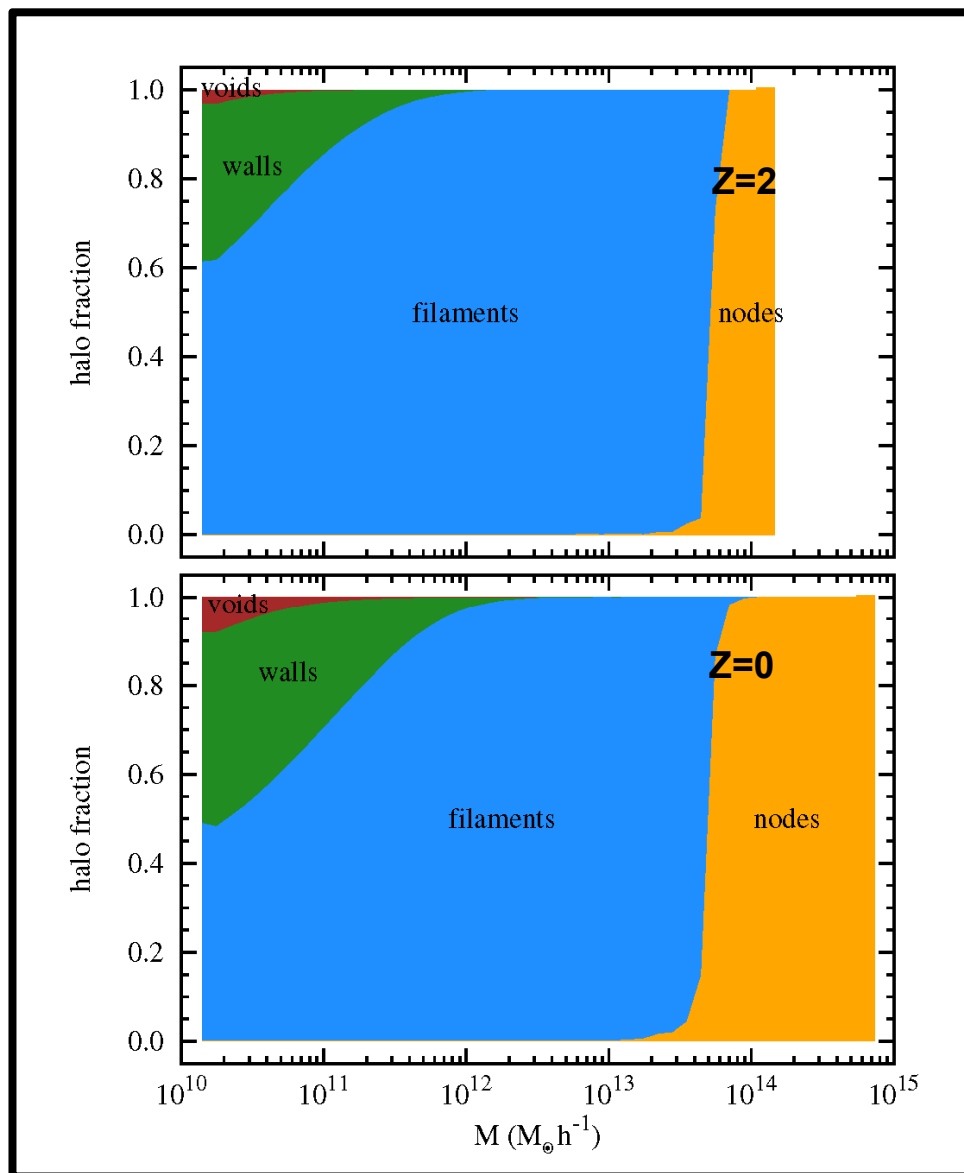
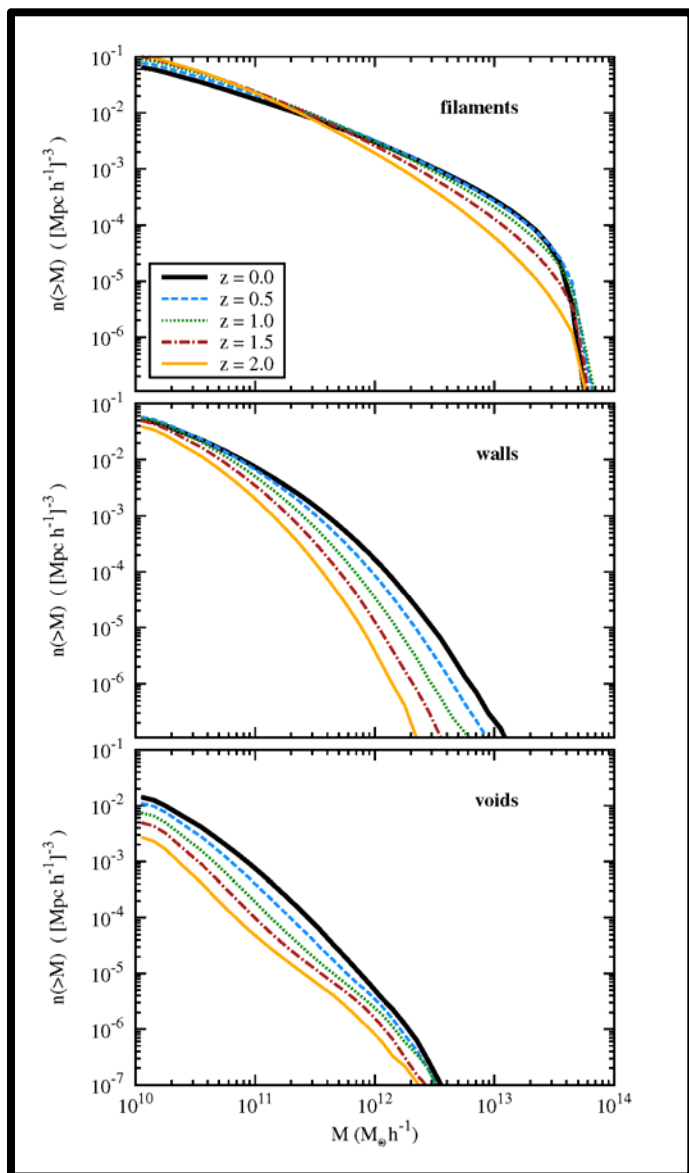
Halos in the Cosmic Web



Halos populating Filaments



Evolving Halo Population



**Dynamics of the
Cosmic Web:**

**Anisotropic Collapse
&
Zeldovich Formalism**

Yakov Borisovich Zel'dovich



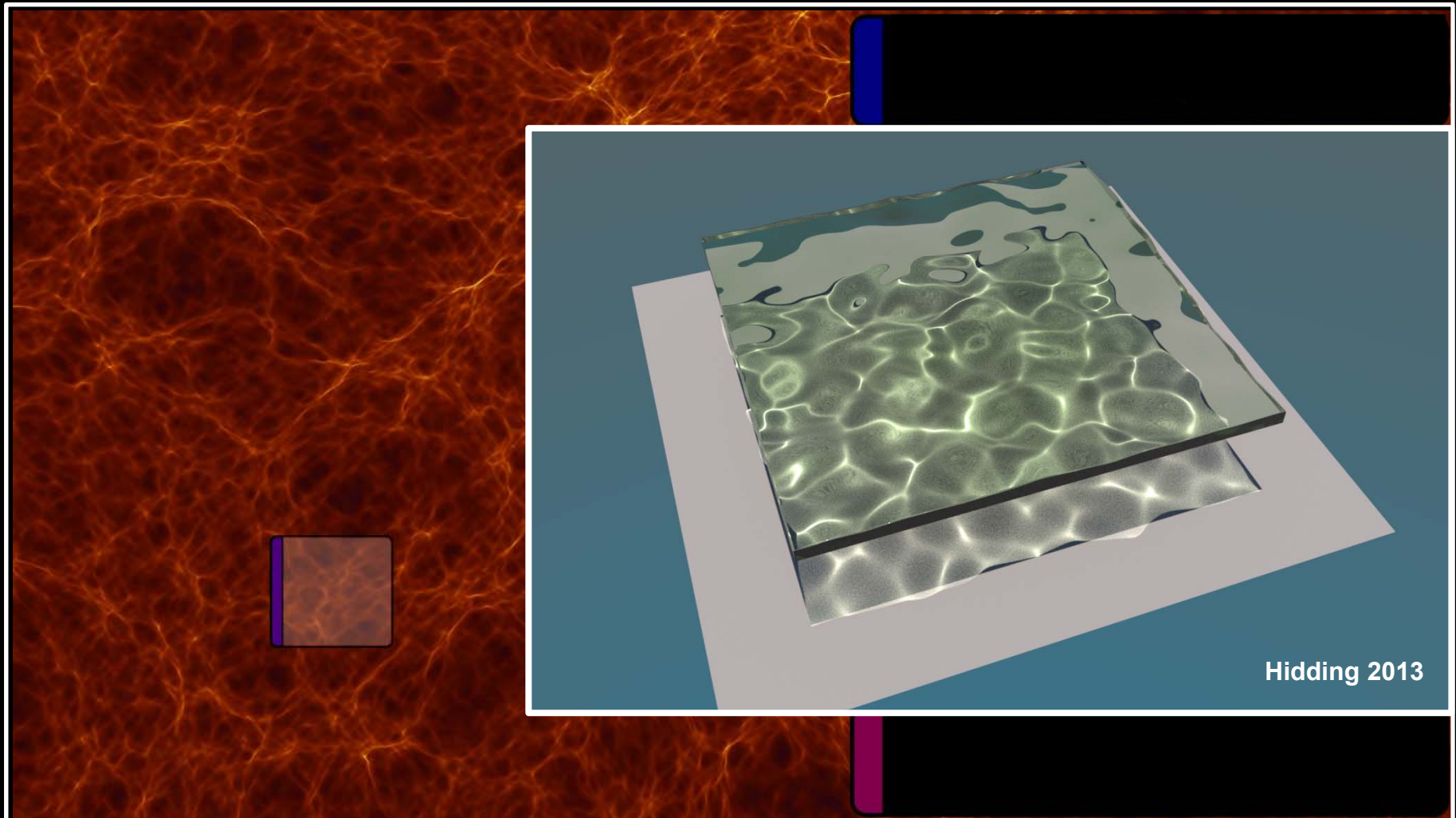
Zel'dovich Approximation

$$\vec{x} = \vec{q} + D(t) \vec{u}(\vec{q})$$

$$\vec{u}(\vec{q}) = -\vec{\nabla} \Phi(\vec{q})$$

$$\Phi(\vec{q}) = \frac{2}{3Da^2 H^2 \Omega} \phi_{lin}(\vec{q})$$

Zel'dovich Approximation

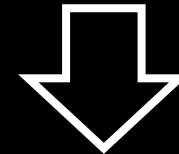


Zel'dovich Approximation

$$\vec{x} = \vec{q} + D(t) \vec{u}(\vec{q})$$

$$\vec{u}(\vec{q}) = -\vec{\nabla} \Phi(\vec{q})$$

$$d_{ij} = -\frac{\partial u_i}{\partial q_j}$$

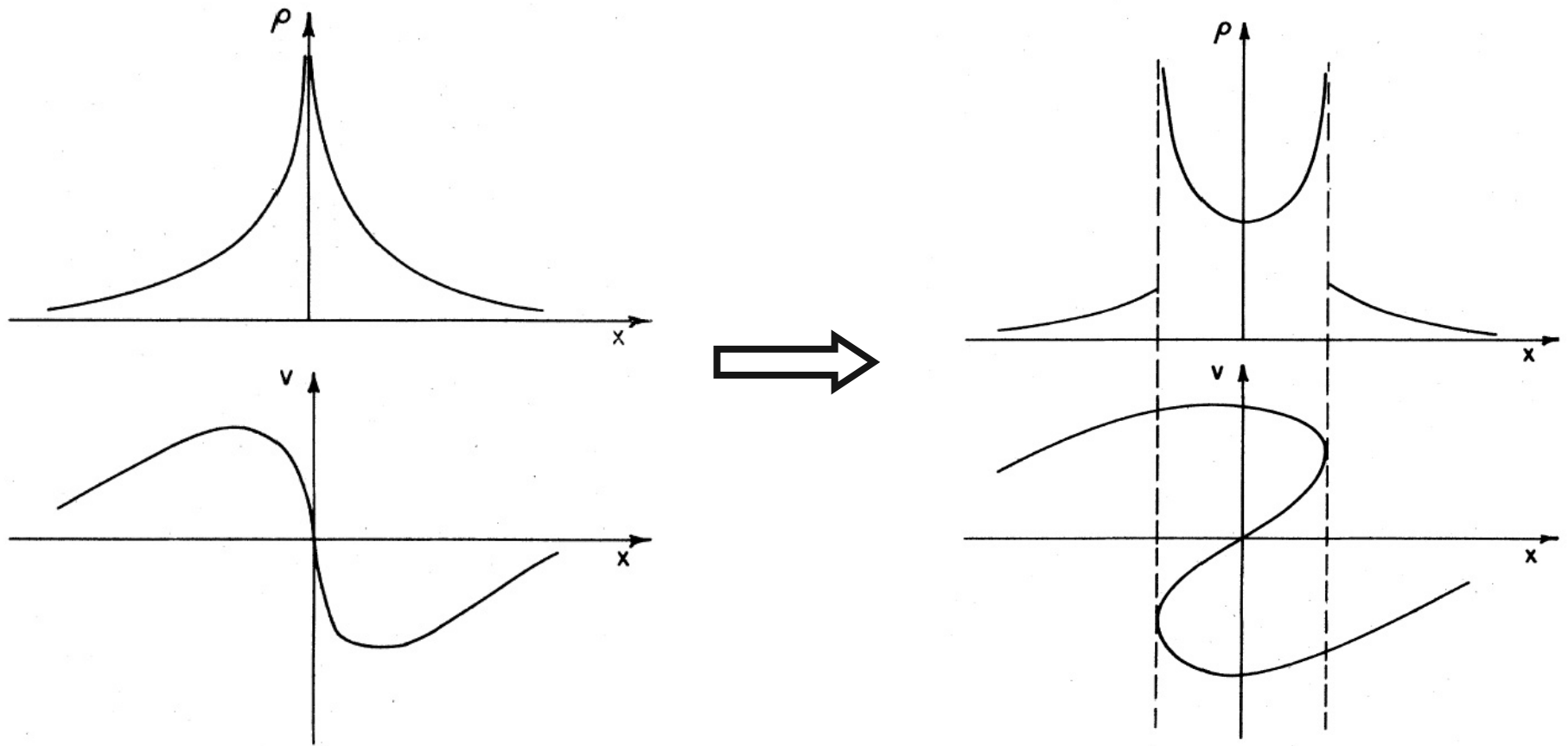


$$\rho(\vec{q}, t) = \frac{\rho_u(t)}{(1 - D(t)\lambda_1(\vec{q}))(1 - D(t)\lambda_2(\vec{q}))(1 - D(t)\lambda_3(\vec{q}))}$$

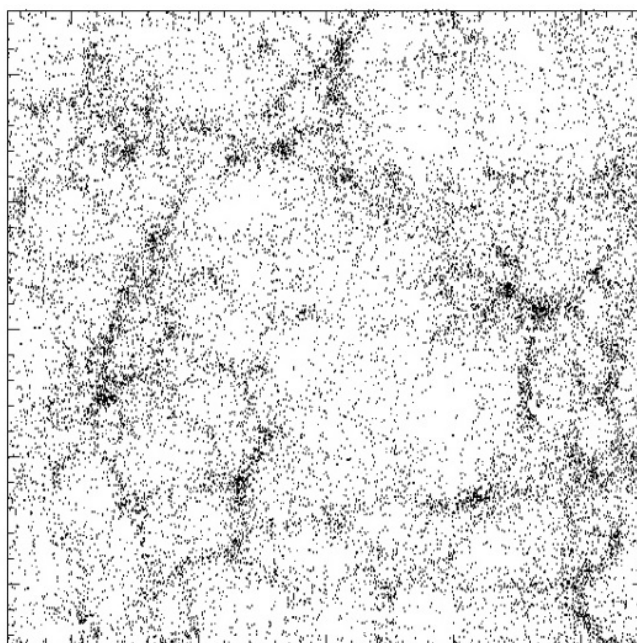
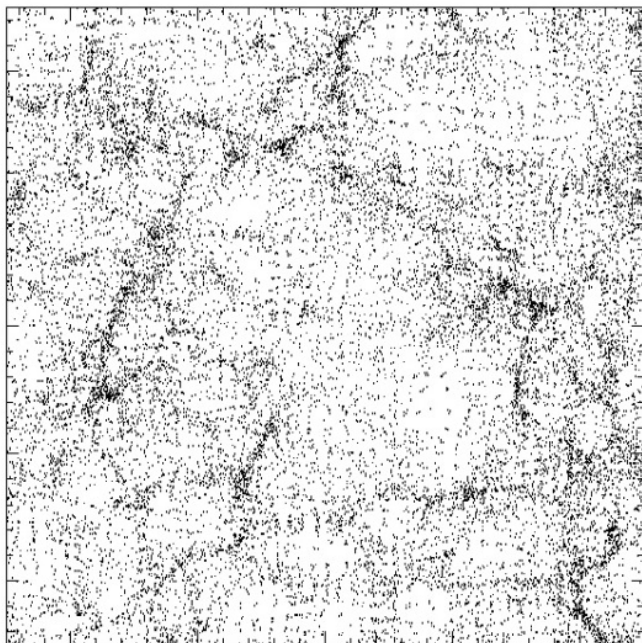
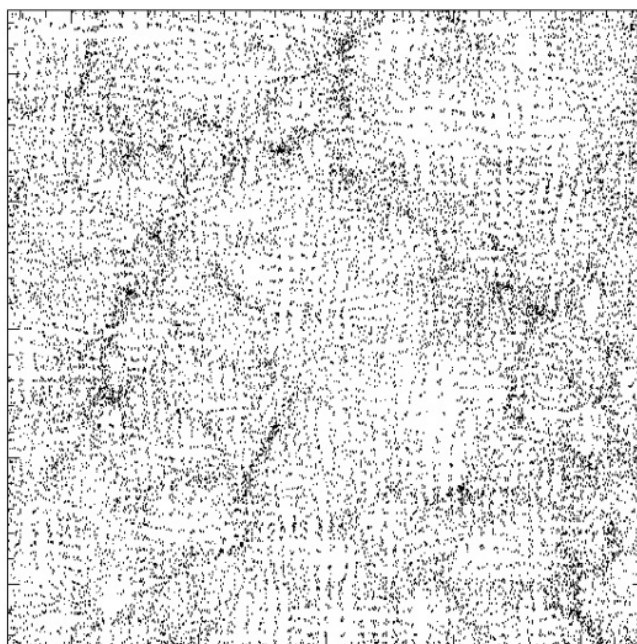
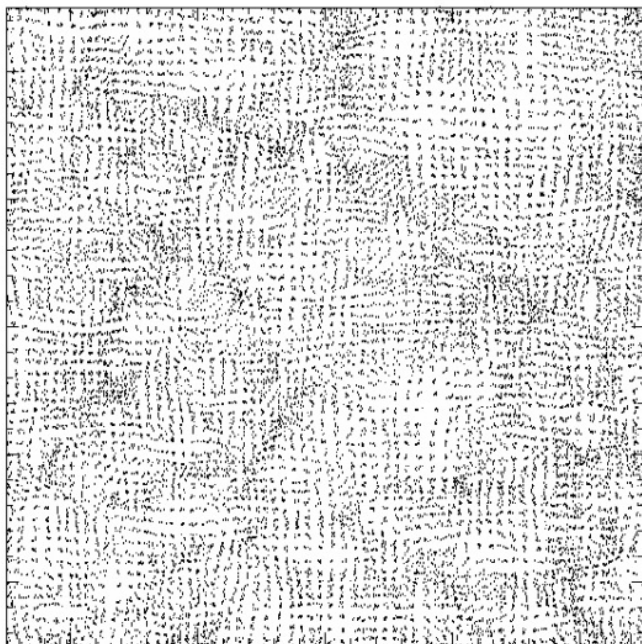
structure of the cosmic web determined by the spatial field of eigenvalues

$$\lambda_1, \lambda_2, \lambda_3$$

Zel'dovich Formalism: Density Evolution



Density Profile through pancake, at moment of formation and shortly thereafter (multistream)



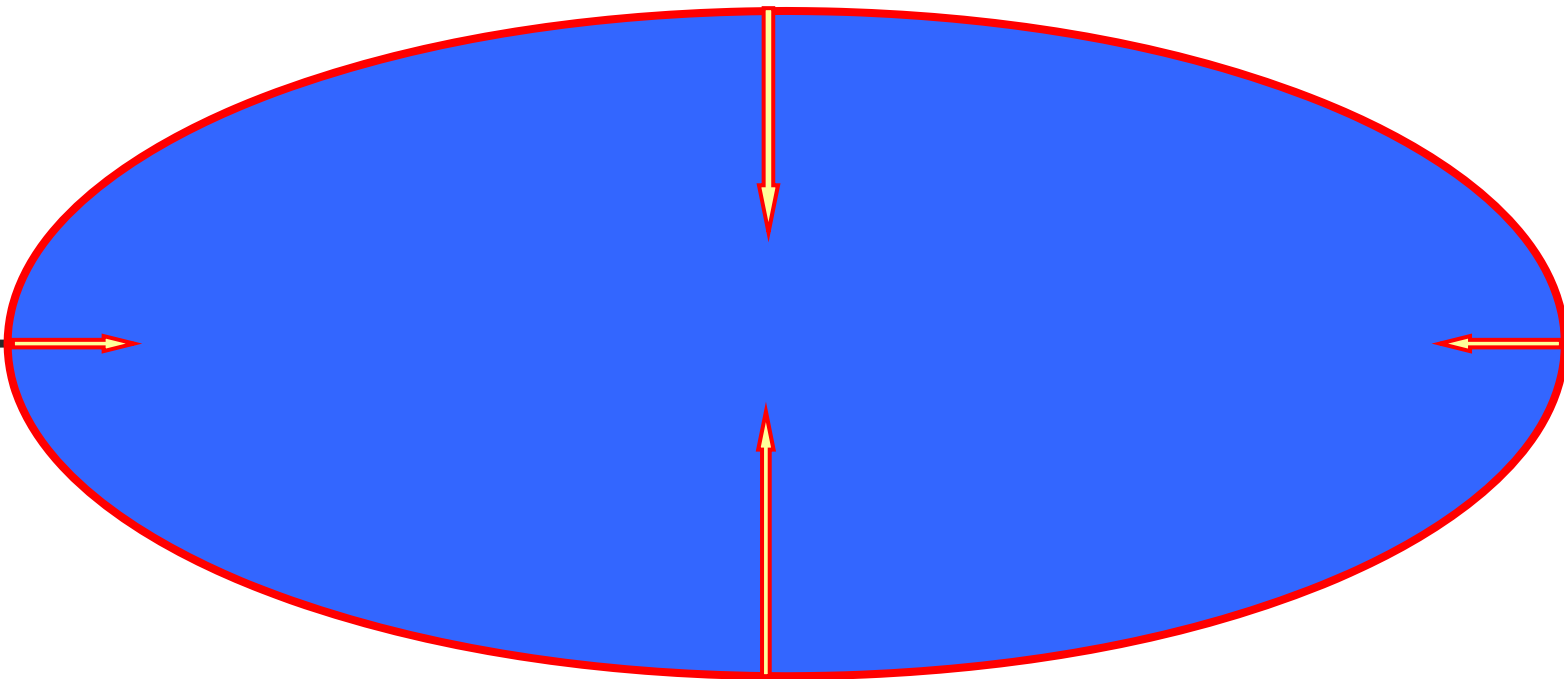
**Cosmic Web
Connectivity:**

**weaving the
Cosmic Tapestry**

Anisotropic Gravitational Collapse

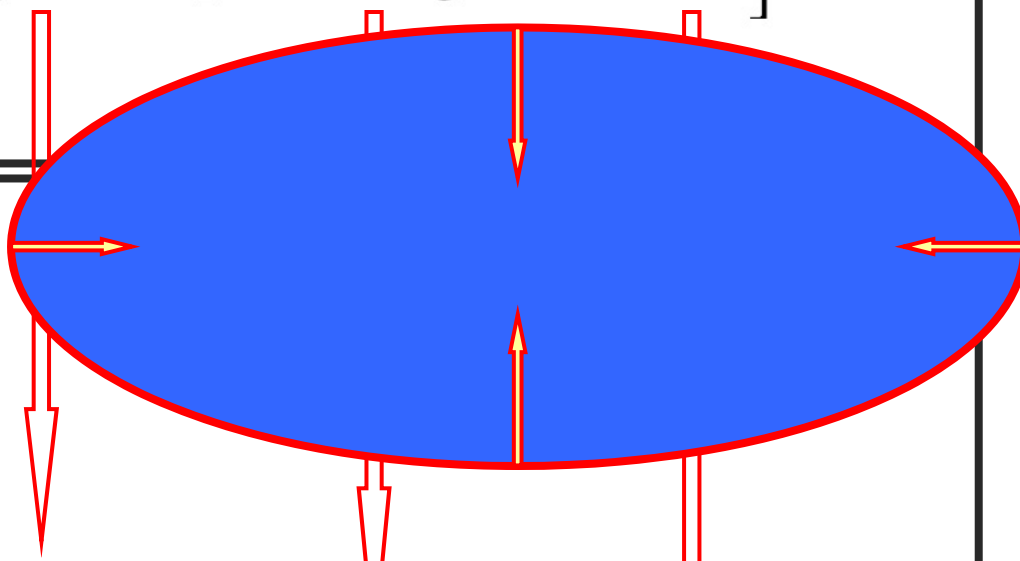
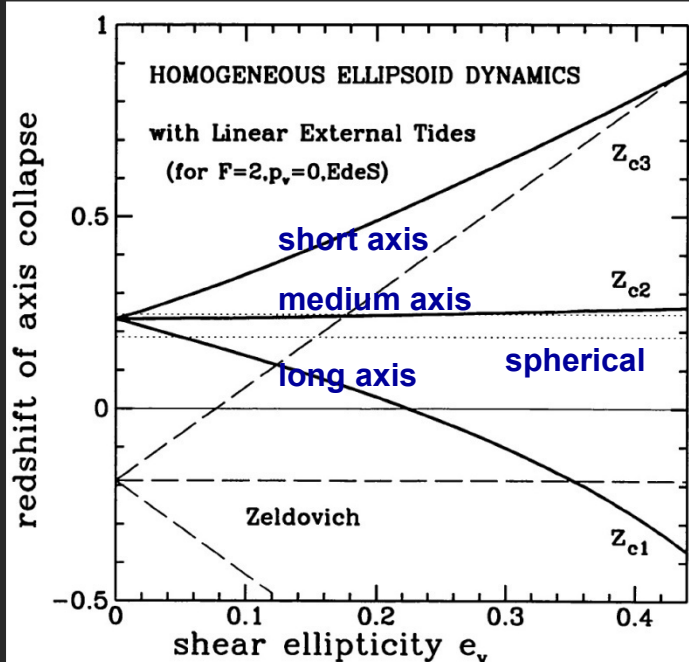
Amplification

small perturbations in gravity along different directions (tidal forces)



Anisotropic (Ellipsoidal) Collapse

$$\frac{d^2 \mathcal{R}_m}{dt^2} = -4\pi G \rho_u(t) \left[\frac{1 + \delta}{3} + \frac{1}{2} \left(\alpha_m - \frac{2}{3} \right) \delta + \lambda'_{vm} \right] \mathcal{R}_m$$



- Self-gravity
- Internal tidal shear (due to shape)
- External tidal shear

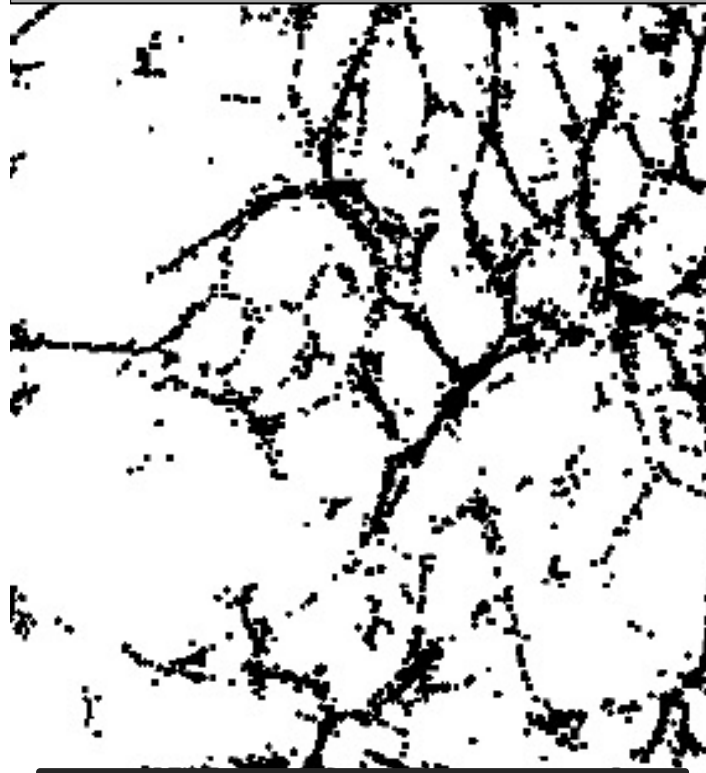
Formative agent of the Cosmic Web:

Tidal strain induced by the Megaparsec Matter Distribution:

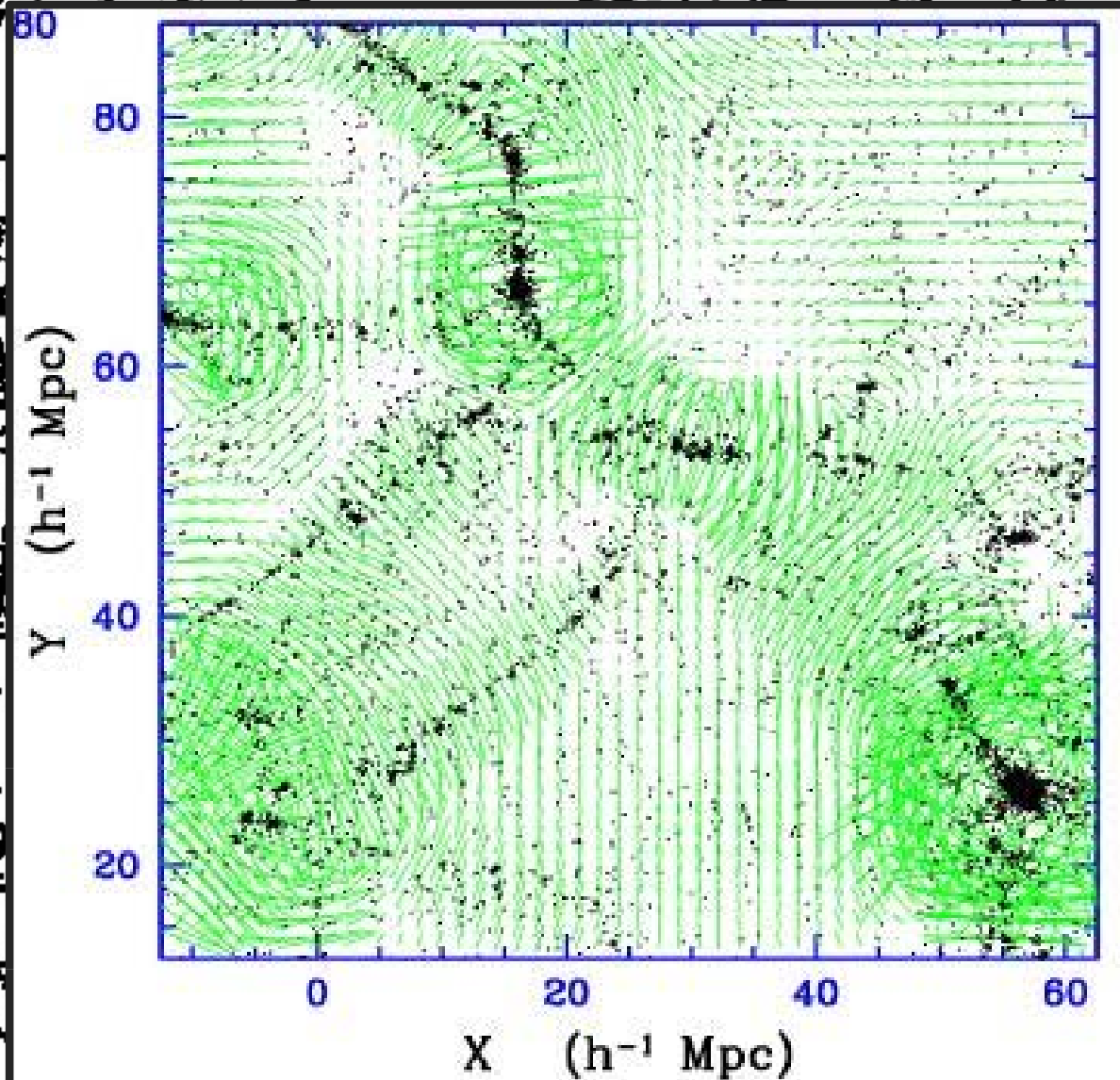
- anisotropic collapse of structures
- connection clusters-filaments:
clusters main agent for stretching filaments

$$T_{ij}(\vec{r}, t) = \frac{3\Omega H^2}{8\pi} \int d\vec{x} \delta(\vec{x}, t) \left\{ \frac{3(x_i - r_i)(x_j - r_j) - |\vec{x} - \vec{r}|^2 \delta_{ij}}{|\vec{x} - \vec{r}|^5} \right\} - \frac{1}{2} \Omega H^2 \delta(\vec{r}, t) \delta_{ij}$$

Tidal Shaping of the Cosmic Web



Tidal Forces
shape the Cosmic Web

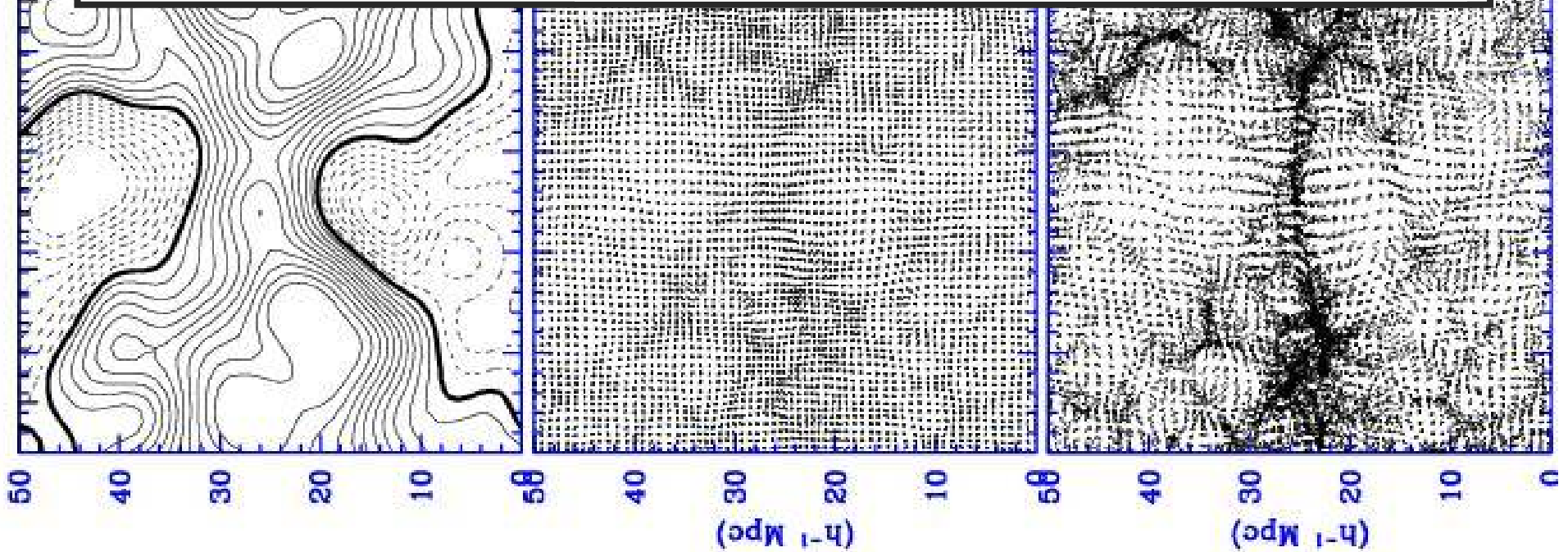




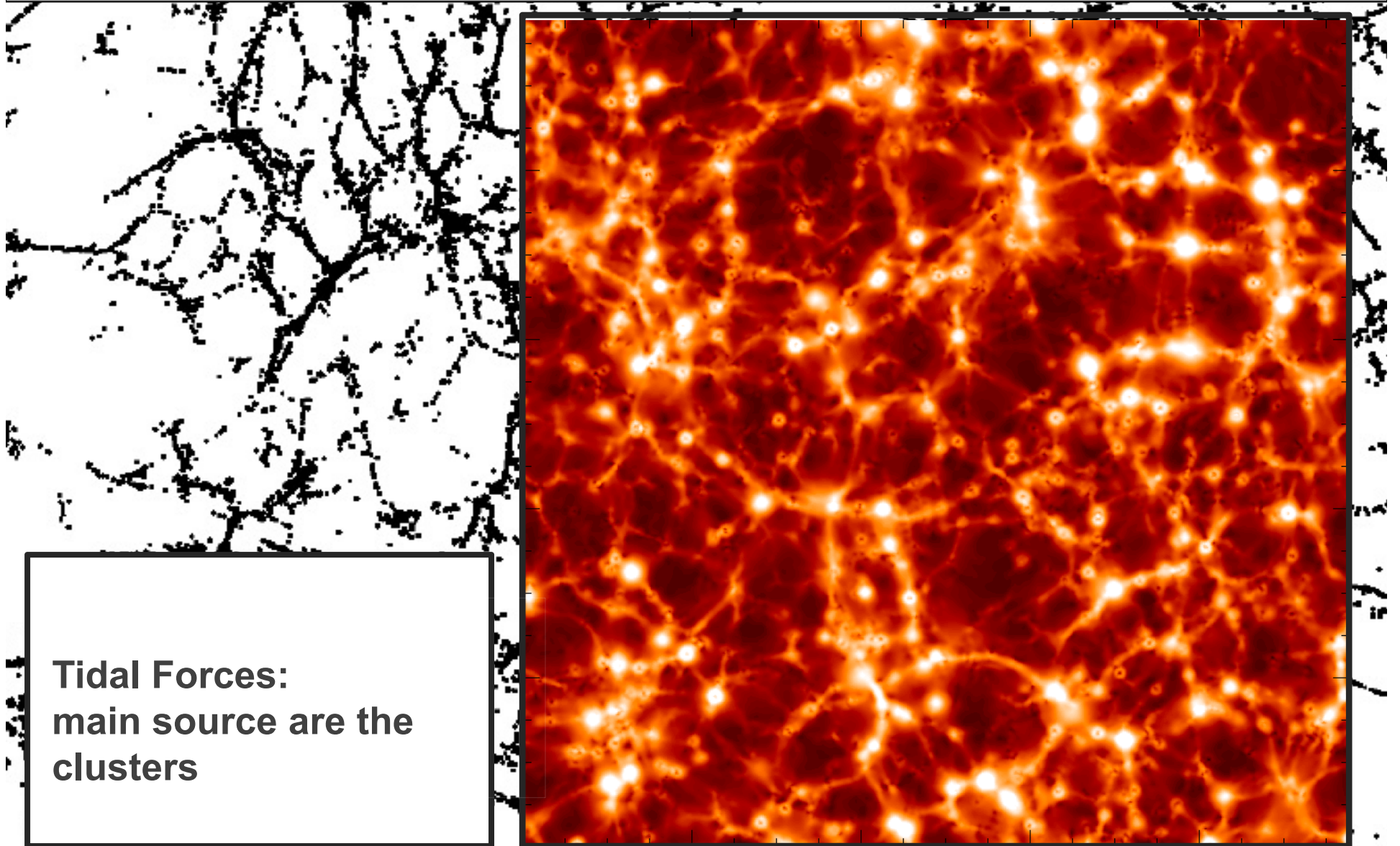
Tidal Constraints:

Example: elongated filamentary feature

Constrained Field:
$$f(\mathbf{x}) = \int \frac{d\mathbf{k}}{(2\pi)^3} \left[\hat{f}(\mathbf{k}) + P(k) \hat{H}_i(\mathbf{k}) \xi_{ij}^{-1} (c_j - \tilde{c}_j) \right] e^{-i\mathbf{k}\cdot\mathbf{x}}$$



Tidal Shaping of the Cosmic Web



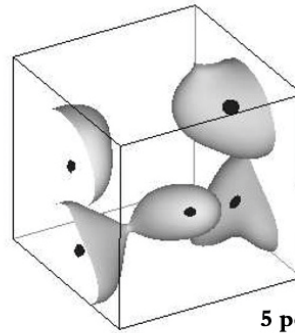
Tidal Forces:
main source are the
clusters

Tidal Shaping of the Cosmic Web

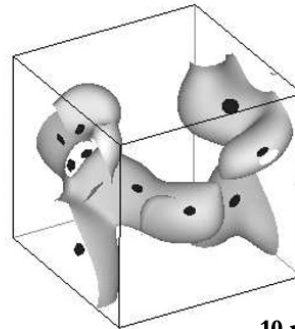
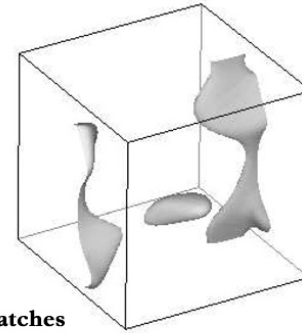
Cosmic Web Theory

**Bond, Kofman &
Pogosyan 1996**

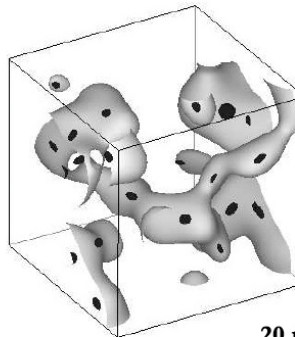
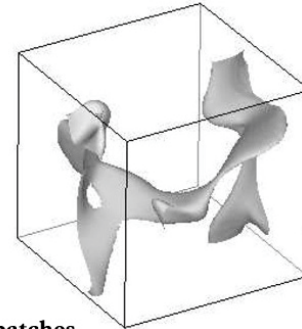
**Tidal Forces:
main source are the
clusters**



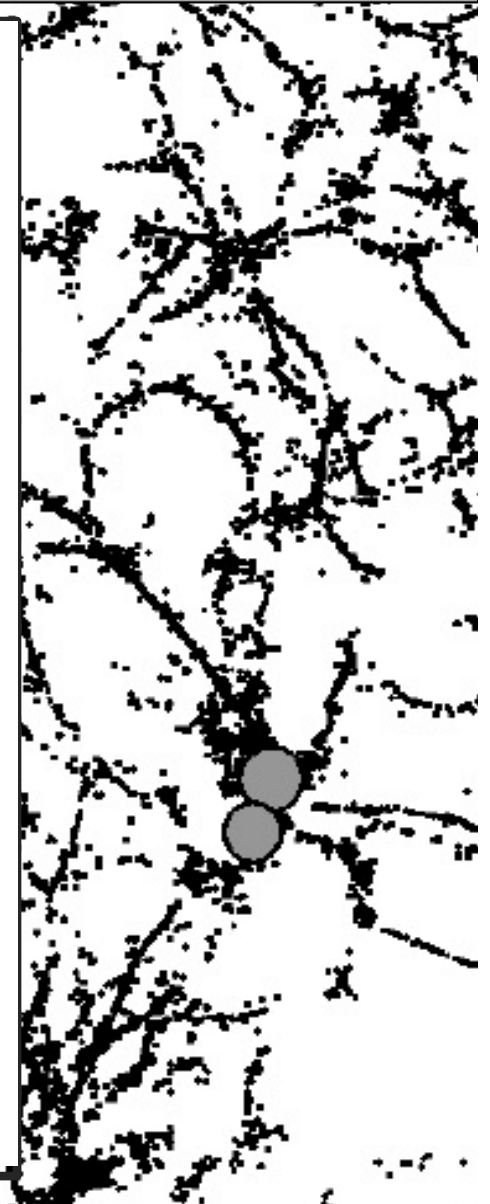
5 peak patches



10 peak patches



20 peak patches

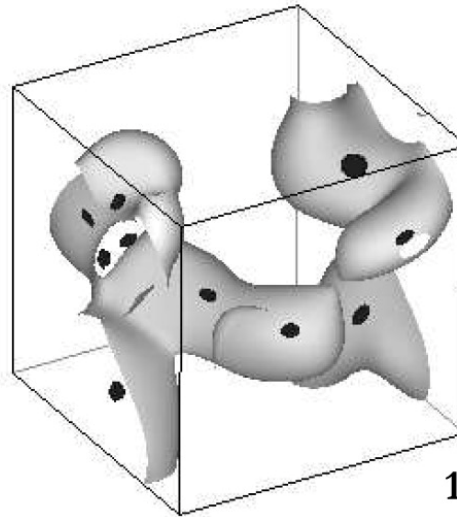


Tidal Shaping of the Cosmic Web

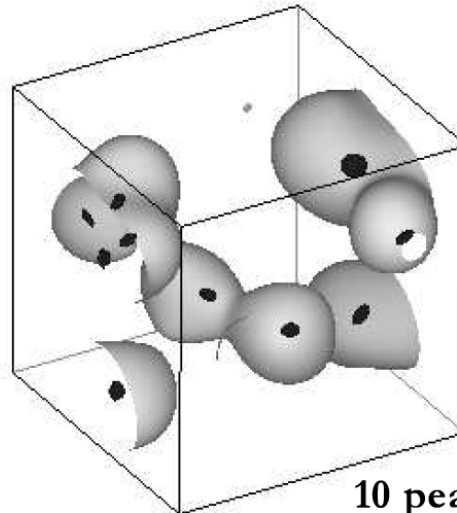
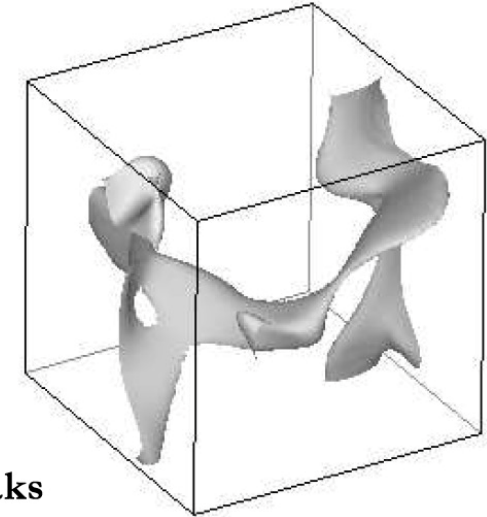
Cosmic Web Theory

Bond, Kofman &
Pogosyan 1996

Tidal Forces:
main source are the
clusters



10 peaks

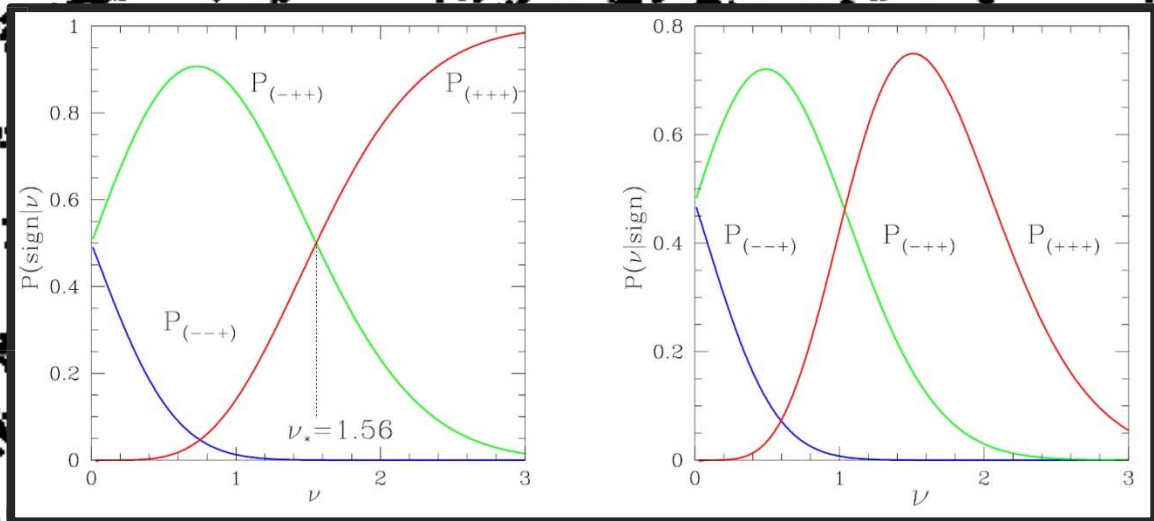


10 peaks, no shear

Tidal Shaping of the Cosmic Web

Cosmic Web Theory

Bond, Kofman &
Pogosyan 1996



Tidal Forces:
main source are the
clusters

Conditional Statistics

Tidal Shear eigenvalues in Gaussian field:

in overdense regions:

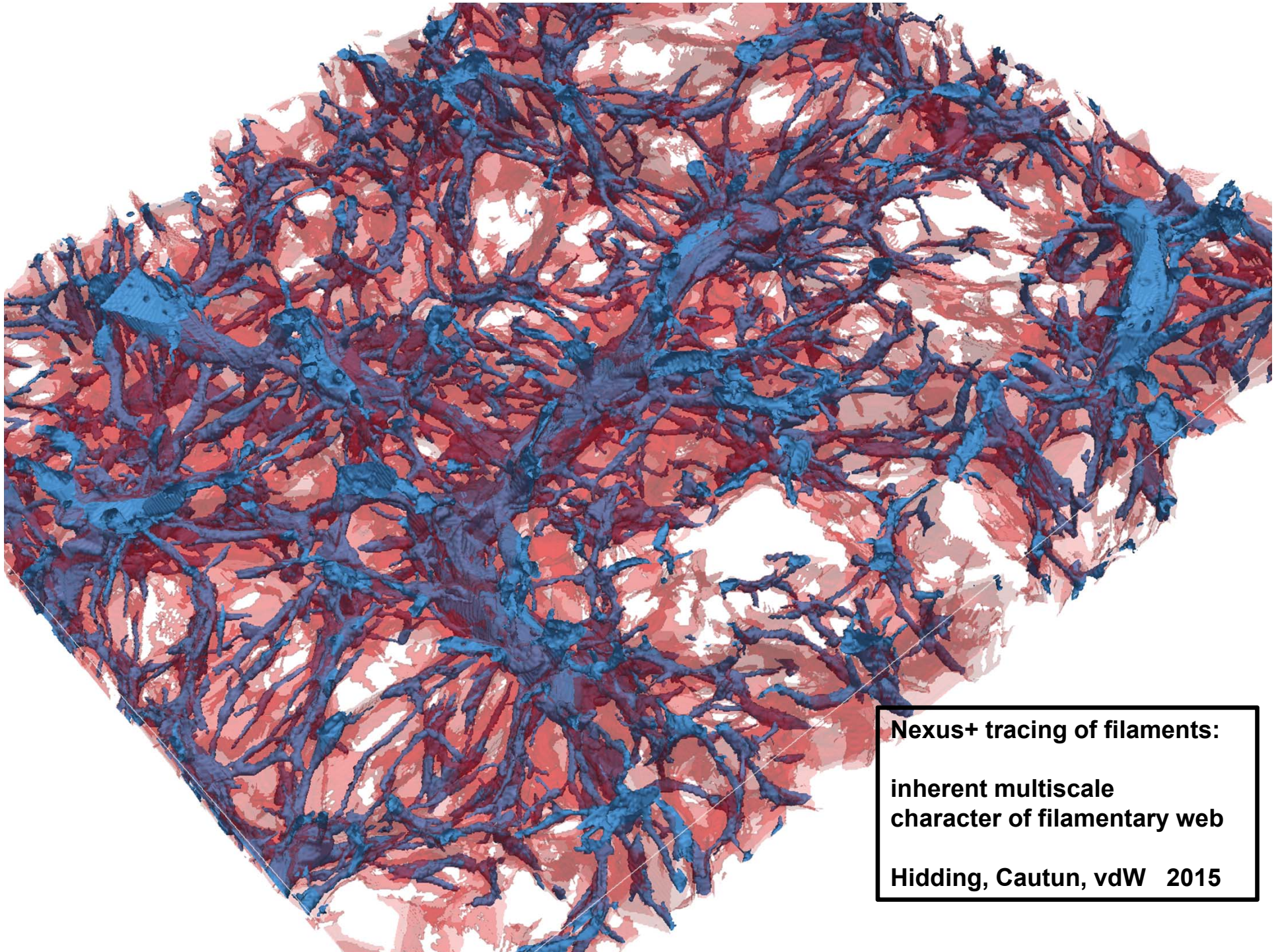
most prominent structures are FILAMENTS

in underdense regions:

most prominent structure are WALLS

Cosmic Web

Hierarchical Evolution

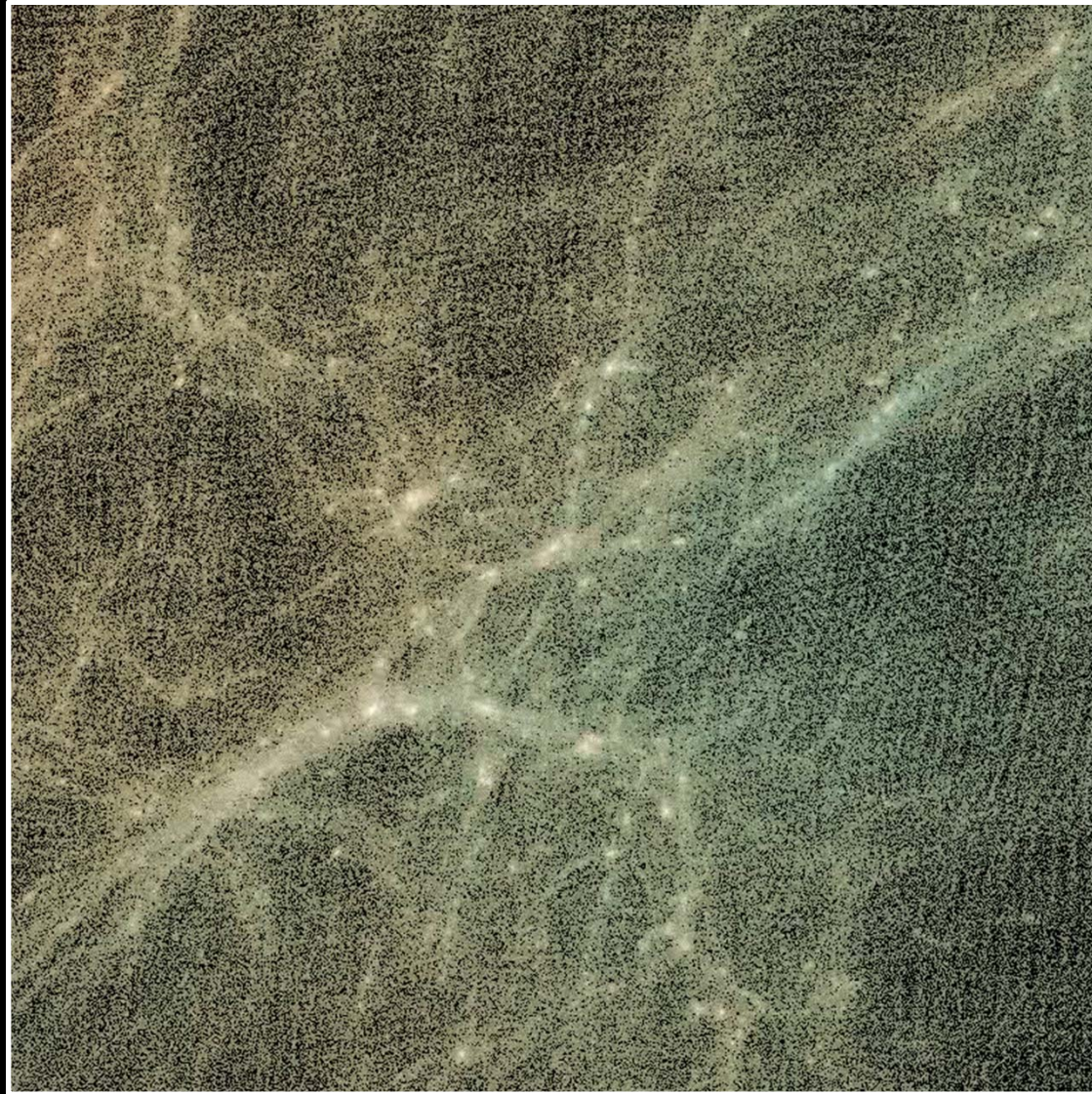


Nexus+ tracing of filaments:

**inherent multiscale
character of filamentary web**

Hidding, Cautun, vdW 2015

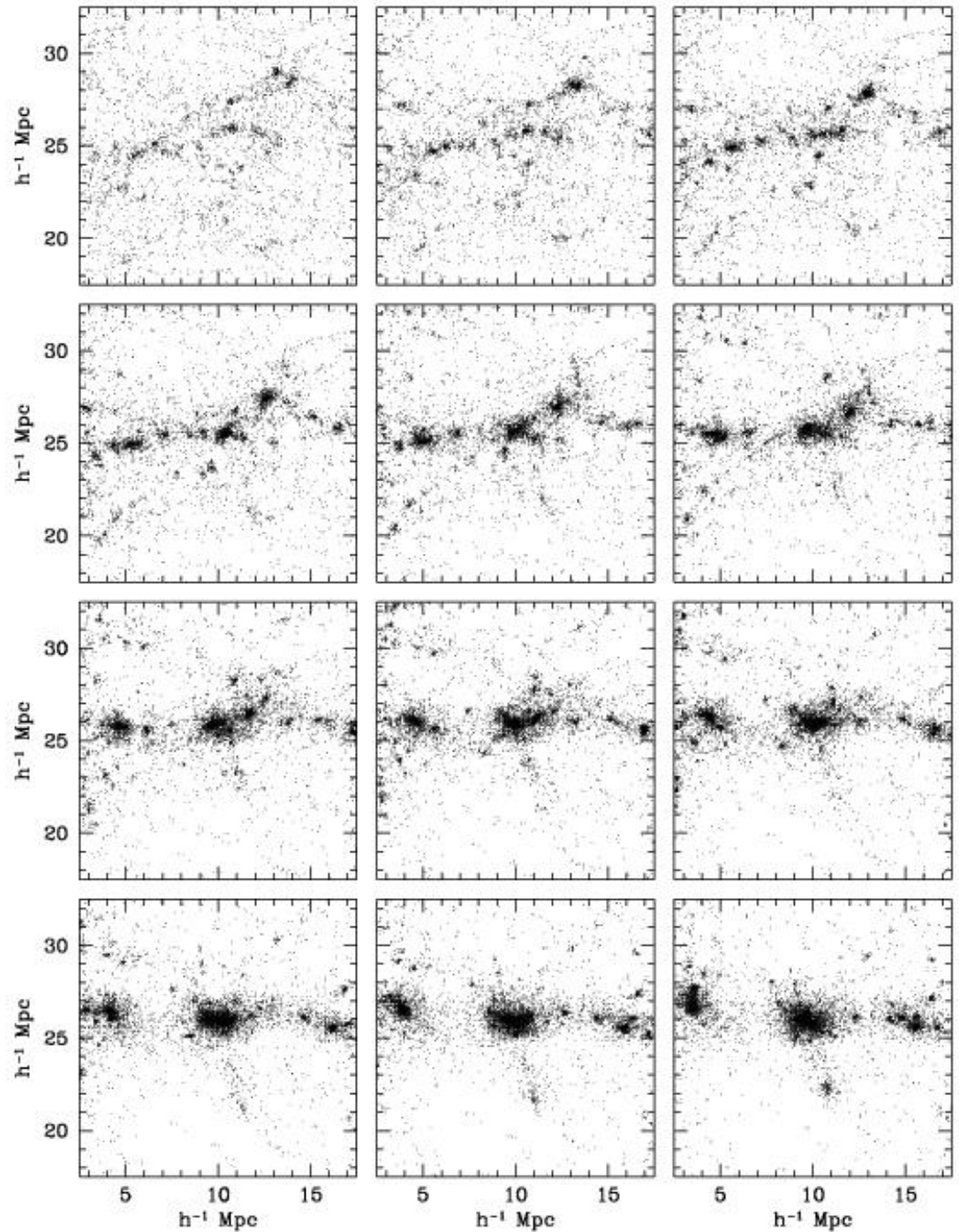
CGV halo & web evolution



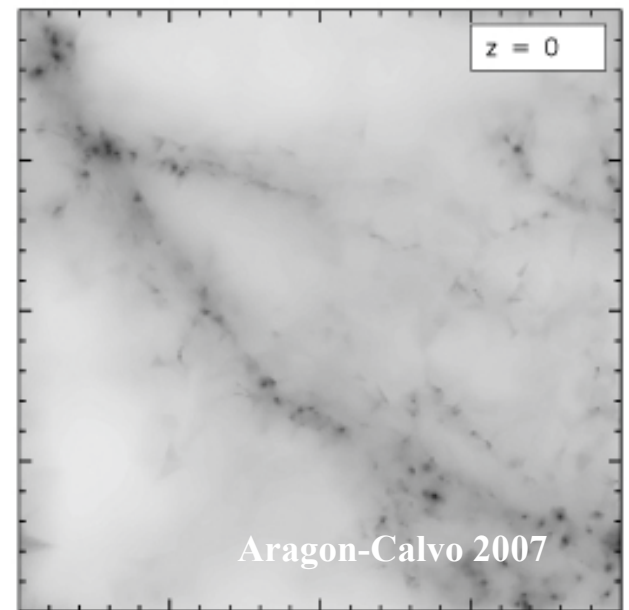
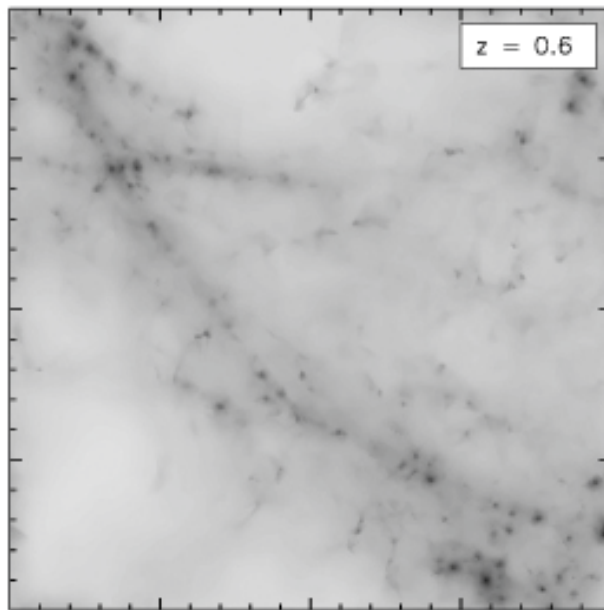
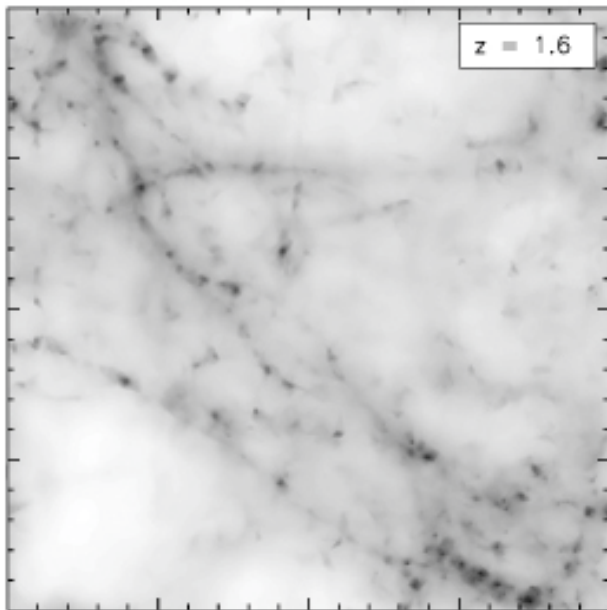
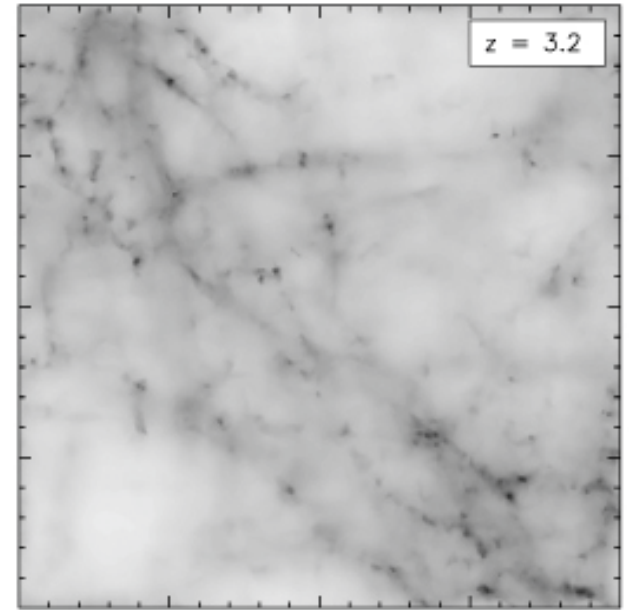
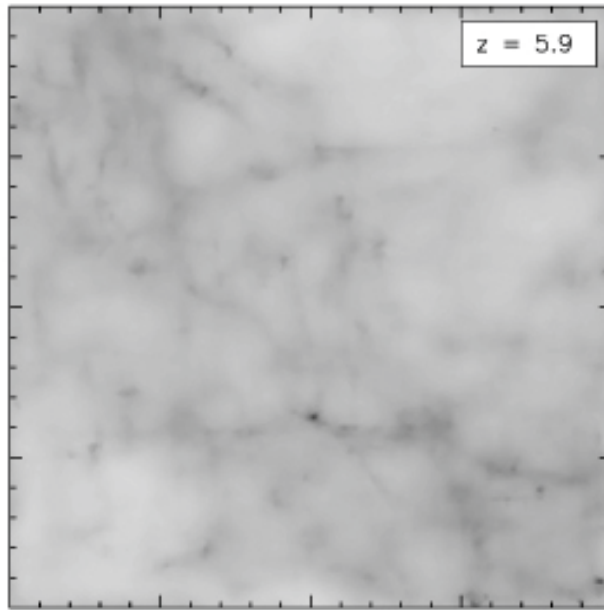
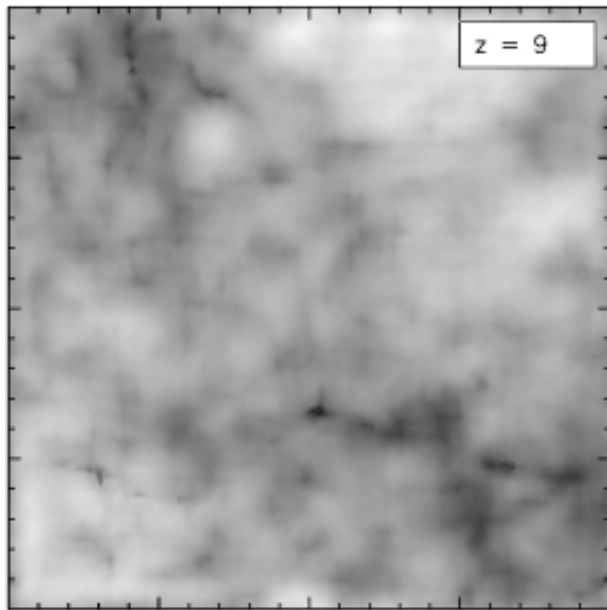
Rieder et al.
2013

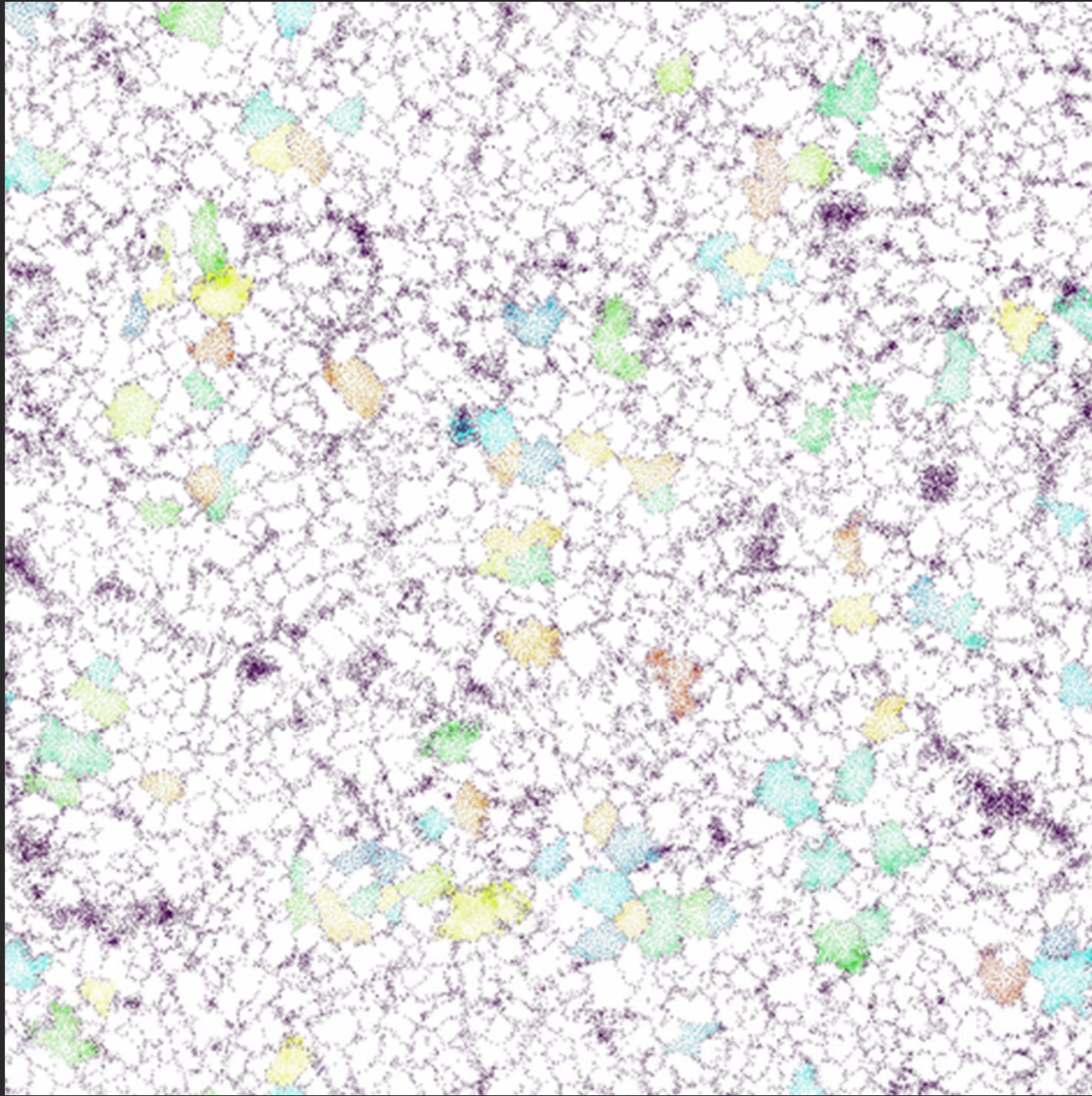
**Structures in the Universe form
by
gradual hierarchical assembly:**

- ❖ **small objects emerge & collapse first,**
- ❖ **then merge with other clumps**
- ❖ **while forming larger objects in hierarchy**



Hierarchical Filament Formation





Void Hierarchy:

“Lagrangian” view:

void-dominated
hierarchical
development
Cosmic Web

Platen & vdW 2004

Sheth & vdW 2004

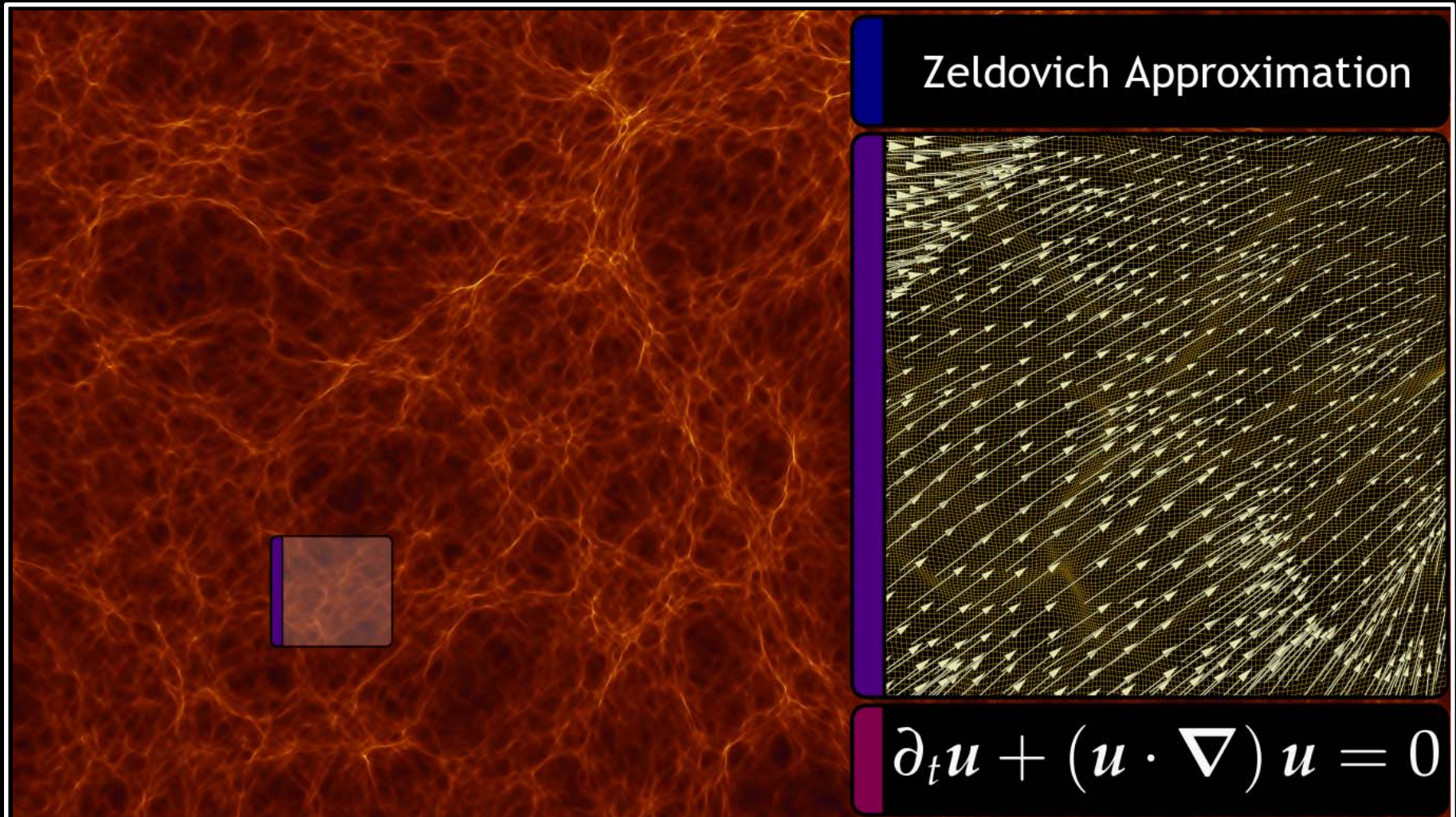
Aragon-Calvo &
Szalay 2012

Hierarchical Dynamics of the Cosmic Web:

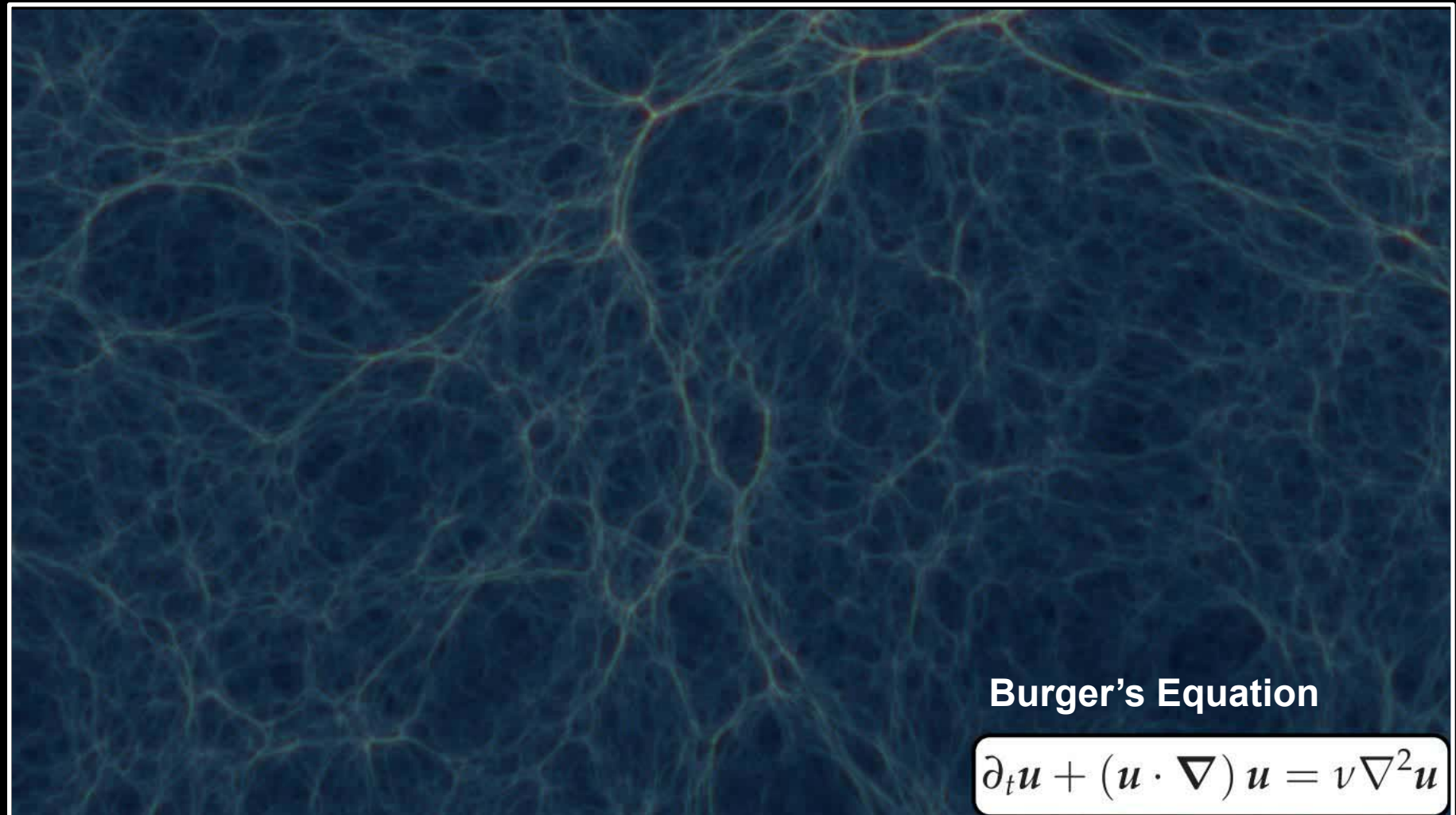
Adhesion

Hidding, vdW et al. 2012,
Hidding, vdW et al. 2016
Hidding, vdW et al. 2018

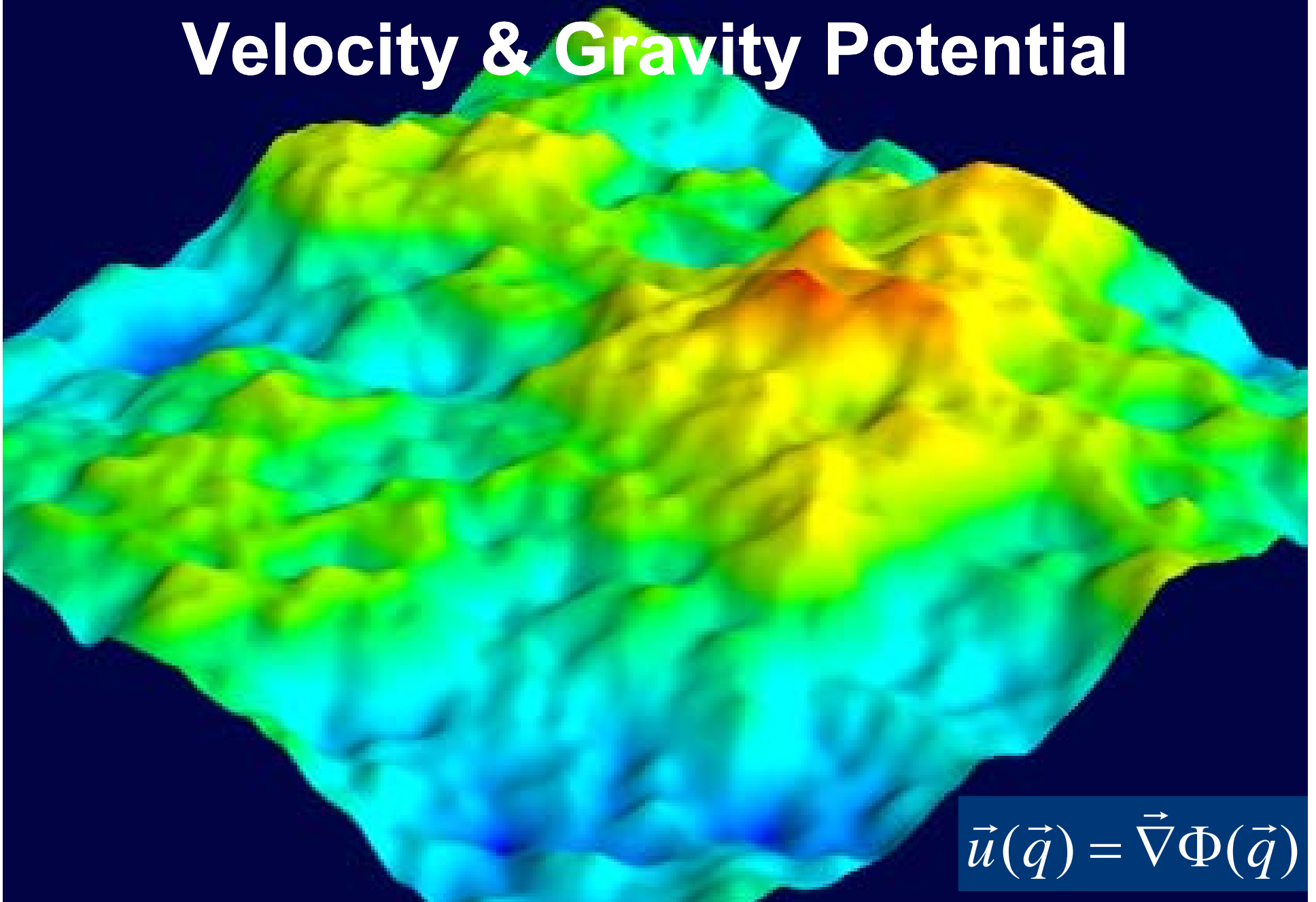
Zel'dovich Approximation



Adhesion Approximation



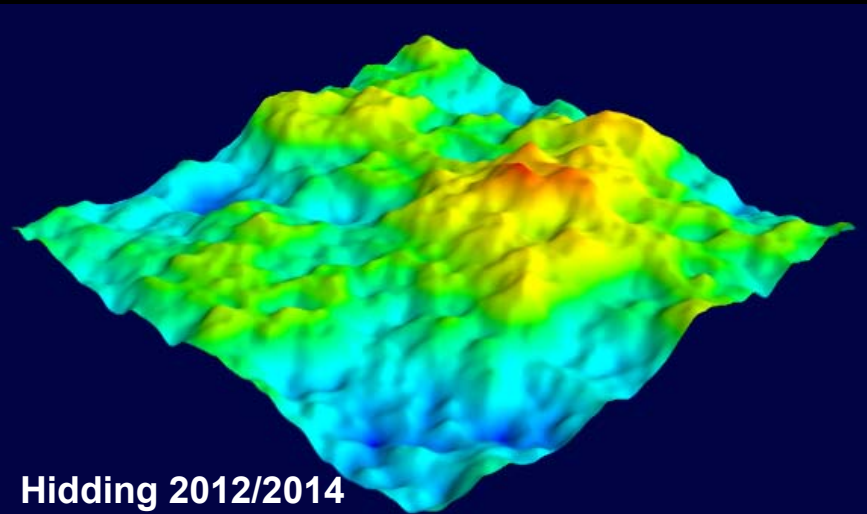
Velocity & Gravity Potential



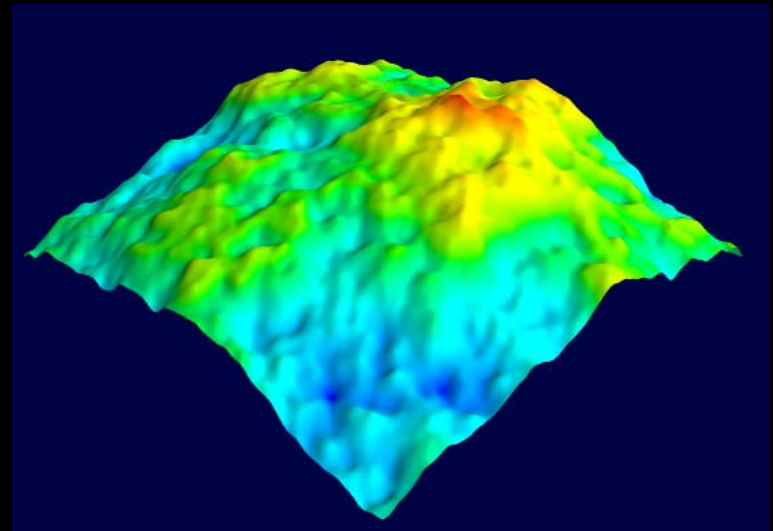
$$\vec{u}(\vec{q}) = \vec{\nabla}\Phi(\vec{q})$$

Burger's Equation: Hopf Solution

$$\frac{\partial \vec{u}}{\partial t} + (\vec{u} \cdot \vec{\nabla}) \vec{u} = \nu \nabla^2 \vec{u}$$

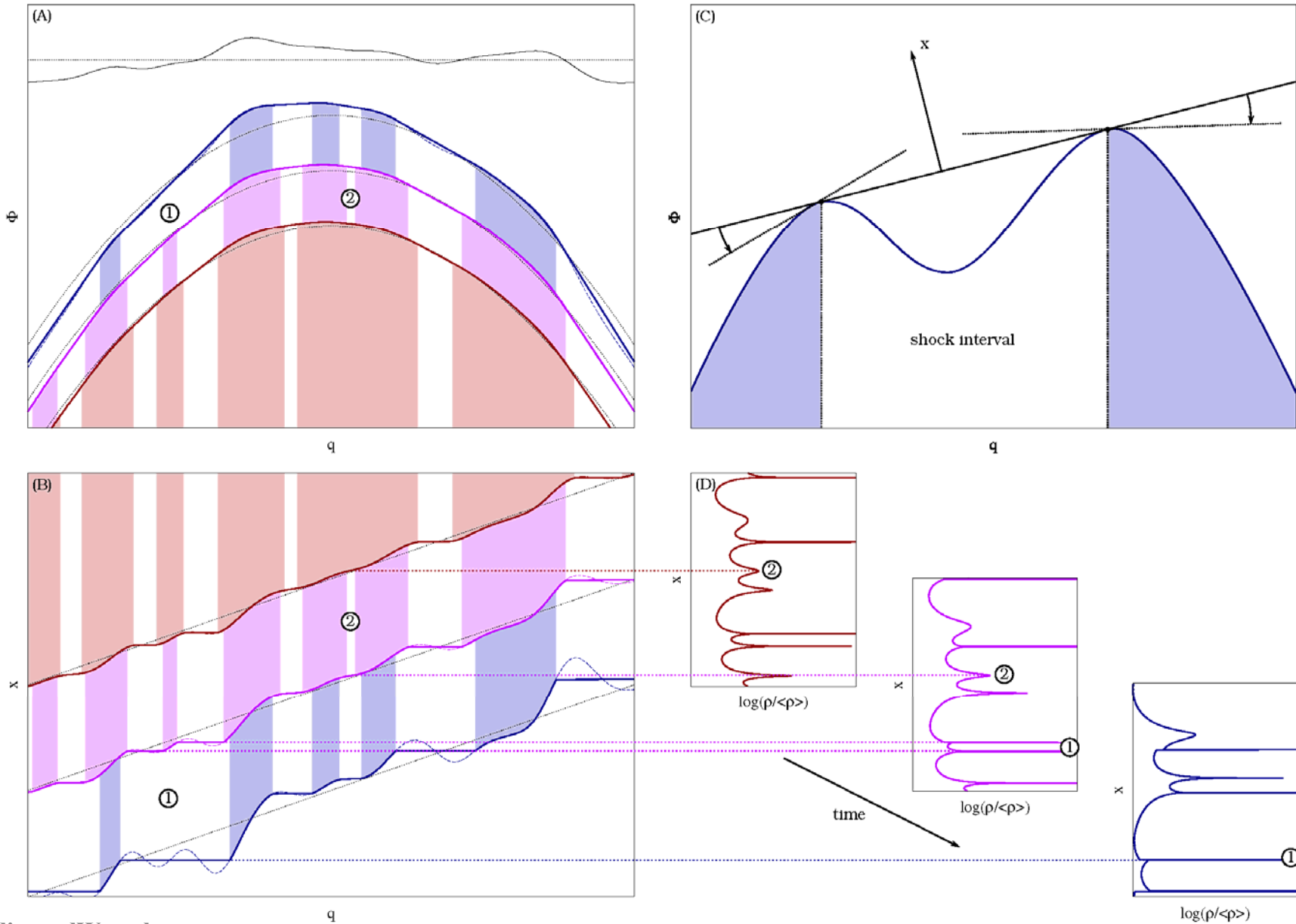


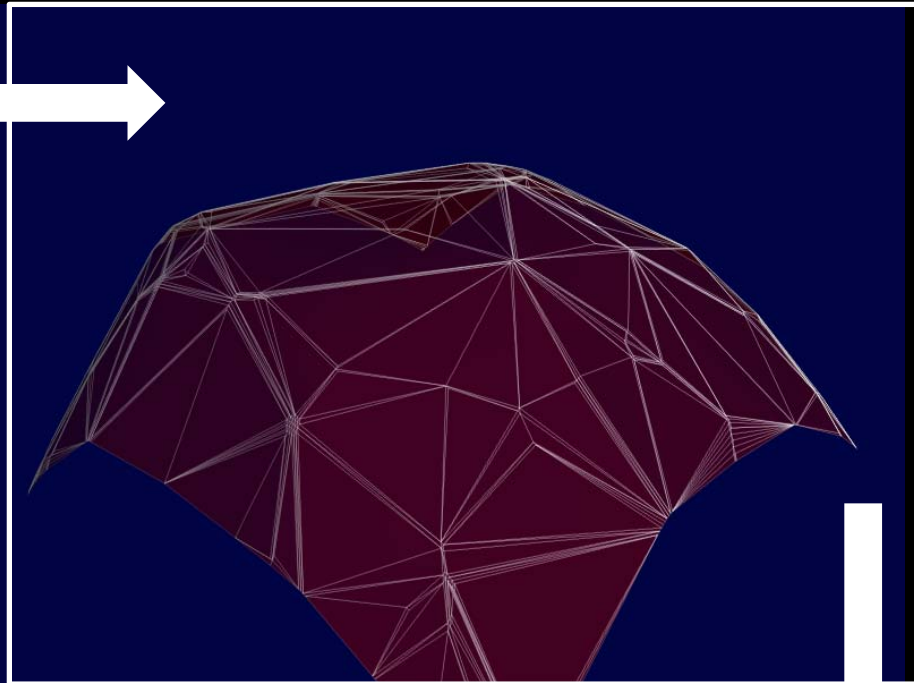
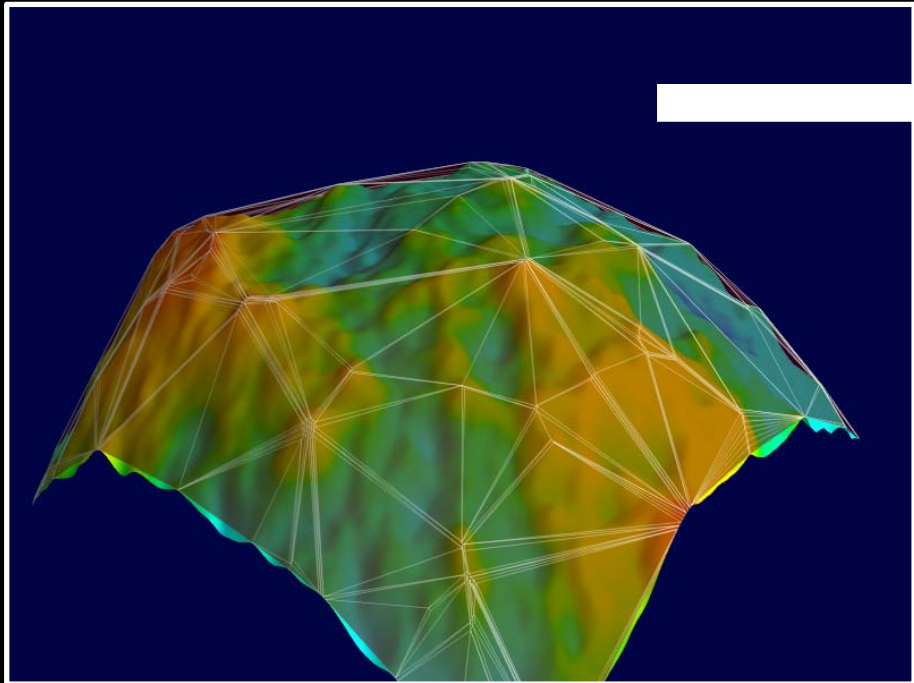
Hidding 2012/2014



$$\Phi(\vec{x}, t) + \frac{x^2}{2} = \max_q \left[\left(t\Phi_0(q) - \frac{q^2}{2} \right) + \vec{x} \cdot \vec{q} \right]$$

Burger's Equation: Hopf Solution



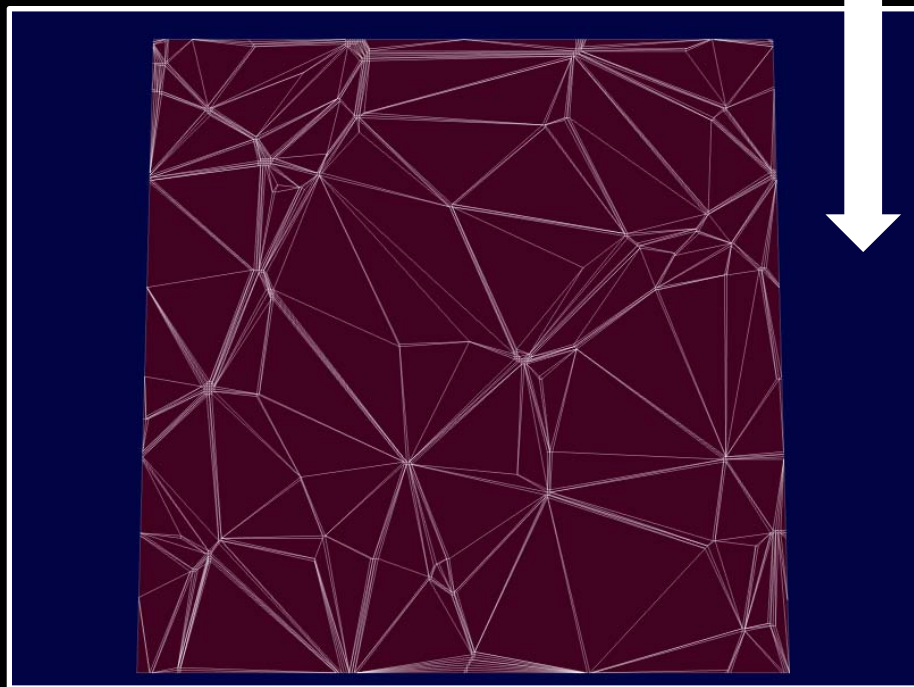


Hidding 2012/2014

Convex Hull
quadratically lifted potential field

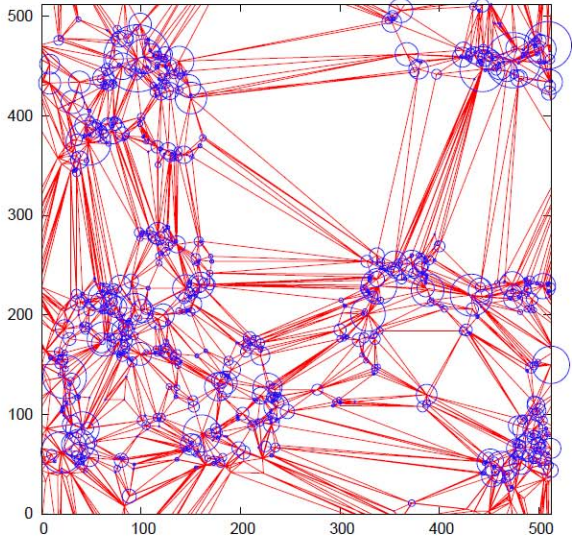
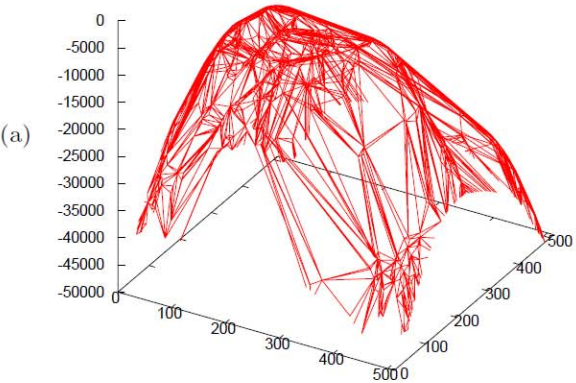


Delaunay tessellation
generated by maxima potential field



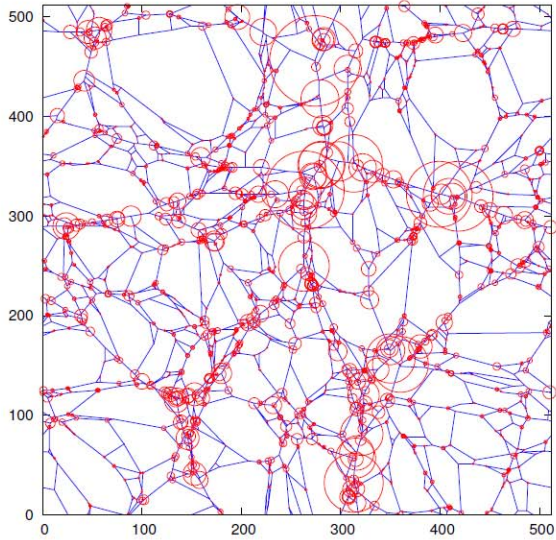
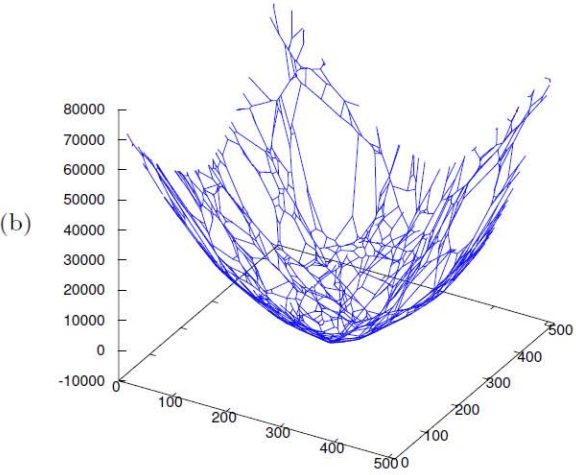
Convex Hull – Legendre transform

Lagrangian Space



Delaunay
(weighted)

Eulerian Space



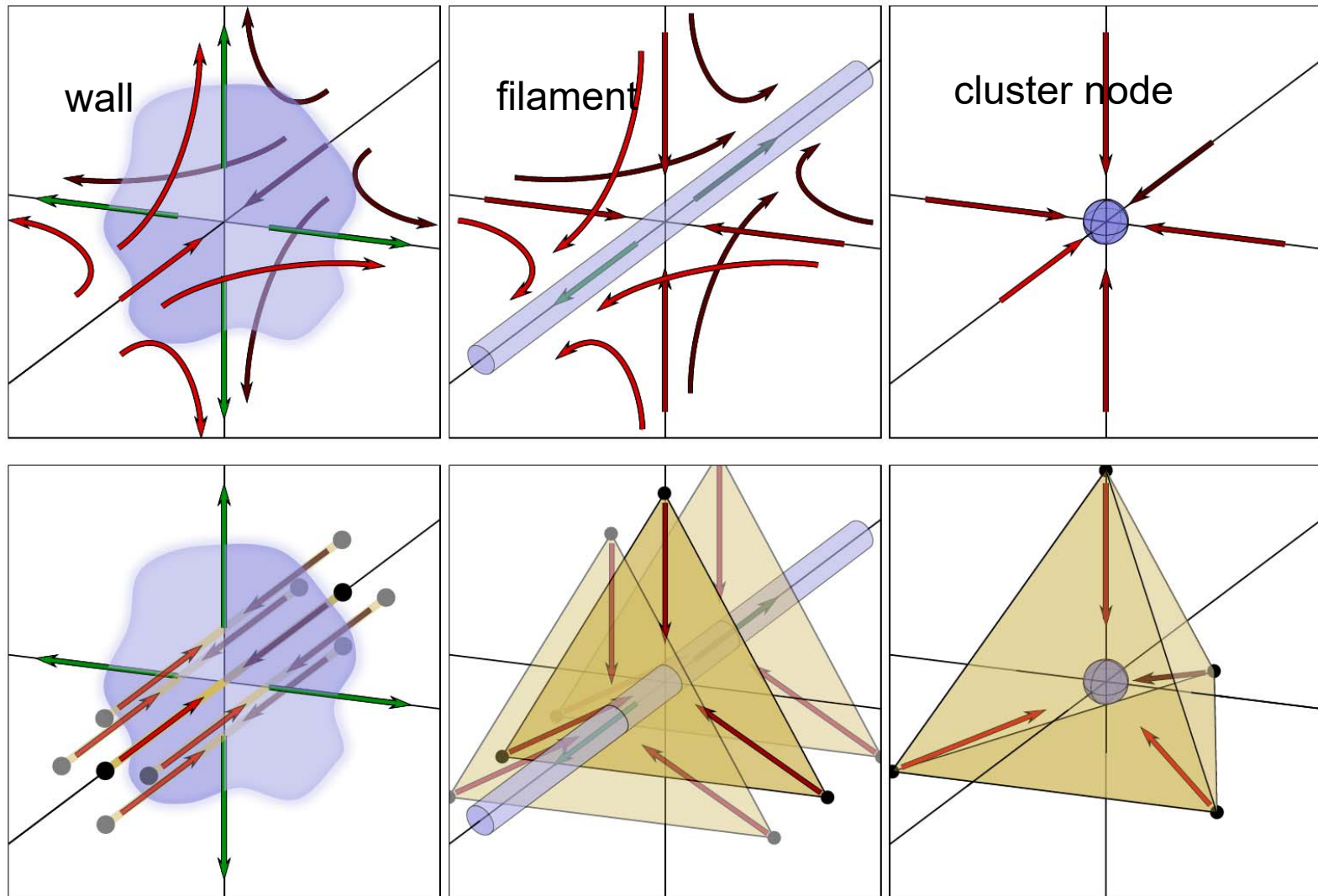
Voronoi
(weighted)

Hierarchical Web Evolution:

**Adhesion simulation
buildup Cosmic Web**

**Johan Hidding
2012**

Eulerian vs. Lagrangian weblike geometry



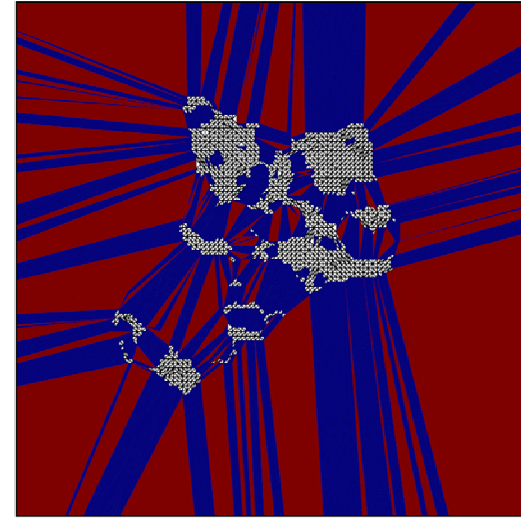
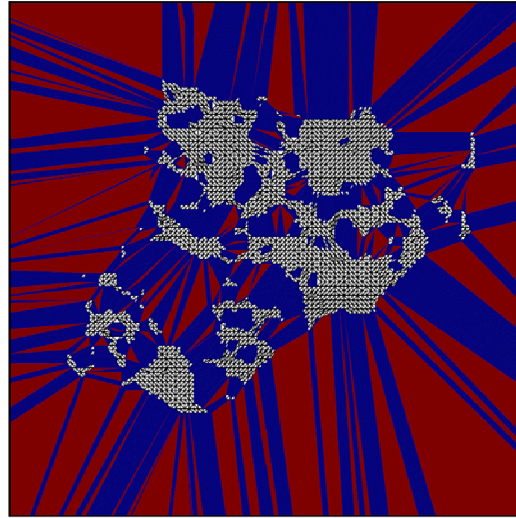
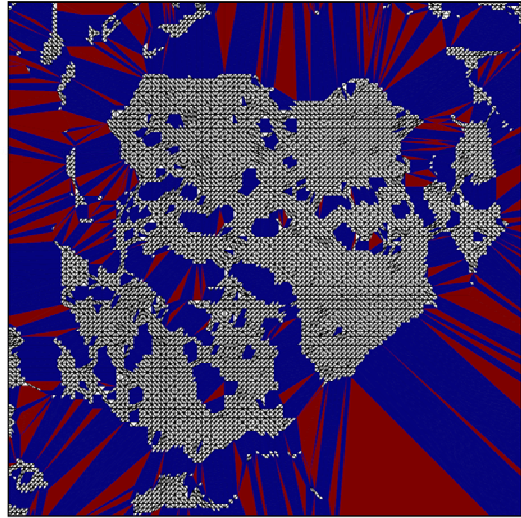
Eulerian

Lagrangian

Source
regions

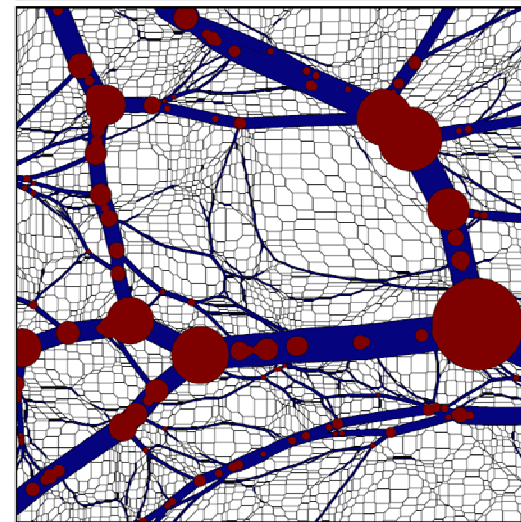
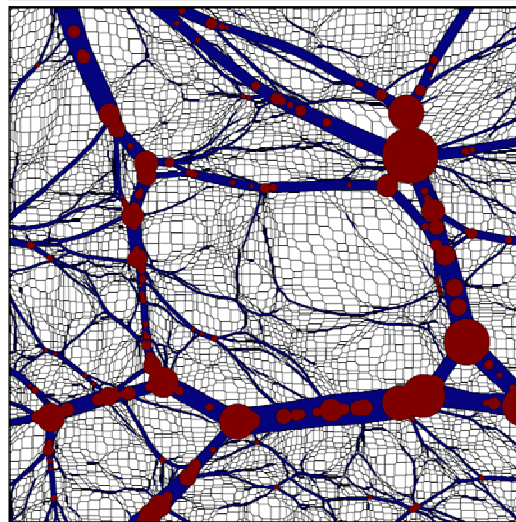
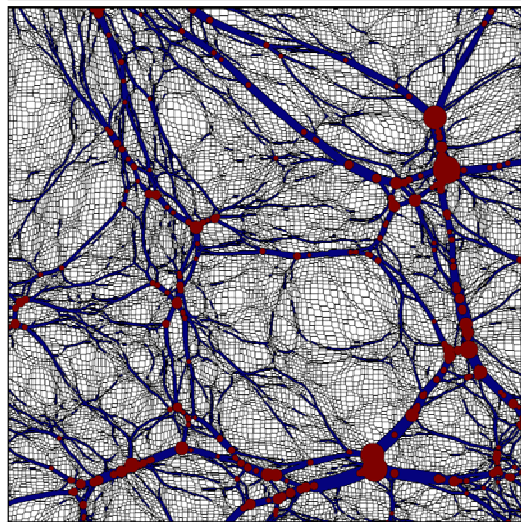
Lagrangian – Eulerian Cosmic Web

Delaunay- Voronoi Tessellations



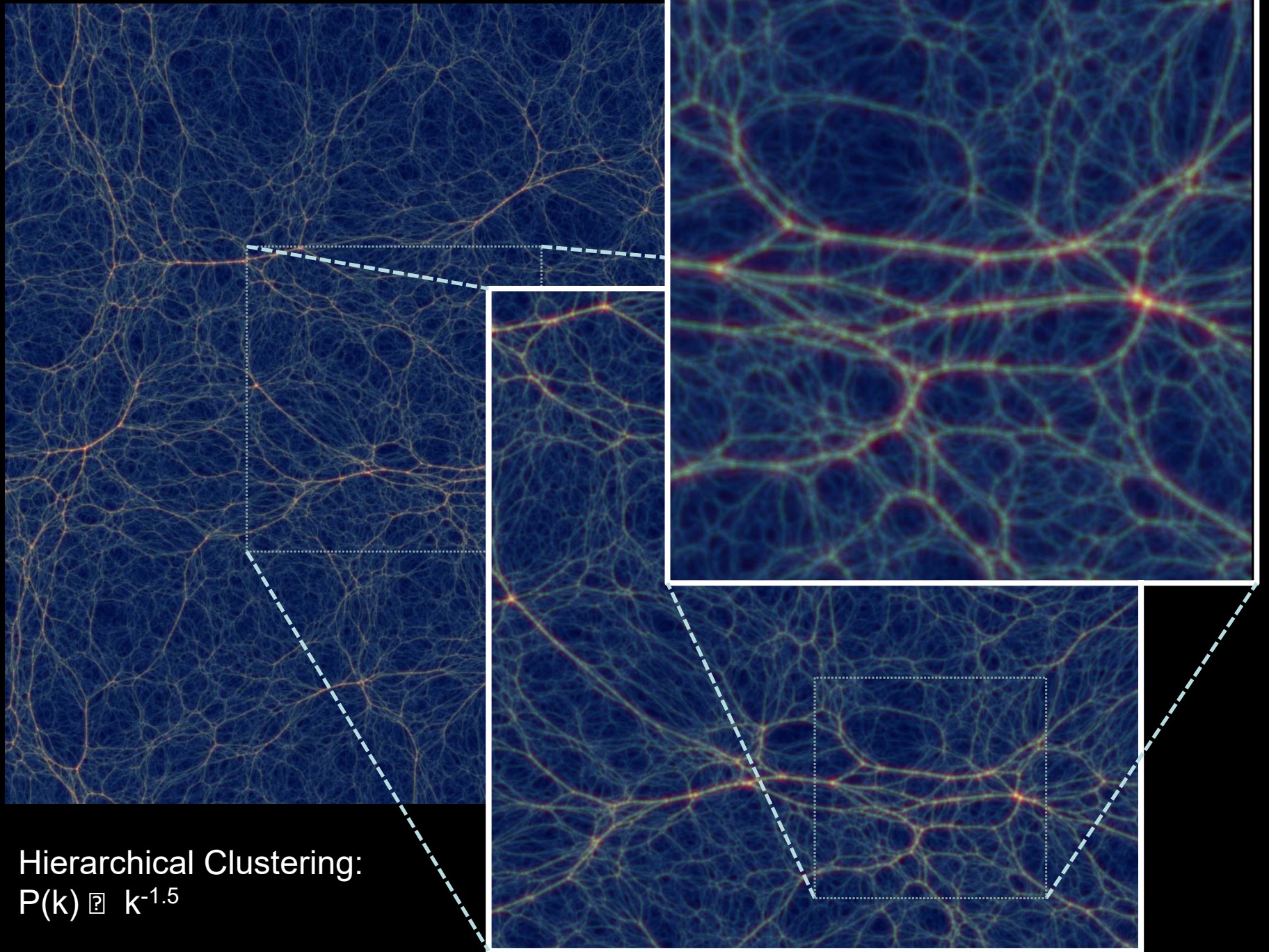
Lagrangian

Delaunay
Tessellation



Eulerian

Voronoi
Tessellation

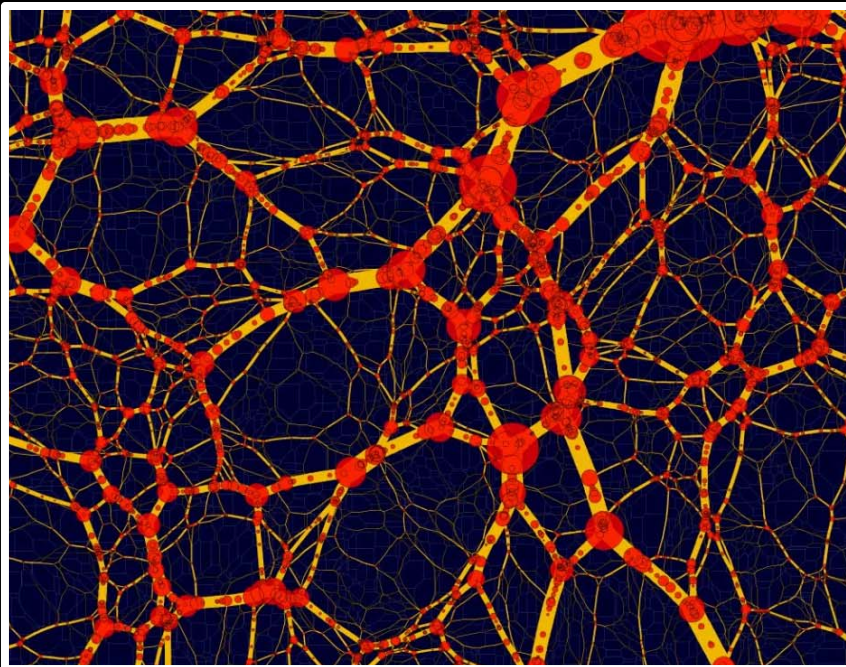


Hierarchical Clustering:
 $P(k) \propto k^{-1.5}$

Cosmological Sensitivity Cosmic Web

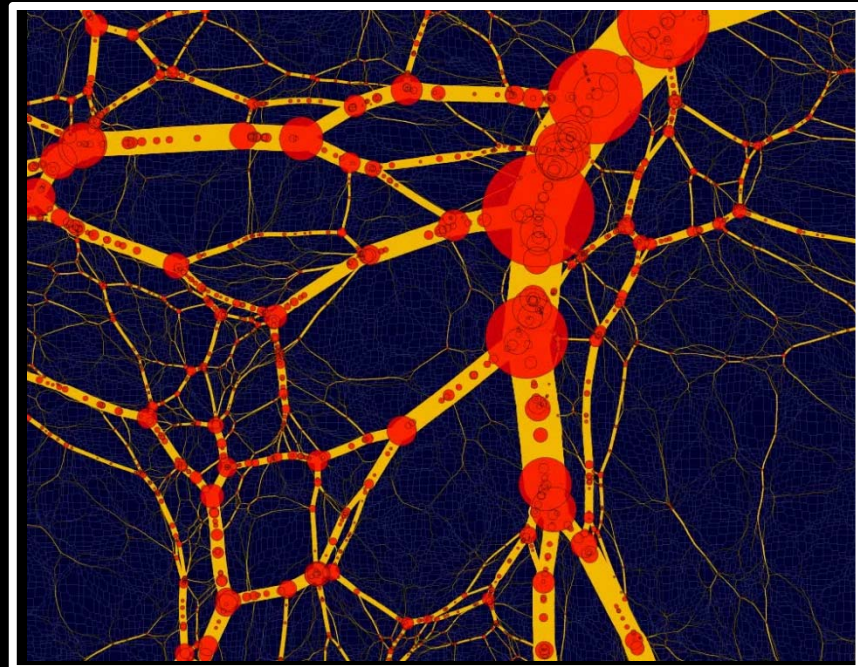
the morphology of the weblike network is highly sensitive to the underlying cosmology

$$P(k) \sim k^{-1.5}$$



Hidding 2012/2014

$$P(k) \sim k^{-2.0}$$



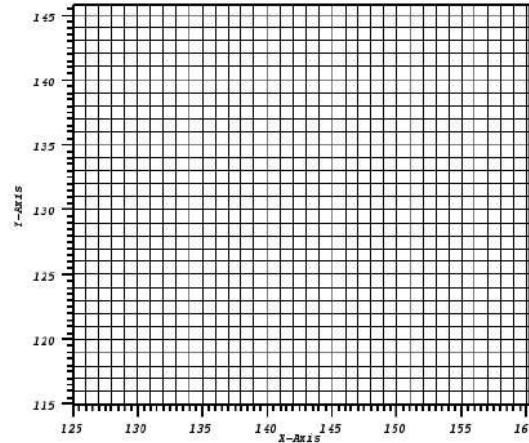
Cosmic Web

Phase-Space Evolution

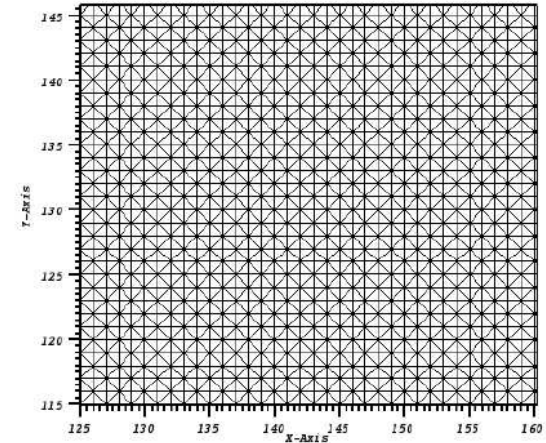
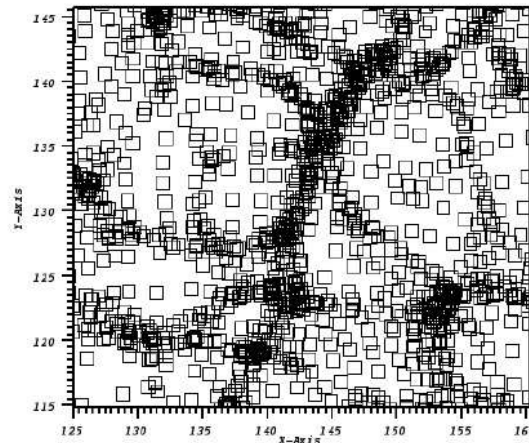
Tessellation Deformation & Phase Space Projection

Translation towards
Multi-D space:

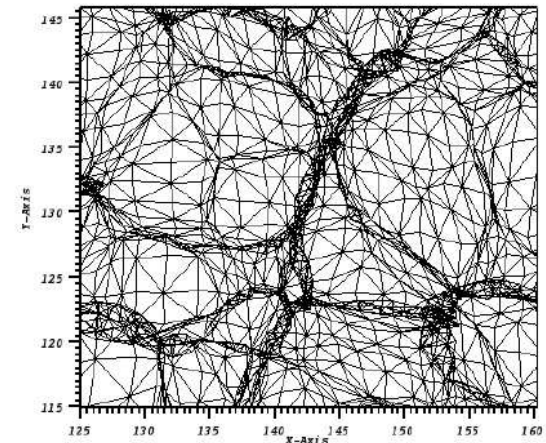
- Look at deformation of initial tessellation
- each tessellation cell represents matter cell
- evolution deforms cell
- once cells start to overlap, manifestation of different phase-space matter streams



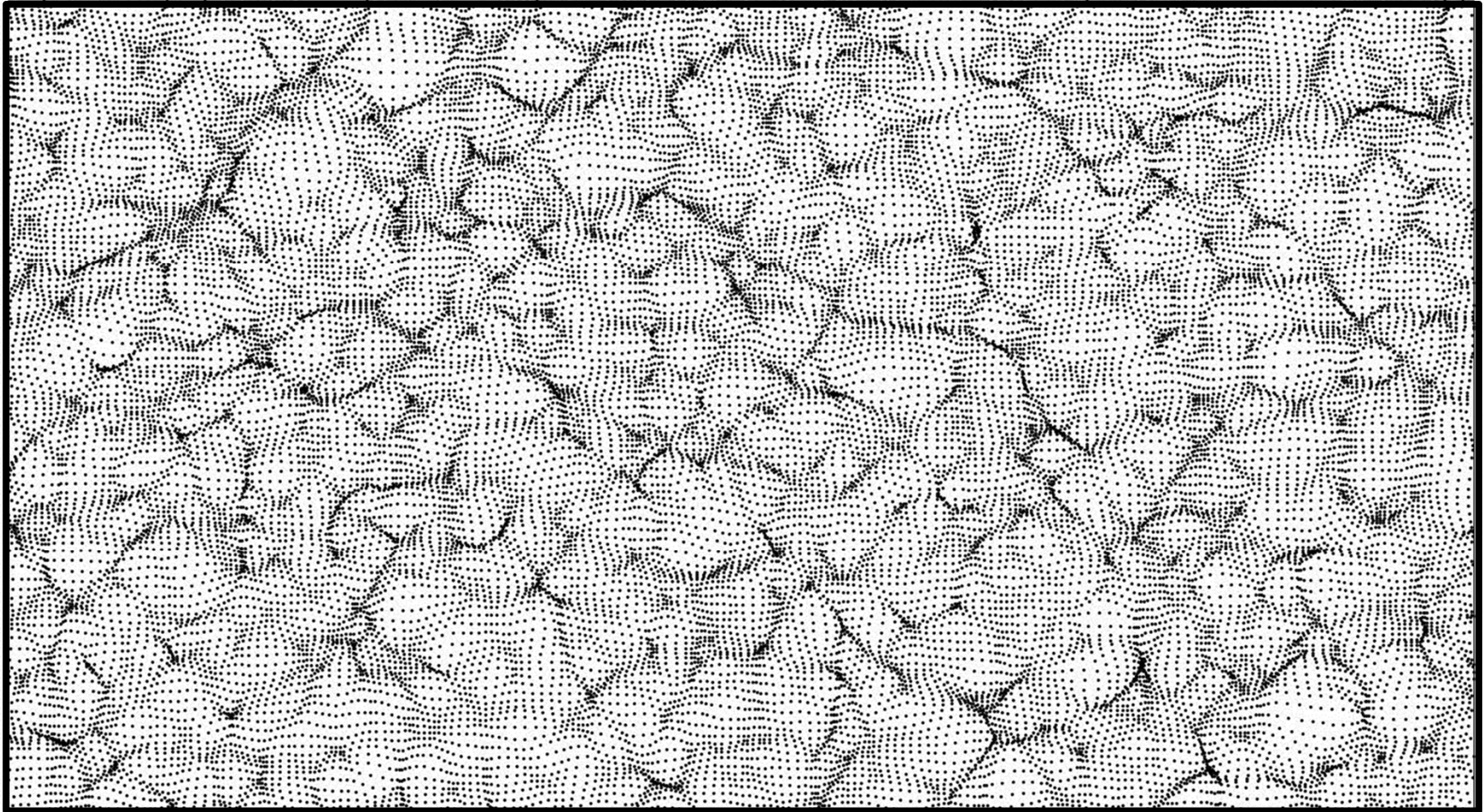
particle displacement



fluid element deformation



Simulation – Discrete Particles



Simulation – Mass Elements



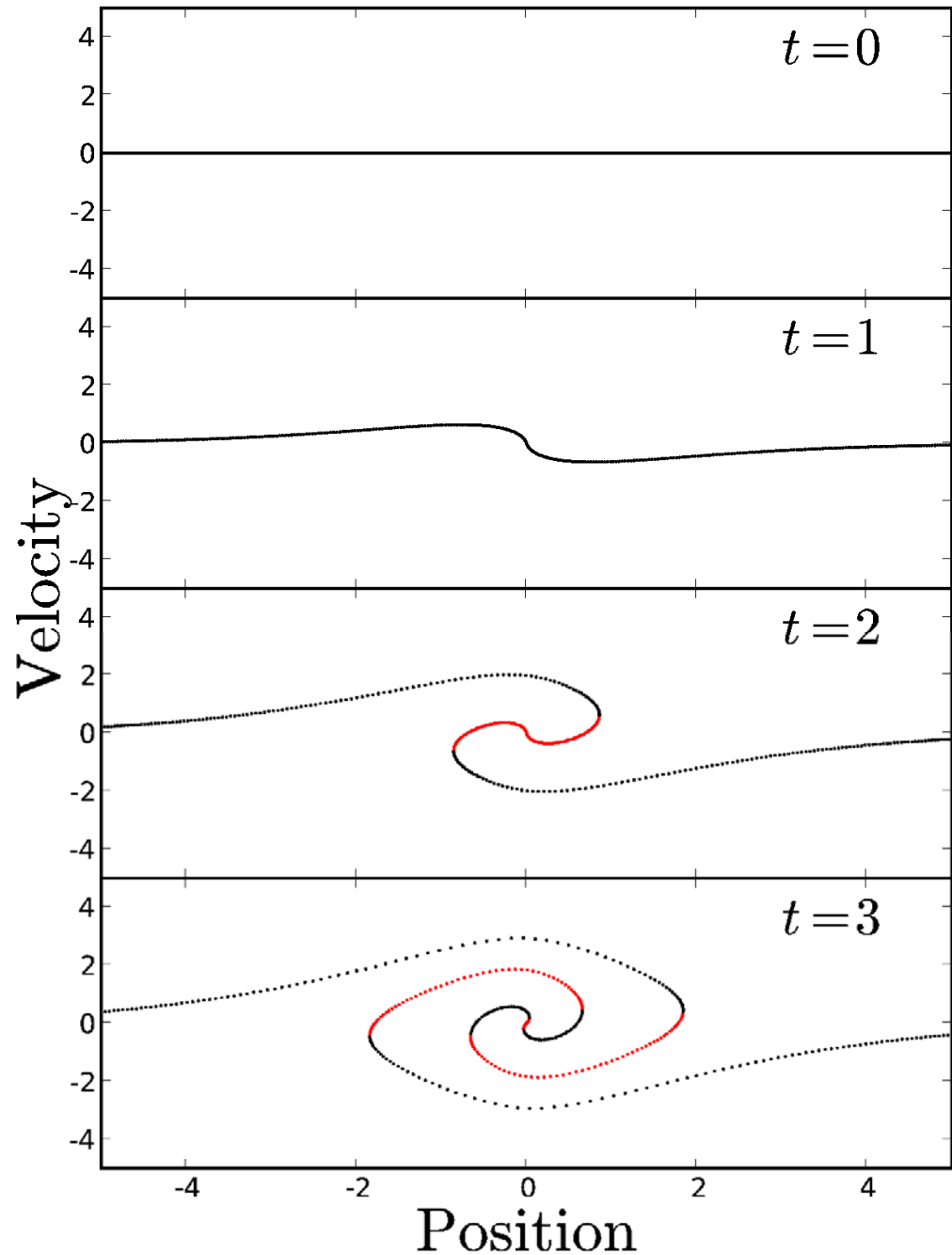
Phase Space Evolution

Dark Matter Phase Space sheet:

3-D structure projection of a folding DM phase space sheet
In 6-D phase space

- Shandarin 2010, 2011
- Neyrinck et al. 2011, 2012
Origami
- Abel et al. 2011

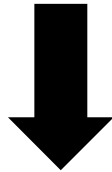
Evolving matter distribution in
position-velocity space – 1D



Phase Space Evolution

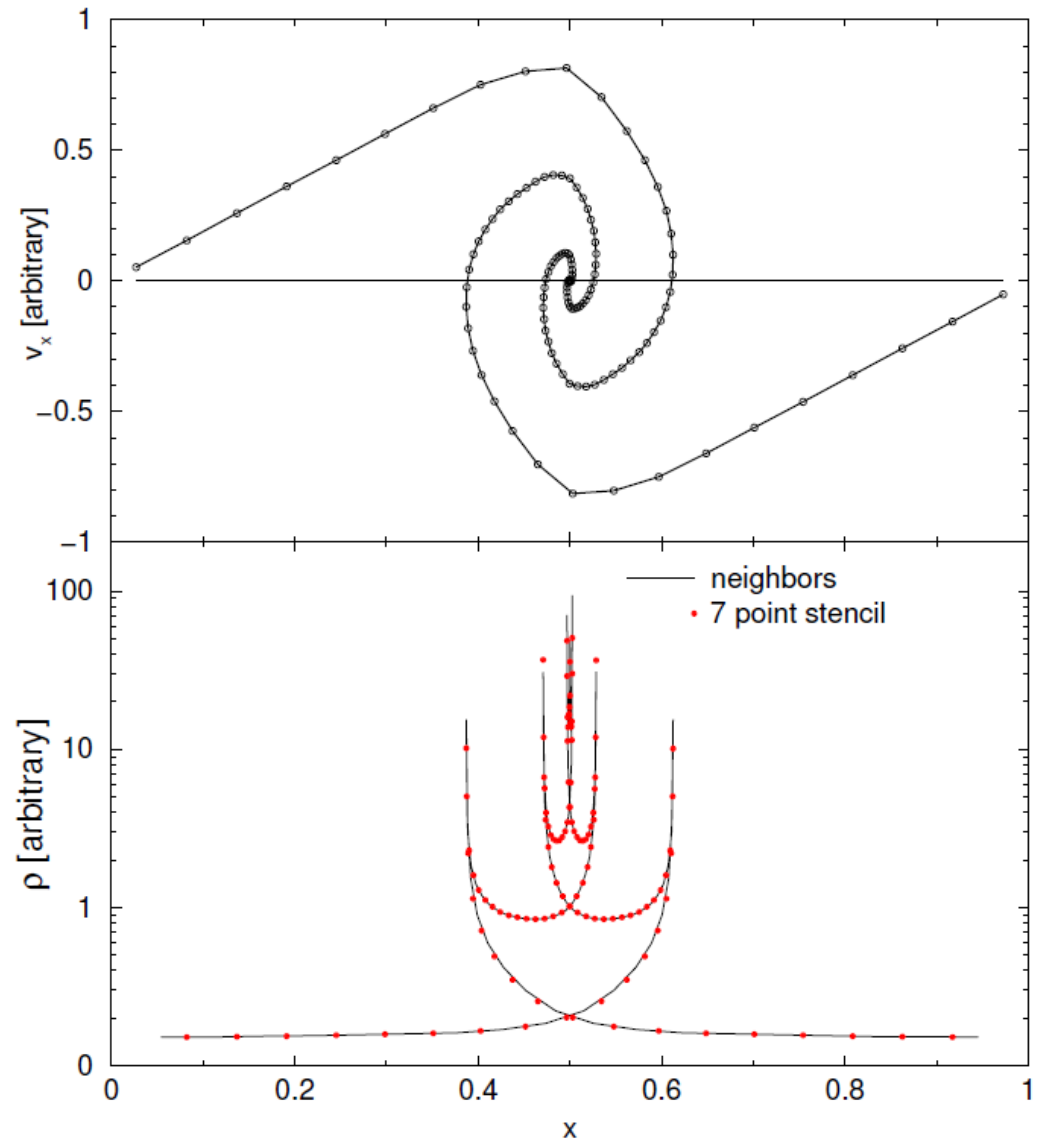
Phase space:

Velocity vs. Position



Density:

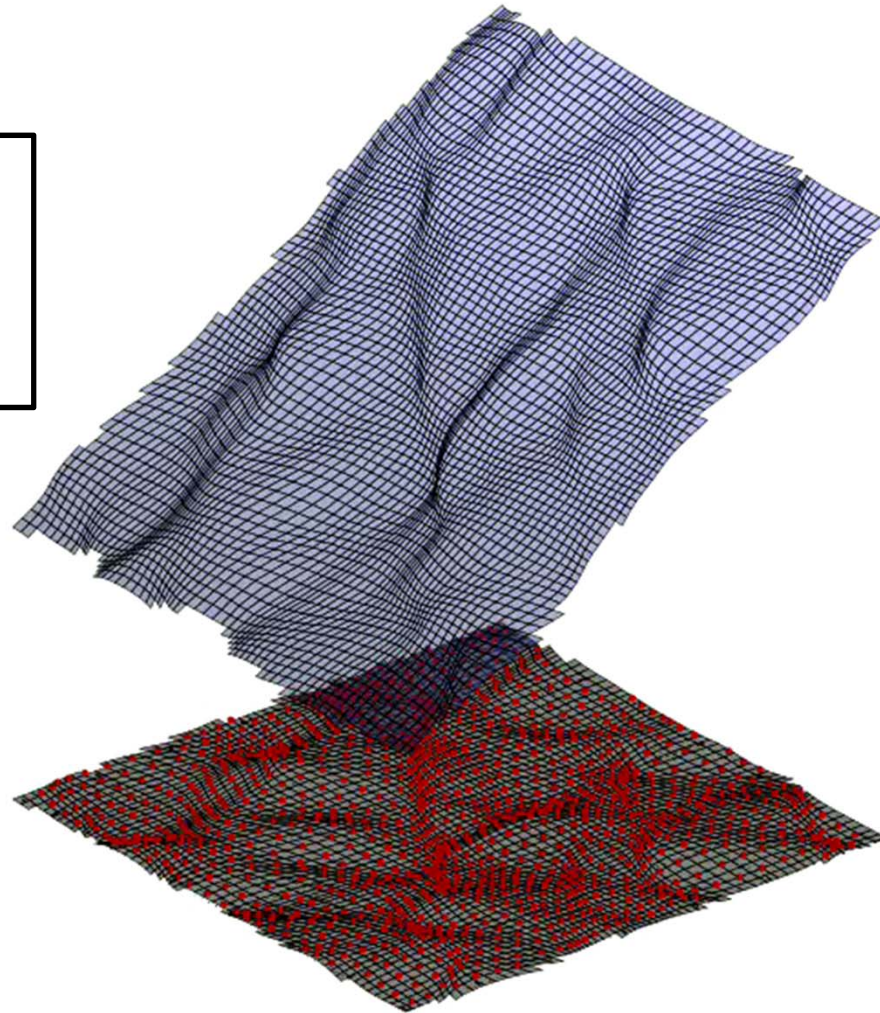
$$\rho(\vec{x}, t) = \int f(\vec{x}, \vec{v}, t) d\vec{v}$$



Phase-Space Evolution

Dynamical Evolution:

folding the
phase-space sheet $\{q,x\}$



Lagrangian
coordinate

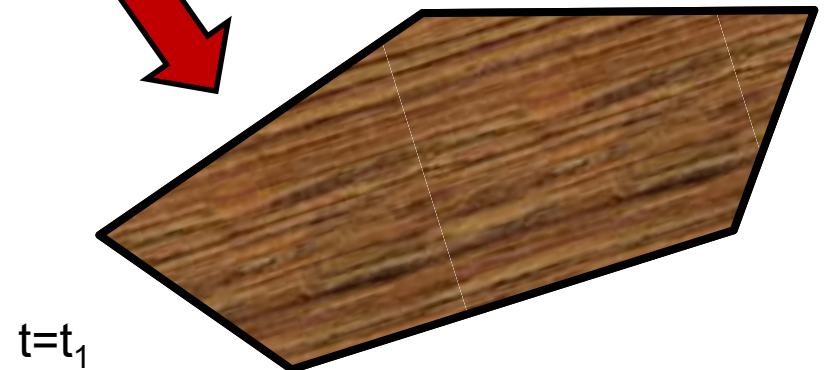
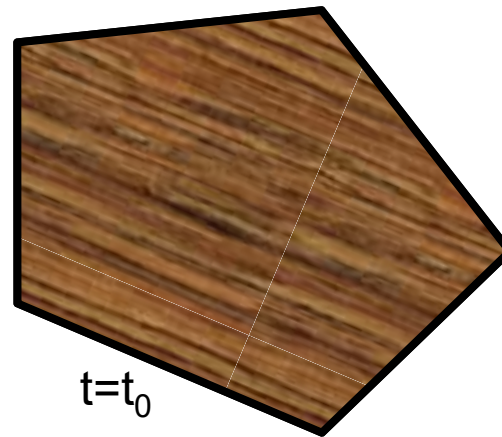
Eulerian plane

Tessellation Deformation & Phase Space Projection

Translation towards
Multi-D space:

- Look at deformation of initial tessellation
- each tessellation cell represents matter cell
- evolution deforms cell

Monostream
Density Evolution



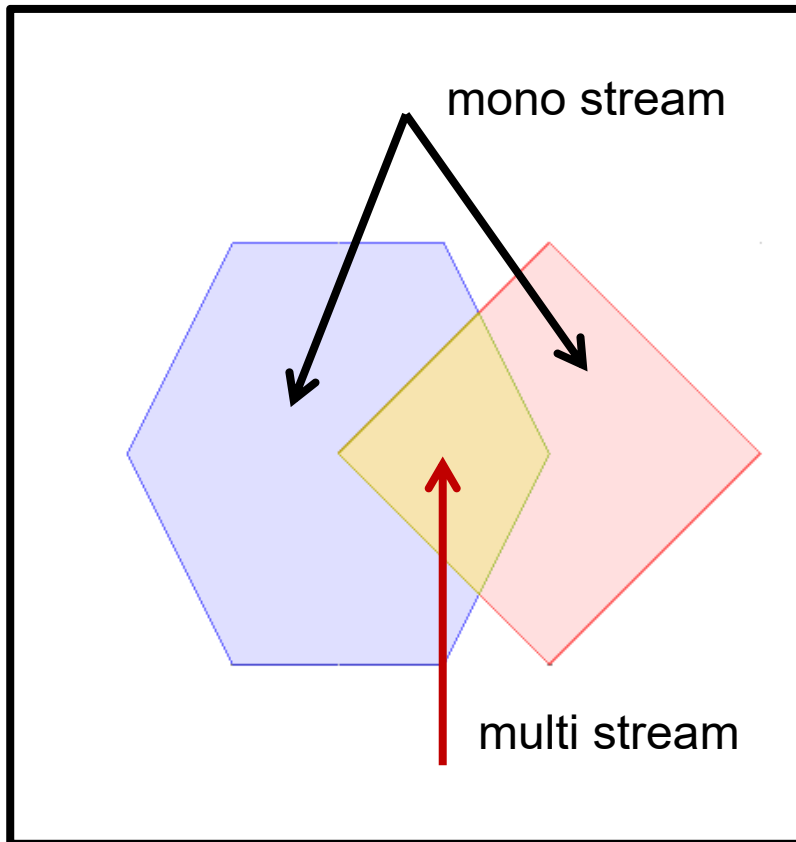
Conservation of mass
(continuity eq.):

$$\rho(\vec{x}, t) = |J(\vec{x}, \vec{q})|^{-1} \rho(\vec{q}) = \left| \frac{\partial \vec{x}}{\partial \vec{q}} \right|^{-1} \rho(\vec{q})$$

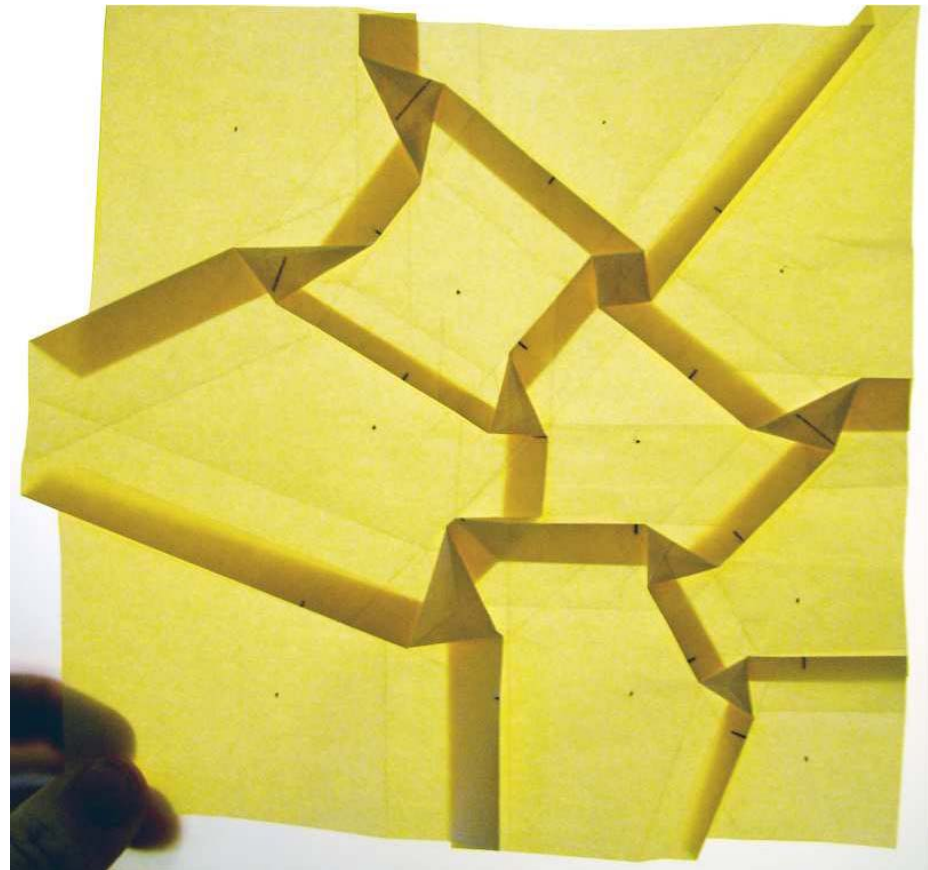


$$\rho(\vec{x}, t_1) = \frac{V_0}{V_1} \rho(\vec{q}, t_0)$$

(Cosmic) ORIGAMI

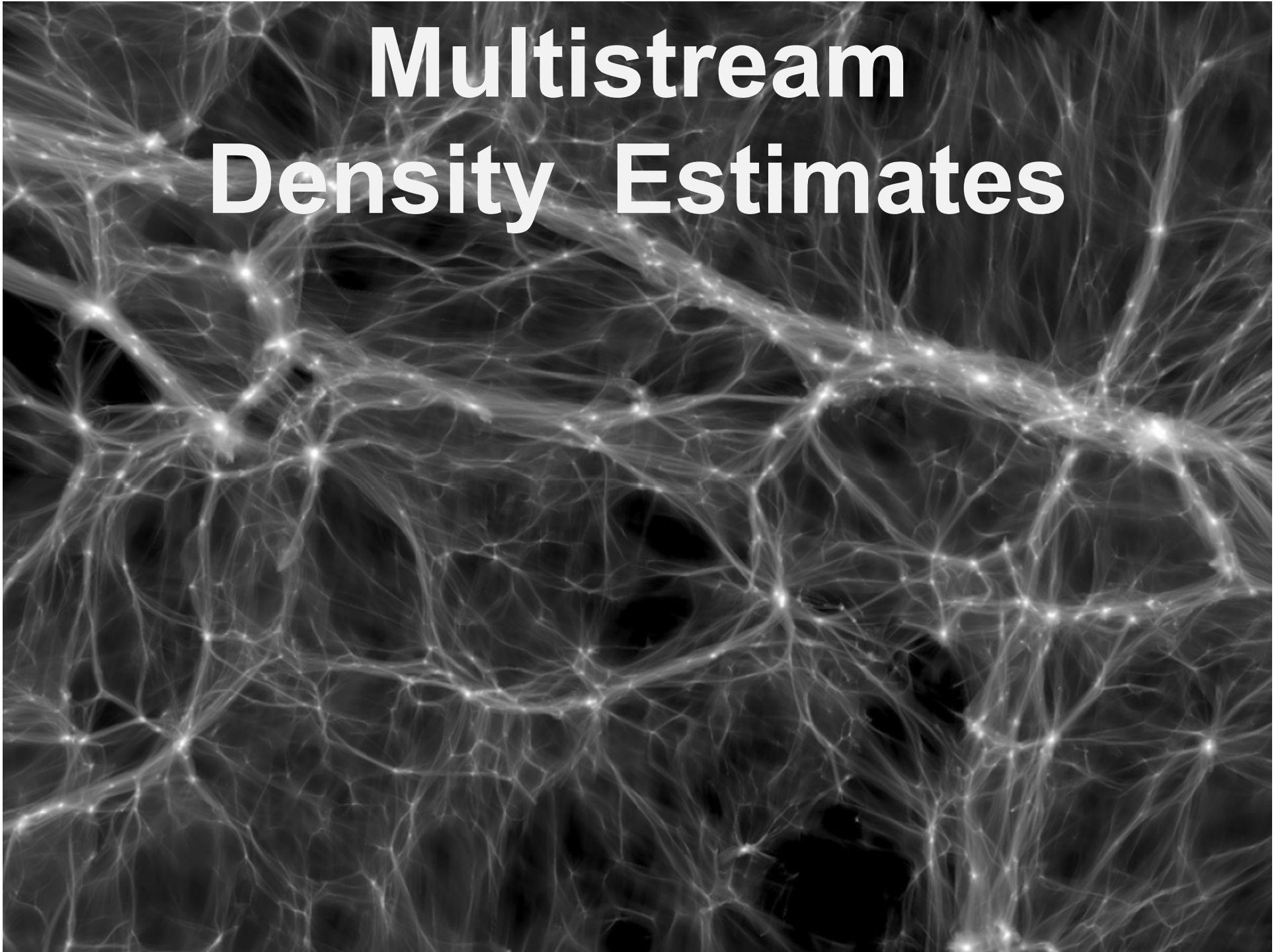


Evolution of dynamical system:
Phase-space folding – Cosmic Origami



$$\rho_{total}(\vec{x}, t_1) = \sum_i \frac{V_{0i}}{V_{1i}} \rho(\vec{q}_i, t_0)$$

Multistream Density Estimates



Cosmic Web Stream Density

Translation towards
Multi-D space:

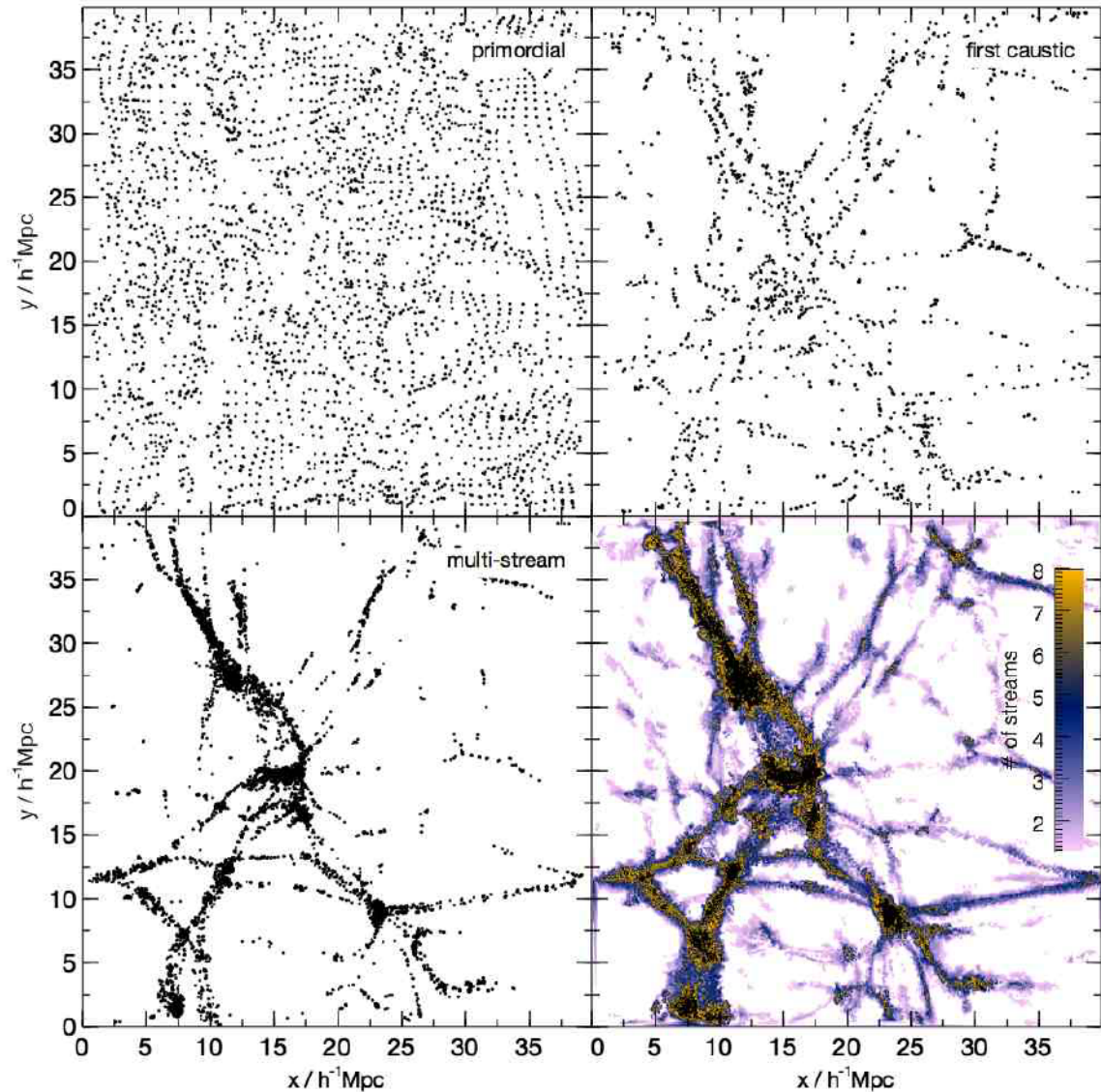
Density of
dark matter streams:

- # phase space folds

=

locally overlapping
tessellation cells

Shandarin 2012
Abel, Hahn & Kaehler 2012
Falck, Neyrinck et al. 2012

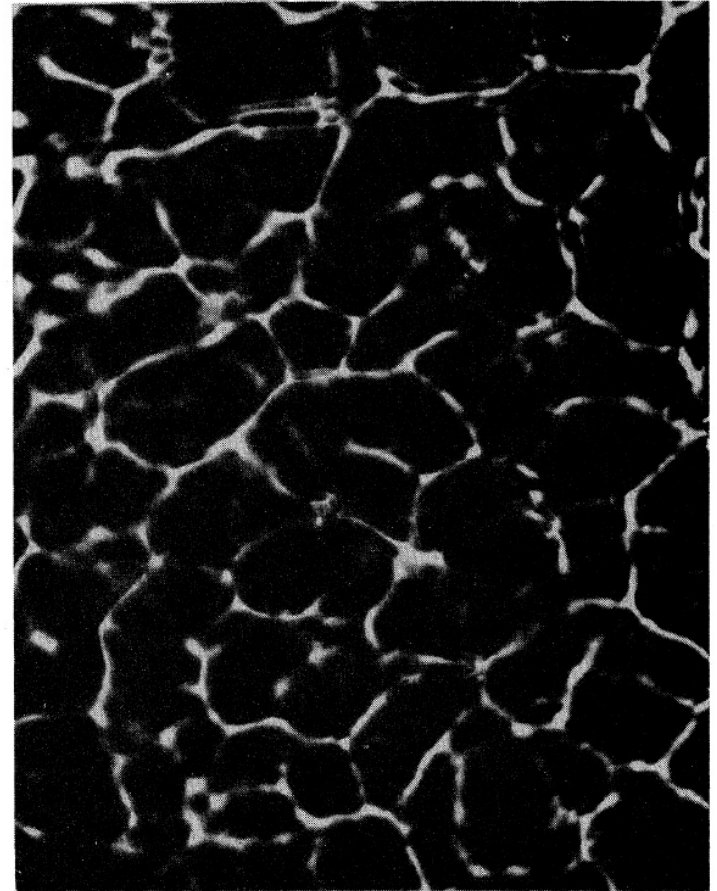
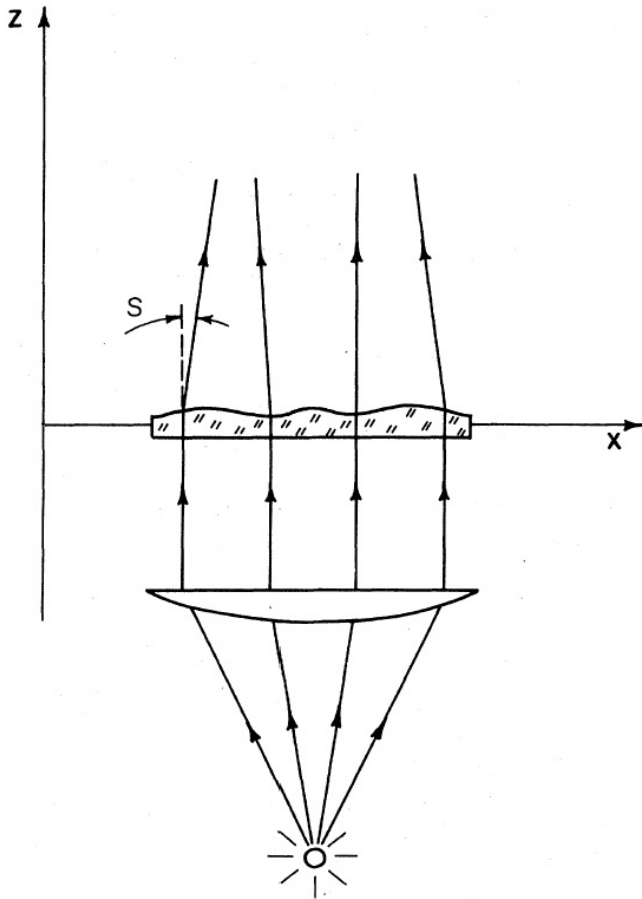


Cosmic Web Skeleton:

Phase-Space Caustics Caustic Conditions

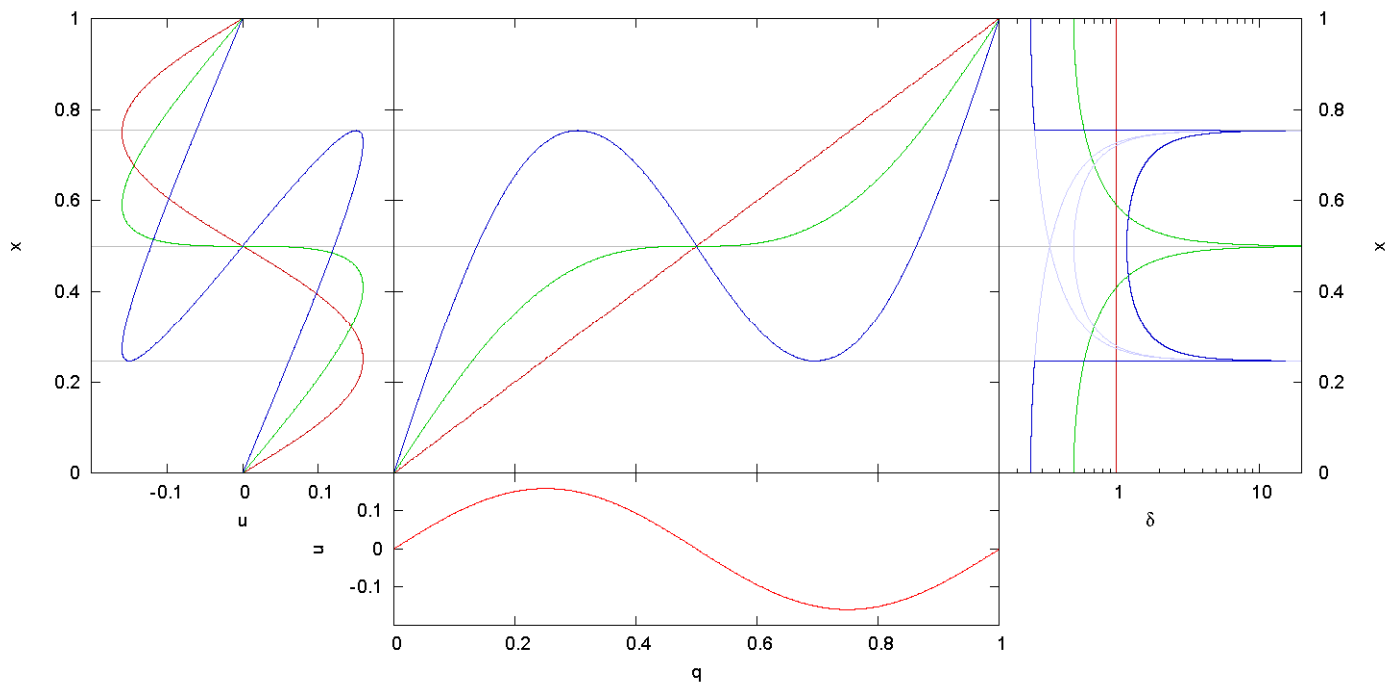
Hidding, Shandarin, vdW. 2014
Feldbrugge, vdW et al. 2017a
Feldbrugge, vdW et al. 2017b

Zel'dovich Formalism: Streaming & Caustics

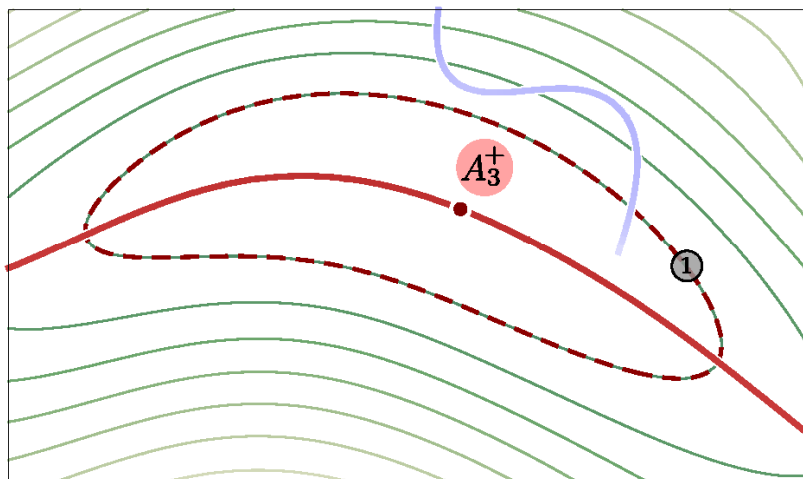


Shandarin & Zeldovich 1989

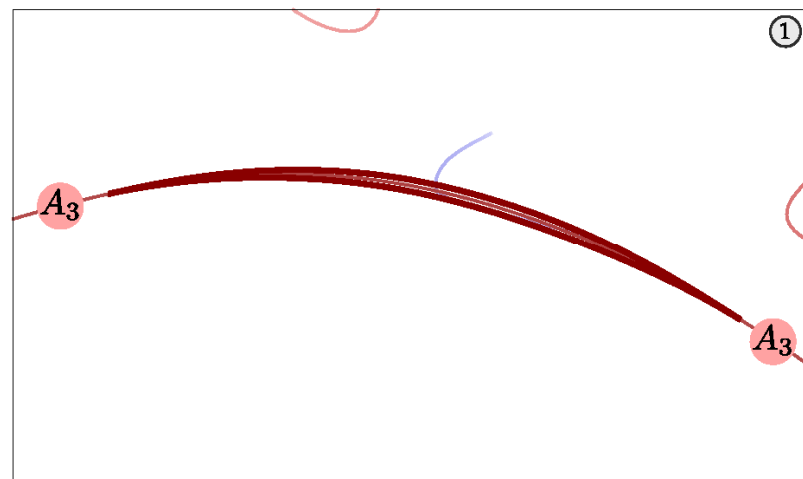
Illustration of the formation of caustics due to
streaming paths of light through deforming medium



**Caustic Formation:
Folds & Cusps**



Lagrangian space: A_2 contours



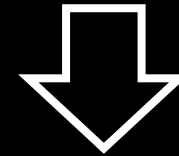
Eulerian space: folds & cusps

Zel'dovich Approximation

$$\vec{x} = \vec{q} + D(t) \vec{u}(\vec{q})$$

$$\vec{u}(\vec{q}) = -\vec{\nabla} \Phi(\vec{q})$$

$$d_{ij} = -\frac{\partial u_i}{\partial q_j}$$

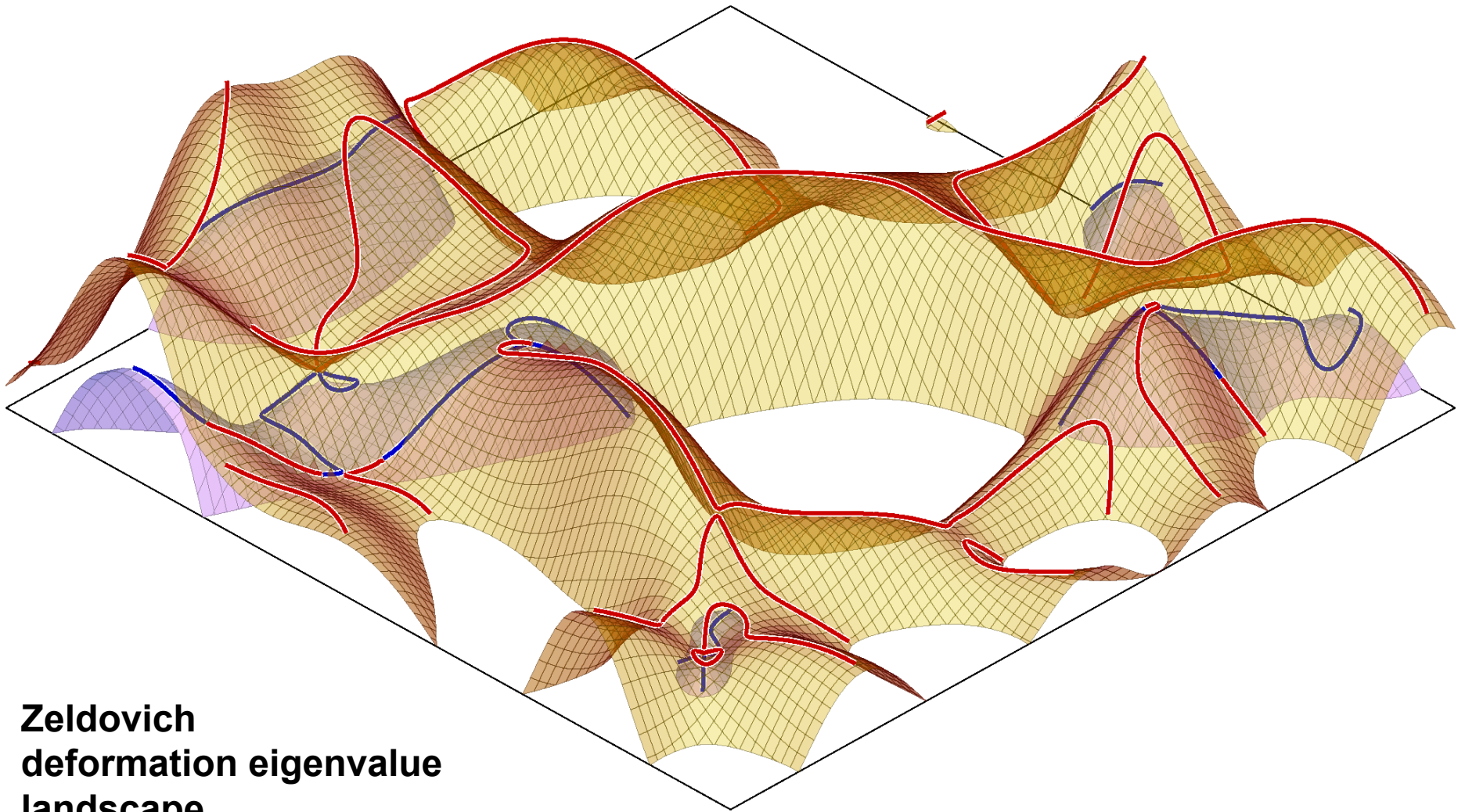


$$\rho(\vec{q}, t) = \frac{\rho_u(t)}{(1 - D(t)\lambda_1(\vec{q}))(1 - D(t)\lambda_2(\vec{q}))(1 - D(t)\lambda_3(\vec{q}))}$$

structure of the cosmic web determined by the spatial field of eigenvalues

$$\lambda_1, \lambda_2, \lambda_3$$

Singularities & Catastrophe: Deformation Field

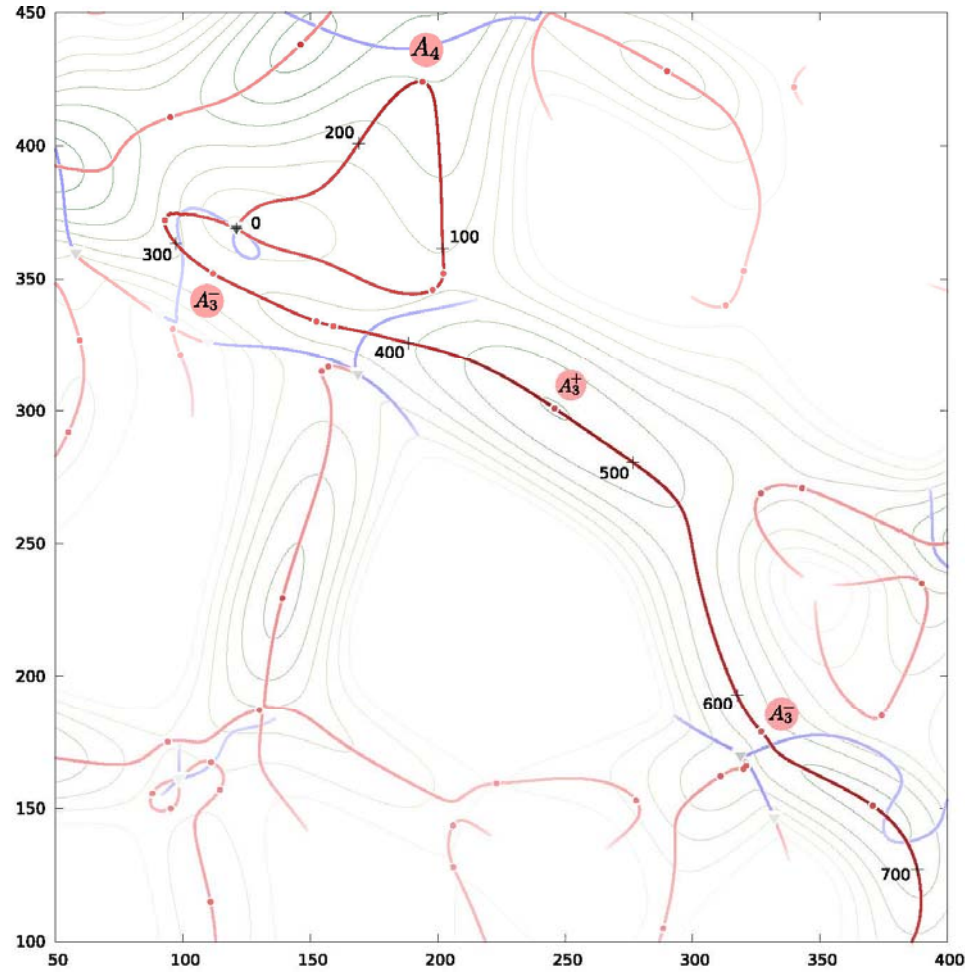


**Zeldovich
deformation eigenvalue
landscape**

Lagrangian Space:

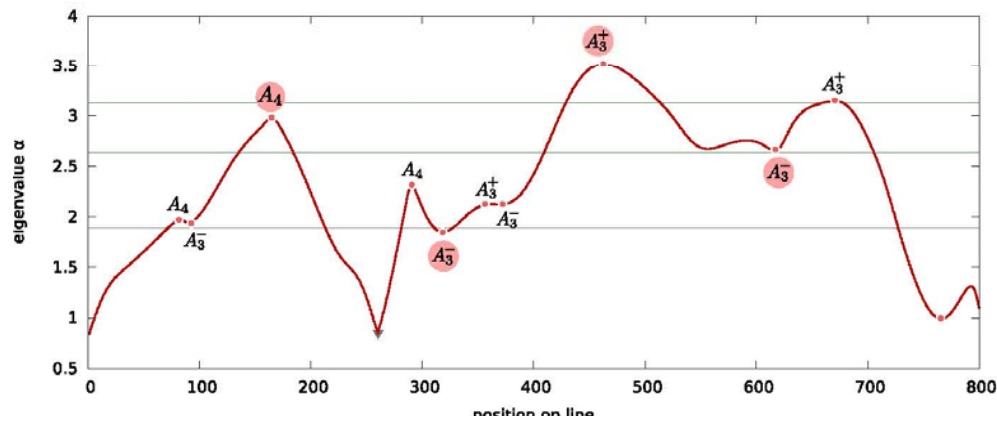
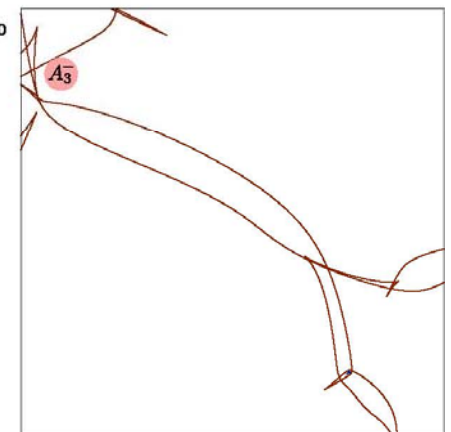
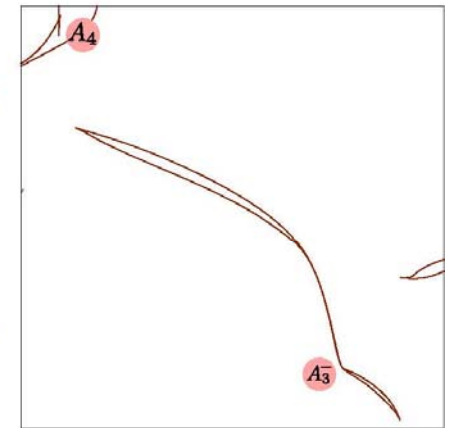
Map

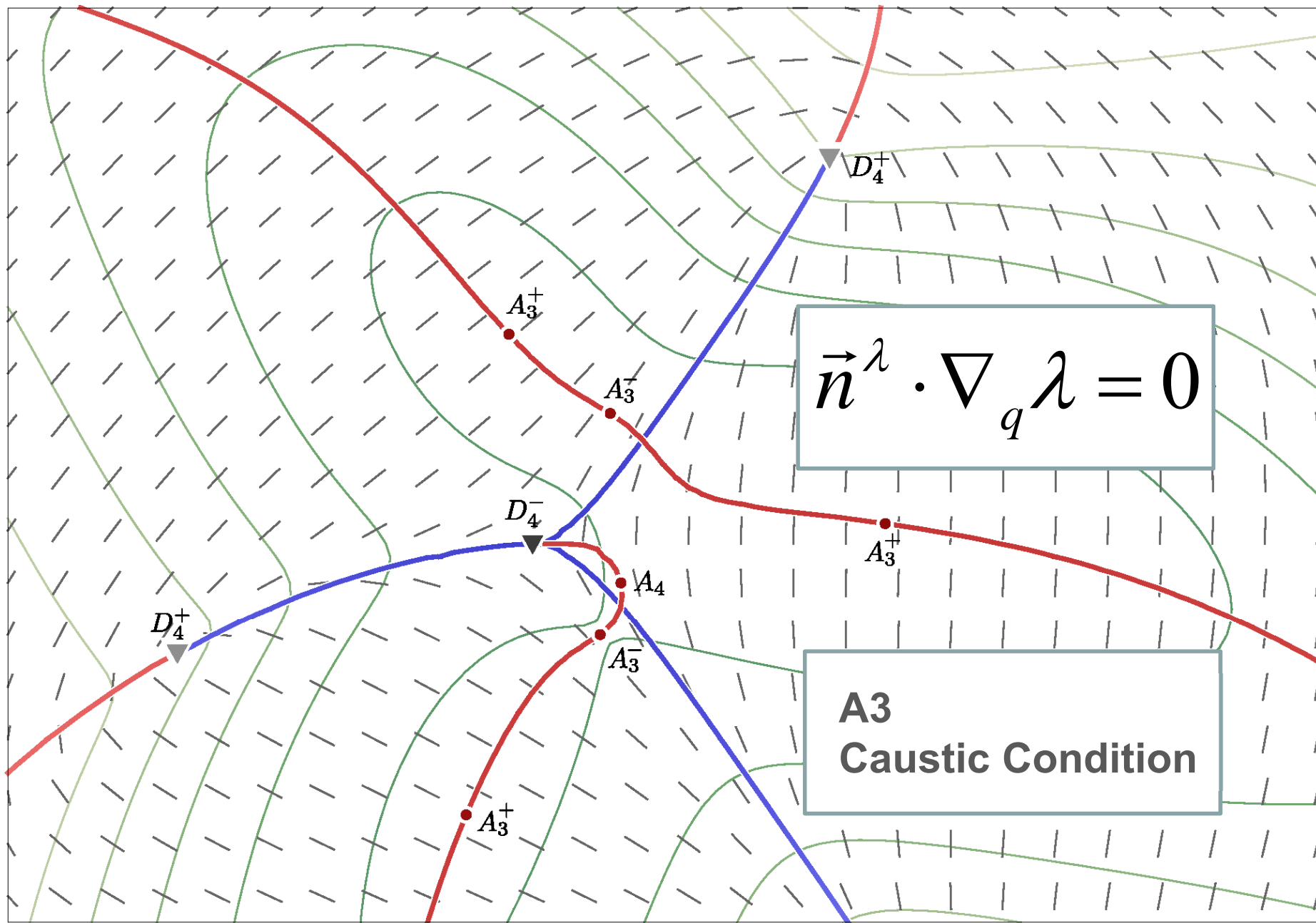
**Deformation Tensor
Eigenvalue λ_1**



Eulerian Space:

**Emerging
Catastrophes**





$$\vec{n}^\lambda \cdot \nabla_q \lambda = 0$$

**A3
Caustic Condition**

Caustic Conditions

In Lagrangian space L (coordinates q),

a singularity forms in a manifold $M \subset L$ at location q_s when at q_s ,

- the deformation tensor eigenvalue $\lambda_i(q_s)$
- the corresponding eigenvector $\vec{v}_i(q_s)$

when at least one nonzero tangent vector \vec{T} such that

$$\{1 - D(t) \lambda_i(q_s)\} \vec{v}_i^*(q_s) \cdot \vec{T} = 0$$

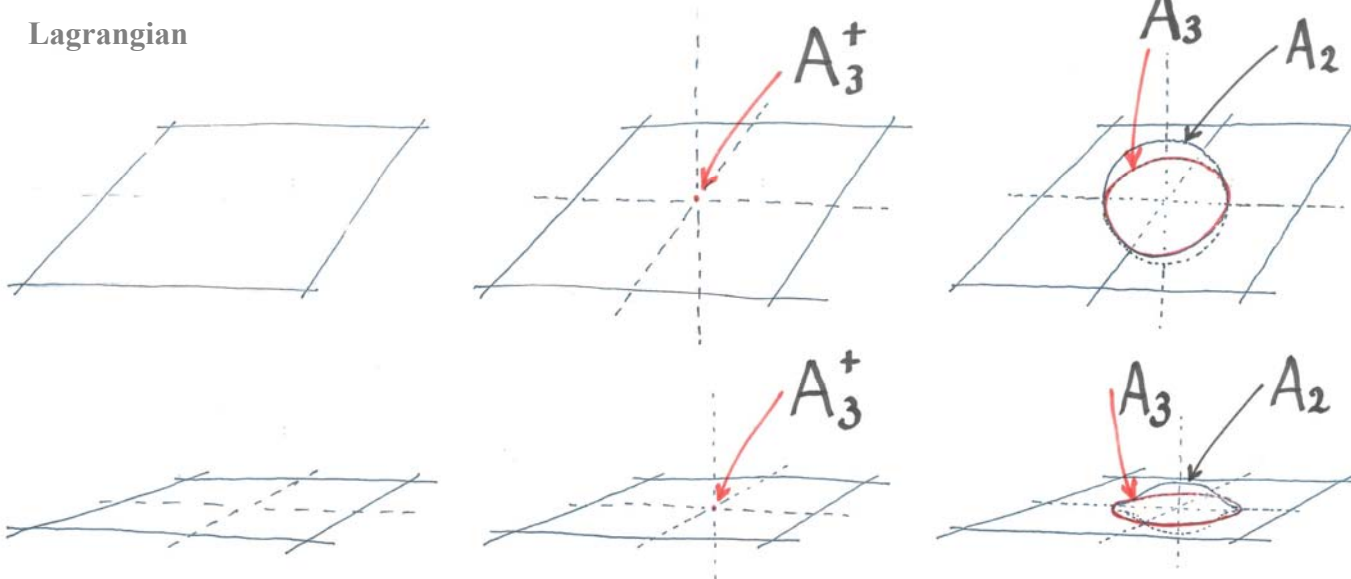


eg., A_3 caustic – cusp singularity –
emerges where:

$$\vec{n}^\lambda \cdot \nabla_q \lambda = 0$$

Feldbrugge, vdW et al. 2017

Lagrangian



Eulerian

Formation of an A_3 cusp, along with A_2 folds

$D=1$

A_2 : folds

A_3 : cusps

$D=2$

A_2 : folds

A_3 : cusps

A_4 : swallowtail

D_4 : umbilics

$D=3$

A_2 : folds

A_3 : cusps

A_4 : swallowtail

A_5 : butterfly

D_4 : umbilics

D_5

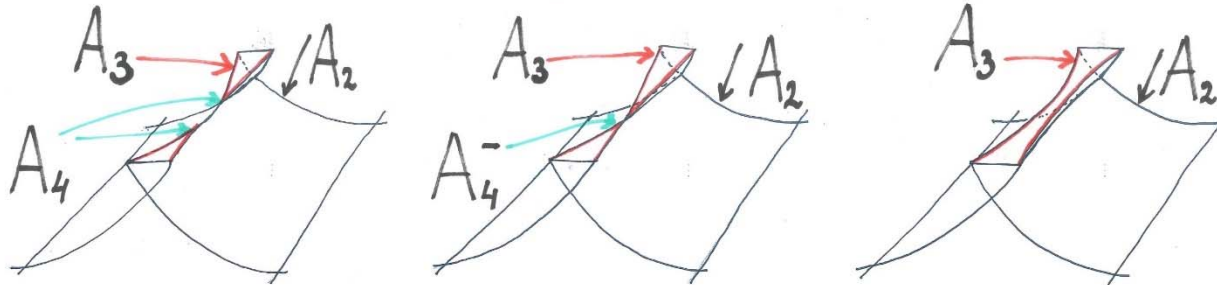
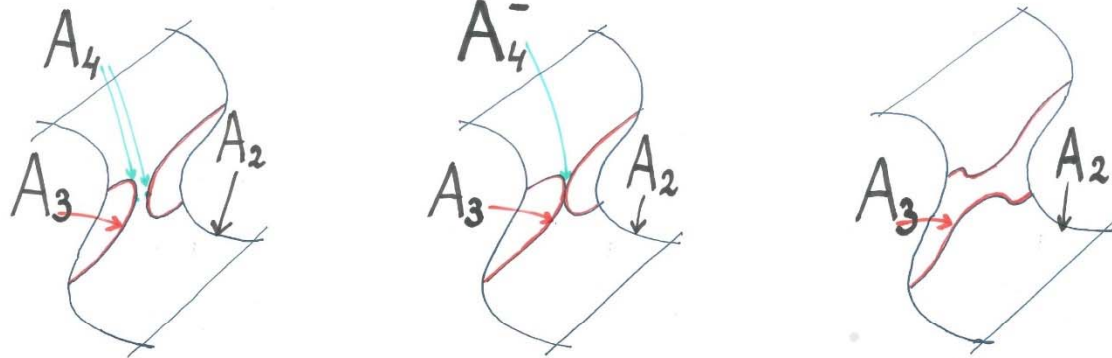
E_5

Catastrophe Theory:

Lagrangian catastrophe/caustic classification V. Arnold

(also see Zeeman, Thom)

Lagrangian



Eulerian

Merging of A_3 cusps at an A_4 swallowtail singularity

$D=1$

A_2 : folds

A_3 : cusps

$D=2$

A_2 : folds

A_3 : cusps

A_4 : swallowtail

D_4 : umbilics

$D=3$

A_2 : folds

A_3 : cusps

A_4 : swallowtail

A_5 : butterfly

D_4 : umbilics

D_5

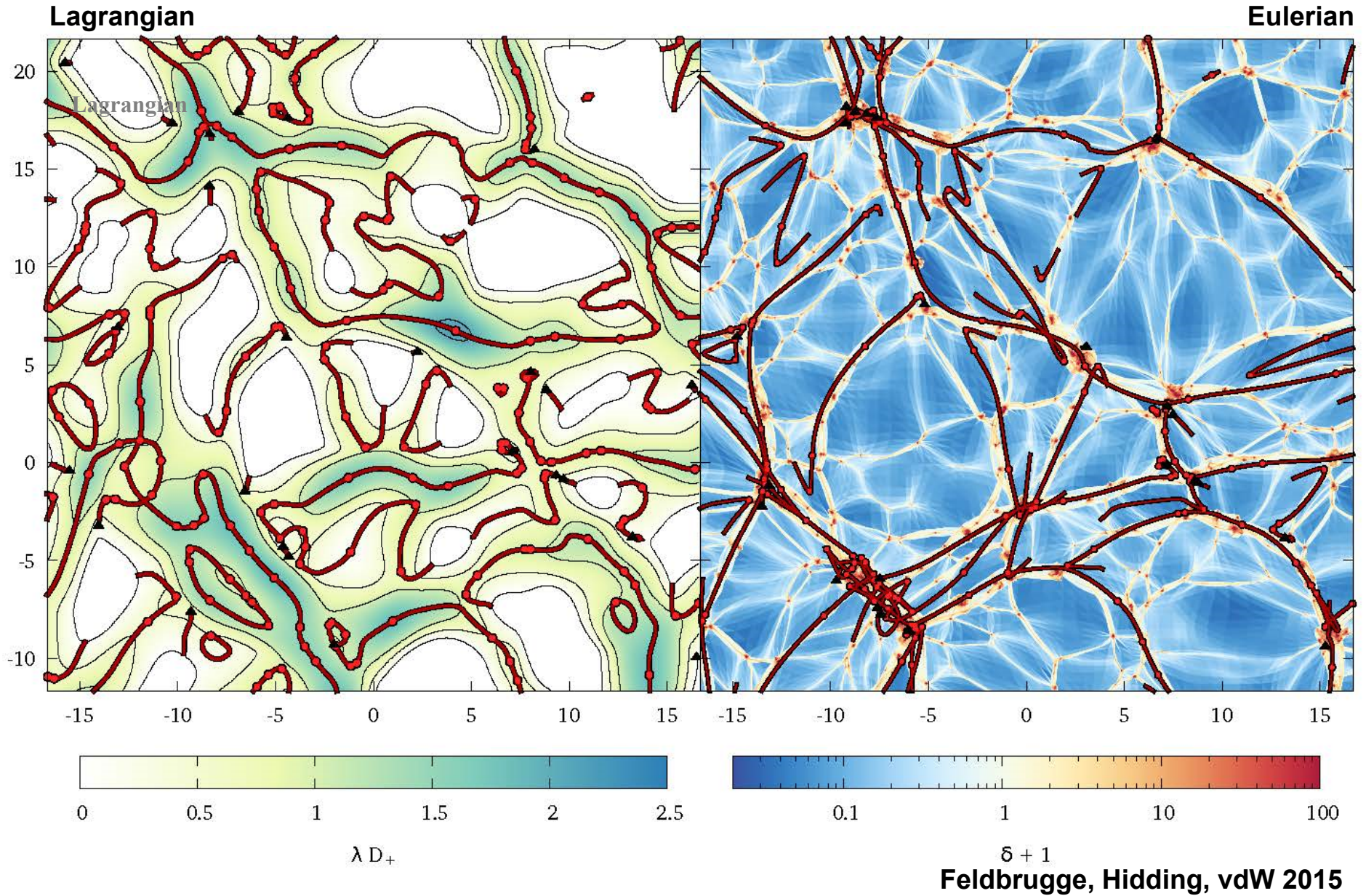
E_5

Catastrophe Theory:

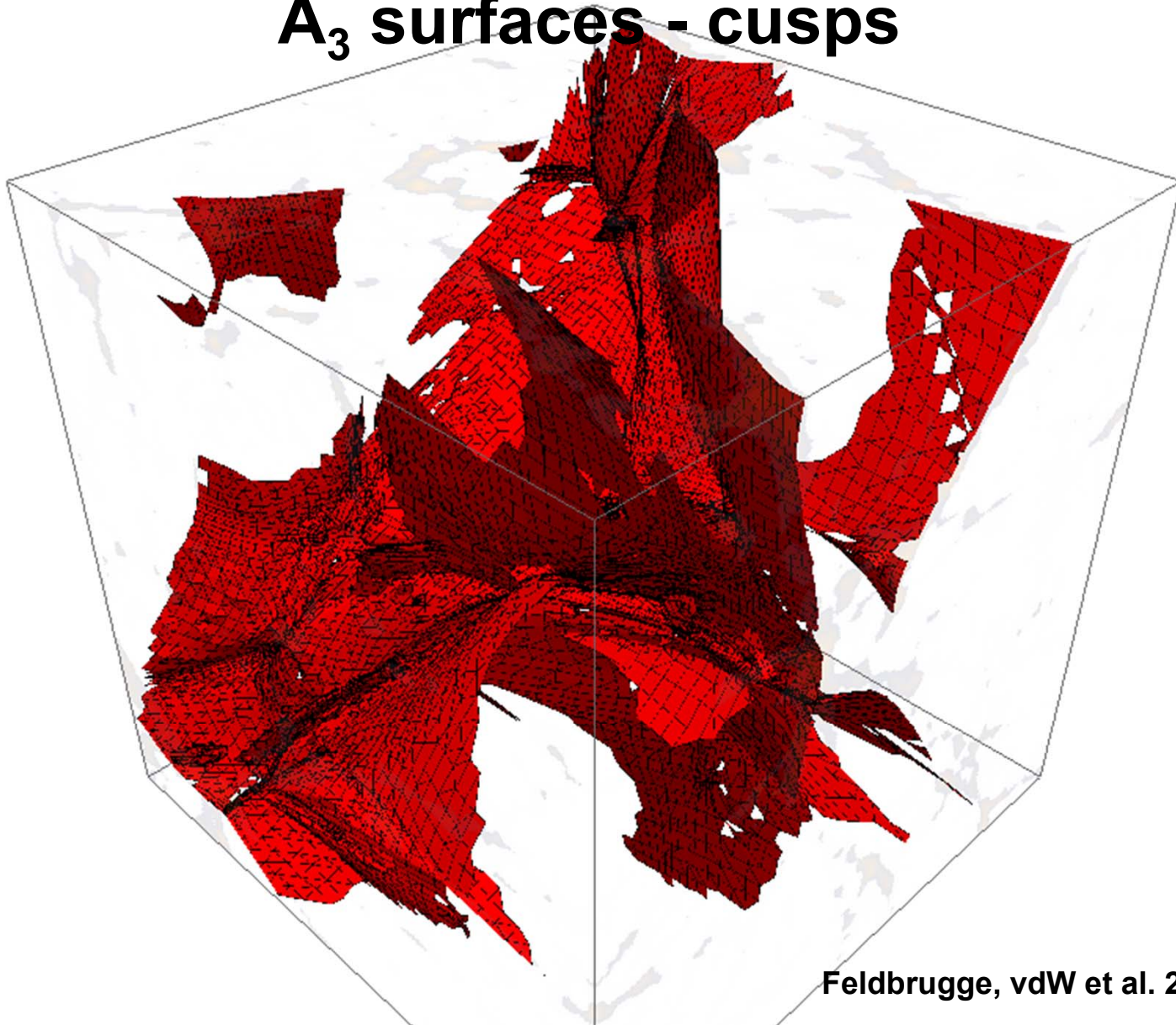
Lagrangian catastrophe/caustic classification V. Arnold

(also see Zeeman, Thom)

Catastrophic Spine of (2D) Cosmic Web

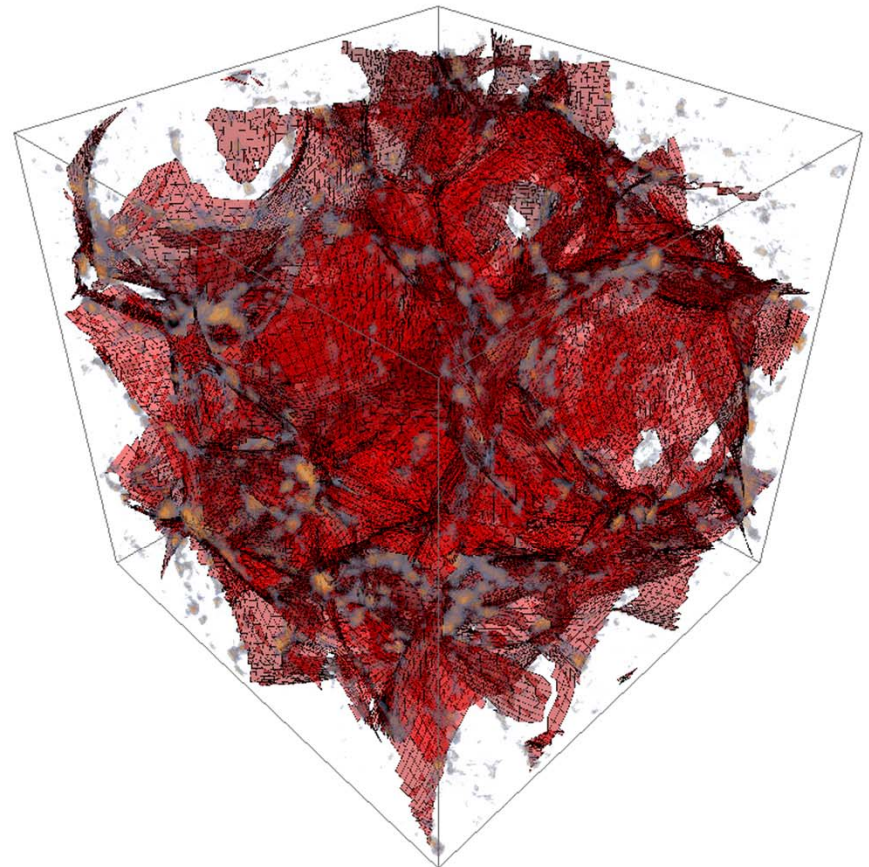
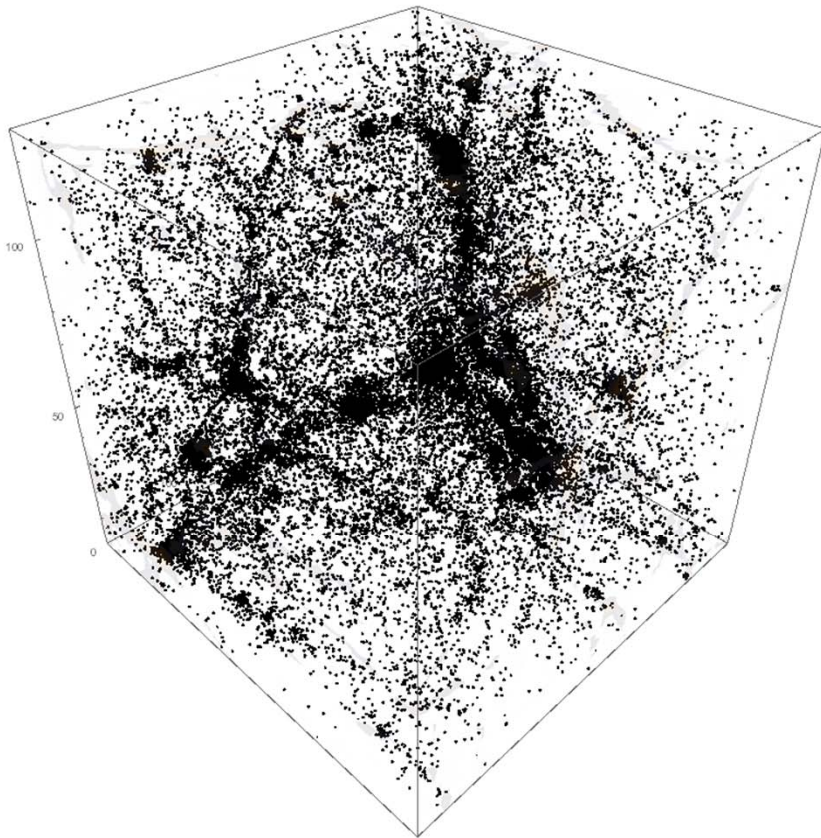


Skeleton (3D) Cosmic Web: A_3 surfaces - cusps

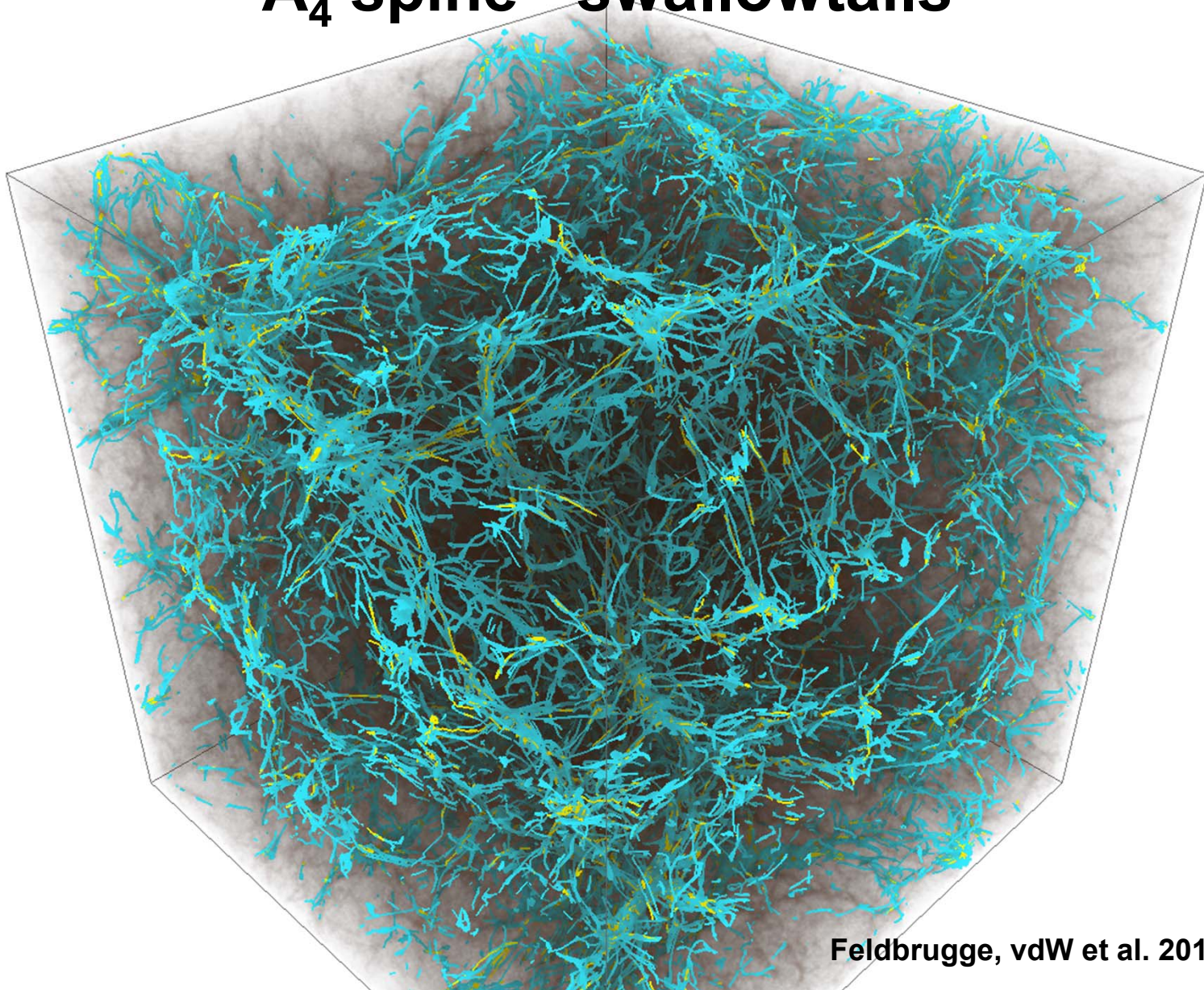


Feldbrugge, vdW et al. 2017b

Skeleton (3D) Cosmic Web: A_3 surfaces - cusps

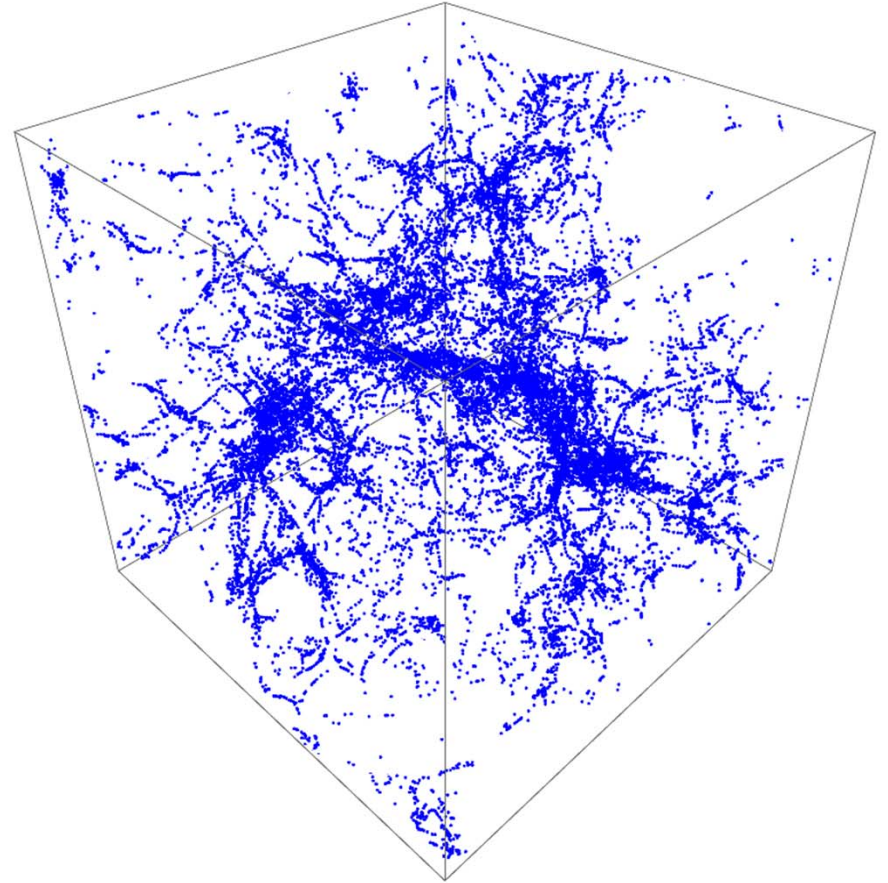
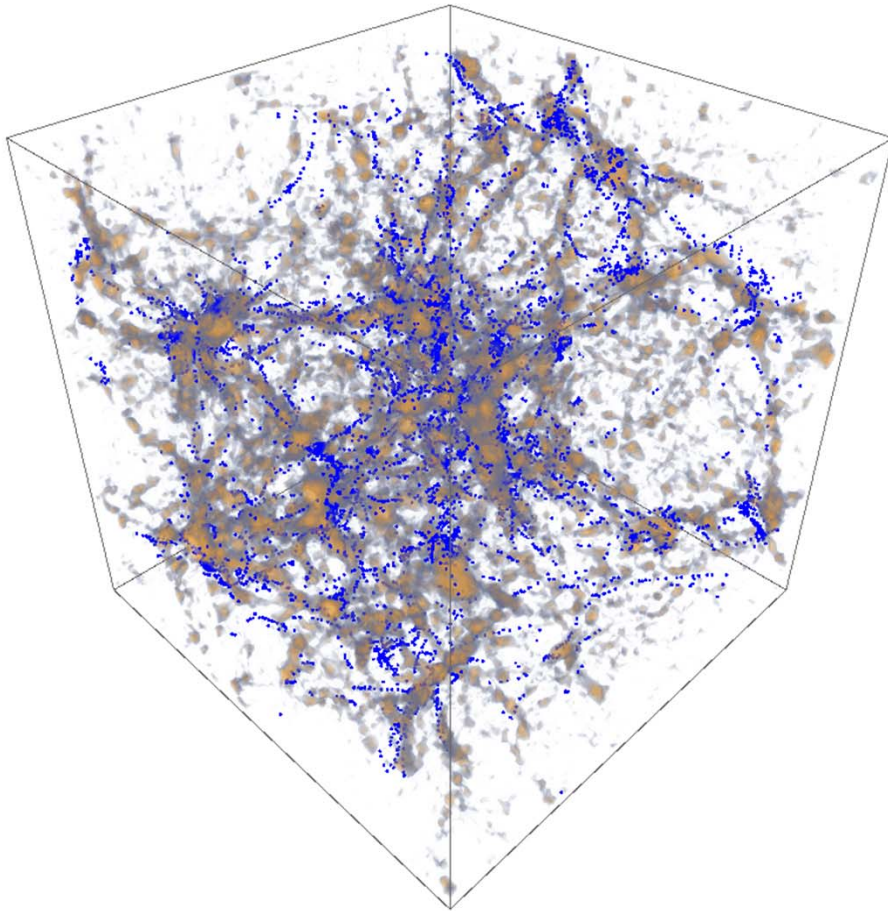


Skeleton (3D) Cosmic Web: A_4 spine - swallowtails

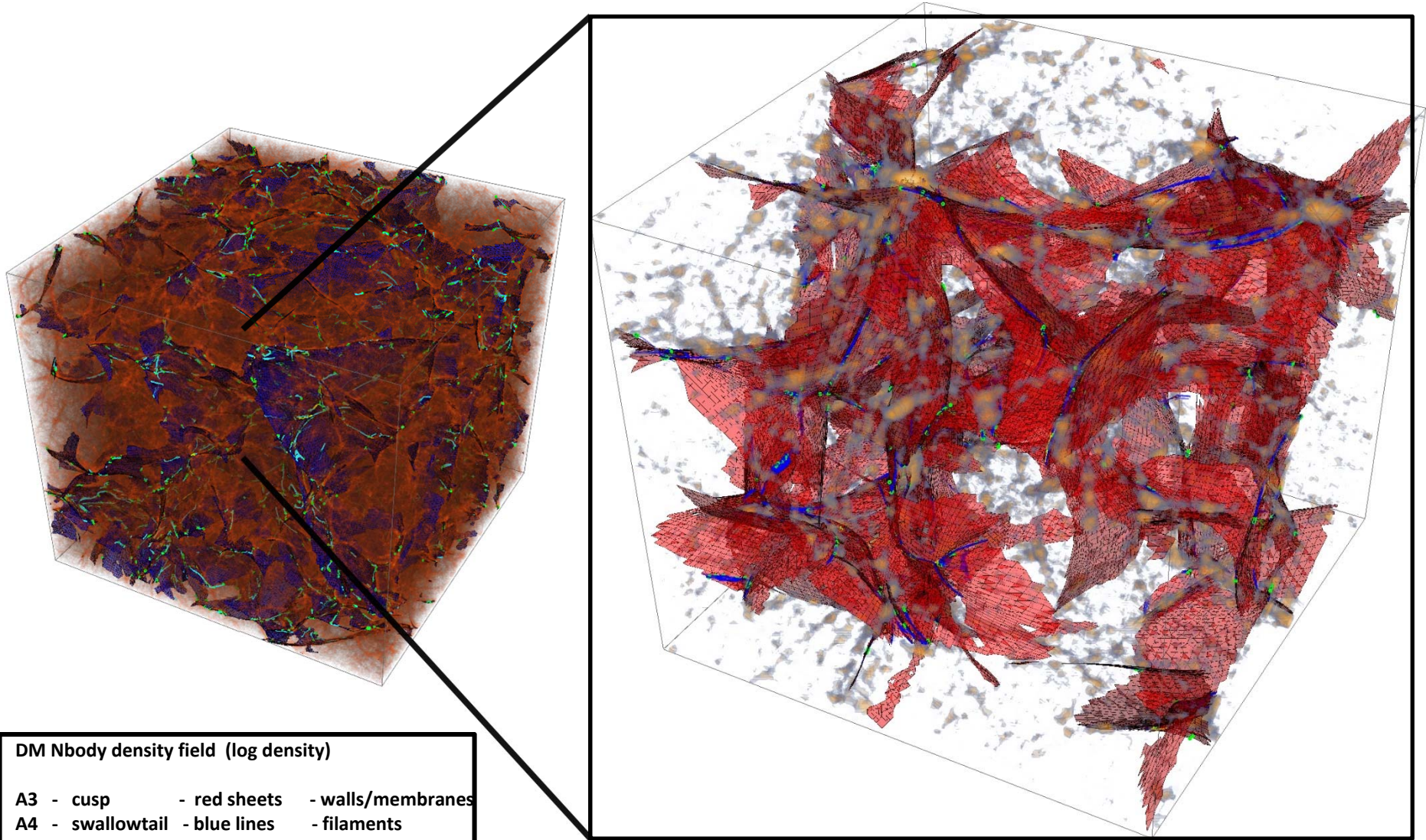


Feldbrugge, vdW et al. 2017b

Skeleton (3D) Cosmic Web: A_4 spine - swallowtails



Skeleton (3D) Cosmic Web: catastrophic connections

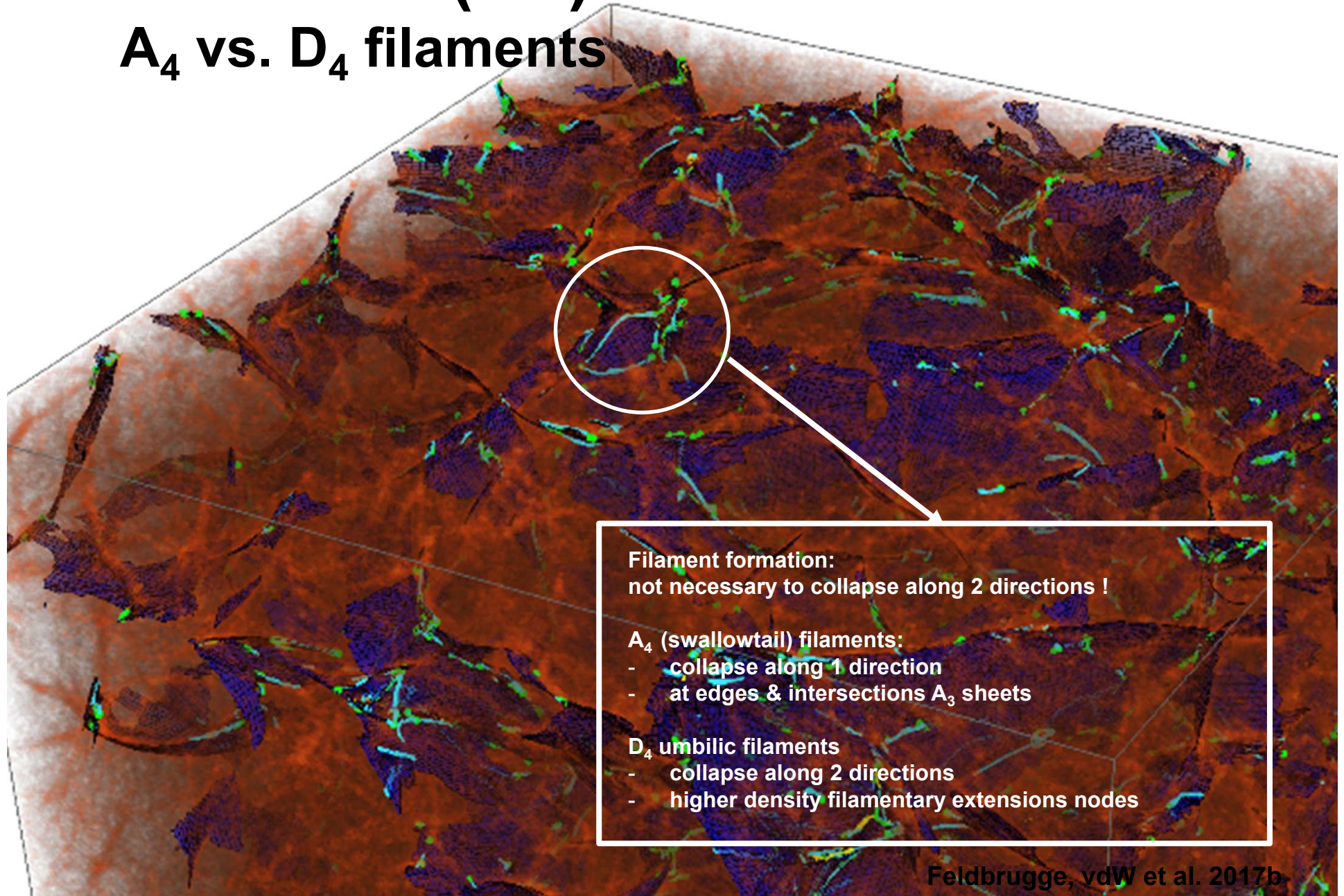




Skeleton (3D) Cosmic Web: catastrophic connections

Singularity class	Singularity name	Feature in the 2D cosmic web	Feature in the 3D cosmic web
A_2	fold	collapsed region	collapsed region
A_3	cuspl	filament	wall or membrane
A_4	swallowtail	cluster or knot	filament
A_5	butterfly	not stable	cluster or knot
D_4	hyperbolic/elliptic	cluster or knot	filament
D_5	parabolic	not stable	cluster or knot

Skeleton (3D) Cosmic Web: A_4 vs. D_4 filaments



Cosmic Web:

(Adhesion)

Local Universe

**Initial
Density & Deformation
Field**

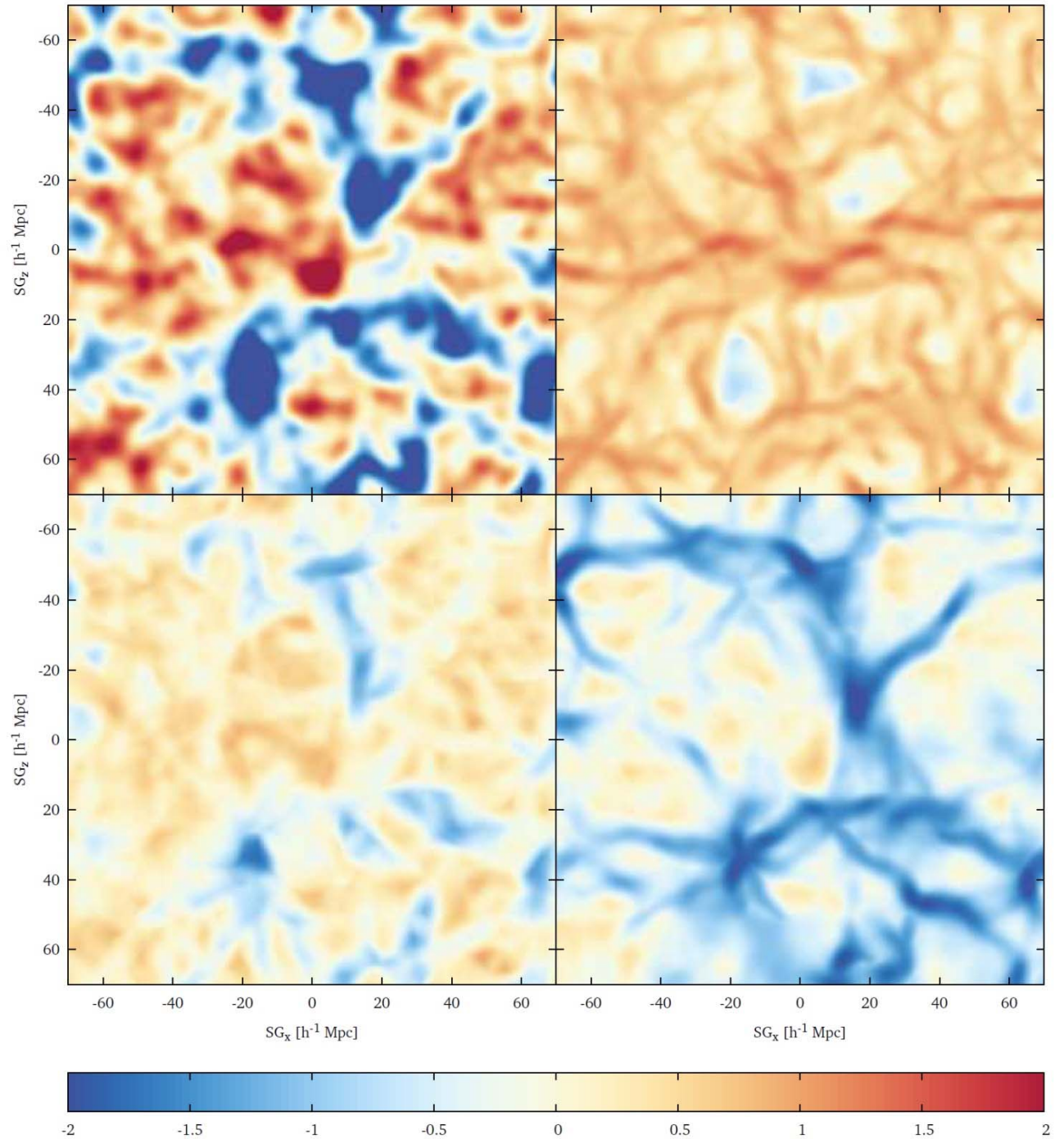
**Local Universe
(SG plane)**

Kitaura & Hess:

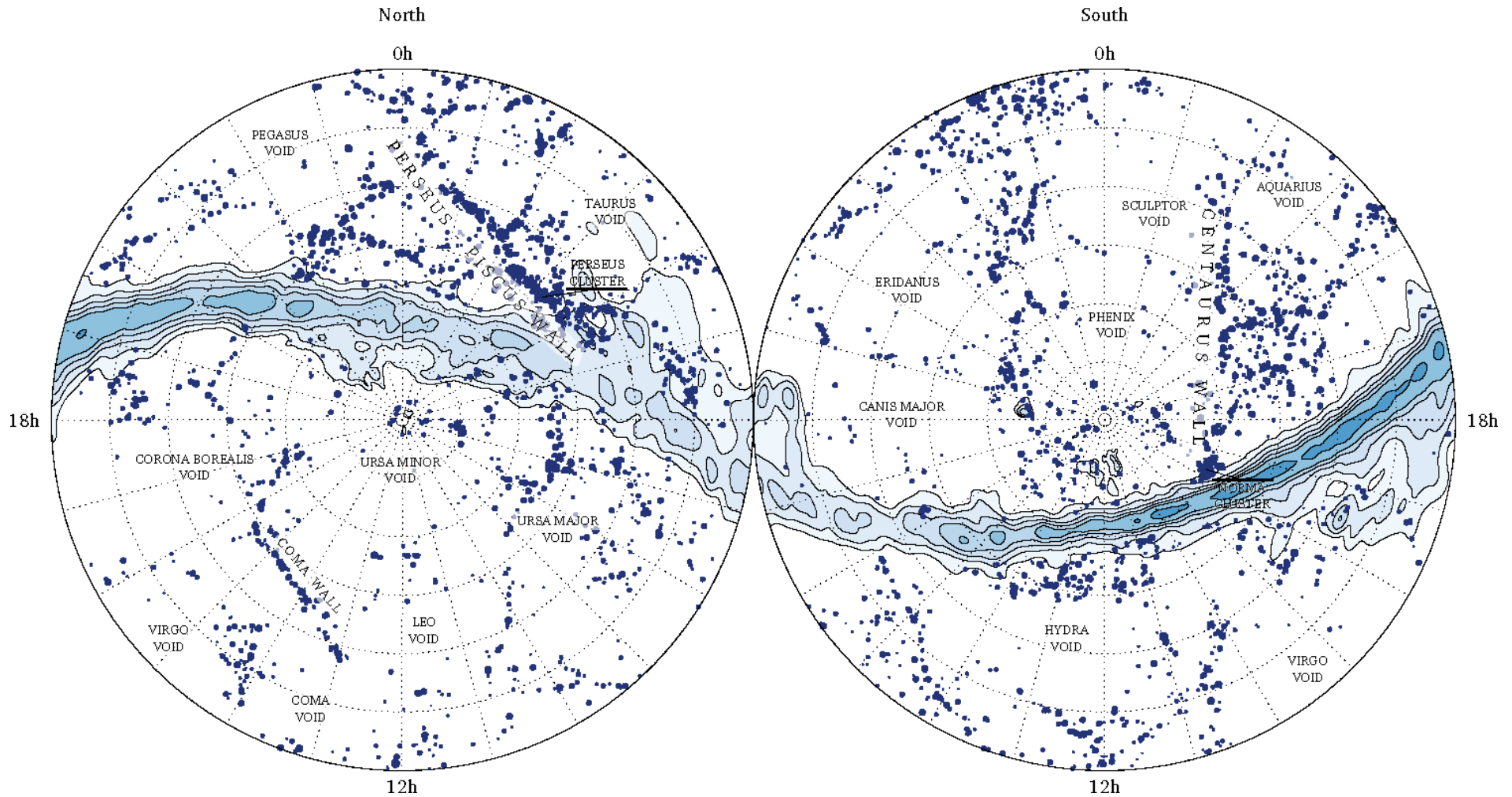
25

2MRS-based

**KIGEN Bayesian Inference
Constrained realizations**



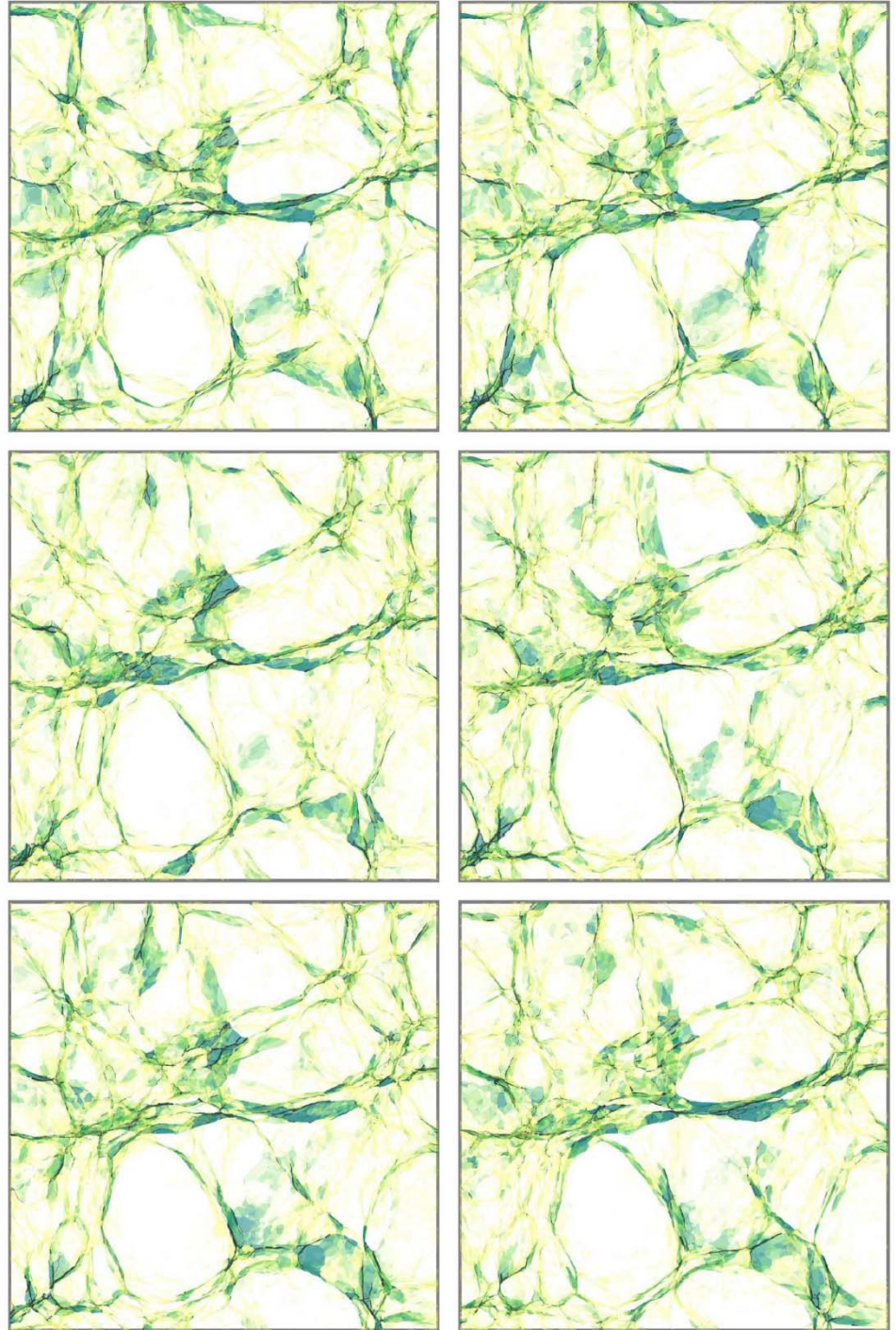
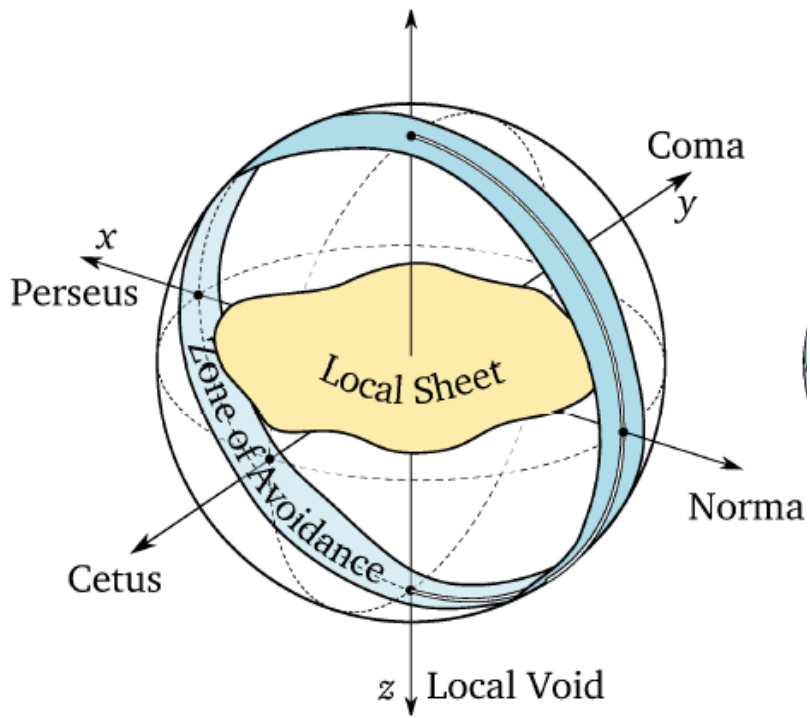
Galaxies up to 50 Mpc ...



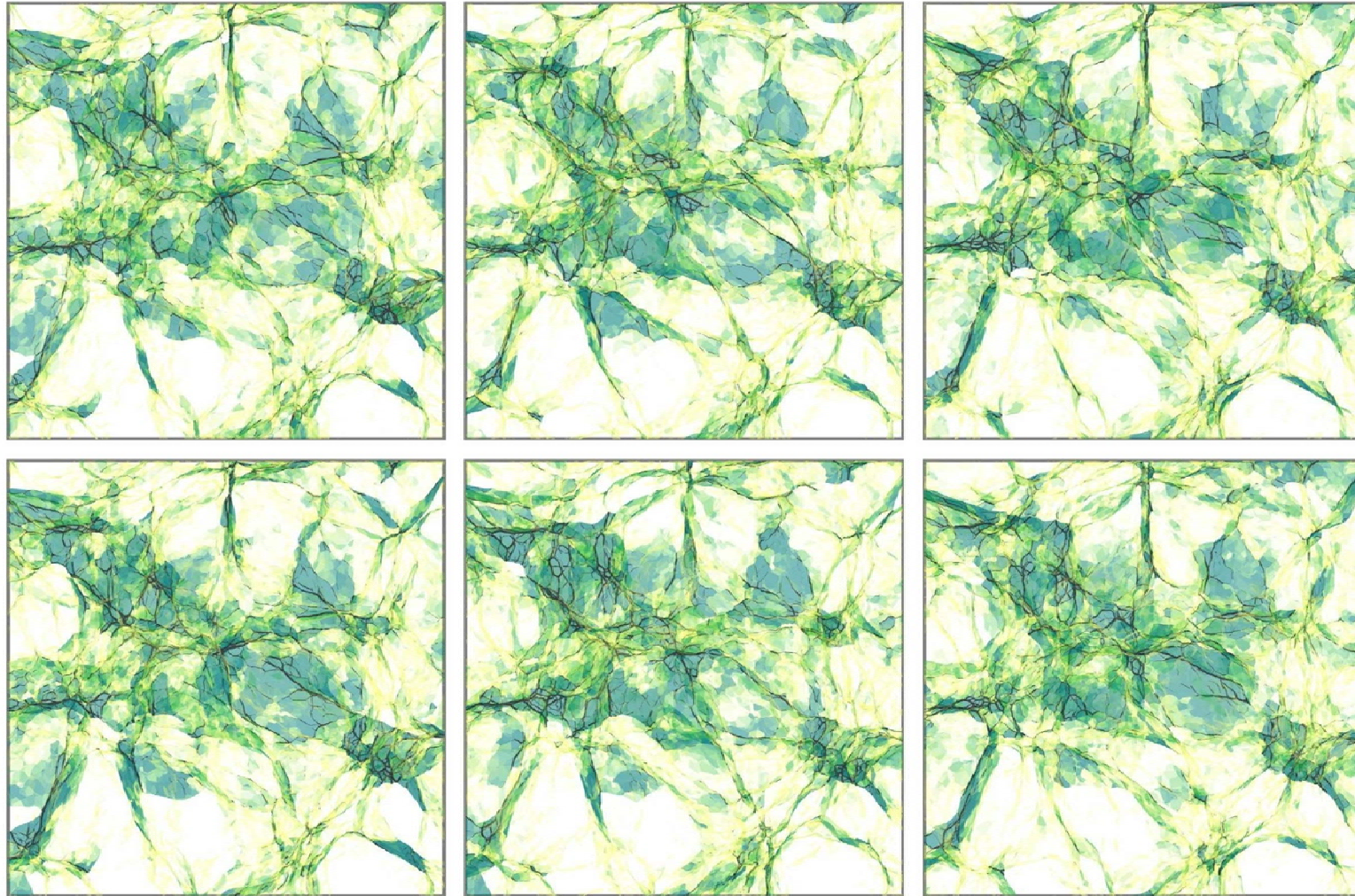
2MRS survey sky map: Hidding 2015

Edge-on view Supergalactic Plane:

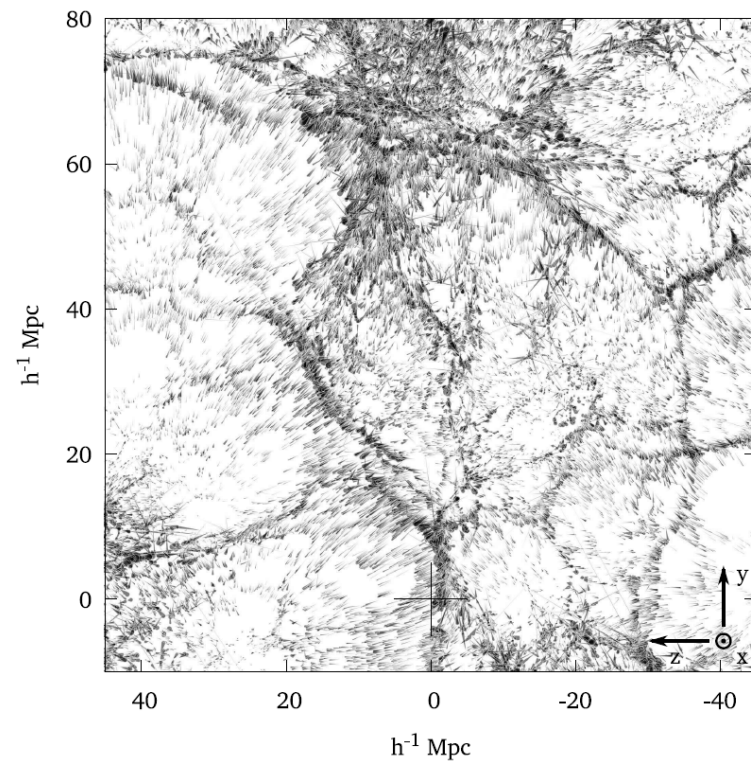
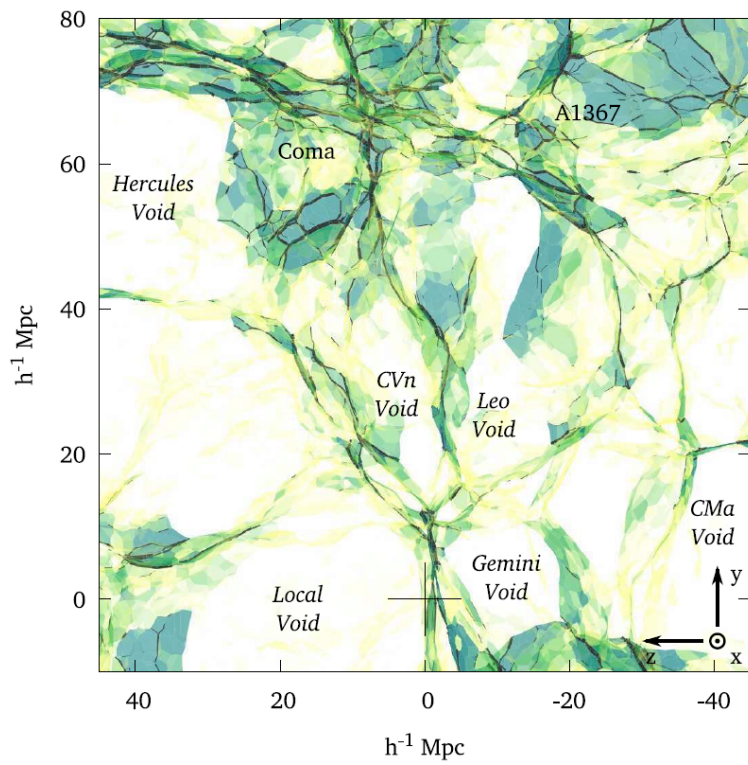
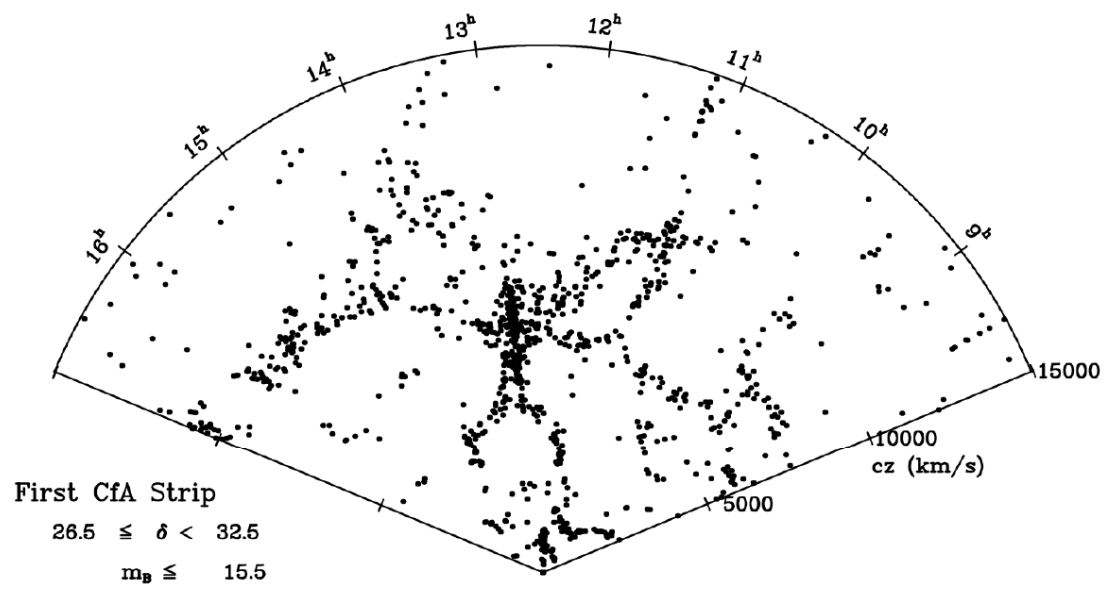
6 constrained adhesion reconstructions



Face-On Supergalactic Plane

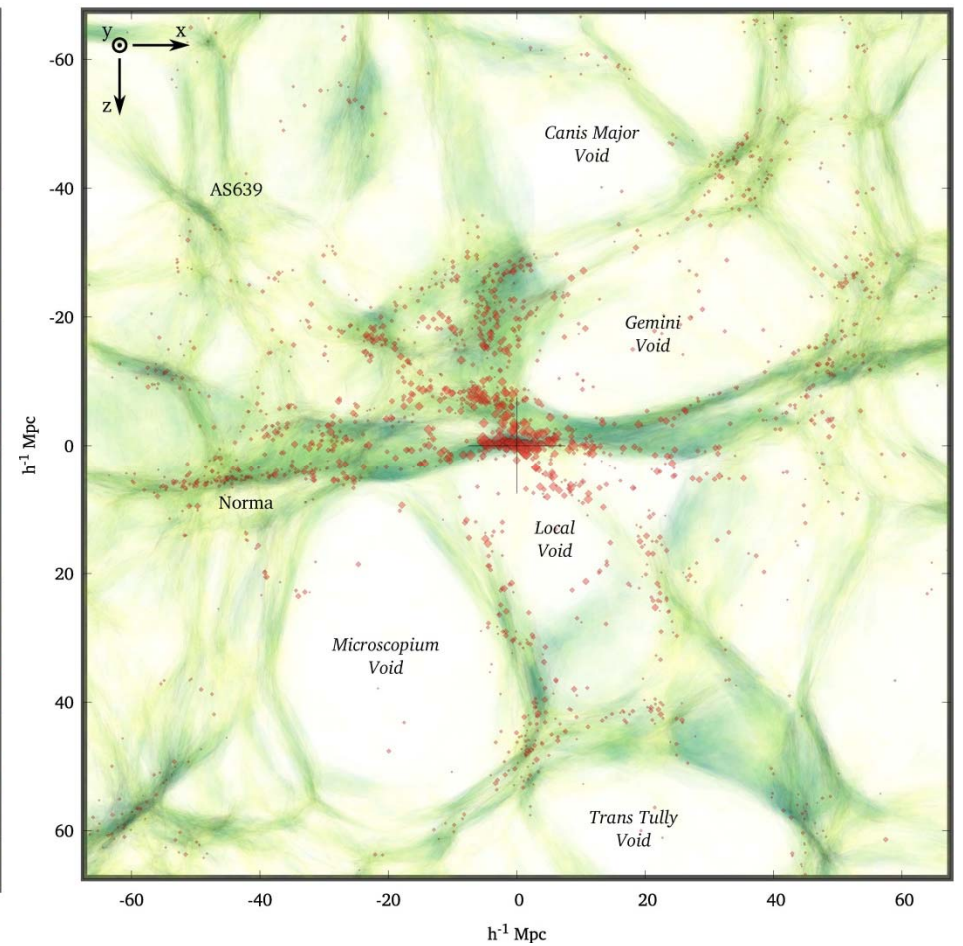
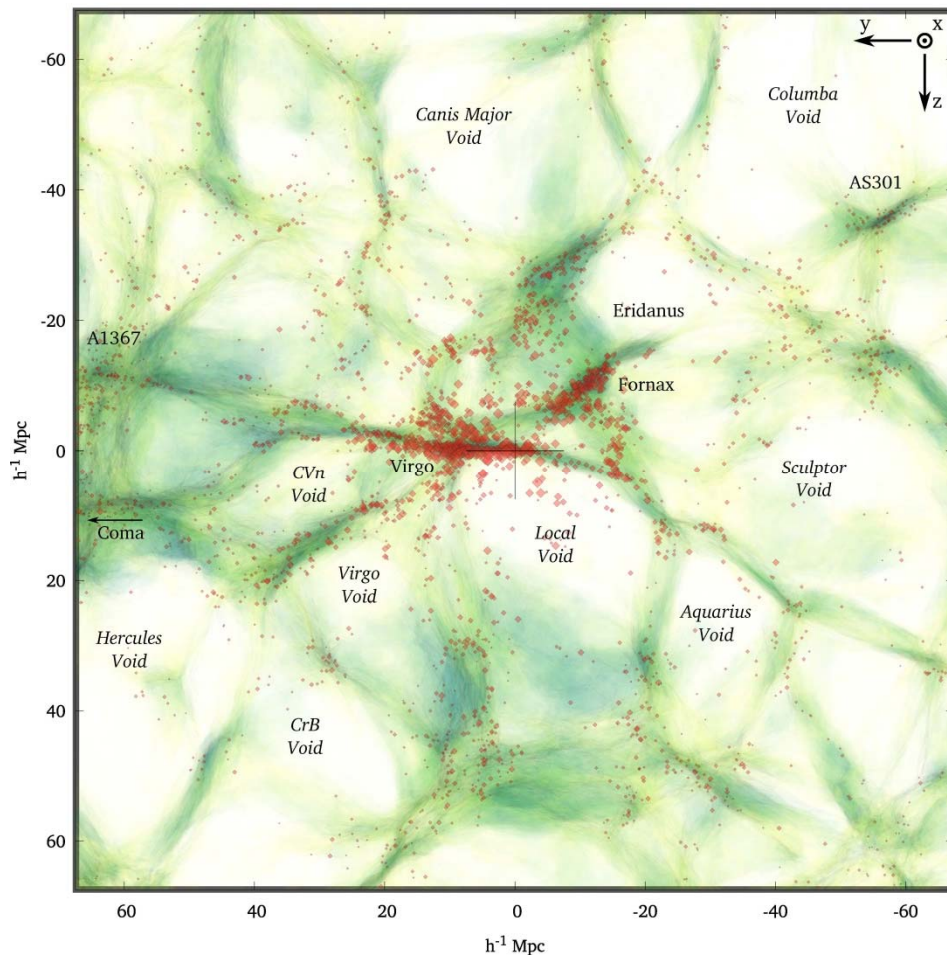


6 constrained adhesion reconstructions



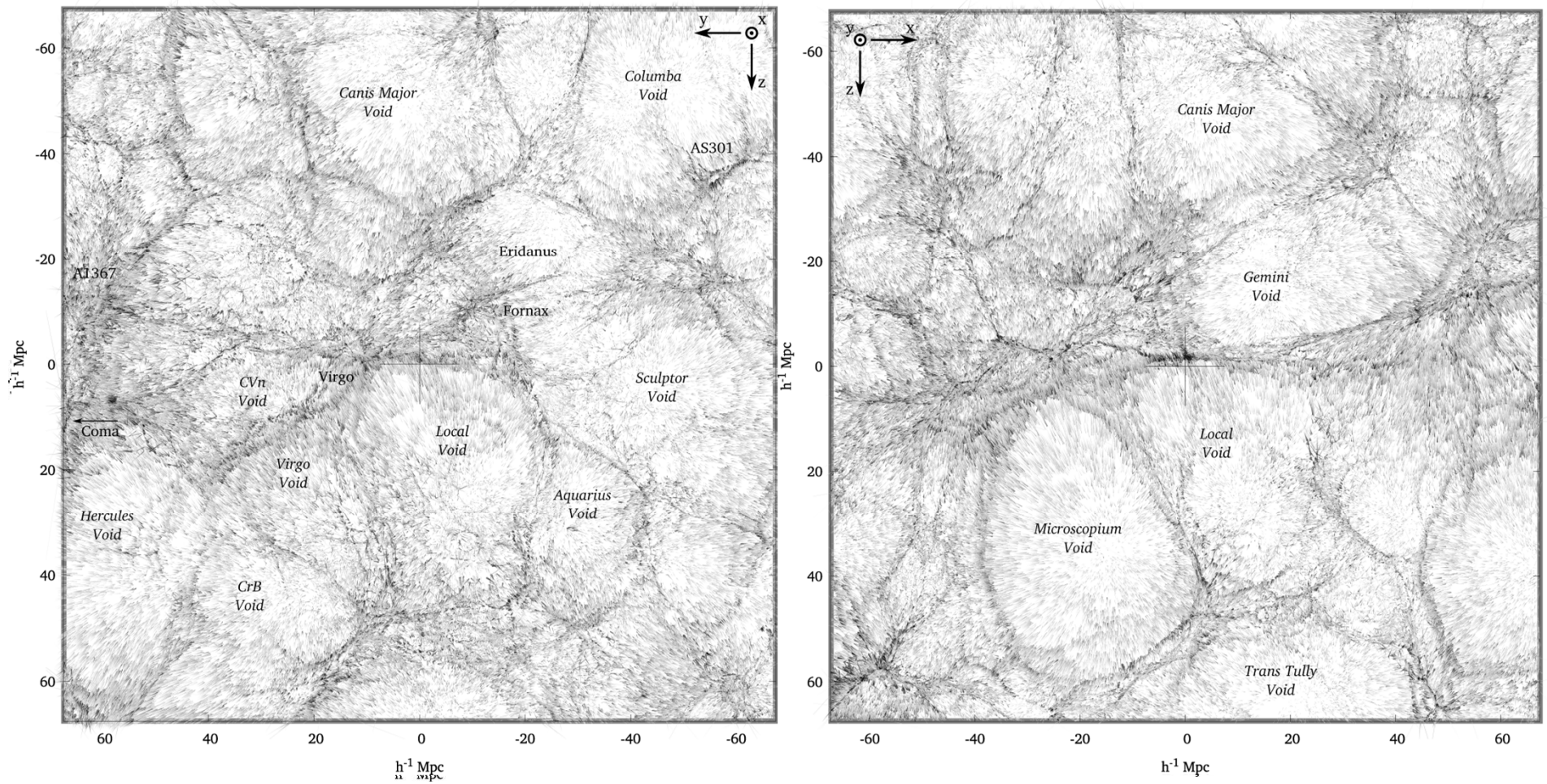
Supergalactic Plane

mean field: edge-on



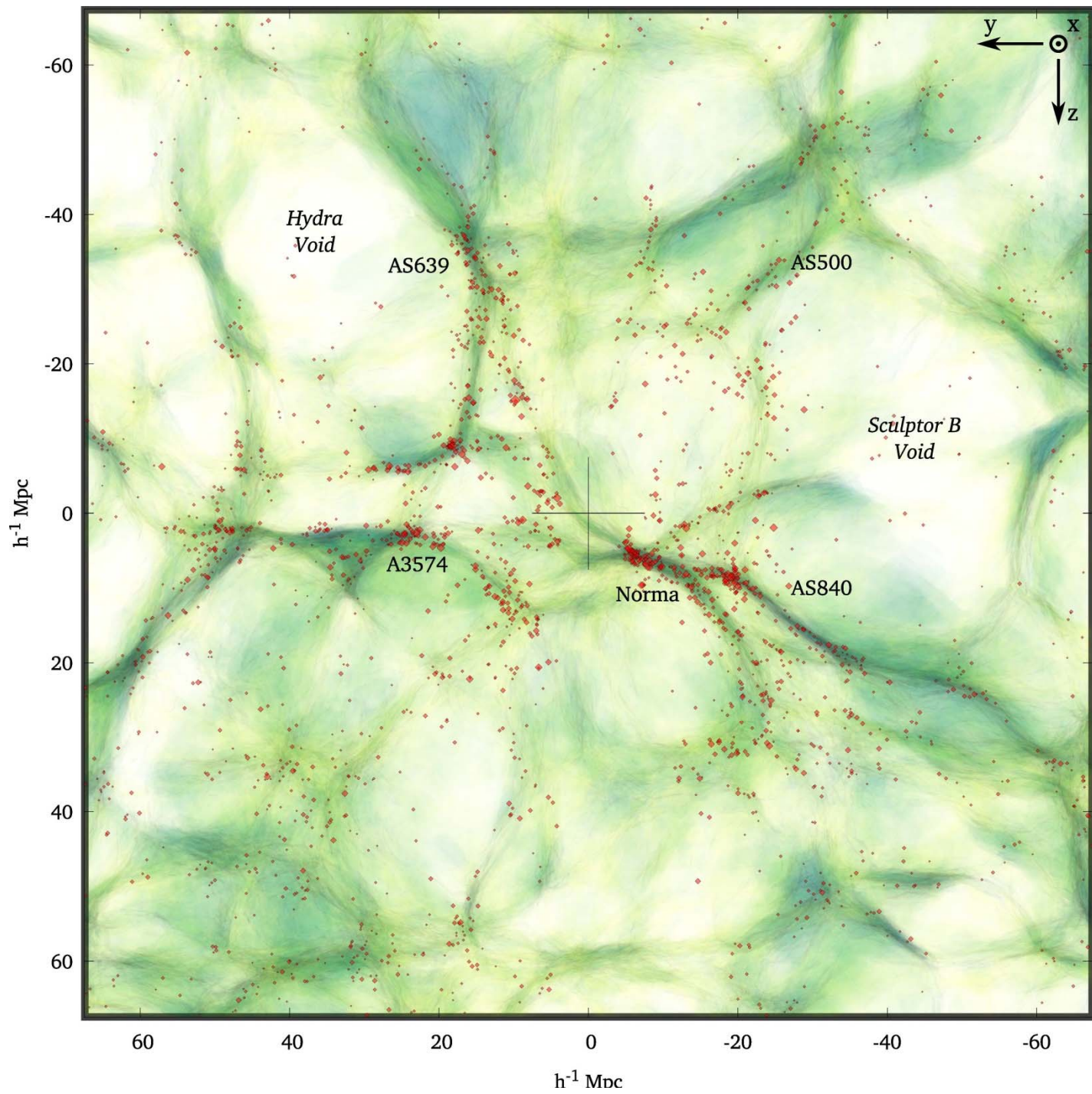
Supergalactic Plane

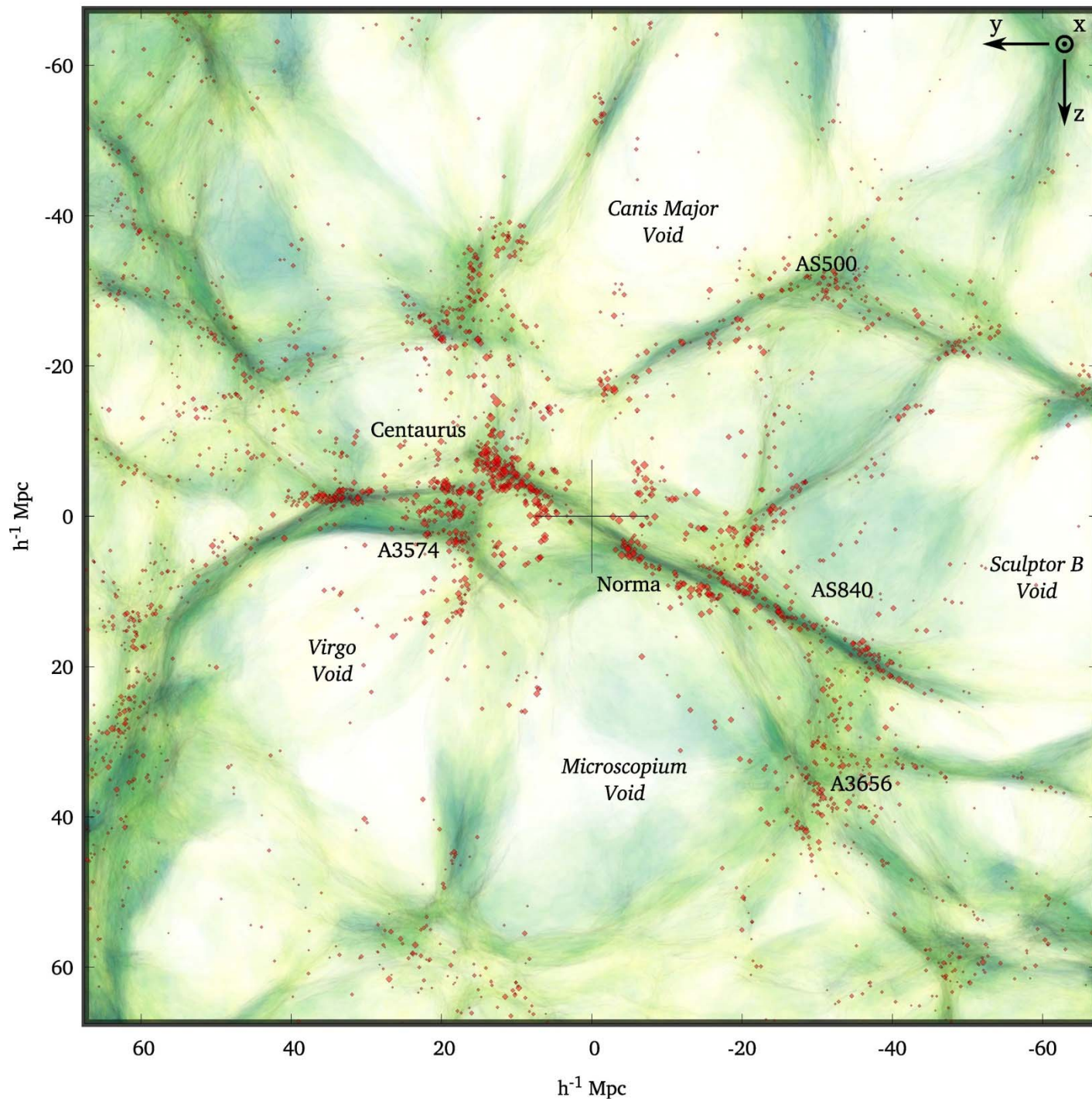
mean field: edge-on

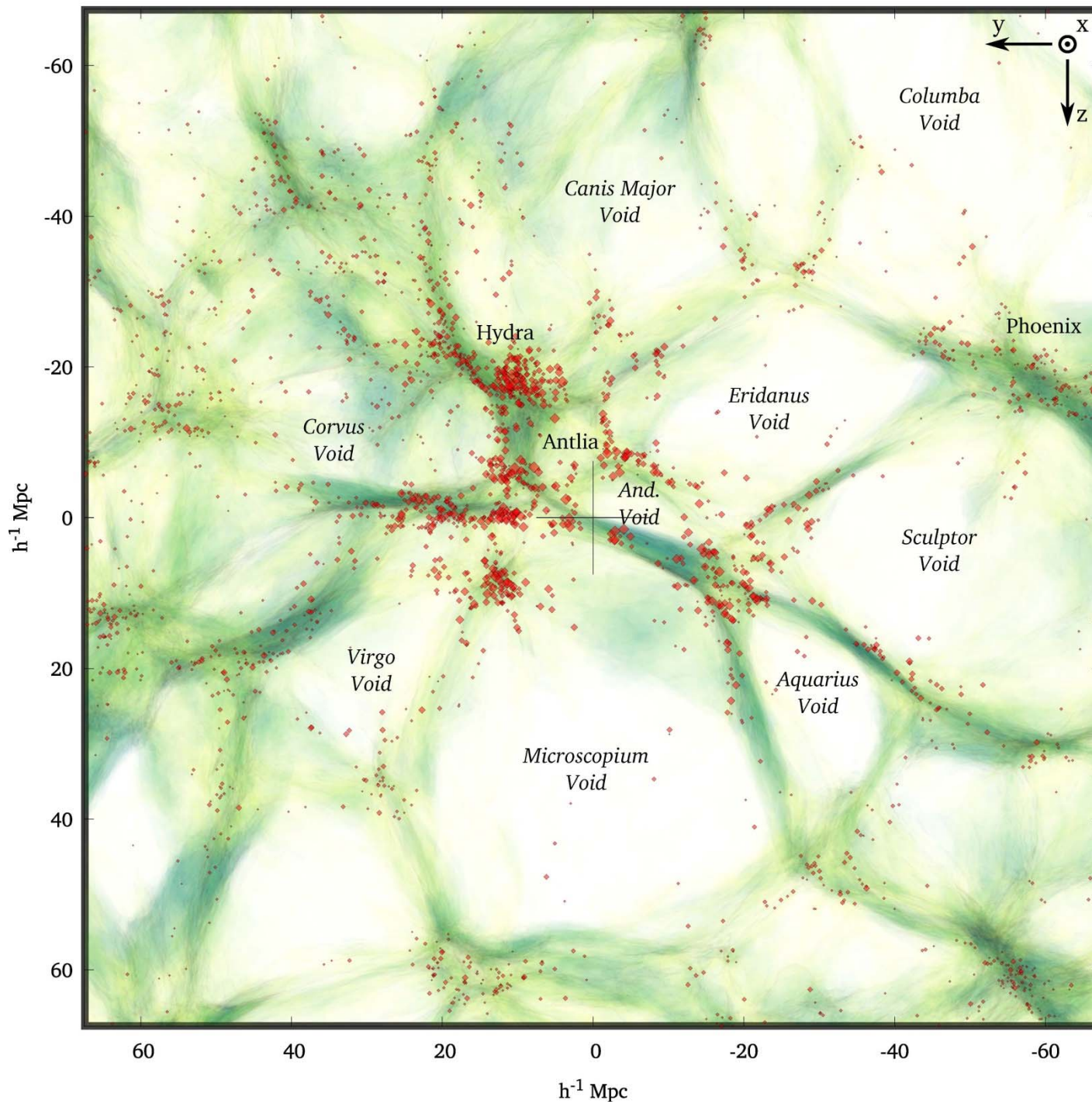


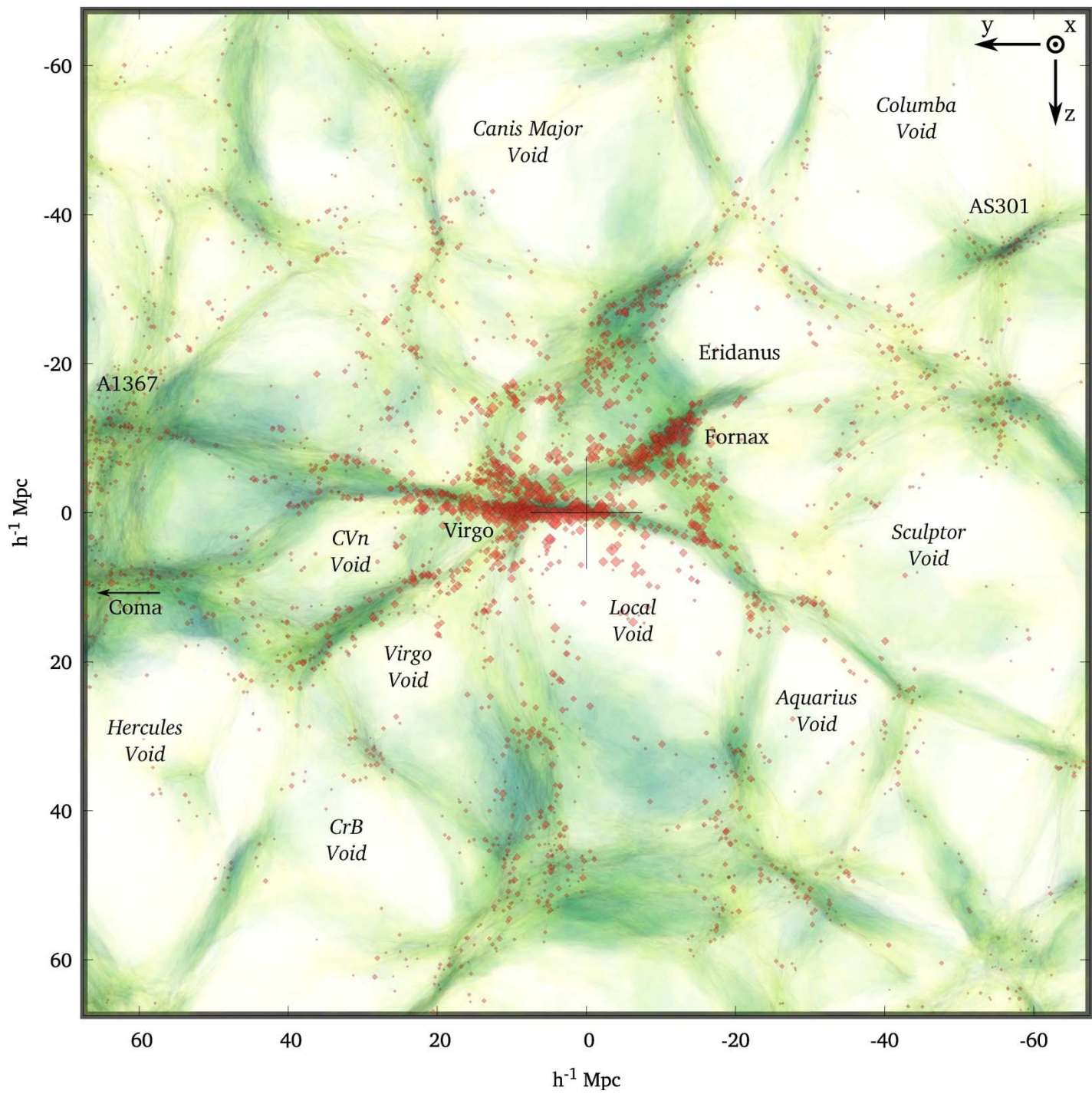
Local Cosmic Web:

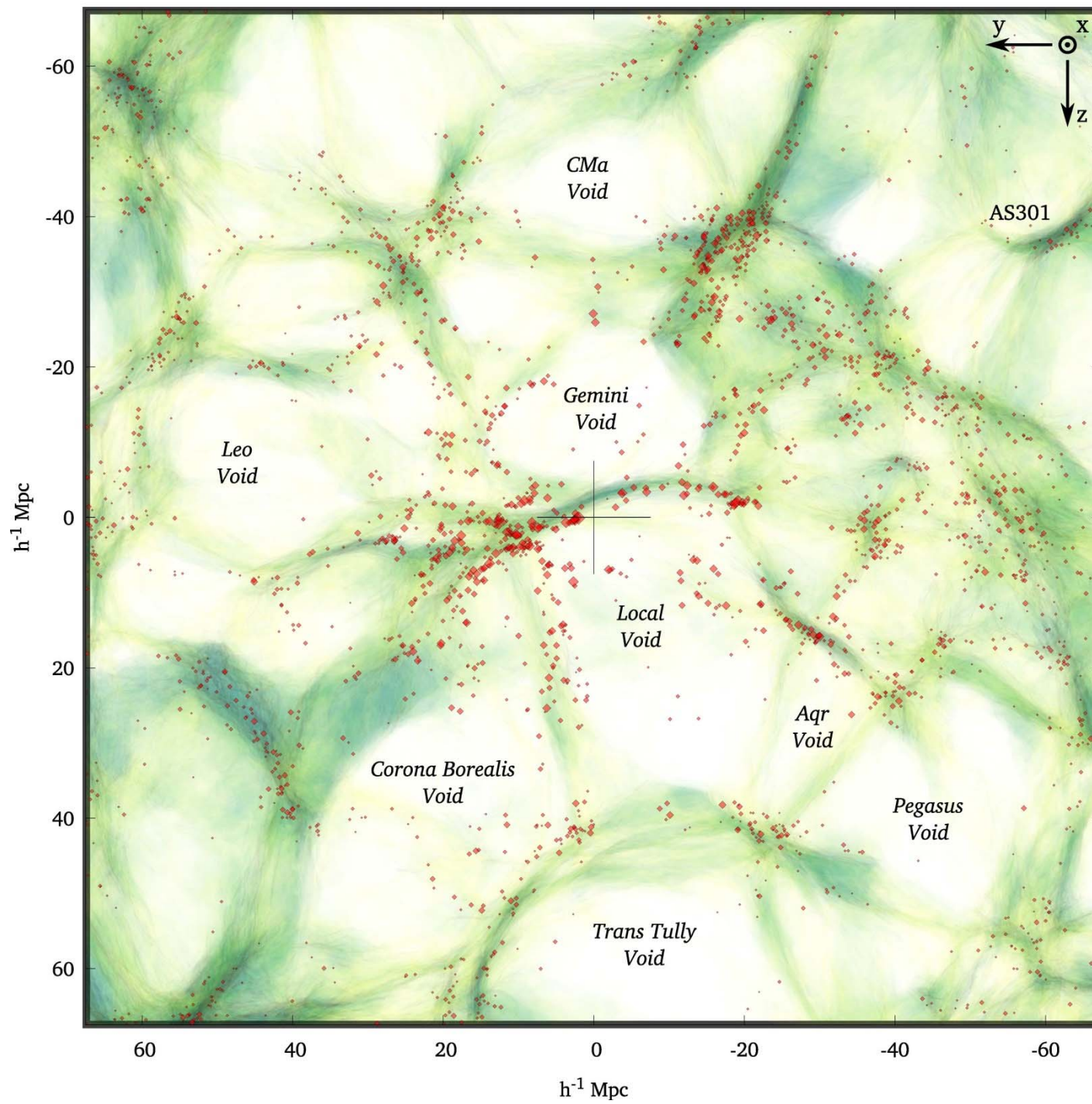
a rough CT-scan

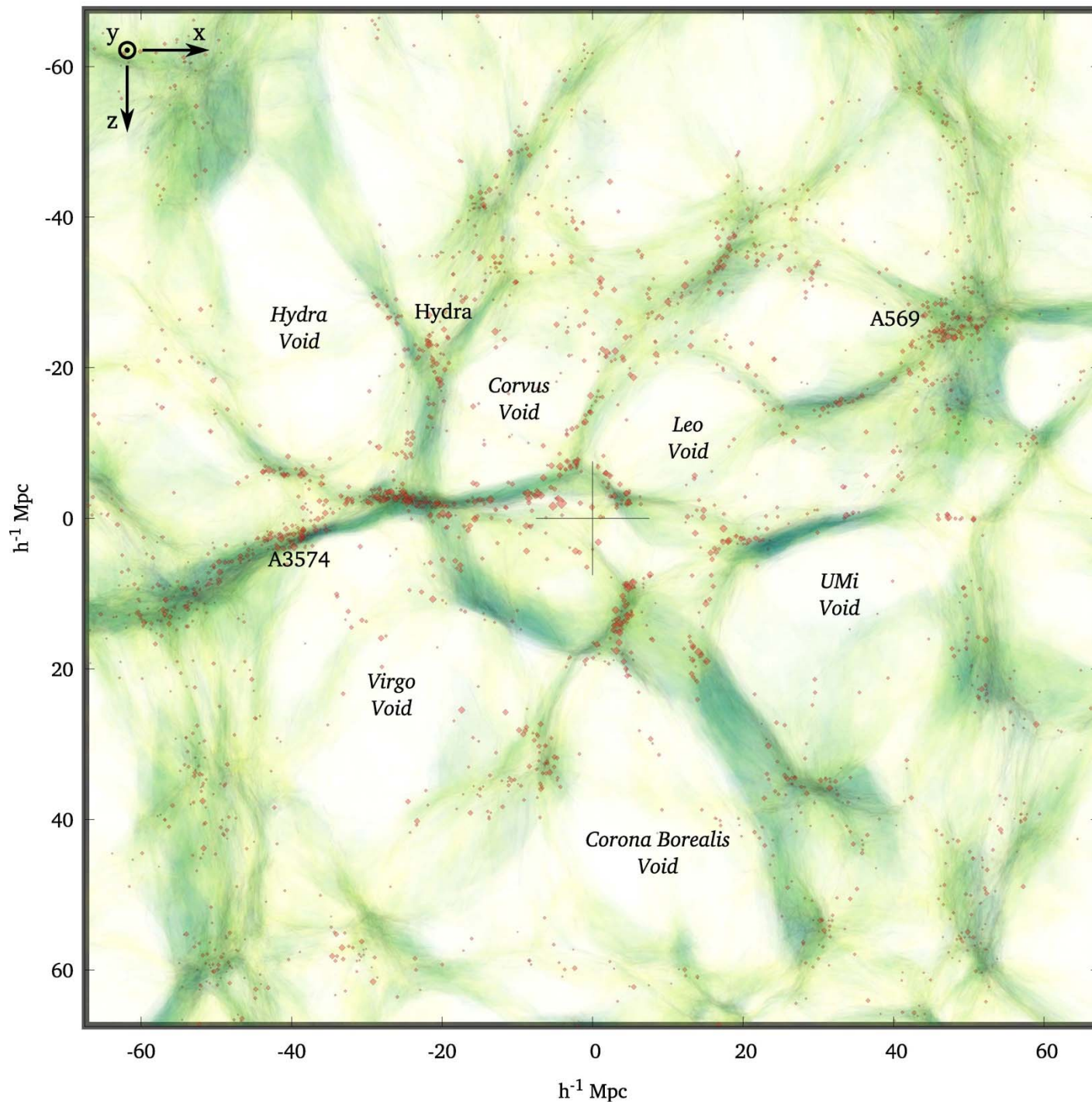


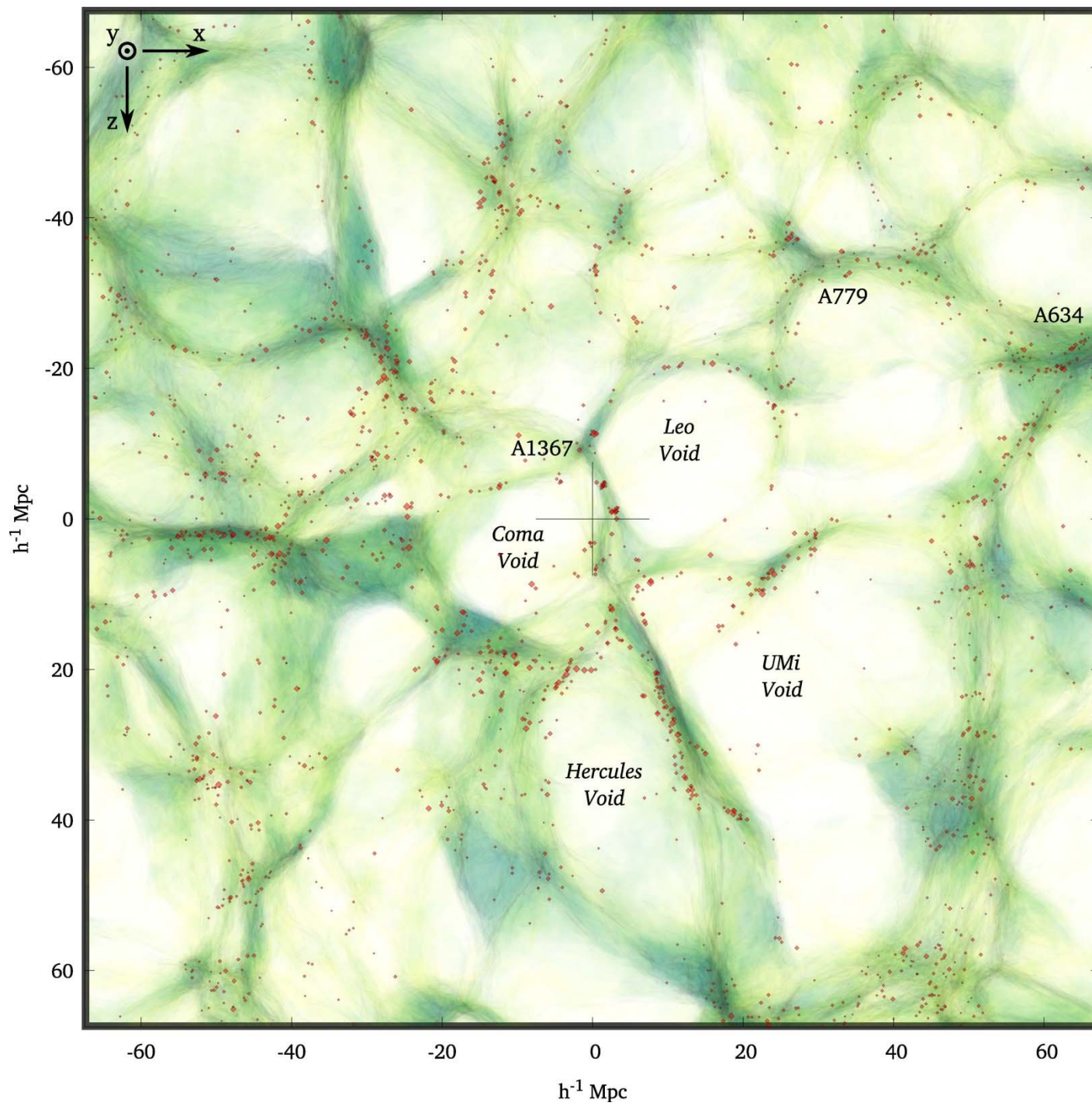








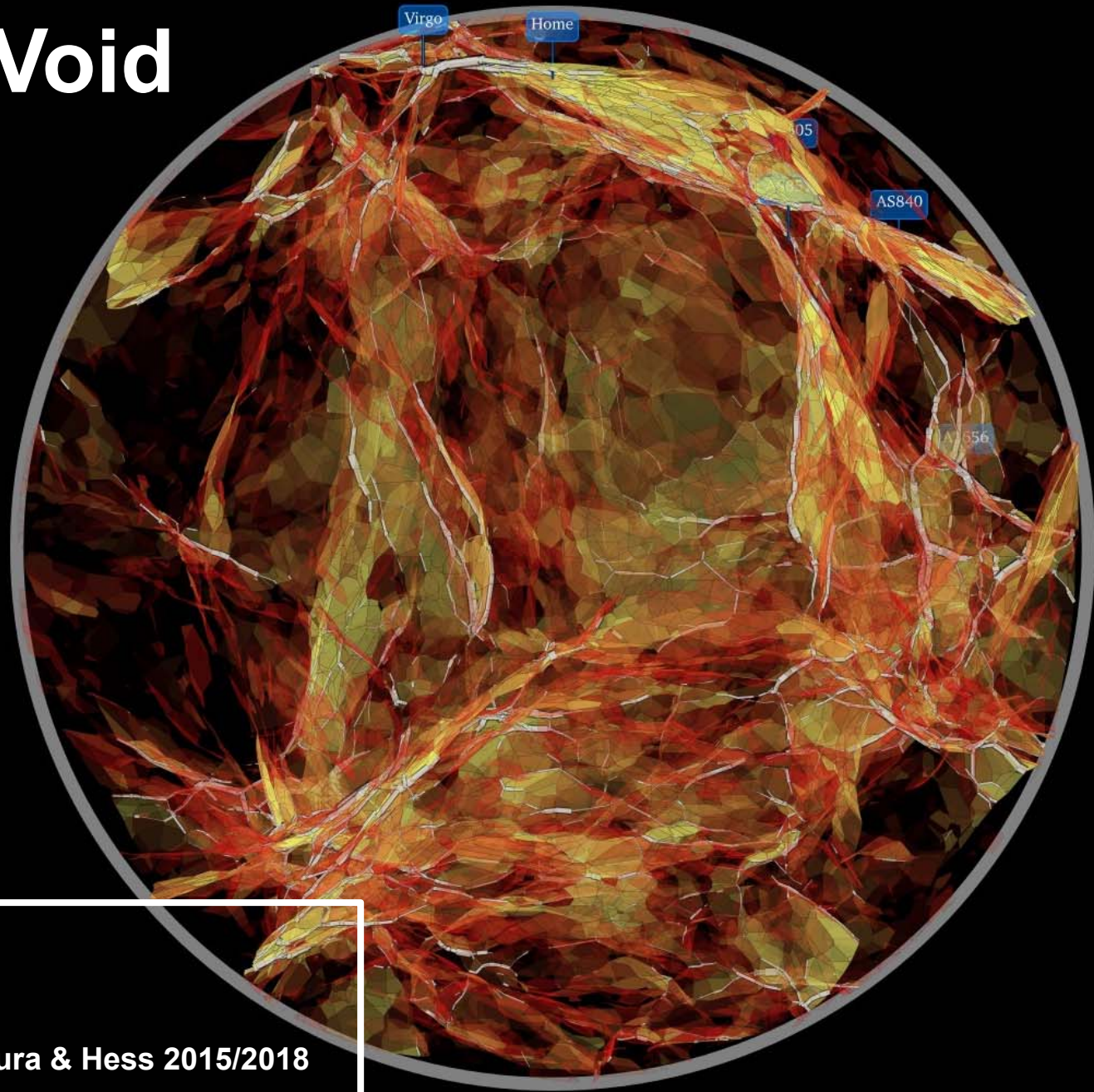




Local Cosmic Web:

the Local Void

Local Void



Local Void

Reconstruction:
Hidding, vdW, Kitaura & Hess 2015/2018

Cosmic Web Summary

- Cosmic Web unique probe of structure formation at transition linear to nonlinear stage.
- Structural and Dynamical analysis of the Cosmic Web poses strong challenges due to complex pattern and multiscale nature.
- Nexus/MMF formalism allows study of the evolving multiscale structure of the Cosmic Web.
- Interplay between morphological elements of filaments, walls, cluster nodes and voids.
- Dynamically cluster nodes dominant, structurally (mass, halo content) the filaments.
- Adhesion formalism highly suited for following the dynamical evolution of the weblike structure.
- Adhesion formalism & tessellation-based solution allow investigation of cosmological sensitivity of the cosmic web.

continued: part 2

Flows & Voids