

# Mock galaxy catalogs with perturbation theory



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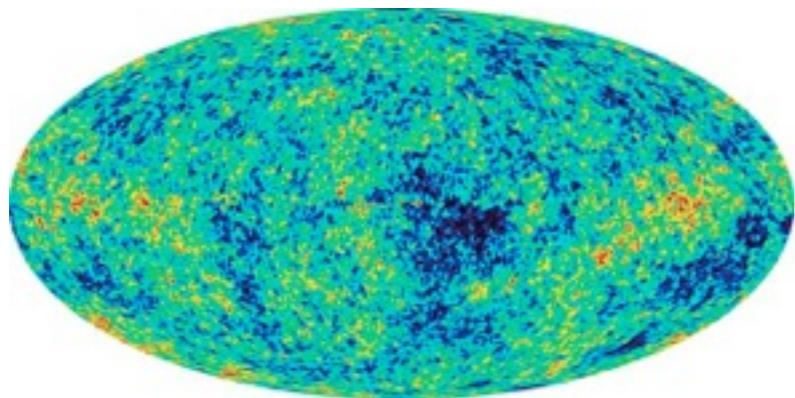
Anatoly Klypin

How can we generate a mock galaxy catalog for present  
large-scale structure surveys?

(BOSS,J-PAS,DESI,EUCLID,4MOST,WEAVE,DES,...)

# The ingredients

I) We start from the primordial fluctuations



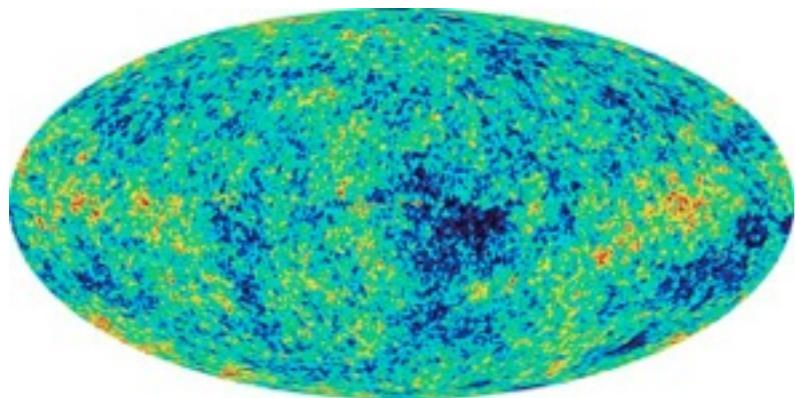
WMAP ~300 000 years after the Big Bang

Planck  $-8.9 < f_{NL} < 14.3$  (2 sigma)  
(Suyama et al., 2013)

# The ingredients

- I) We start from the primordial fluctuations
  - i) Gaussian
  - ii) or non-Gaussian

Scoccimarro, Hui, Manera, Chang Chang 2012



WMAP ~300 000 years after the Big Bang

Planck  $-8.9 < f_{NL} < 14.3$  (2 sigma)  
(Suyama et al., 2013)

## 2) We simulate structure formation

Why not simulate everything?

Full gravity and hydrodynamical solver in an expanding background



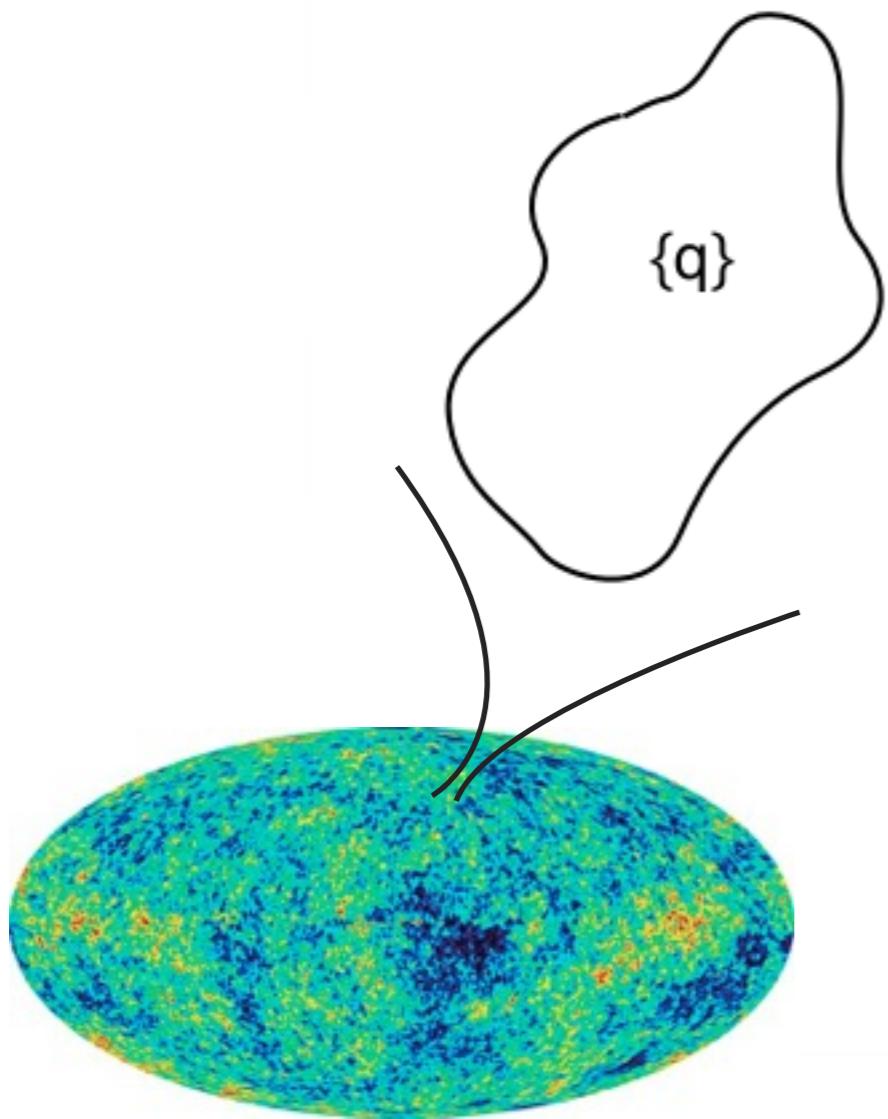
Vogelsberger et al 2014

about  $(70 \text{ Mpc}/\text{h})^3$  !! too small volumes for our purposes!!

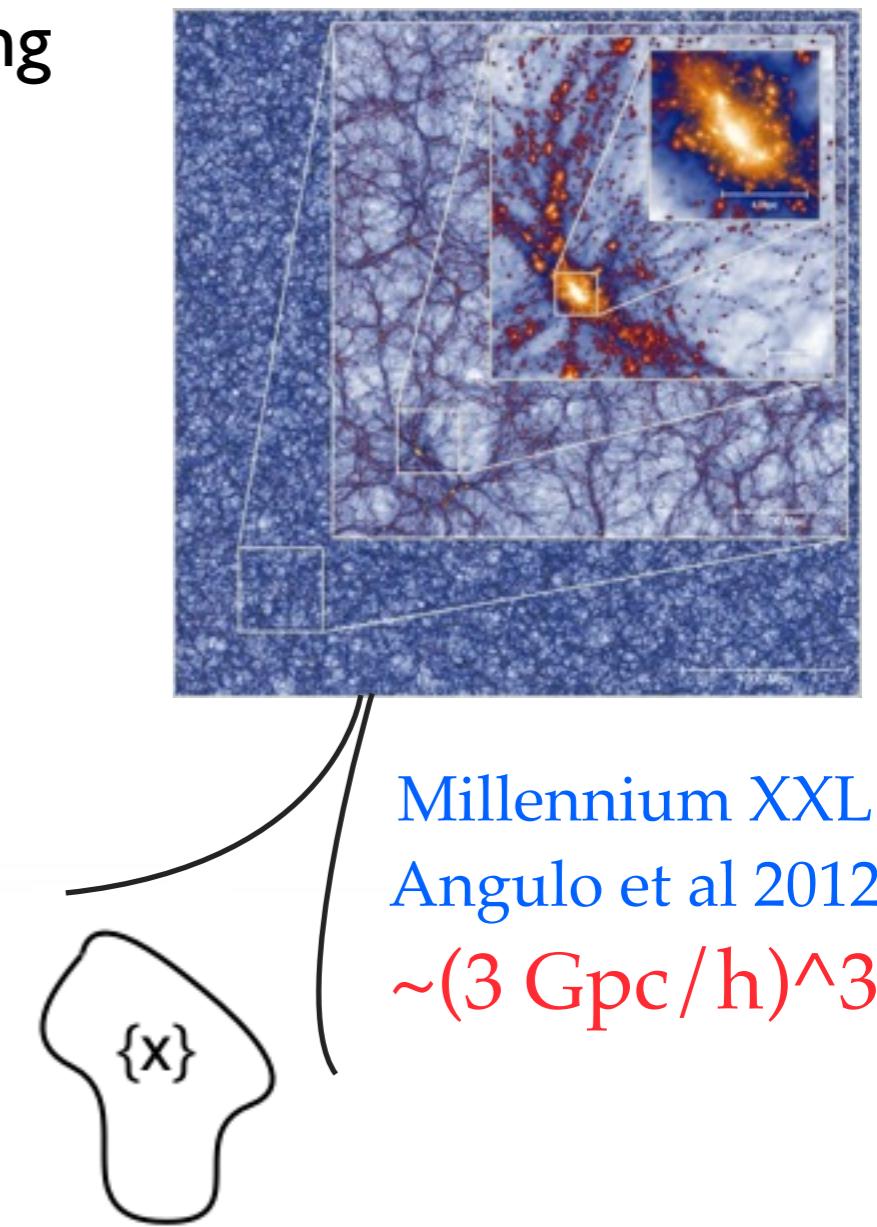
## 2) We simulate structure formation

Full gravity solver dark matter only in an expanding background, solution to the Vlasov equations  
Monte Carlo approach: N-body code

Lagrangian coordinates



Displacement field  
 $\Psi(q)$



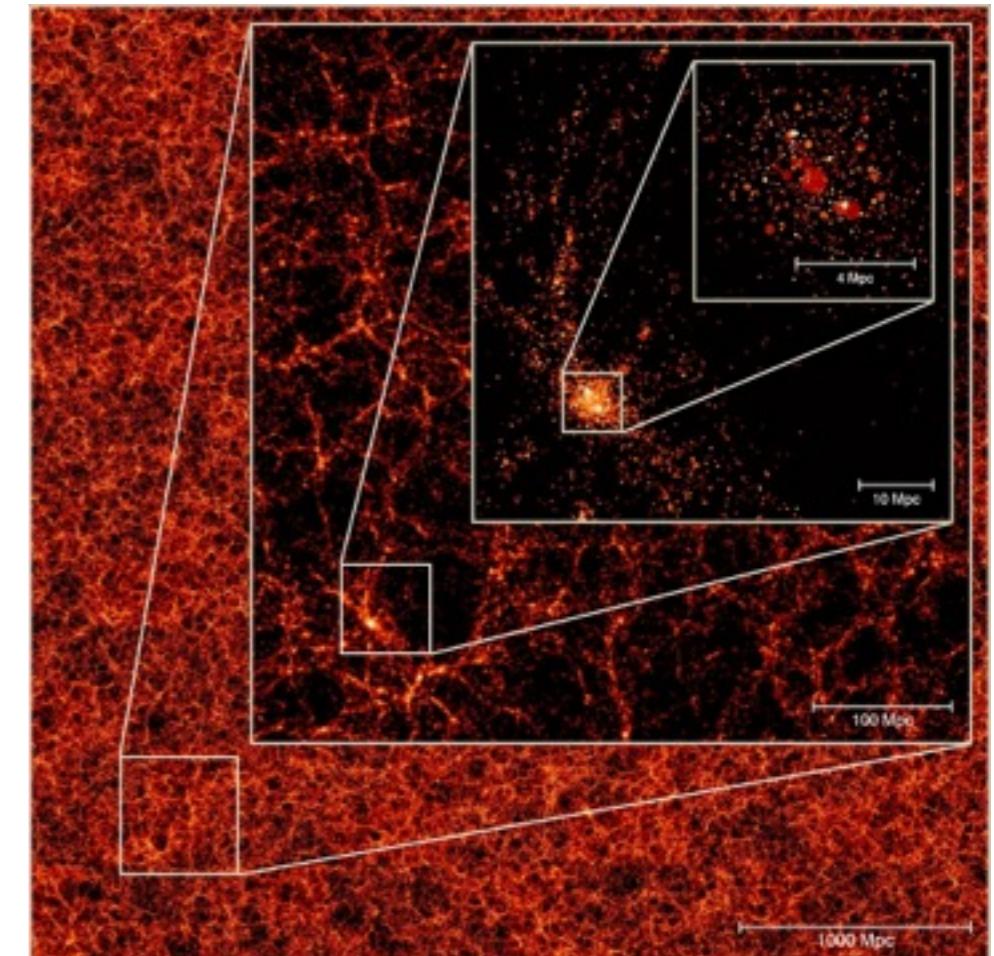
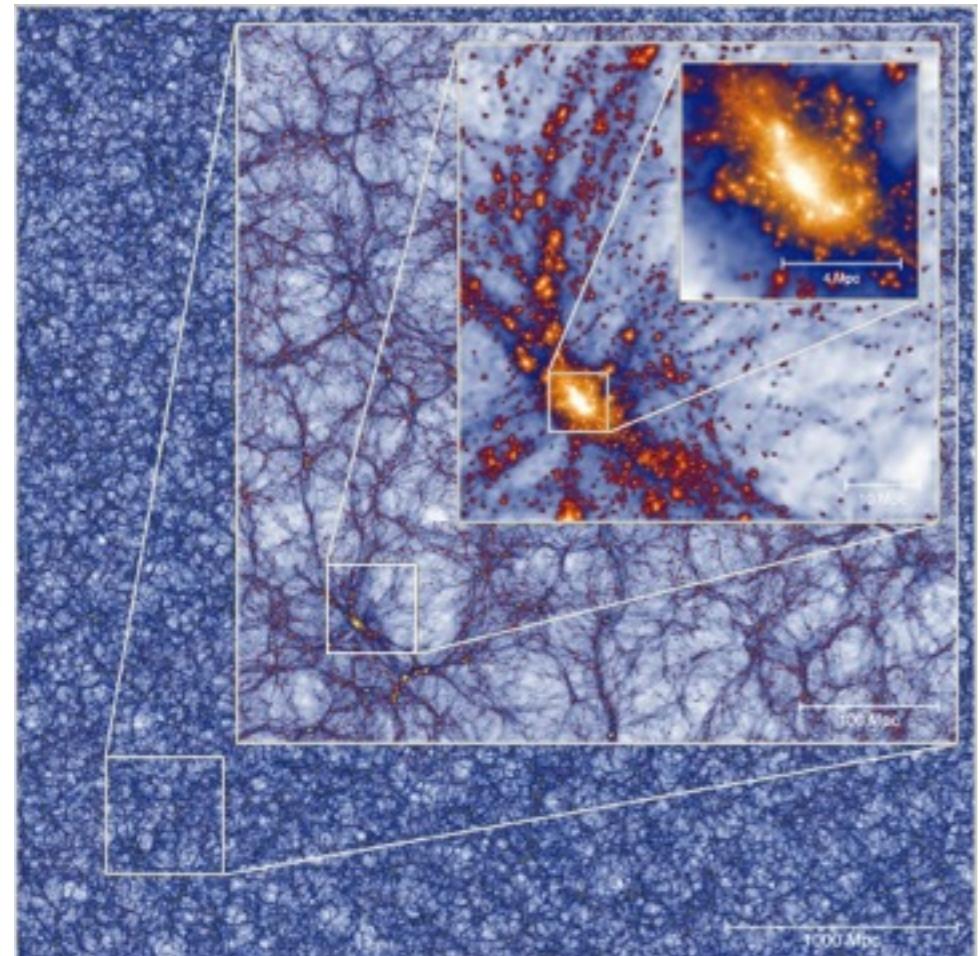
Eulerian coordinates

$\sim 13.7$  billion years after the Big Bang

WMAP

### 3) We run a halo finder

Knebe et al. 2011



Millennium XXL  
Angulo et al 2012

## 4) We produce a galaxy catalog based on either:

- **semi-analytic model**

Cole 2000; Haton 2003; Croton 2006; Bower 2006;  
Monaco 2007; Benson 2010; deLucia & Blaizot 2007; Baugh 2006

- **halo occupation distribution**

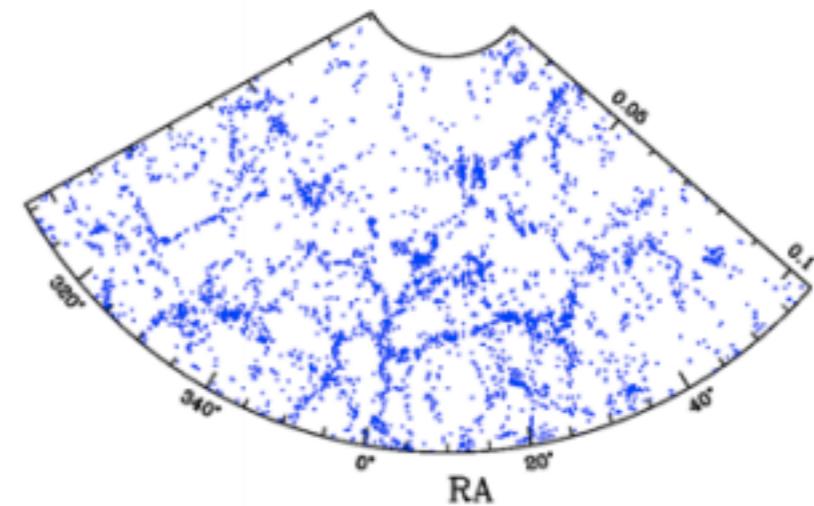
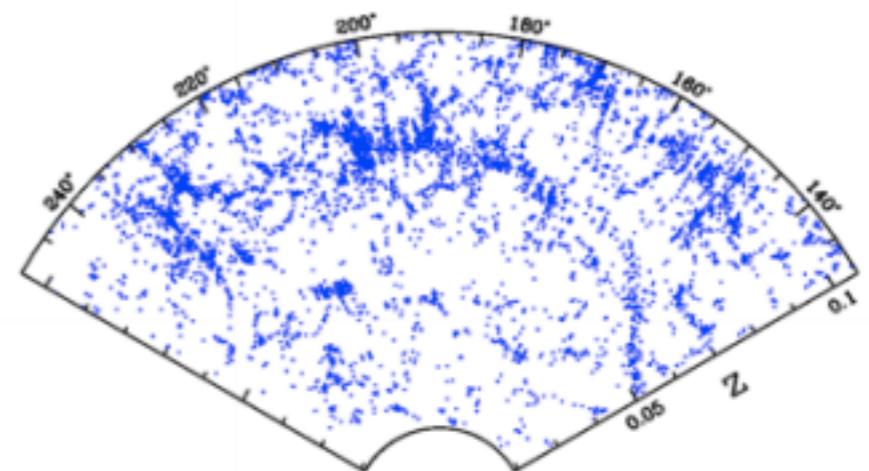
Berlind & Weinberg 2002; Zheng 2005; Zehavi et al 2011

- **abundance matching**

Kratsov 04, Tasitsiomi 04, Vale&Ostriker04, Conroy 06,  
Behroozi10, Trujillo-Gomez 11, Nuza 12

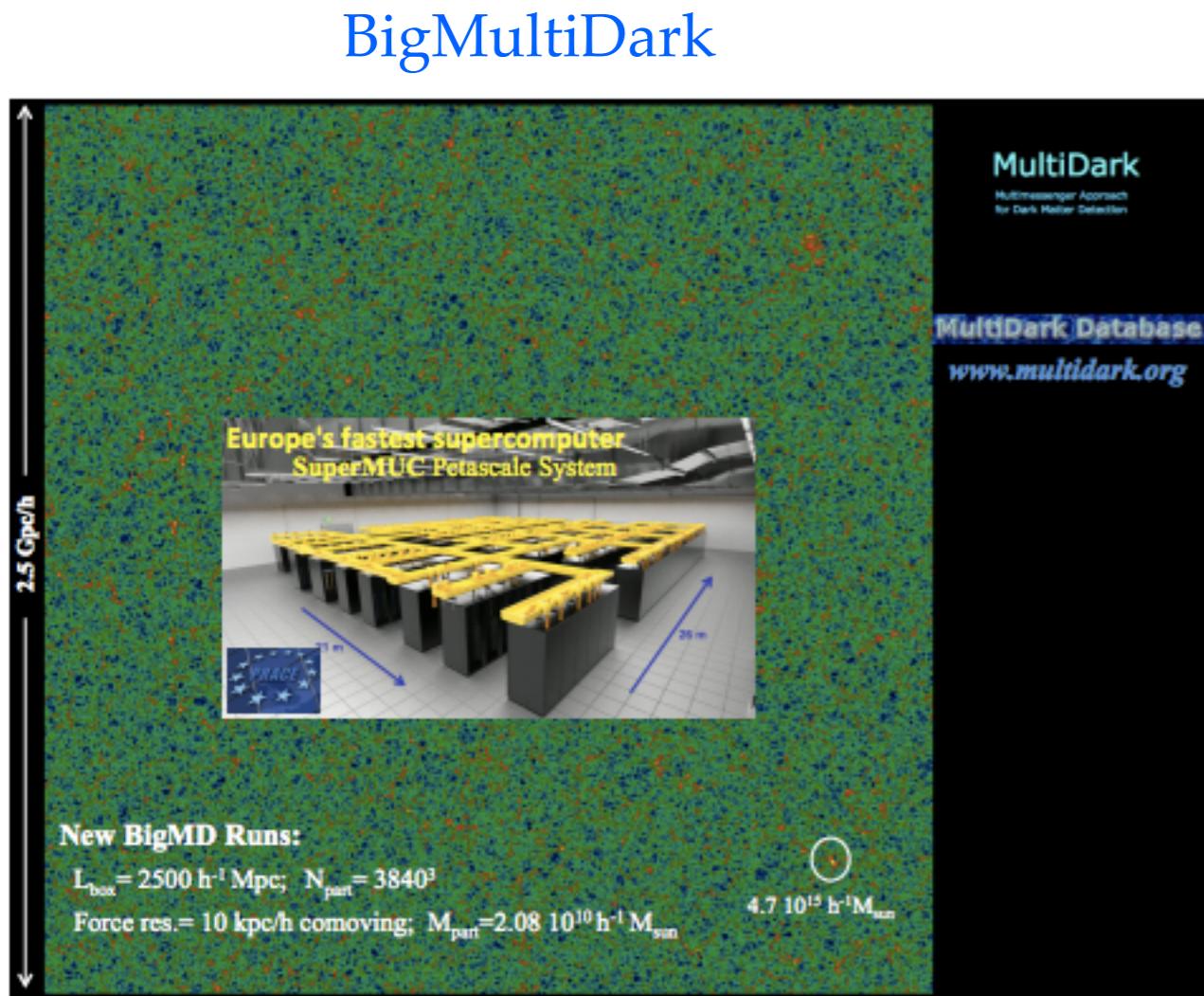
## 5) We apply observational effects

- ⌘ selection function (magnitude cut)
- ⌘ survey mask
- ⌘ redshift-space distortions



extraordinary effort in Spain!

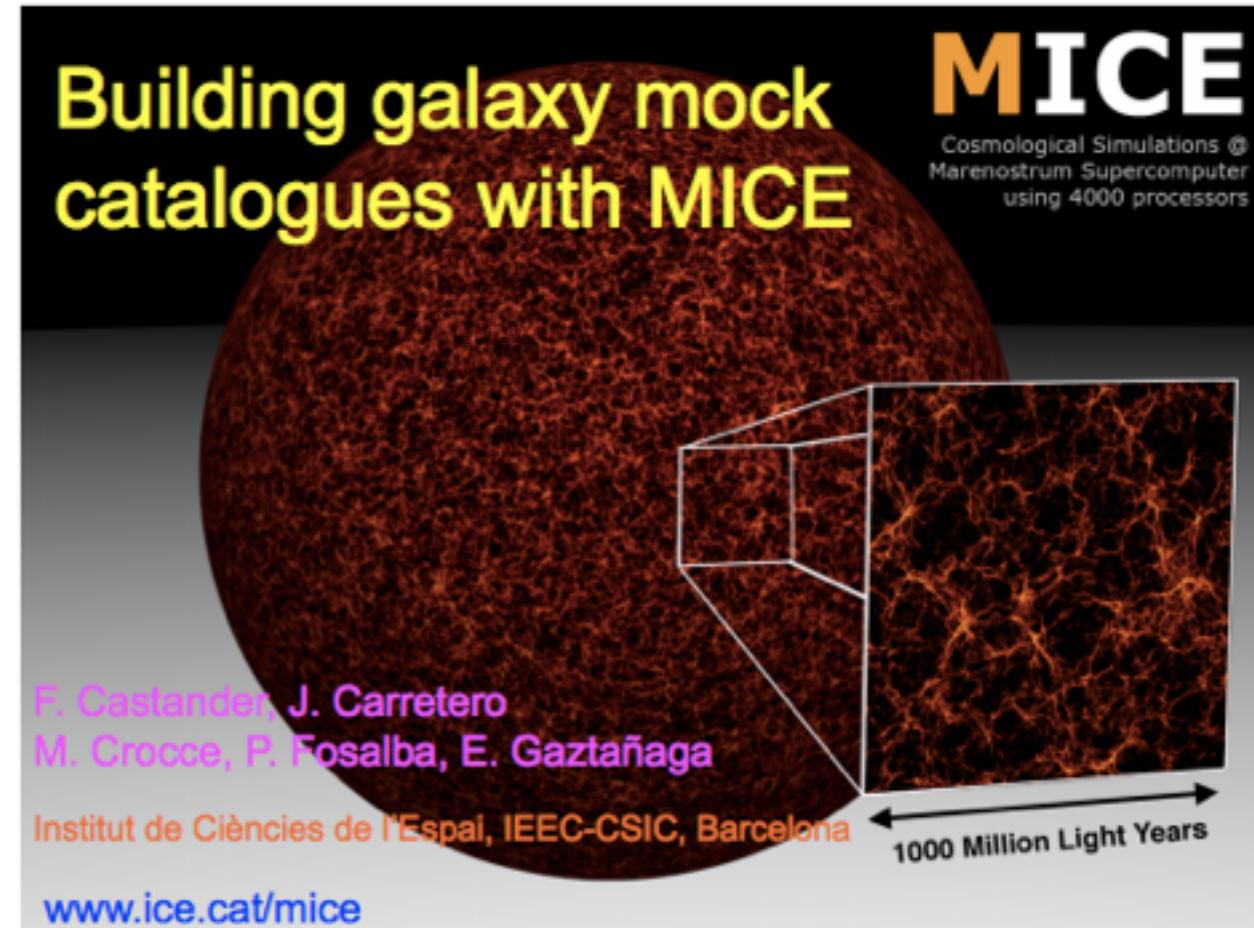
or with people from Spain involved:  
BigMultiDark/MICE/  
MXXL Raul Angulo/  
PThalos Marc Manera/  
PATCHY FK



see Paco Prada's talk

$\sim(2.5 \text{ Gpc}/h)^3$

remember Pablo Fosalba's talk



MICE  $\sim(3 \text{ Gpc}/h)^3$

END OF MY TALK?

However,  
this effort can only be done a couple of times,  
but not thousands of times!

we need to scan different cosmologies,  
different seeds (cosmic variance)

to estimate error bars/covariance matrices  
to measurements based on our unique Universe;

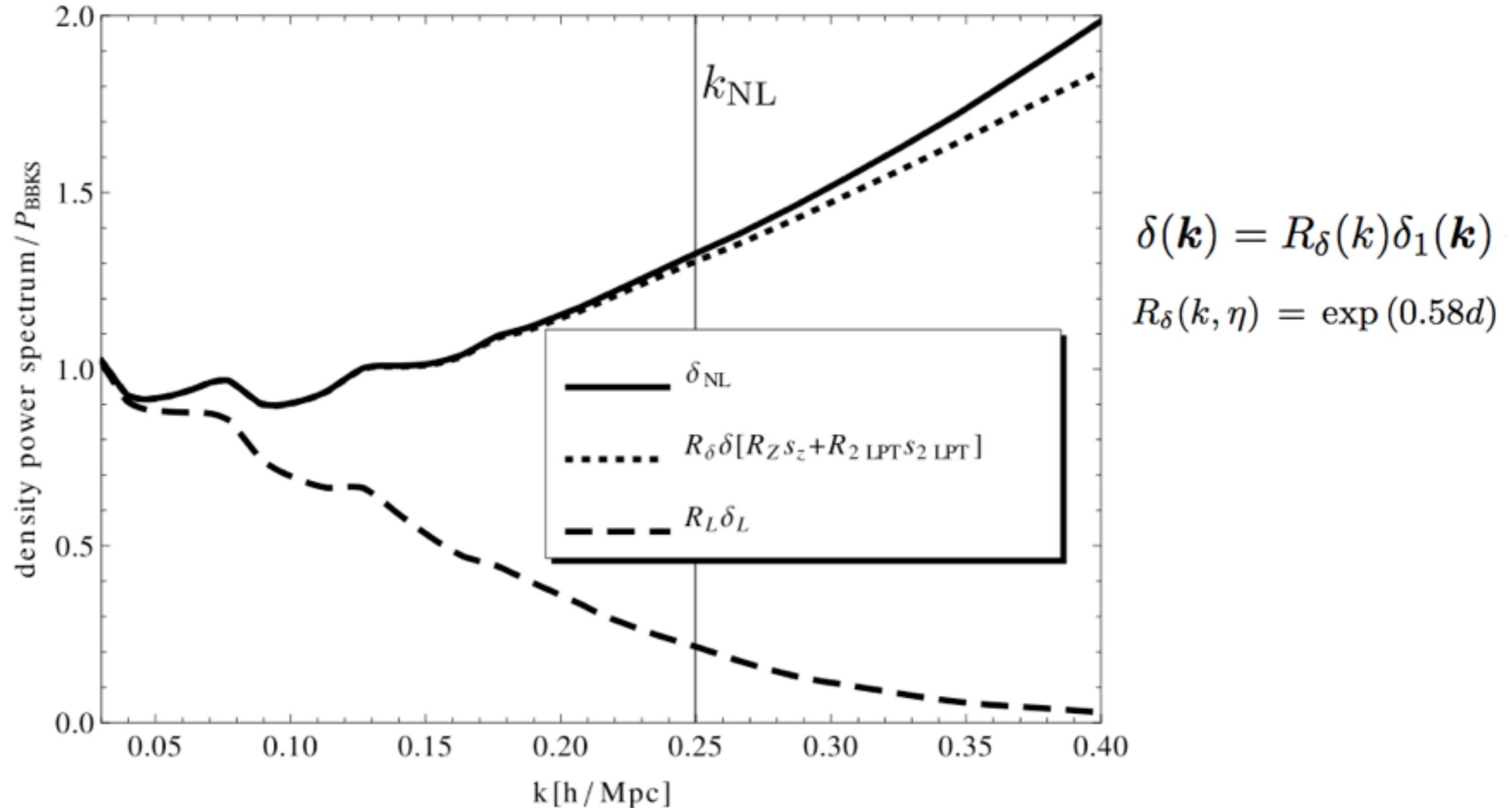
to test analysis tools with different realisations  
in a statistical relevant way

What is the bottle-neck of the computations?

What is the bottle-neck of the computations?

I. the gravity solver

# Perturbative approaches to model BAOs



Tassev & Zaldarriaga 2012

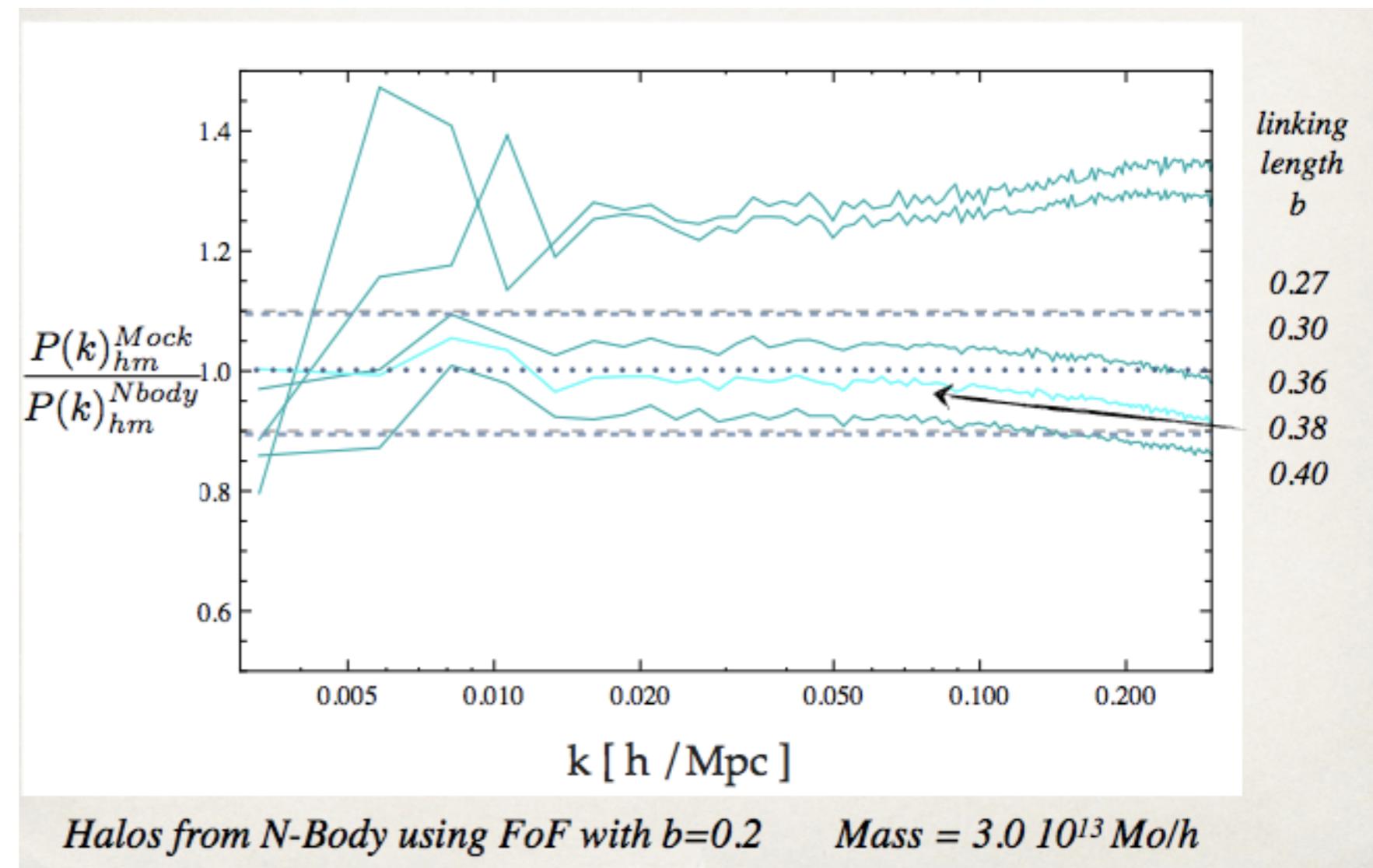
deviation in the power spectrum  
due to perturbative approach!

let us use approximate gravity solvers!

pioneering works by

1. Scoccimarro & Sheth 2002 (PThalos)  
2LPT
2. Monaco et al 2002 (Pinocchio)  
Zeldovich (being improved to 2LPT)  
includes merging histories
3. Tassev et al 2013 (COLA)  
make N-body code faster
4. White et al 2014 (QPM)  
use quasi PM solver

# PThalos



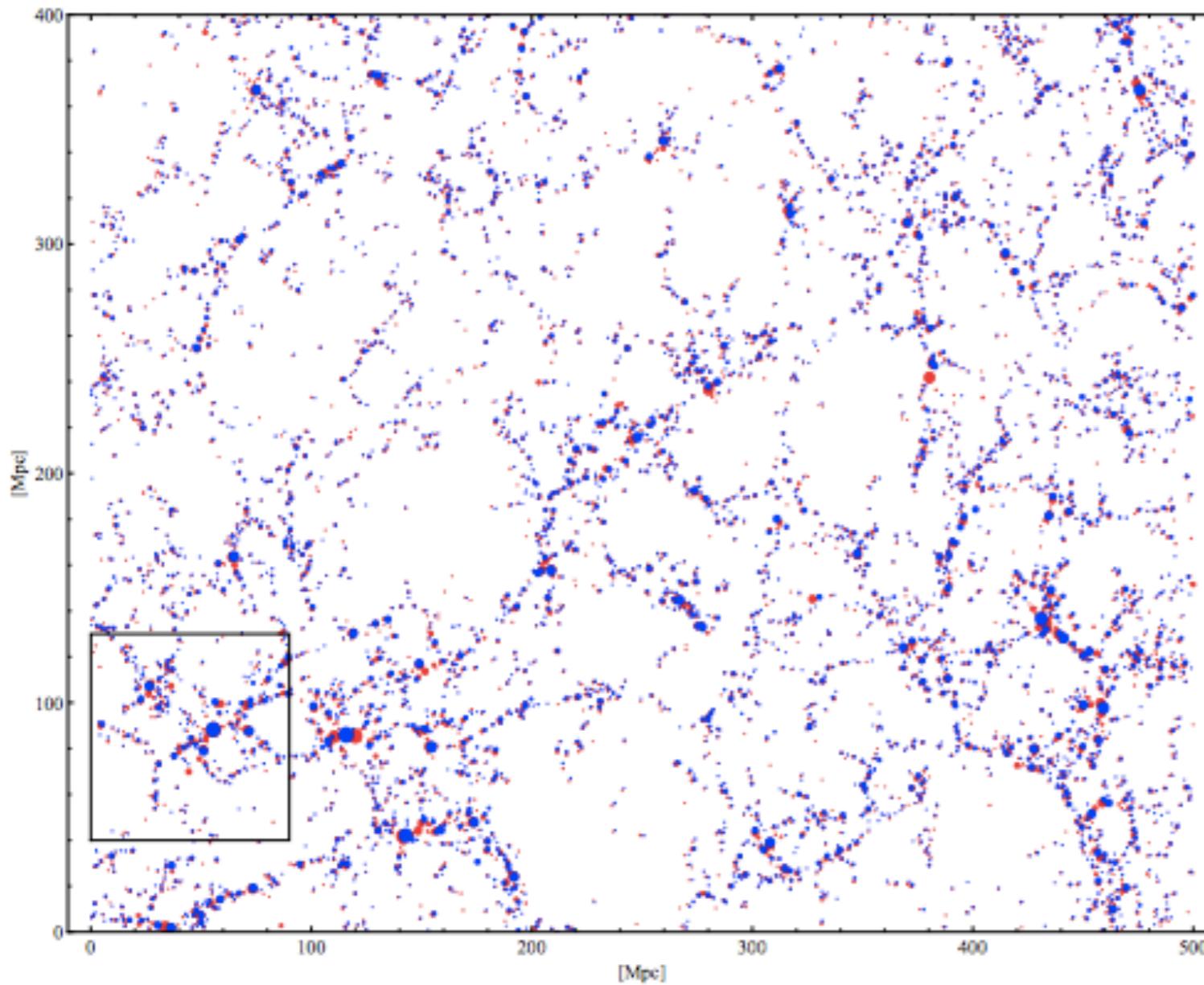
calibration with N-body  
1000 mocks done!

about 10 % deviation in the  
power-spectrum at  $k \sim 0.25$   
needs to resolve halos

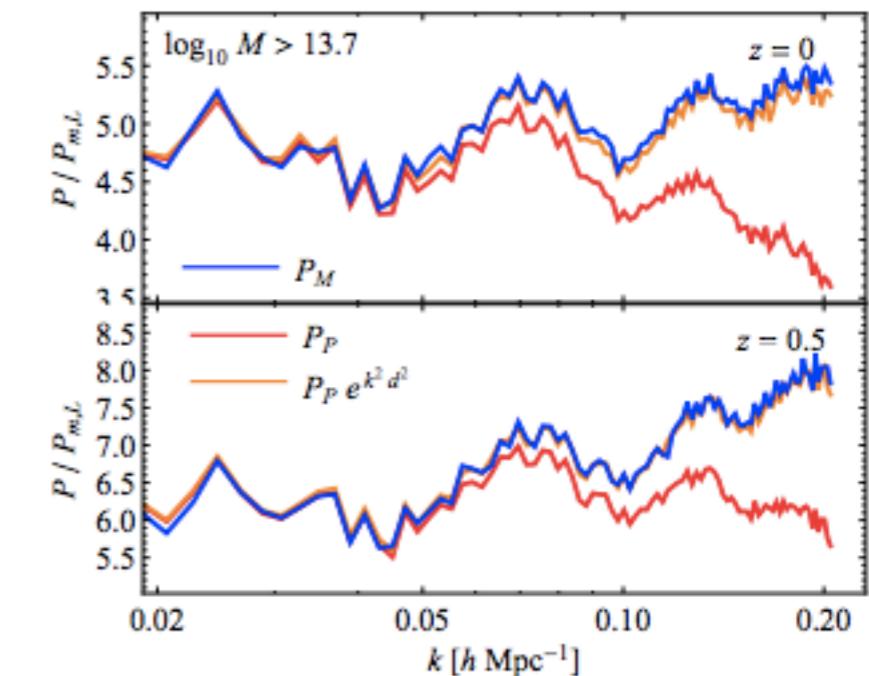
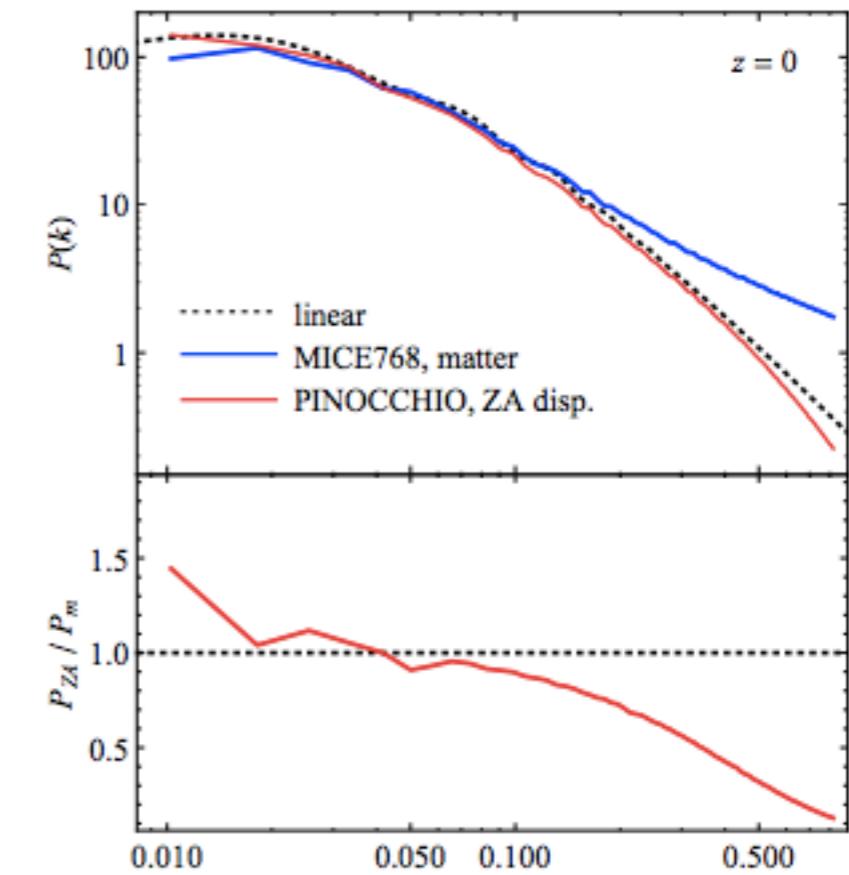
*see galaxy mocks from Manera M. & BOSS collaboration 2012 & 2014,  
MNRAS*

# Pinocchio

*Monaco et al 2013*



fast + predictive (merger trees)



deviation in the power spectrum  
needs to resolve halos

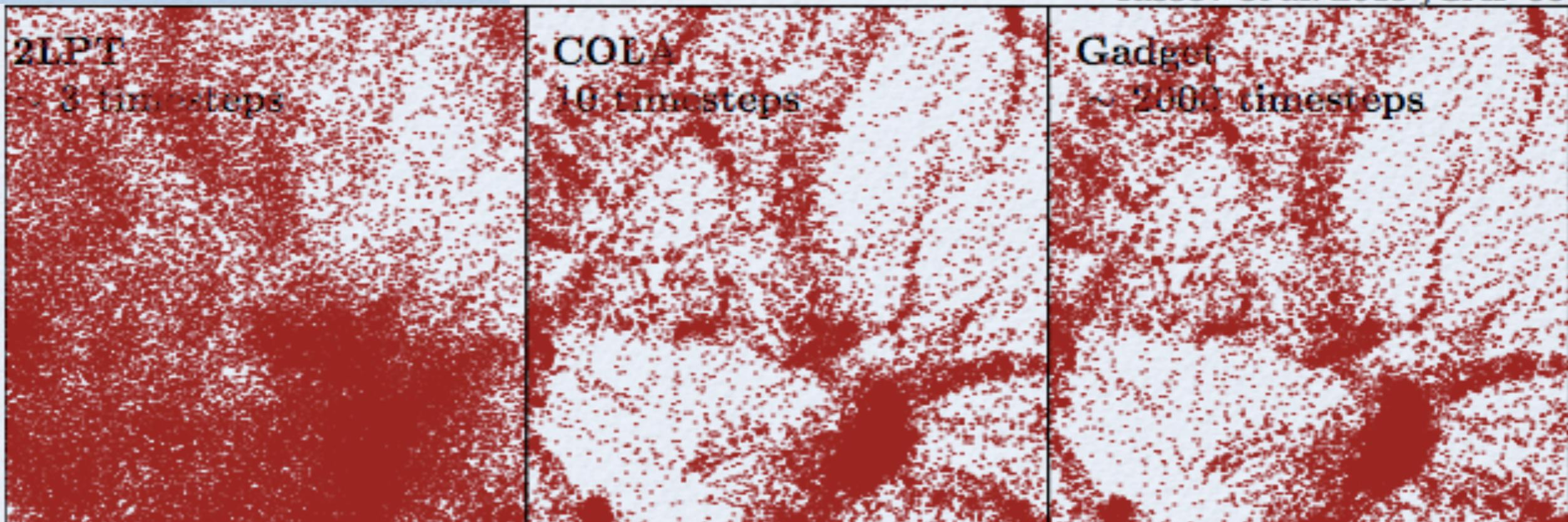
# COLA 10-timestep simulations

Koda et al 2014

WiZ-COLA simulation

2LPT + Particle Mesh force correction

Tassev et al. 2013 JCAP 06 36



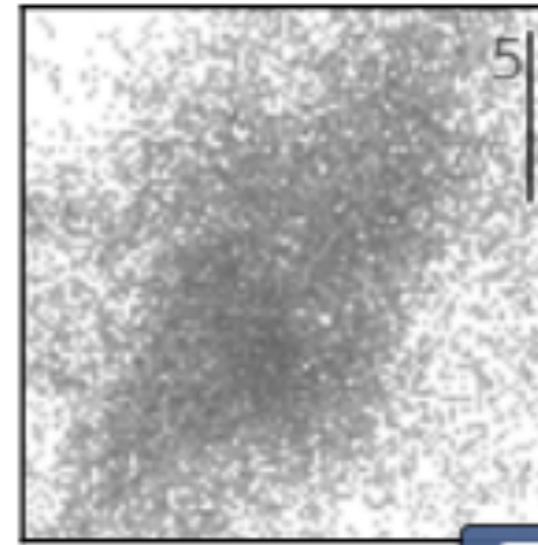
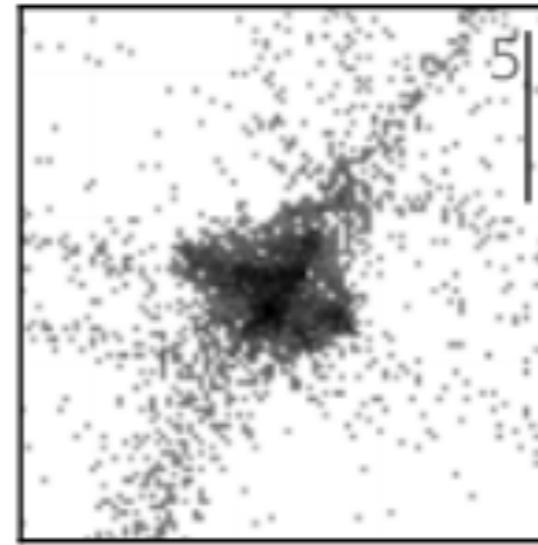
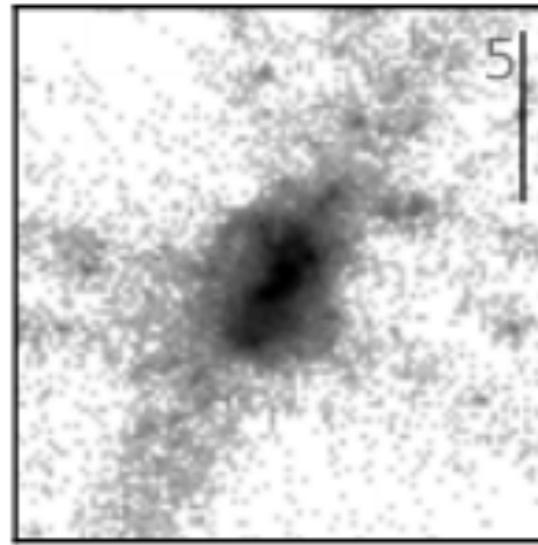
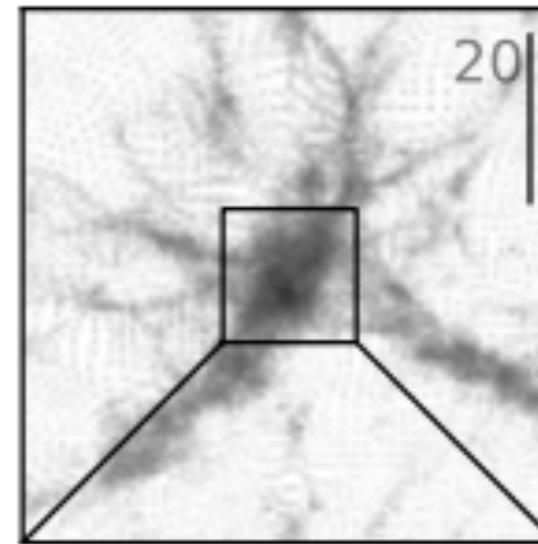
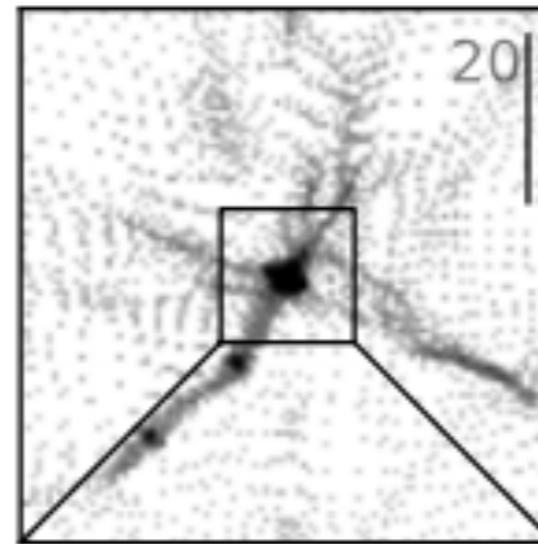
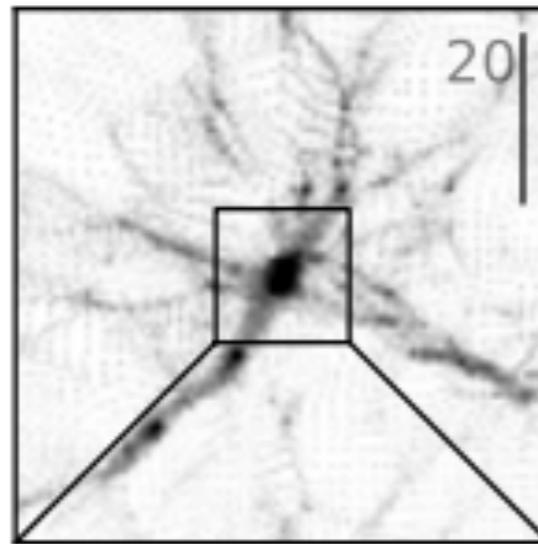
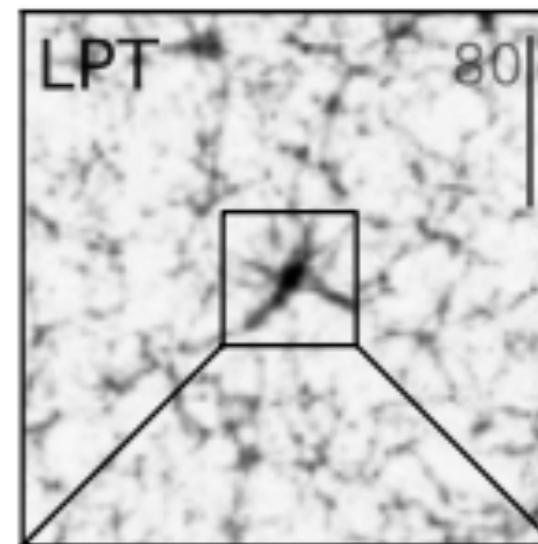
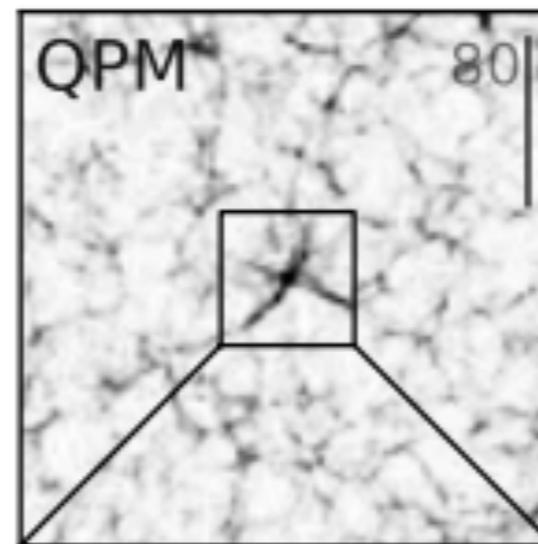
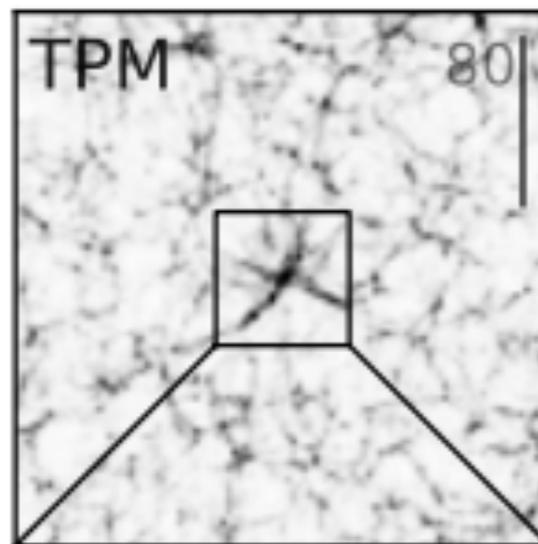
**2LPT (left):** very fast but resolves high-mass haloes only  $\sim 10^{13} M_{\odot}$

Manera et al. 2013 MNRAS 428 1036 (BOSS)

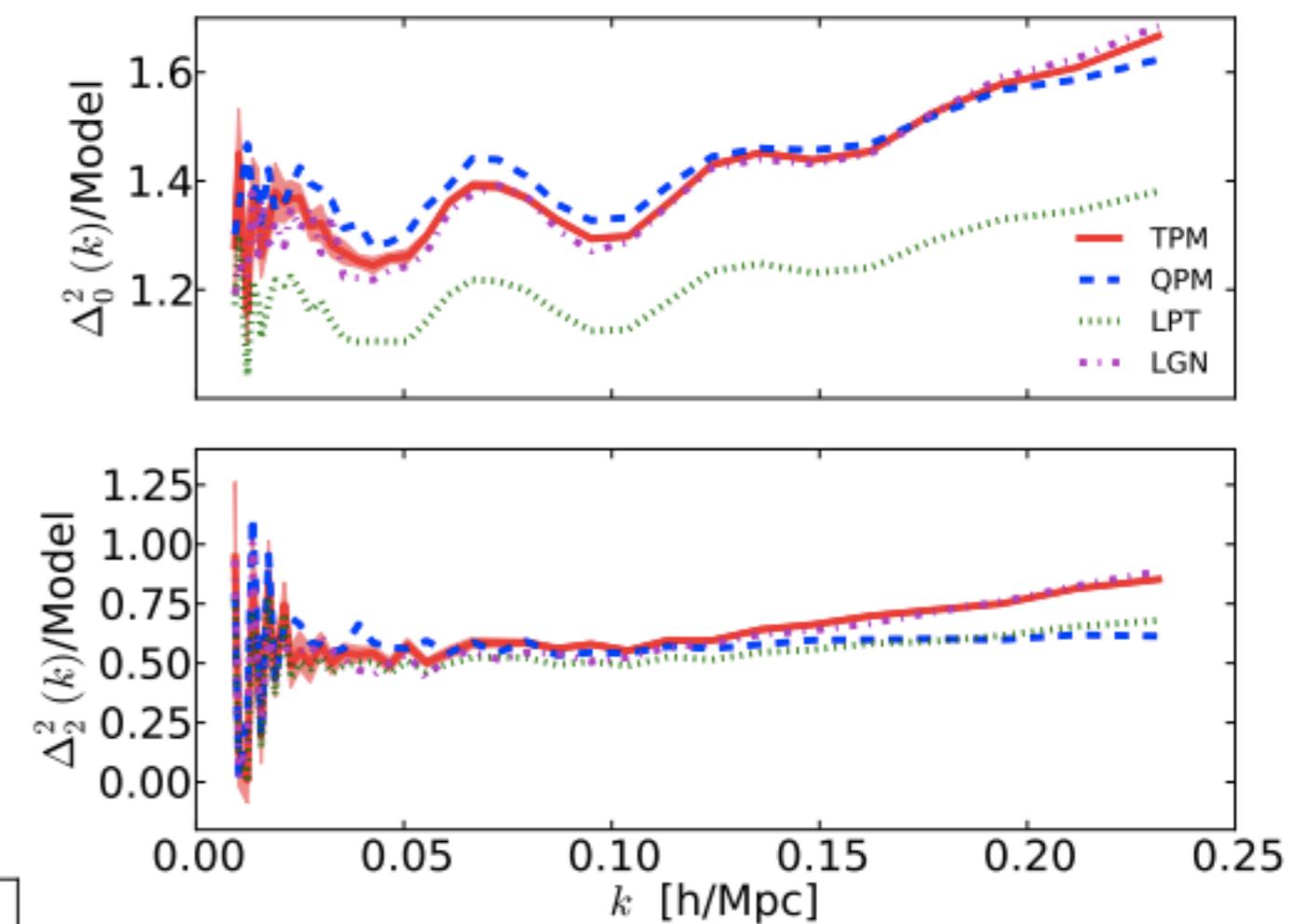
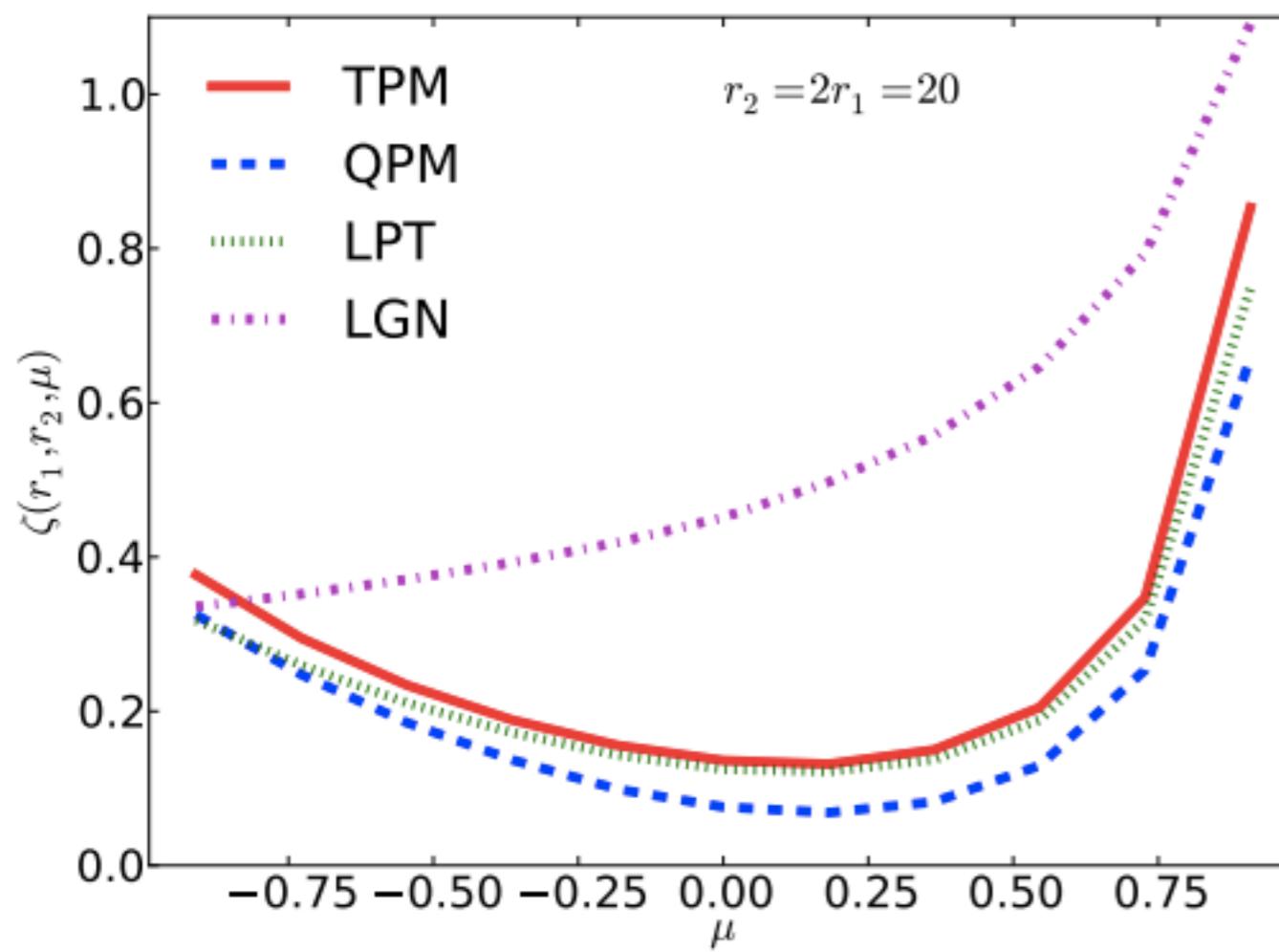
**COLA (middle):** COmoving Lagrangian Acceleration (COLA) method.

- resolves halo mass ( $\sim 5\%$ )
- accurate large-scale structure
- more than 100 times faster than usual simulations
- with 2LPT, larger timestep is allowed at high  $z \rightarrow$  better halo mass

faster than common N-body,  
but needs to resolve halos



White et al 2013



fast, but approximate PM method  
leads to worse 3pt statistics than LPT  
is the BAO damping correctly  
modelled?

What is the bottle-neck of the computations?

1. the gravity solver
2. resolution (number of particles)

Let us use low resolution simulations and augment the missing halos!

# Nonlinear scale-dependent biasing

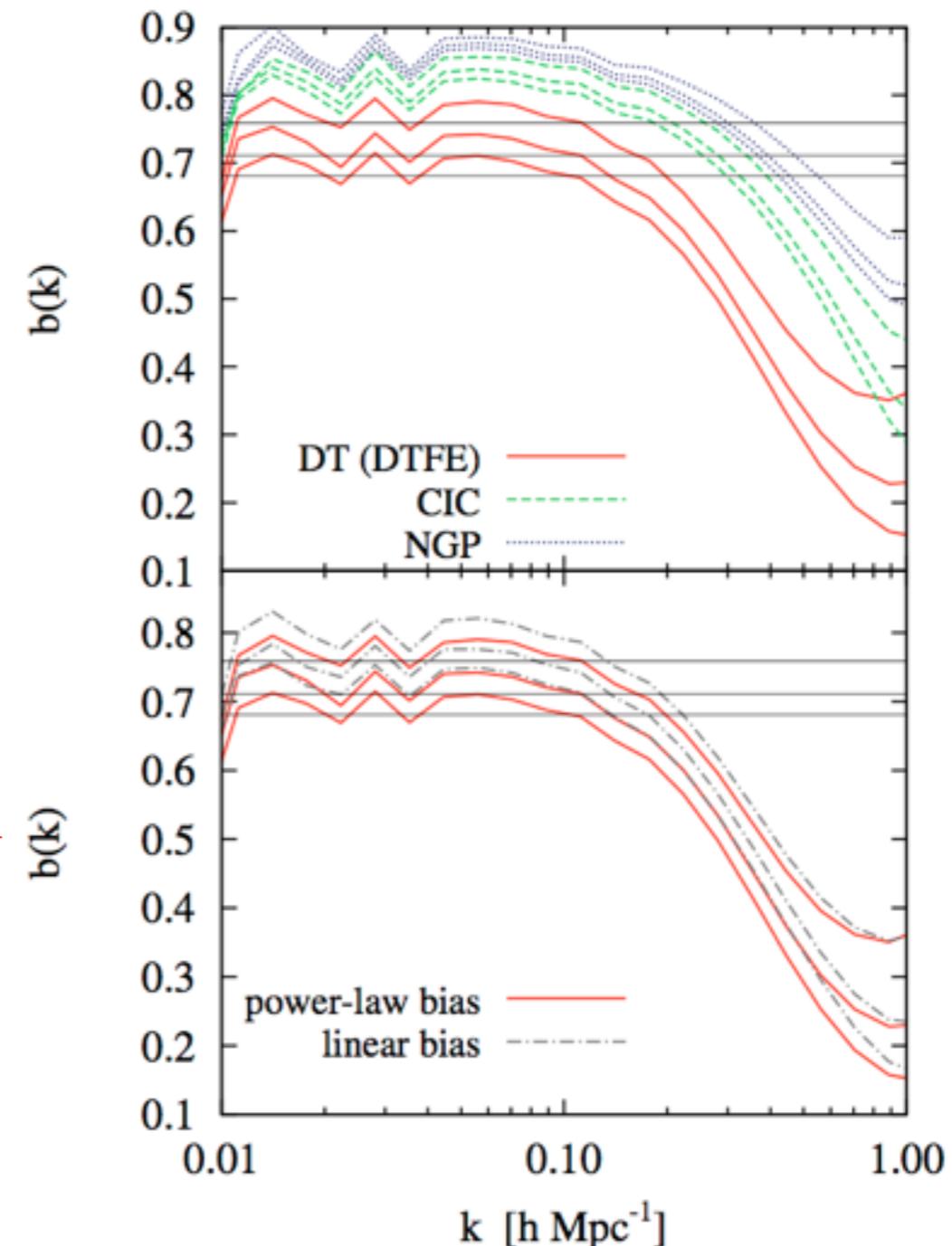
exponential bias

$$\langle N \rangle = f (1 + \delta)^{\text{bias}_E}$$

*de la Torre, S. & Peacock, J. 2012*

*Cen, R. & Ostriker, J. P. 1993*

is equivalent to an infinite expansion  
a la Fry & Gaztañaga 1993  
and can be interpreted as a  
Lagrangian bias in the lognormal  
approximation



*Angulo et al 2014 with Fry & Gaztañaga 1993*

Let us ask a different question:

How can I generate a distribution of halos/galaxies in a statistical way?

(of a certain type within a certain mass range)

the answer is:

we need all the higher order statistics from a reference sample  
+ a way to draw from such a higher order PDF:

$$N_h \leftarrow \mathcal{P}(N_h | \xi_1^h, \xi_2^h, \xi_3^h, \xi_4^h, \dots)$$

# How can we do it?

## Method I:

If we know the higher order correlations for the logarithm of the density field, we can perform multidimensional Edgeworth expansions:

$$P(\Phi) = (\det(\mathbf{S}))^{-1/2} G(\boldsymbol{\nu}) \quad (43) \quad \text{Kitaura 2012}$$

$$\times \left[ 1 + \frac{1}{3!} \sum_{i'j'k'} \langle \Phi_{i'} \Phi_{j'} \Phi_{k'} \rangle_c \sum_{ijk} S_{ii'}^{-1/2} S_{jj'}^{-1/2} S_{kk'}^{-1/2} h_{ijk}(\boldsymbol{\nu}) \right. \quad \text{Colombi 1994}$$

$$+ \frac{1}{4!} \sum_{i'j'k'l'} \langle \Phi_{i'} \Phi_{j'} \Phi_{k'} \Phi_{l'} \rangle_c \sum_{ijkl} S_{ii'}^{-1/2} S_{jj'}^{-1/2} S_{kk'}^{-1/2} S_{ll'}^{-1/2} h_{ijkl}(\boldsymbol{\nu})$$

$$+ \frac{1}{6!} \sum_{i'j'k'l'm'n'} \left[ \dots \right] \quad \text{complicated + expensive!}$$

$$\times \left[ \frac{1}{3!3!2} \sum_{j_1 \dots j_6 \in [1, \dots, 6]} \tilde{\epsilon}_{j_1 \dots j_6} \langle \Phi_{i'_{j_1}} \Phi_{i'_{j_2}} \Phi_{i'_{j_3}} \rangle_c \langle \Phi_{i'_{j_4}} \Phi_{i'_{j_5}} \Phi_{i'_{j_6}} \rangle_c \right]_{10}$$

$$\times \left. \sum_{ijklmn} S_{ii'}^{-1/2} S_{jj'}^{-1/2} S_{kk'}^{-1/2} S_{ll'}^{-1/2} S_{mm'}^{-1/2} S_{nn'}^{-1/2} h_{ijklmn}(\boldsymbol{\nu}) + \dots \right],$$

# How can we do it?

## Method I:

If we know the higher order correlations for the logarithm of the density field, we can perform multidimensional Edgeworth expansions:

$$P(\boldsymbol{\nu}) = G(\boldsymbol{\nu}) [1 + \mathcal{S}(\boldsymbol{\nu}) + \mathcal{K}(\boldsymbol{\nu}) + \dots] \quad \text{Kitaura 2012}$$

$$\Phi \equiv \ln \rho - \langle \ln \rho \rangle \quad \nu_i \equiv \sum_j S_{ij}^{-1/2} \Phi_j$$

$$\mathcal{S}(\boldsymbol{\nu}) \equiv \frac{1}{3!} \sum_{ijk} \kappa_{ijk} h_{ijk}(\boldsymbol{\nu}) = \frac{1}{3!} \sum_{i'j'k'} \xi_{i'j'k'} \tilde{h}_{i'j'k'}(\boldsymbol{\nu}) \quad (60)$$

$$= \frac{Q_3}{3!} \sum_{i'j'k'} [S_{i'j'} S_{i'k'} + S_{i'j'} S_{j'k'} + S_{i'k'} S_{j'k'}] \tilde{h}_{i'j'k'}(\boldsymbol{\nu})$$

$$= Q_3 \left[ \frac{1}{2} \sum_i \Phi_i^2 \eta_i - \frac{1}{2} \sum_i S_{ii} \eta_i - \sum_i \Phi_i \right],$$

$$\eta_i \equiv \sum_j S_{ij}^{-1} \Phi_j$$

Let us imagine we would know the halo/galaxy density field, i.e. the expected number of halos/galaxies per finite volume (cell).

# Stochastic biasing

$$N_h \sim \mathcal{P}(N_h | \rho_h)$$

caution! we still need to know the deviation from Poissonity!

over-dispersion modelled by the NB PDF:

$$P(N_i | \lambda_i, \beta) = \frac{\lambda_i^{N_i}}{N_i!} \frac{\Gamma(\beta + N_i)}{\Gamma(\beta)(\beta + \lambda)^{N_i}} \frac{1}{(1 + \lambda/\beta)^\beta}$$

*non-Poissonian PDFs:*

*Kitaura, Yepes & Prada 2014, MNRAS*

*W.C. Saslaw, A.J.S. Hamilton, 1984, ApJ, 276, 13*

*Sheth R. K., 1995, MNRAS, 274, 213*

*stochastic bias:*

*Dekel A., Lahav O., 1999, ApJ, 520, 24*

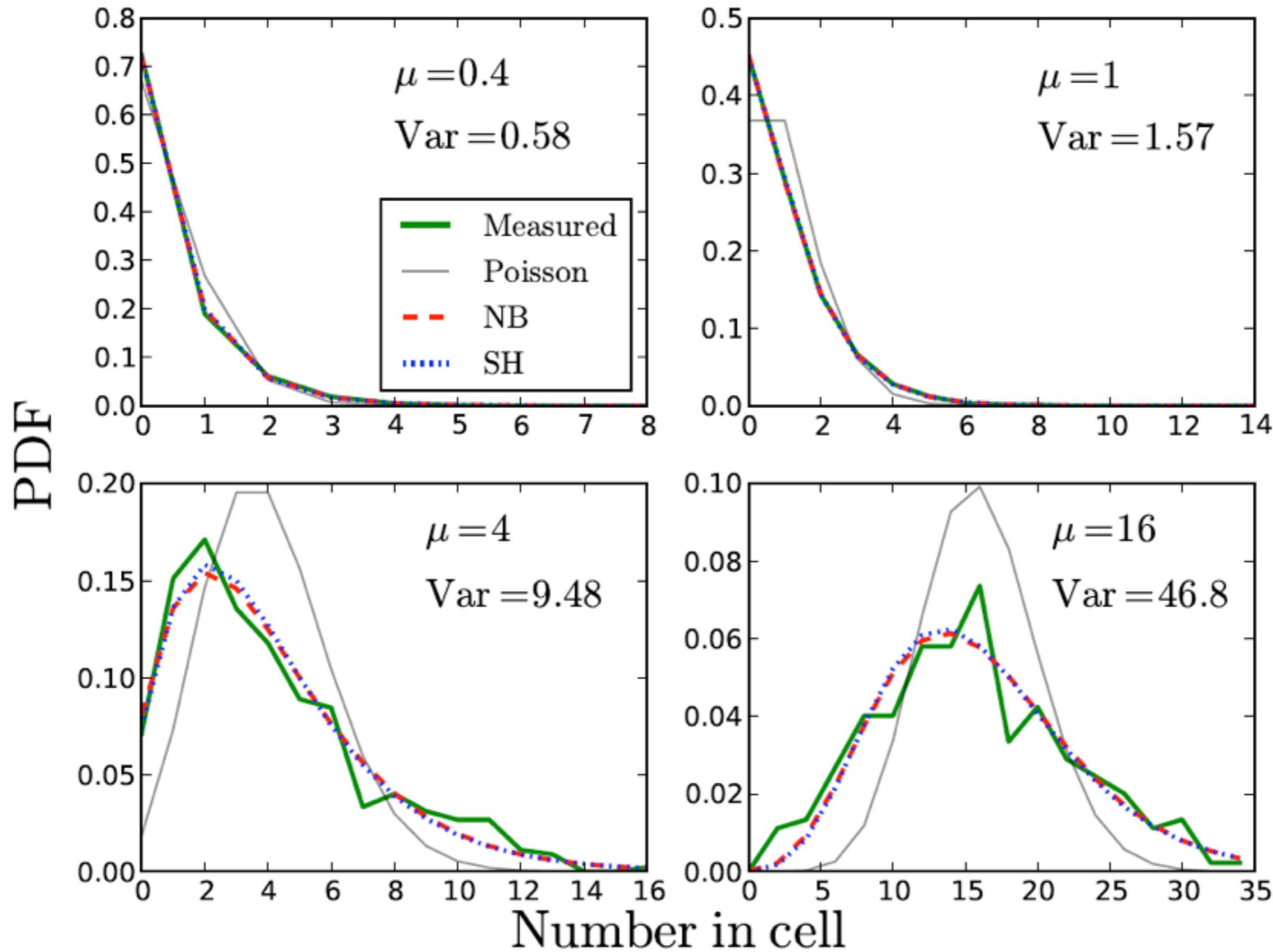
*Sheth R. K., Lemson G., 1999, MNRAS, 304, 767*

*and many more see references in e.g. Kitaura et al 2013*

*Somerville et al 2001, MNRAS, 320, 289*

*Casas-Miranda et al 2002, MNRAS, 333, 730*

*Neyrinck M et al 2013; Aragon-Calvo M. 2013*



# Deterministic biasing

we need to know the (deterministic) biasing,  
but this implies knowing all the higher order correlation functions!

$$B(\rho_h | \rho_M) = B(\rho_h | \rho_M, \xi_1^h, \xi_2^h, \xi_3^h, \xi_4^h, \dots)$$

$$N_h \curvearrowleft \mathcal{P}(N_h | B(\rho_h | \rho_M, \xi_1^h, \xi_2^h, \xi_3^h, \xi_4^h, \dots))$$

# Deterministic biasing parametrization

*Fry & Gaztañaga 1993*

$$\rho_h = f_h^a \sum_i a_i \delta_M^i$$

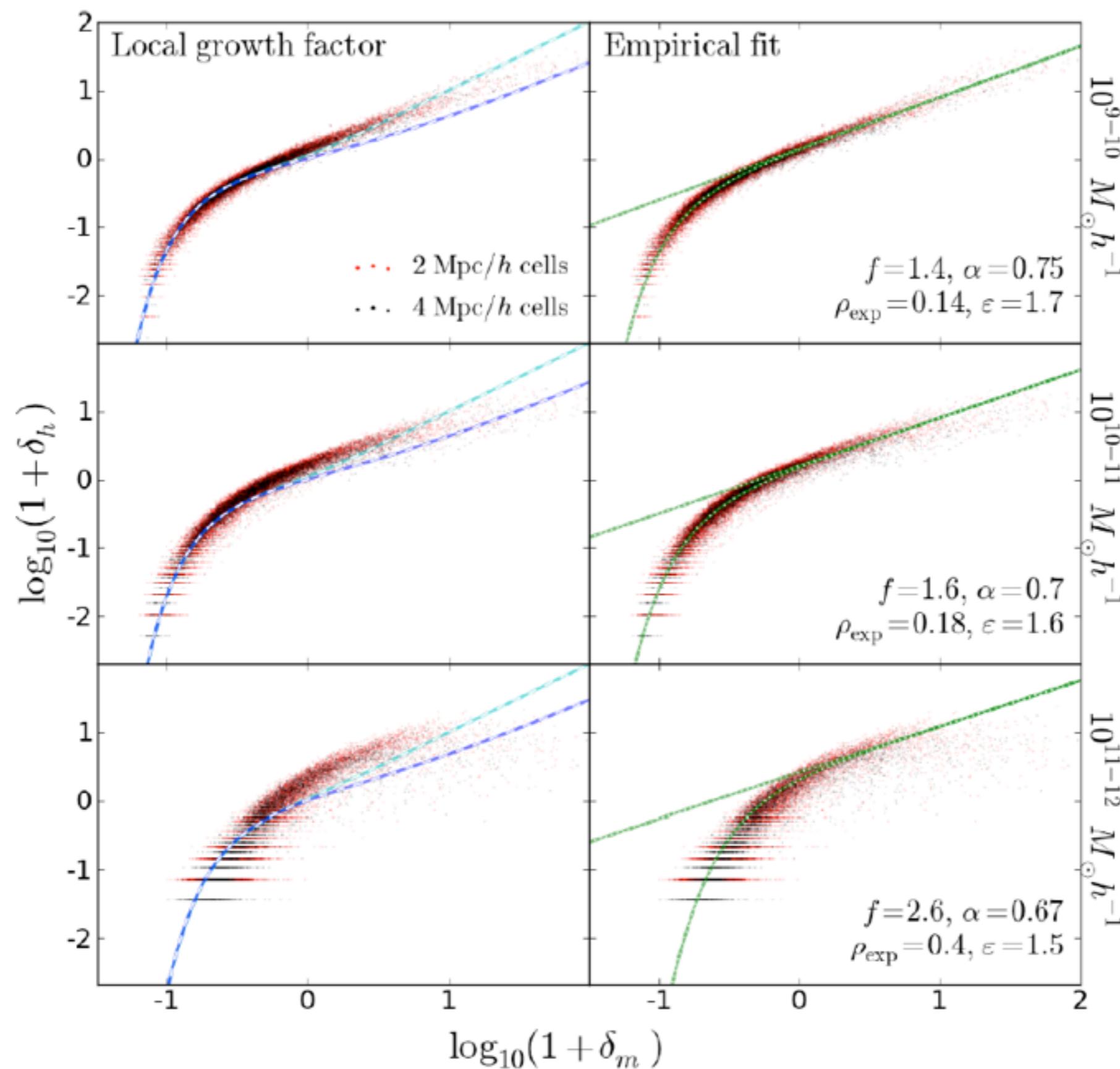
*Cen & Ostriker 1993*

$$\rho_h = f_h^b \exp \left[ \sum_i b_i \log (1 + \delta_M)^i \right]$$

*Kitaura, Yepes & Prada 2014; Neyrinck et al 2014*

$$\rho_h = f_h \theta(\rho_M - \rho_{\text{th}}) \rho_M^\alpha \exp \left[ - \left( \frac{\rho_M}{\rho_\epsilon} \right)^\epsilon \right]$$

Neyrinck M et al 2013; Aragon-Calvo M. 2013



How can we do it?

Method II:

given the dark matter field  
(from low resolution N-body or approximate solver)  
parametrize the bias  
and constrain the bias parameters, in such a way that  
the higher order correlation functions are matched

expensive!

How can we do it?

Method III:

*Kitaura et al in prep*

$$\bar{N}_h = \langle \rho_h \rangle \leftarrow \xi_1^h$$

$$P_h(k) \leftarrow \xi_2^h$$

$$\mathcal{P}^1(\rho) = \int_{-\sqrt{-1}\infty}^{\sqrt{-1}\infty} \frac{dt}{2\pi\sqrt{-1}} \exp(t\rho + \mathcal{C}(t))$$

$$\mathcal{P}_h^1(B(\rho_h | \rho_M)) \leftarrow \{\xi_1^h, \xi_2^h, \xi_3^h, \xi_4^h, \dots\}$$

$$N_h \curvearrowleft \mathcal{P}(N_h | B(\rho_h | \rho_M, \bar{N}_h, P_h(k), \mathcal{P}_h^1))$$

our approach:

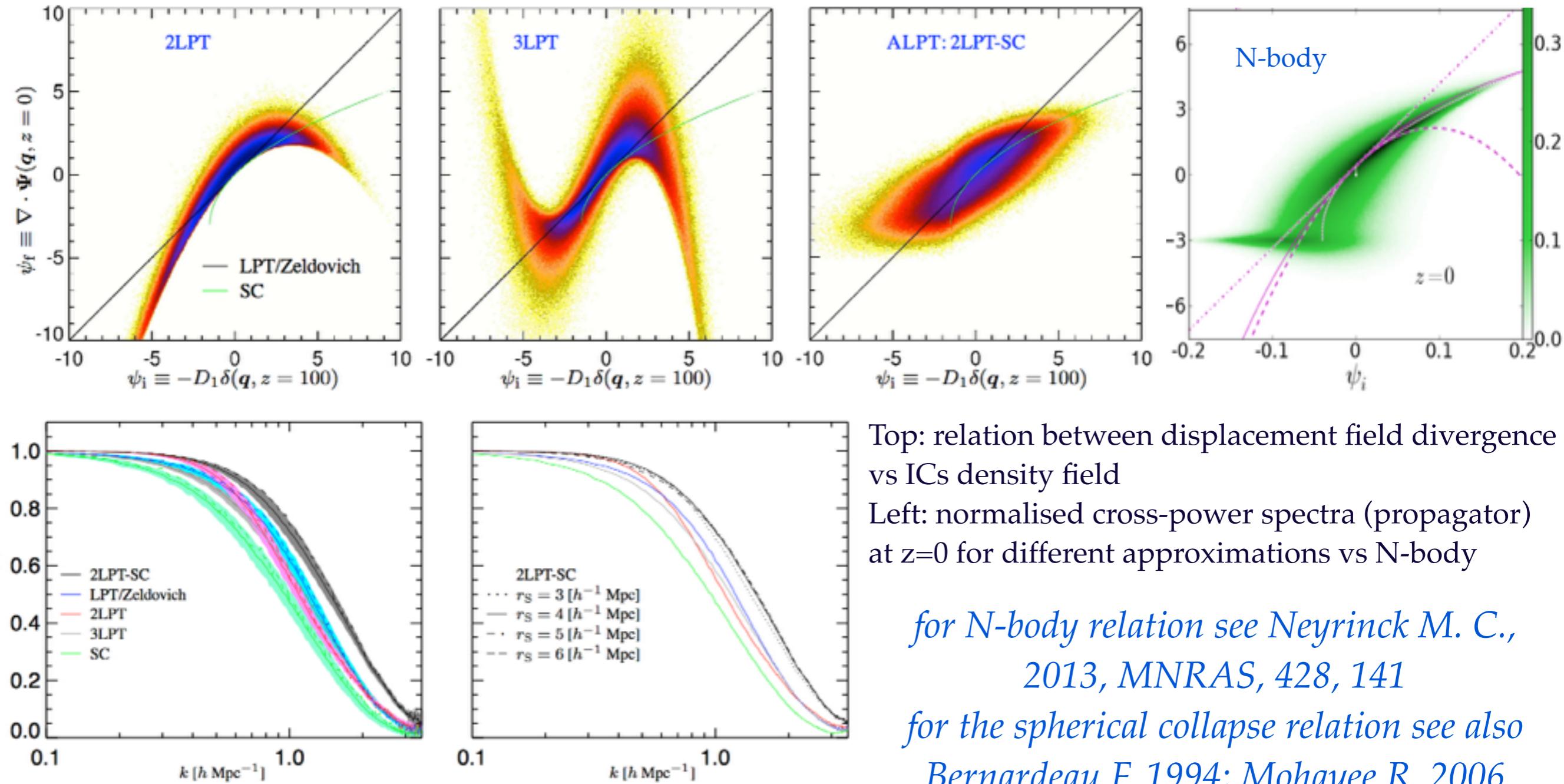
Let us use low resolution + approximate gravity solvers  
and augment all the missing halos!

- ✿ The approximate gravity solver accurately models the higher order statistics of the dark matter density field.  
(low N-body resolution or perturbation theory based method)
- ✿ The biasing model accurately connects the dark matter phase- space distribution with the halo distribution.

**Simple efficient accurate one-step gravity solver...**

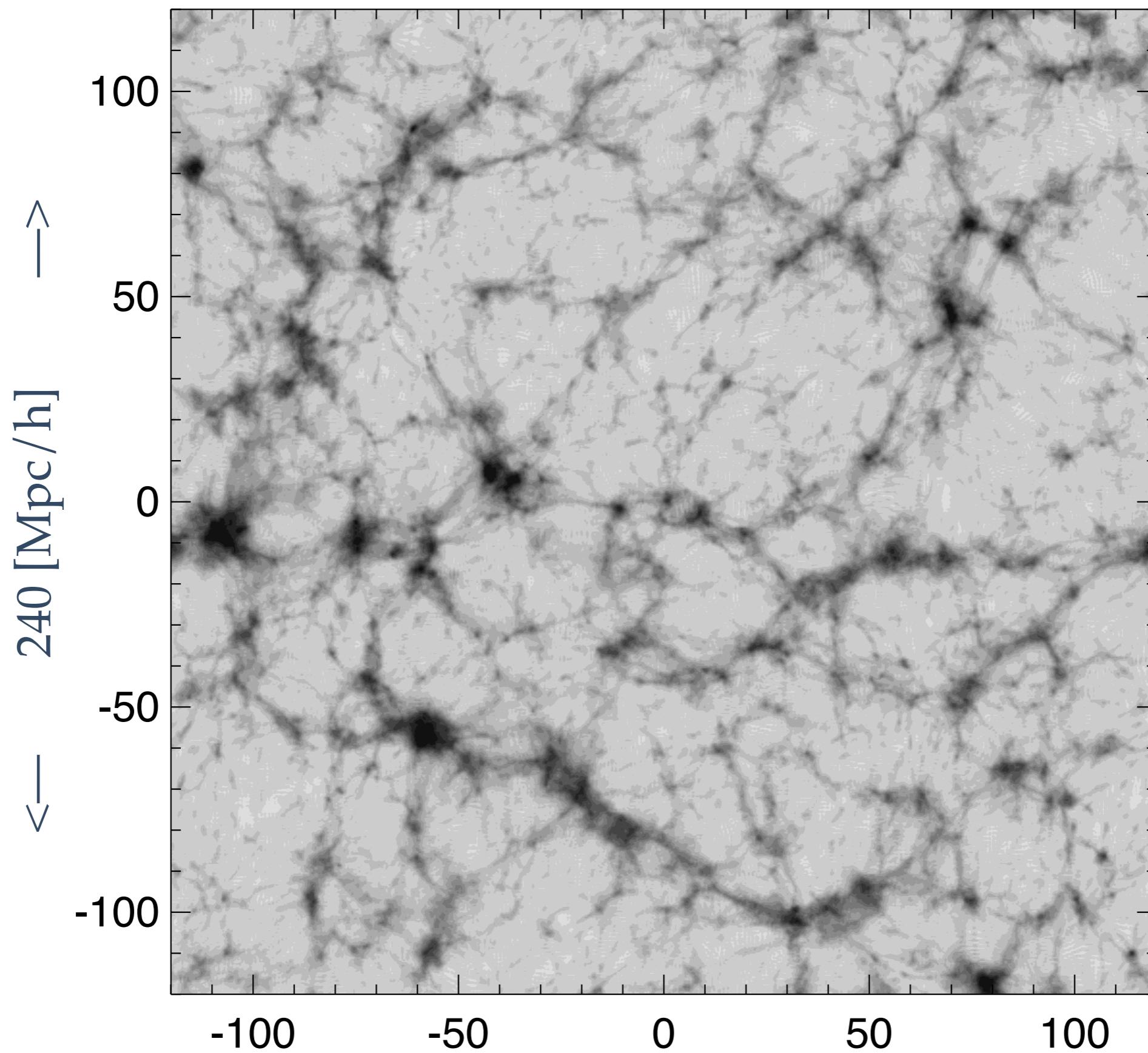
# ALPT:Augmented Lagrangian Perturbation Theory

*Kitaura F. S. & Heß S. 2013, MNRAS, 435, L78*

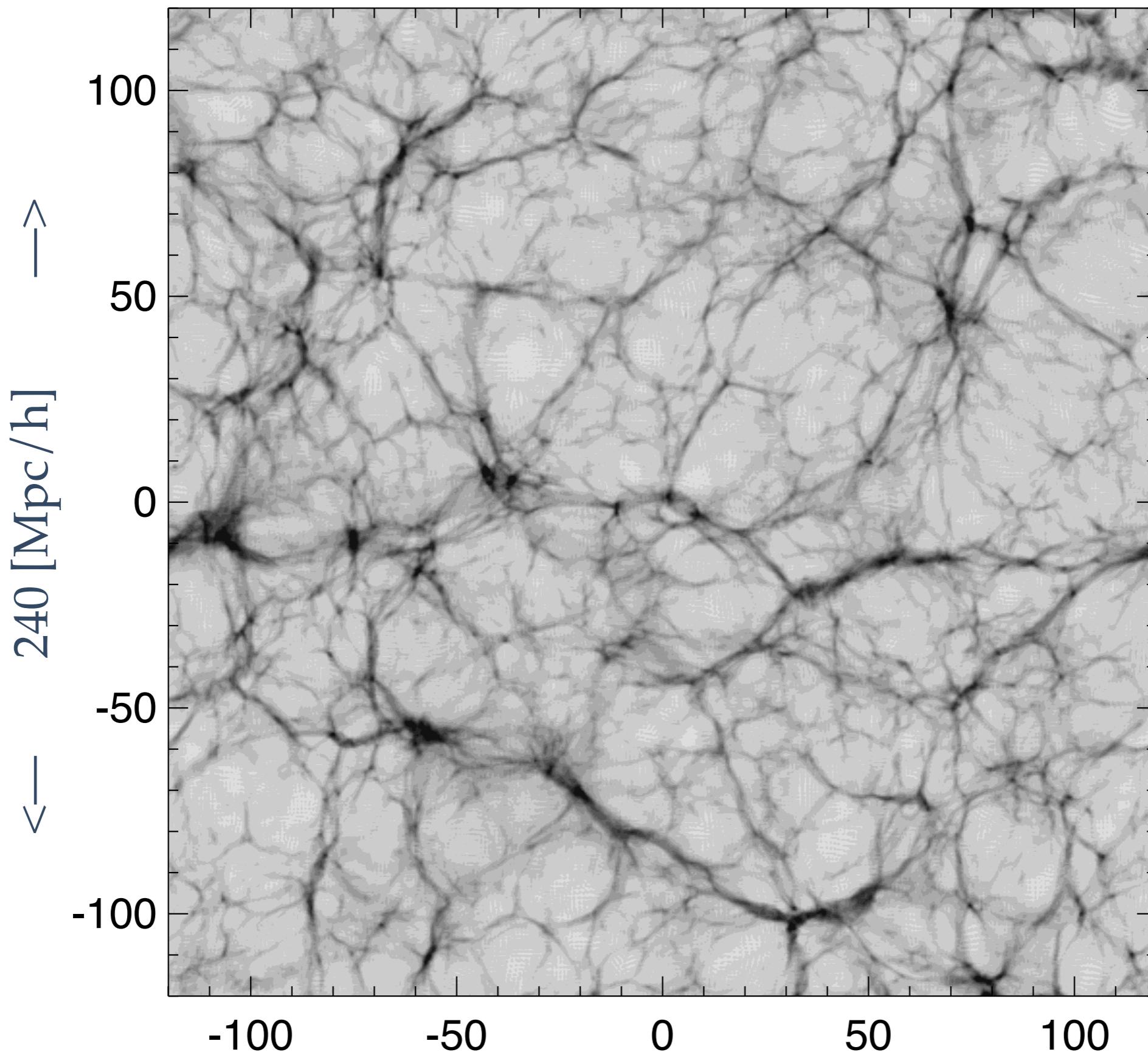


*see also Tashev S. & Zaldarriaga M., 2012, JCAP, 4, 13 for other LPT improvements with transfer functions (less correlated with the N-body solution than ALPT)*

2LPT  $z=0$



# ALPT $z=0$



# Calibration with N-body simulations for CMASS LRG type galaxies

we are performing mocks for BOSS, 4MOST, JPAS, EUCLID,...

Reference N-body simulation (Gadget): BIGMULTIDARK

Volume:  $(2500 \text{ Mpc}/\text{h})^3$

*Hess et al in prep*

Number of particles:  $3840^3$  (2M cpu hs) *Prada et al in prep*

halos selected with bdm (density peaks) according to  $\text{vmax} > \sim 350 \text{ km/s}$  (LRGs)

-> I consider 8 sub-volumes of  $(1250 \text{ Mpc}/\text{h})^3$

Simulations with **PATCHY**: PerturbAtion Theory Catalog generator of

Halo/galaxY distributions

*Kitaura, Yepes & Prada 2014, MNRAS*

Volume:  $(1250 \text{ Mpc}/\text{h})^3$

Grid number of cells:  $512^3$

**53 times lower resolution required!**

Resolution of the grid:  $(2.4 \text{ Mpc}/\text{h})^3$

same cosmology (Planck-like)

same redshift:  $z=0.577$

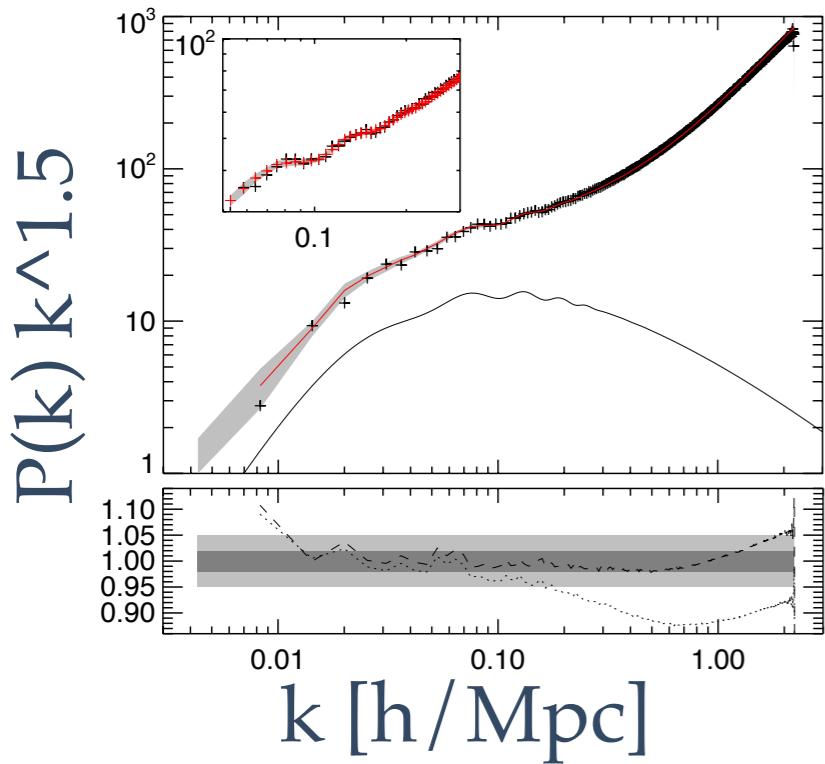
on my laptop (quad core i7, 4 cpus+4 virtual cpus, 8 Gb RAM)

about 15 mins

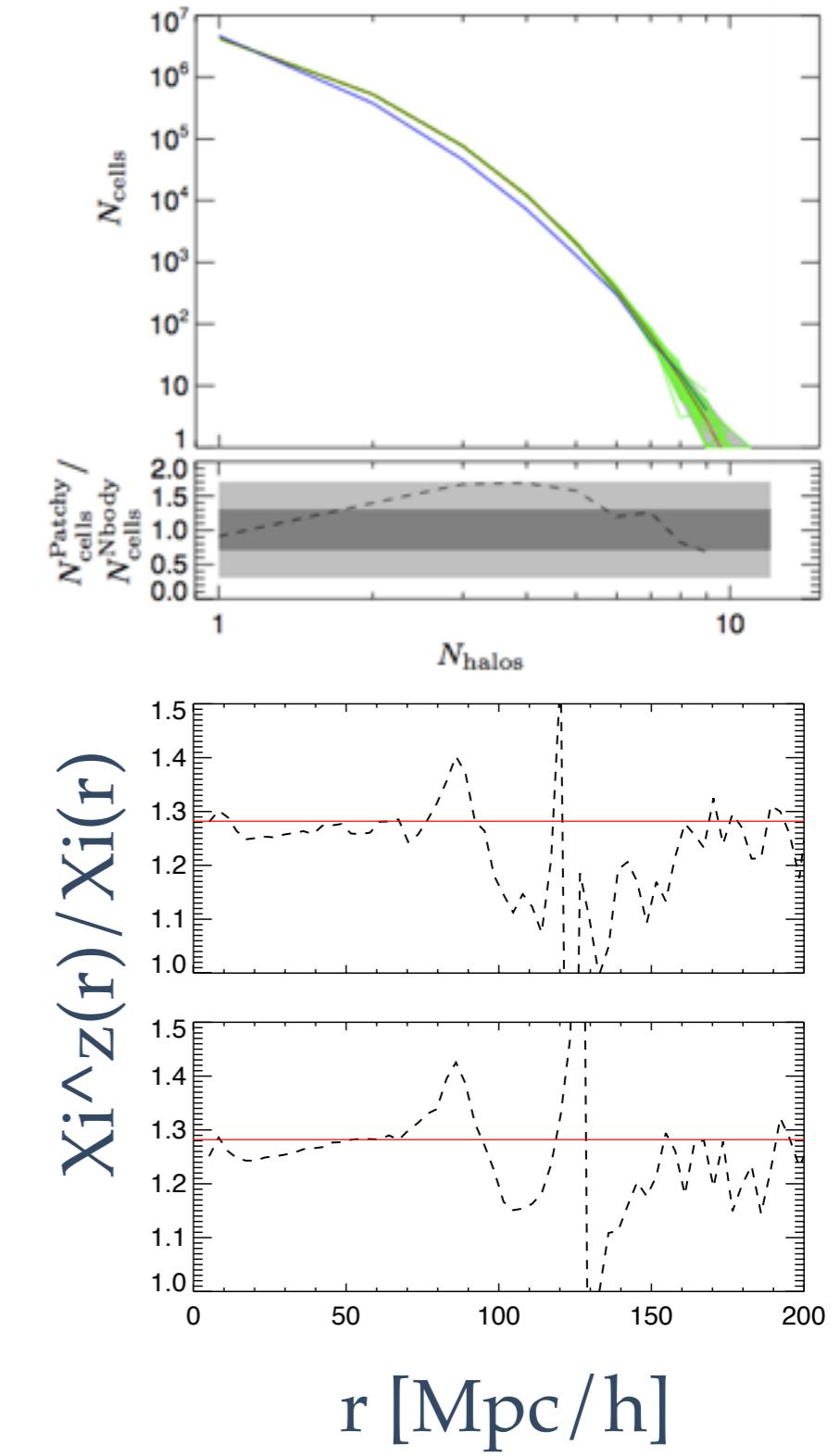
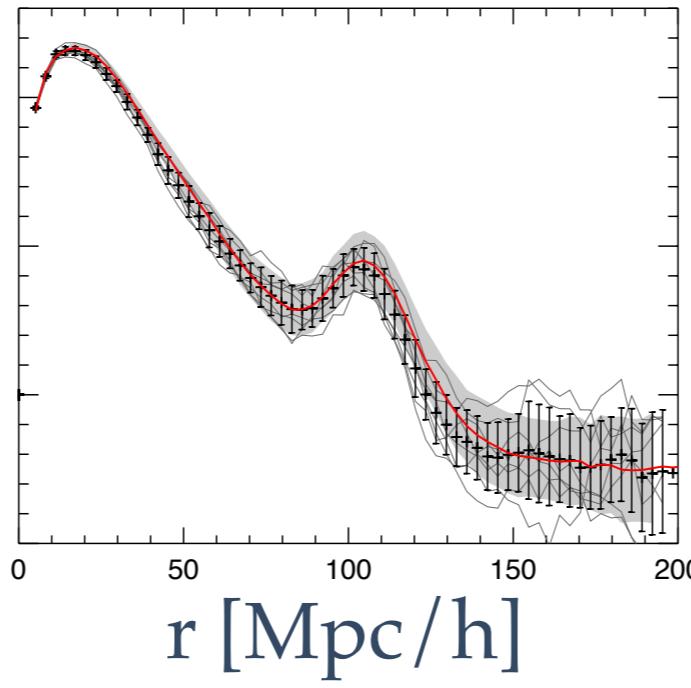
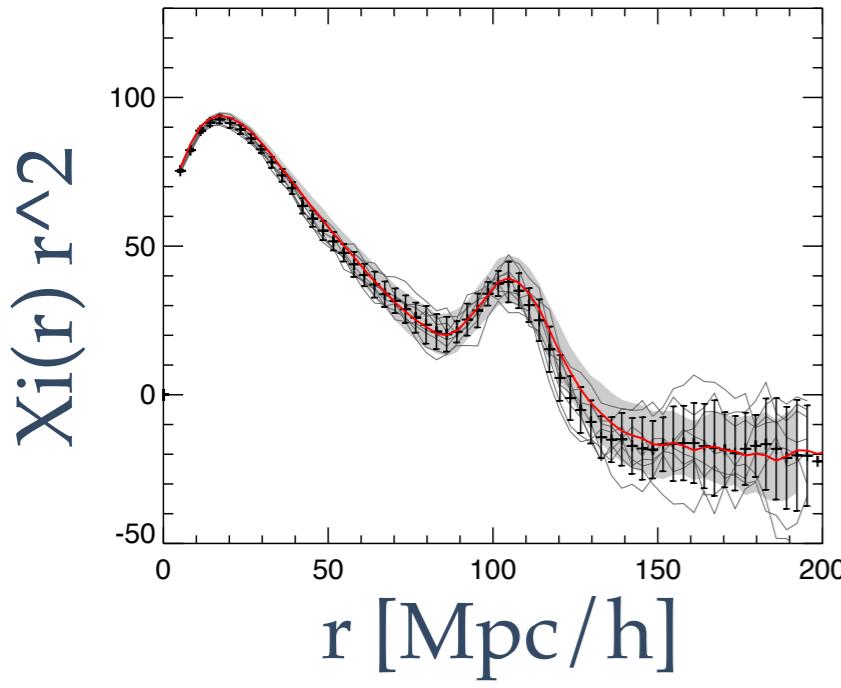
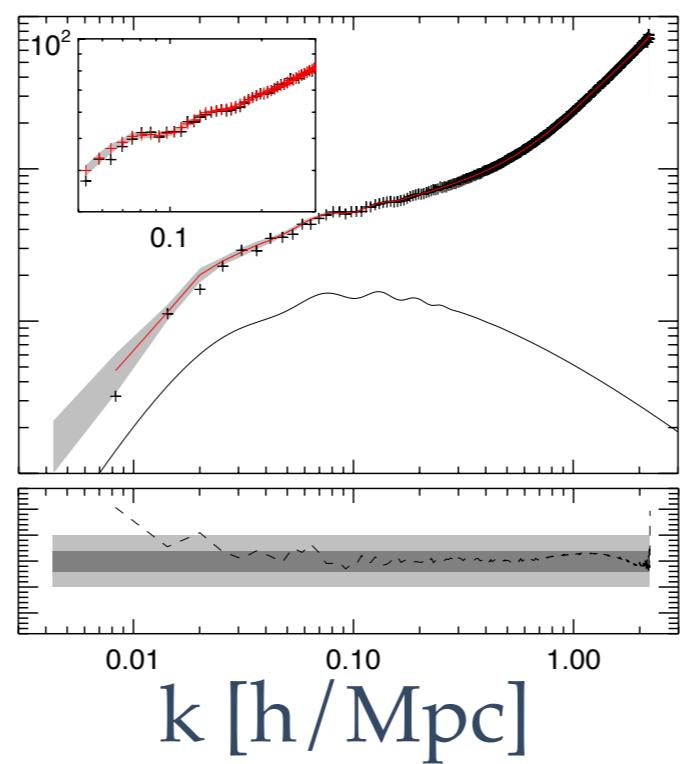
# Calibration with N-body simulations

*Kitaura, Yepes & Prada 2014, MNRAS*

real-space



redshift-space

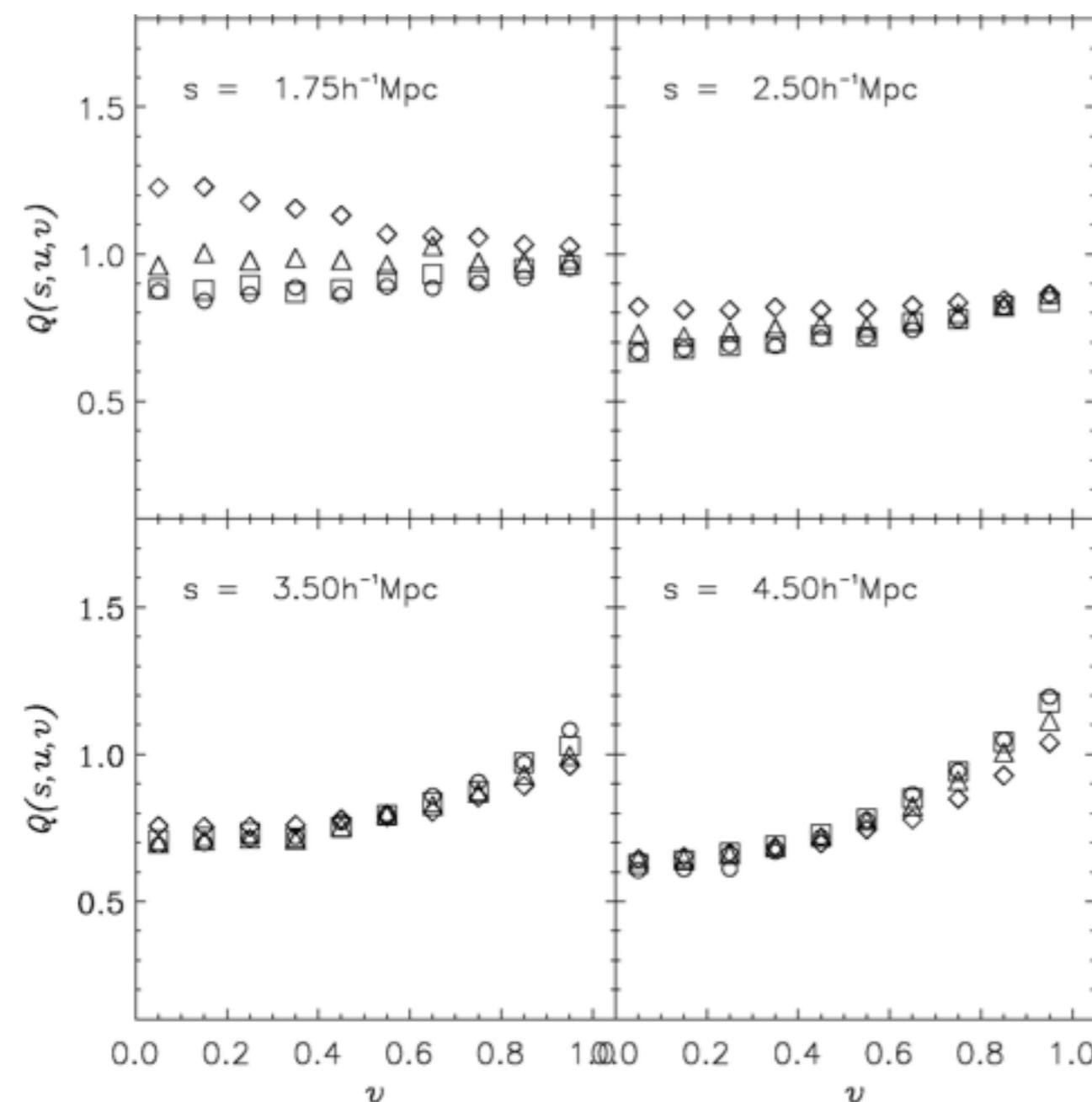


# Three-point function

*calculations by Volker Müller*

- ◊  $u=1.5$
- △  $u=2.5$
- $u=3.5$
- $u=4.5$

N-body

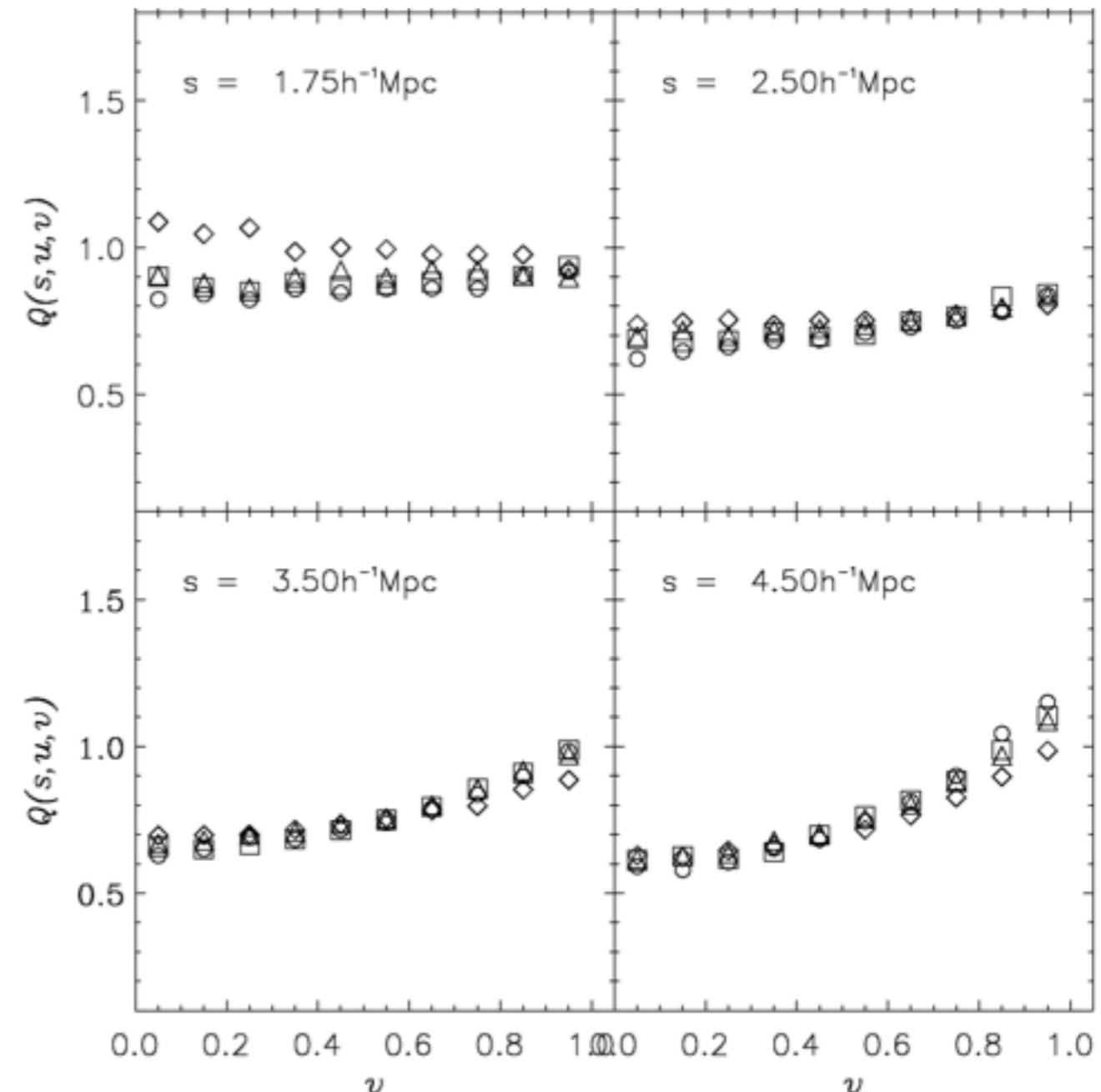


Triangle sides:  $s$ ,  $su$ , and  $s(u+v)$

The 3-point function is described by the hierarchical ansatz

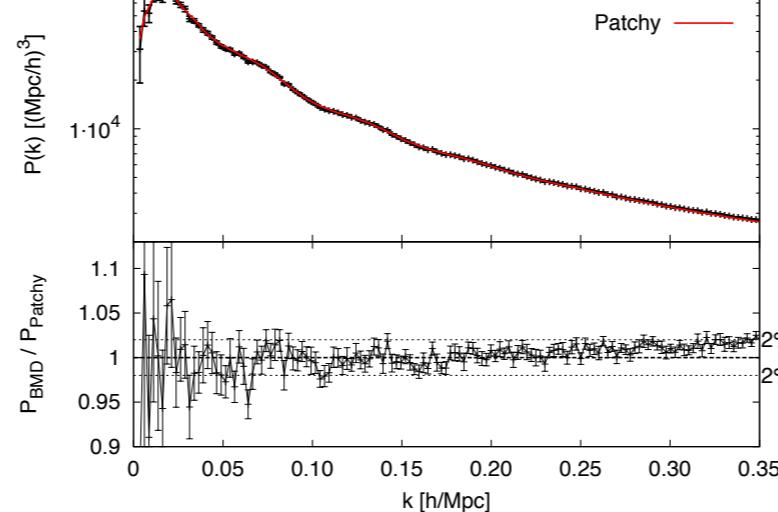
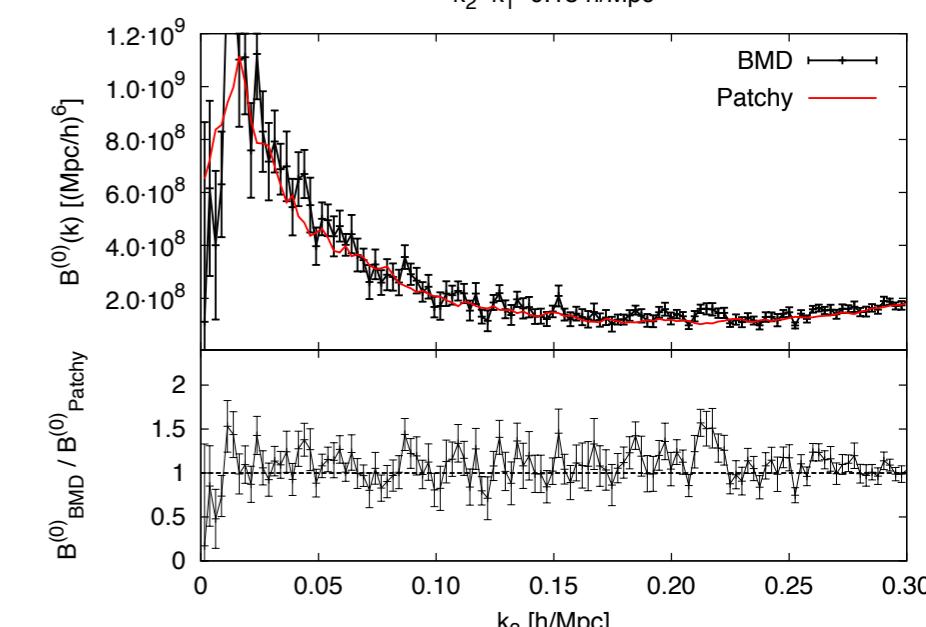
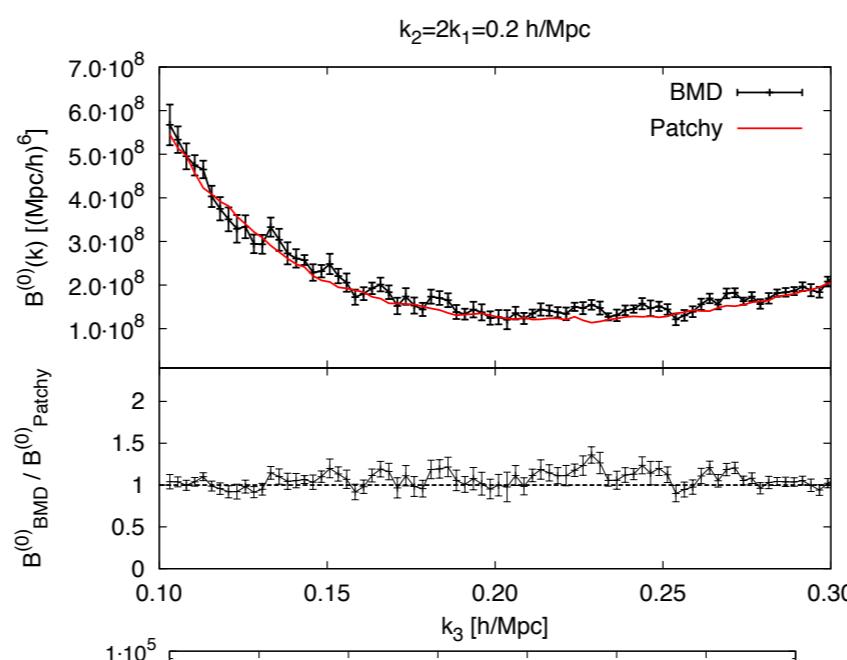
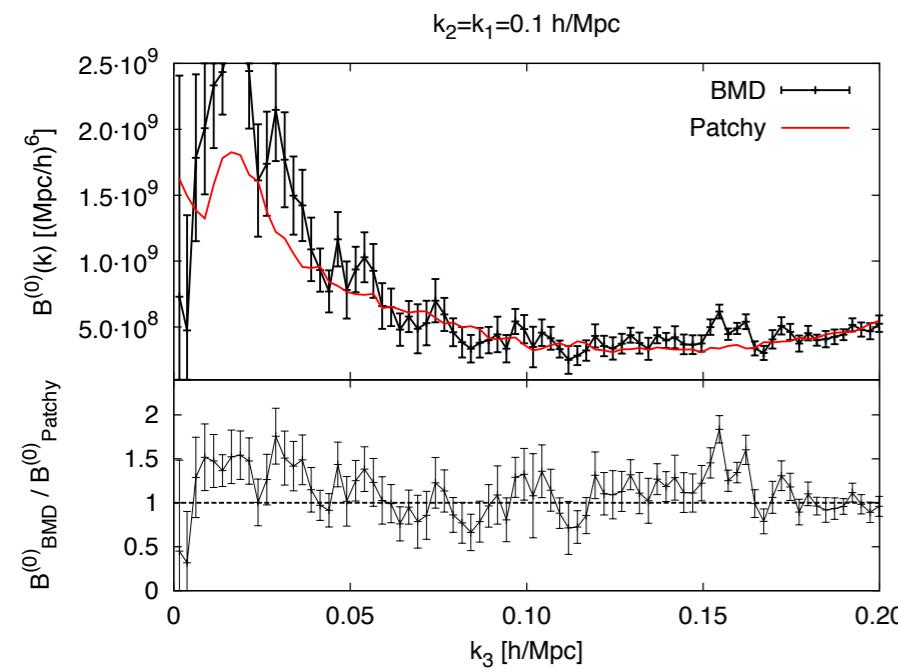
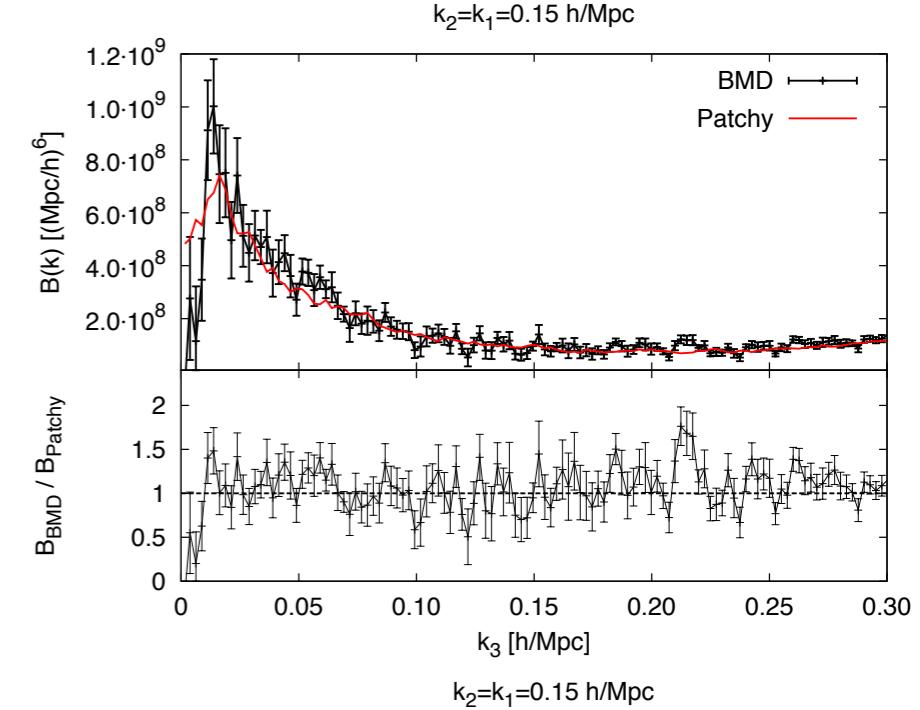
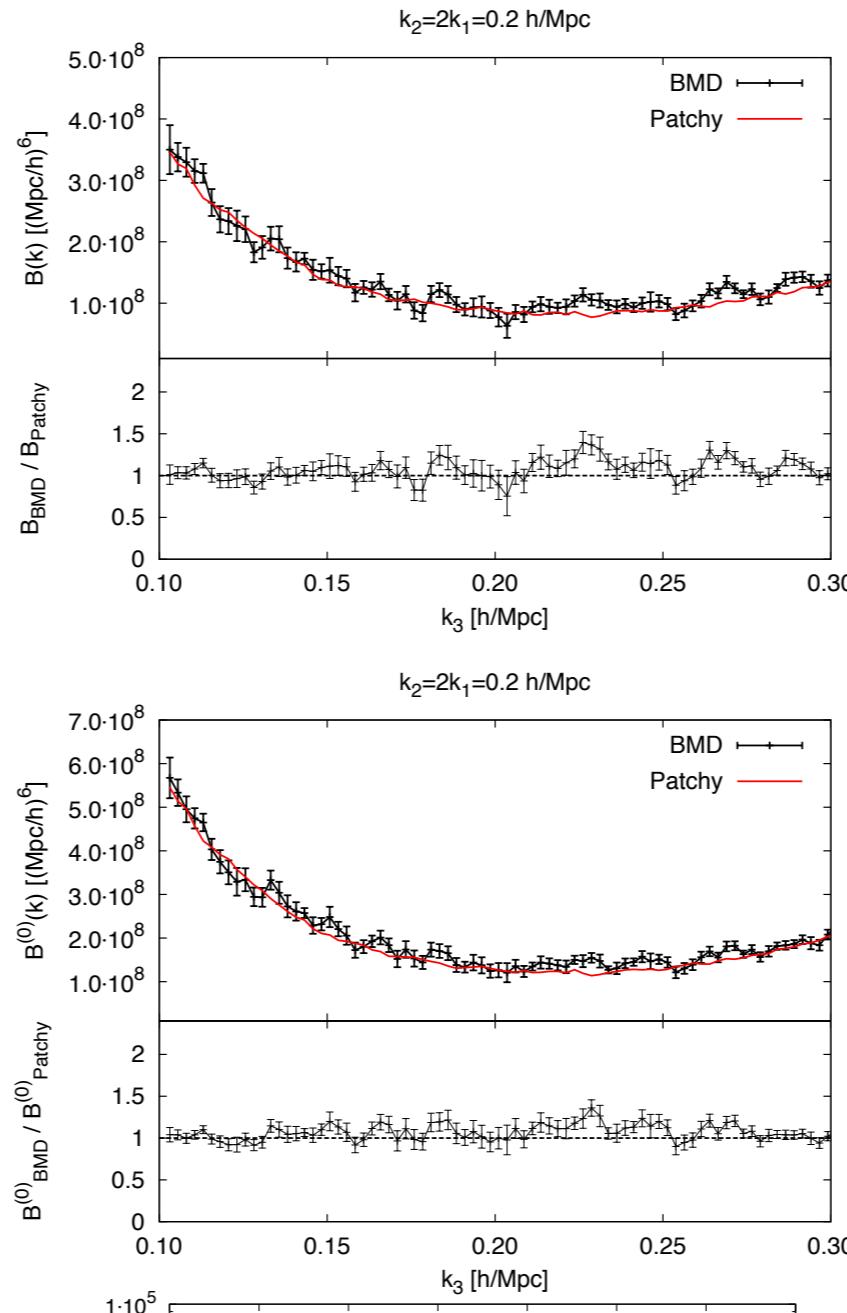
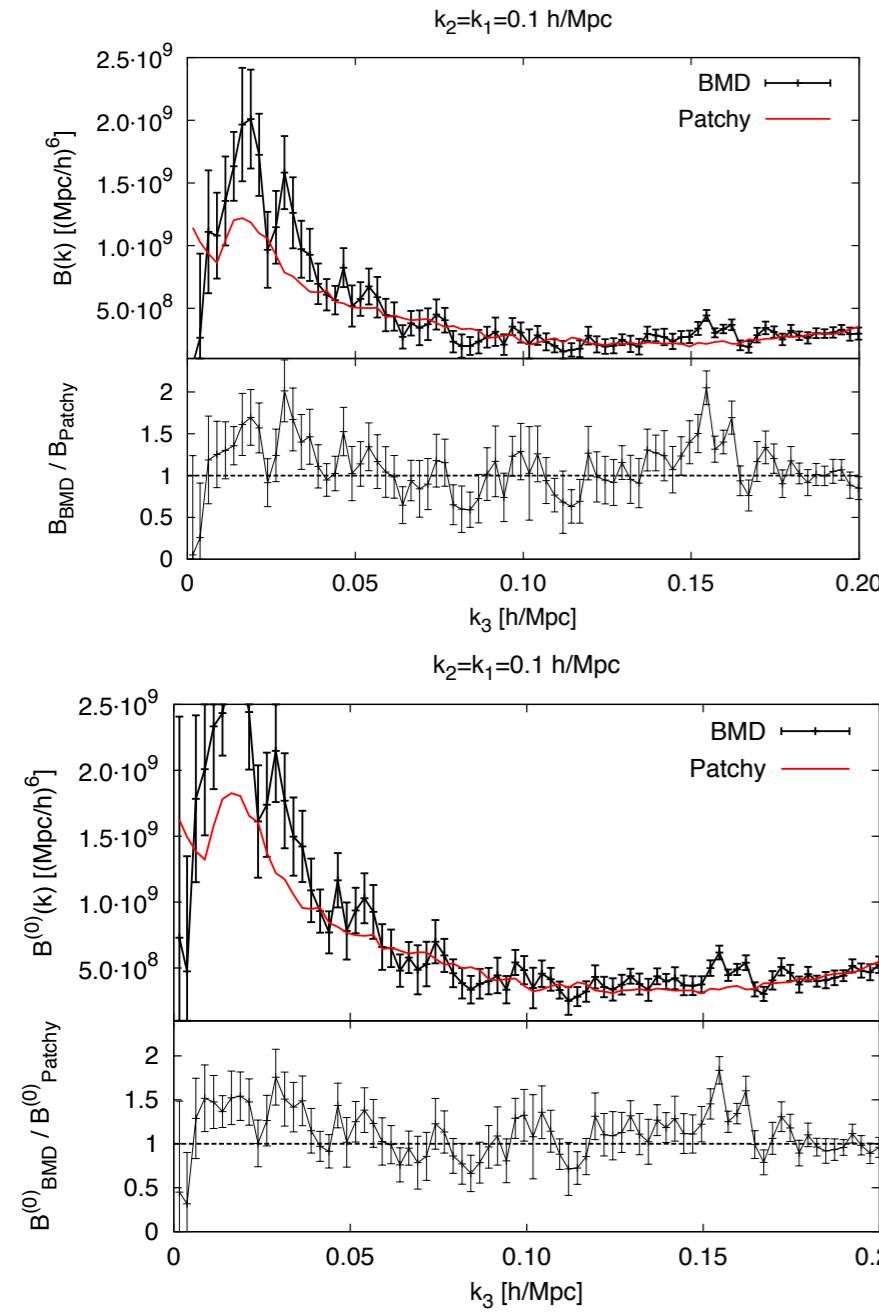
$Q(s,u,v) = (s,u,v)/(r_{12} r_{23}) + \text{c.c.}$ ,  
i.e. the increase from  $v=0$  to 1 means transition to linear structures.

ALPT in PATCHY



*calculations by Hector Gil-Marin*

# Bispectrum



# What parameters are found for LRGs?

$$\rho_h = f_h \theta(\rho_M - \rho_{th}) \rho_M^\alpha \exp\left[-\left(\frac{\rho_M}{\rho_\epsilon}\right)^\epsilon\right]$$

Why do LRGs have a constant linear bias of about 2?

mainly because they reside in the high density peaks!  
 $\rho_{th}$  and not  $\alpha$ !

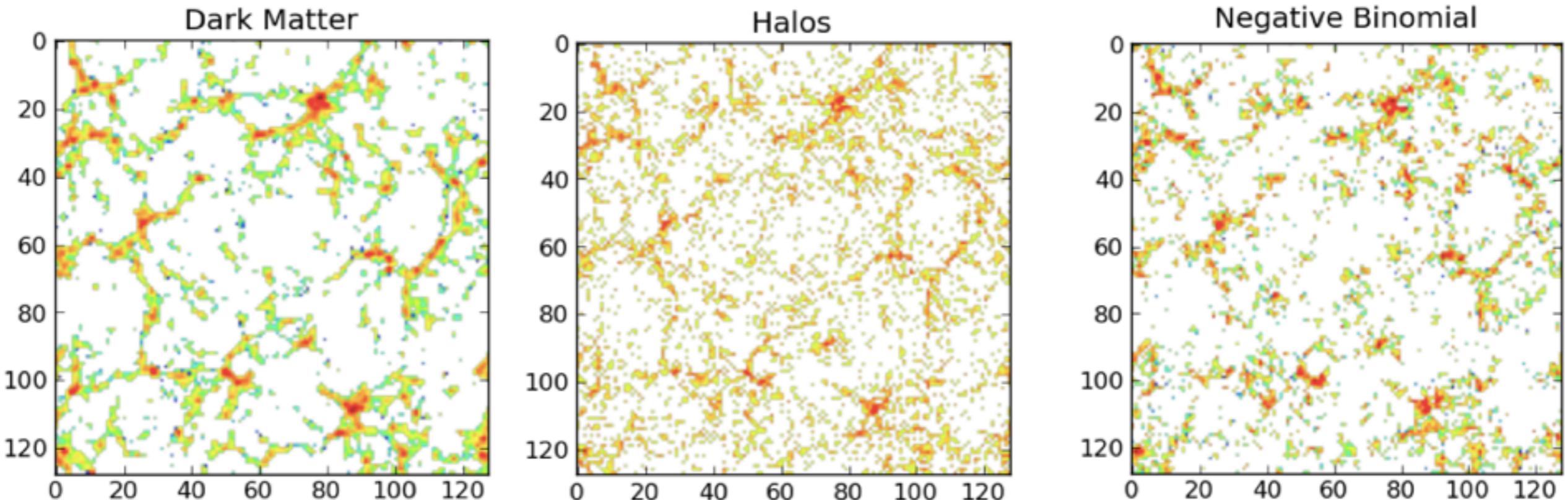
Can we apply such a stochastic  
nonlinear, scale-dependent biasing  
model for density reconstructions?

# Bayesian density reconstruction from biased galaxy data (e.g. eLGs)

$$\rho_h = f_h \theta(\rho_M - \rho_{\text{th}}) \rho_M^\alpha \exp \left[ - \left( \frac{\rho_M}{\rho_\epsilon} \right)^\epsilon \right]$$

*Ata, Kitaura & Müller in prep*

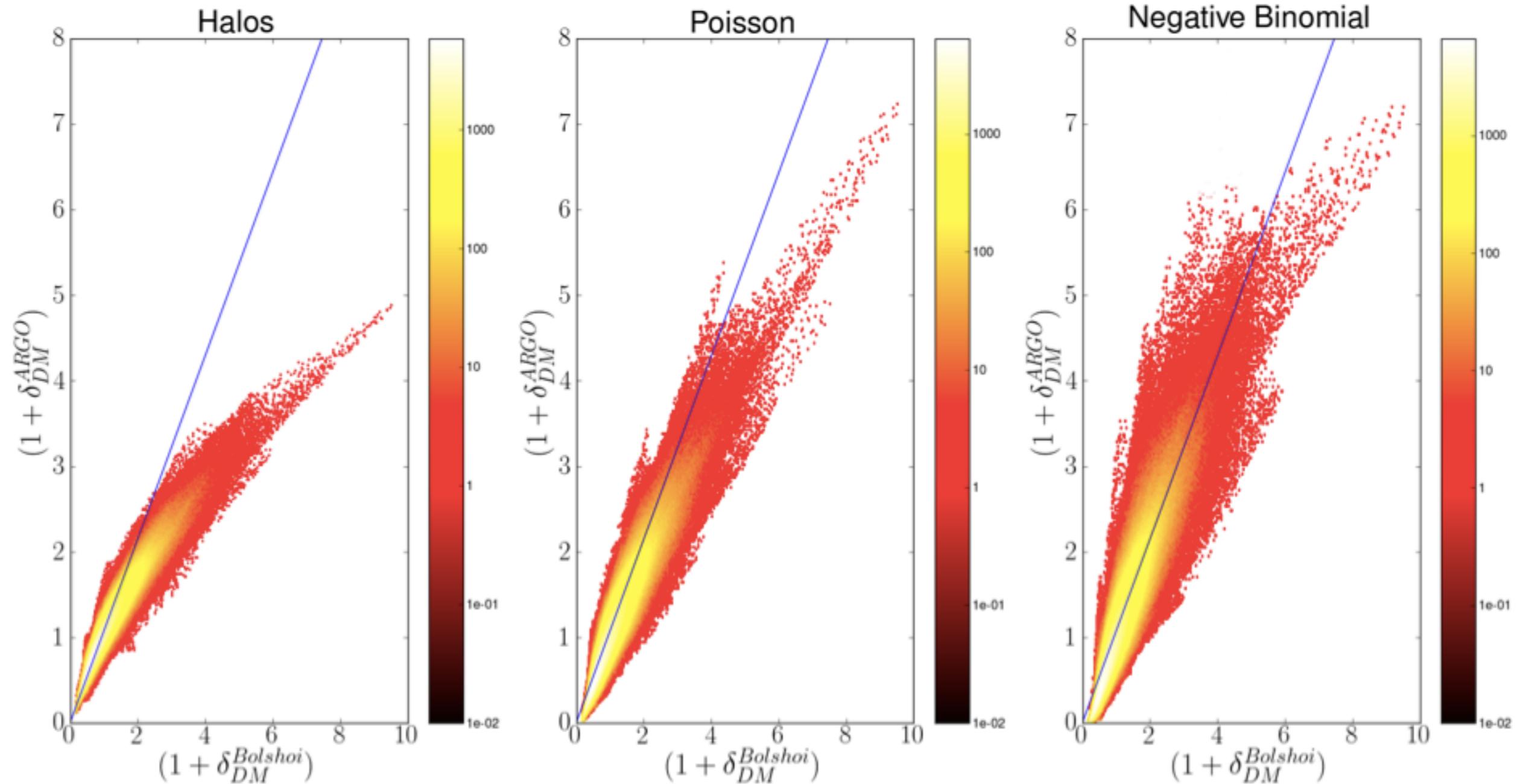
$$P(N_i | \lambda_i, \beta) = \frac{\lambda_i^{N_i}}{N_i!} \frac{\Gamma(\beta + N_i)}{\Gamma(\beta)(\beta + \lambda)^{N_i}} \frac{1}{(1 + \lambda/\beta)^\beta}$$



Bayesian approach with the ARGO-code

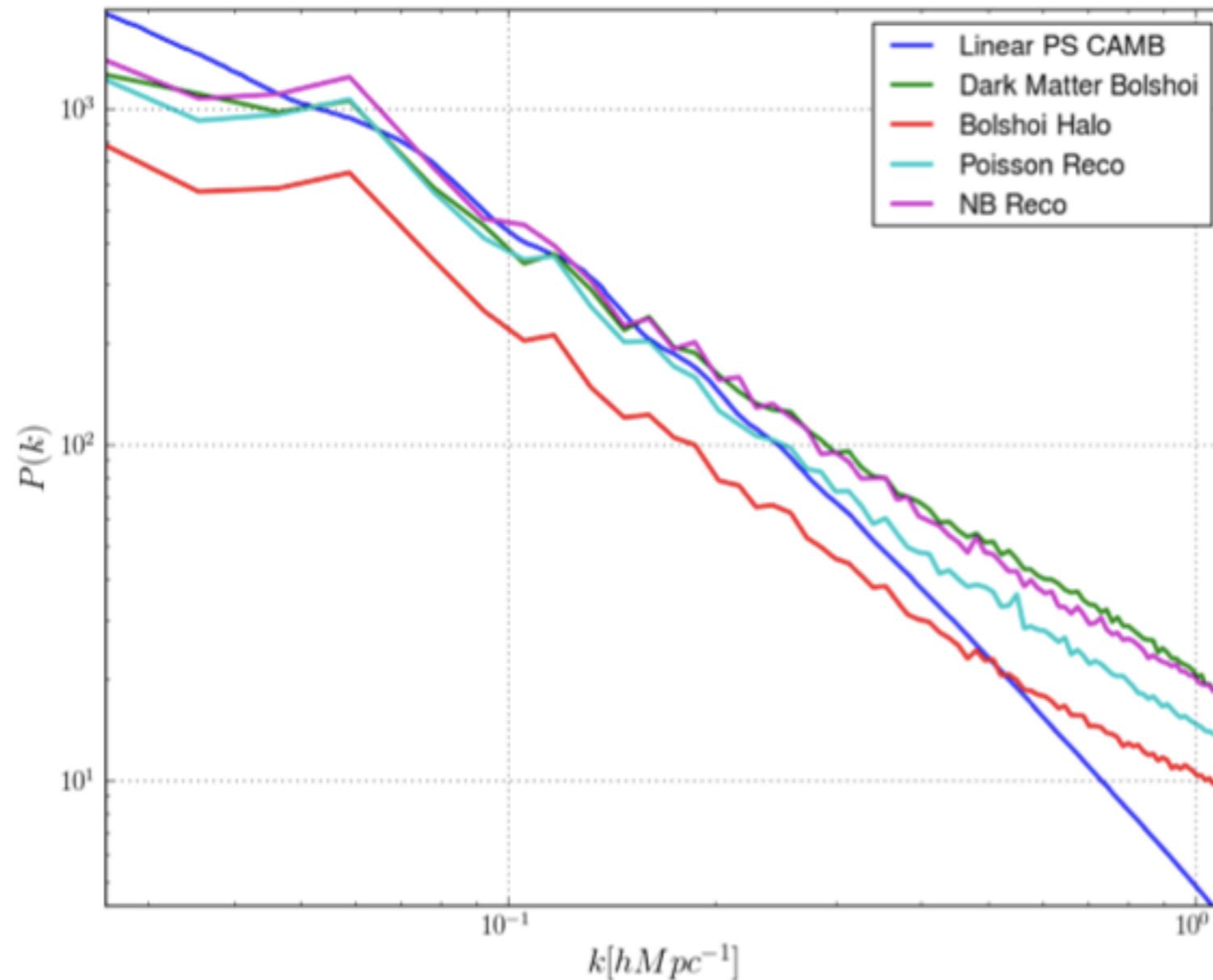
*Kitaura & Enßlin 2008; Kitaura et al 2010; Kitaura et al 2012*

# Bayesian density reconstruction from biased galaxy data (e.g. eLGs)



Ata, Kitaura & Müller in prep

# Bayesian density reconstruction from biased galaxy data (e.g. eLGs)



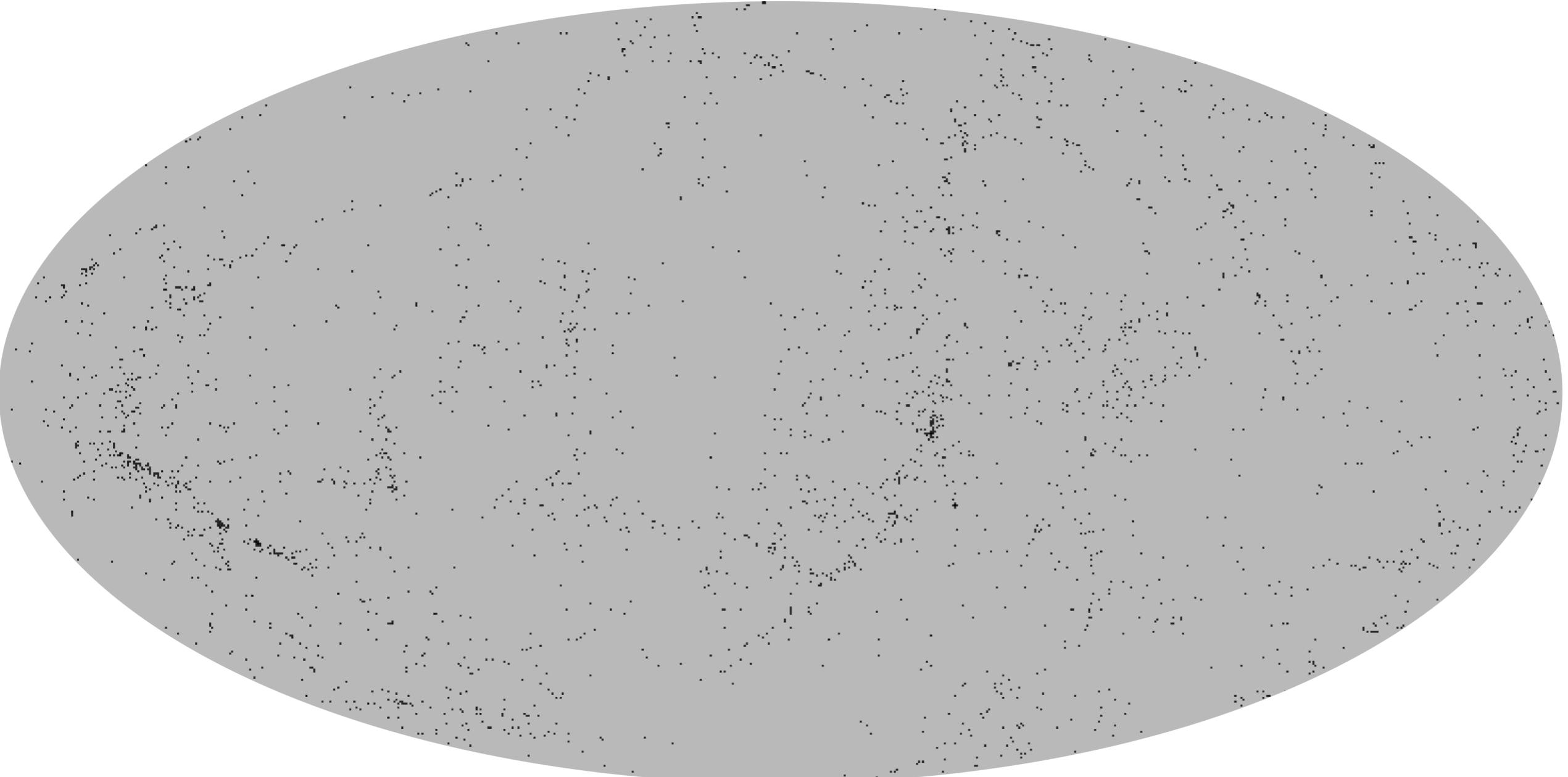
*Ata, Kitaura & Müller in prep*

# Conclusions

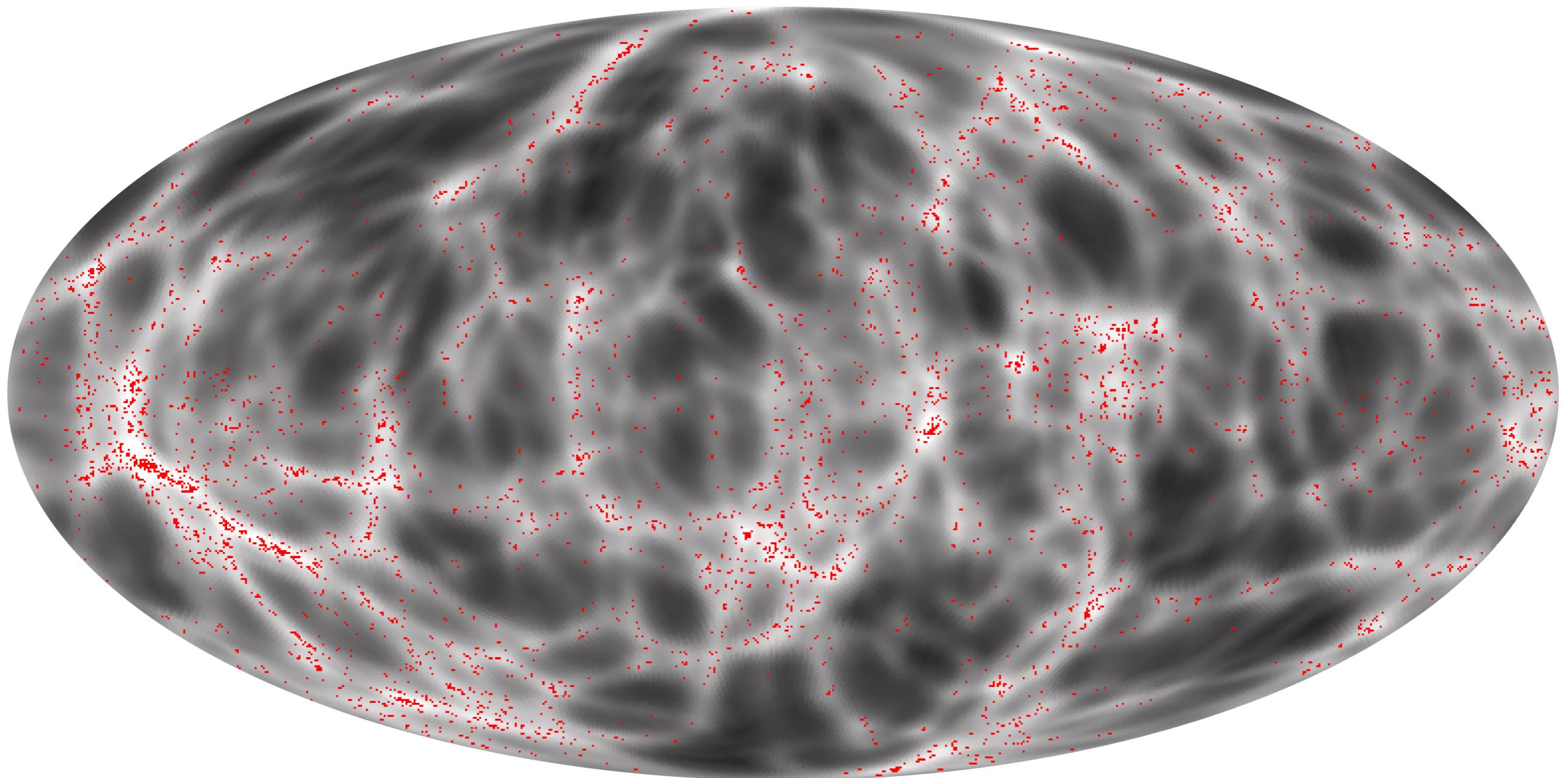
- Mock galaxy catalogs are necessary and important to test our theoretical models, estimate systematic errors/covariances, cosmic variance, etc
- Detailed state-of-the-art simulations are required (full gravity solvers, hydrodynamical simulations, feedback, etc.) to provide reference samples.
- We need thousands of mocks. → This cannot be done with full solvers!
- Approximate methods are required!
- There is a variety of methods: **PThalos, PINOCCHIO, PATCHY, QPM, COLA**.  
This is good!

Regarding PATCHY:

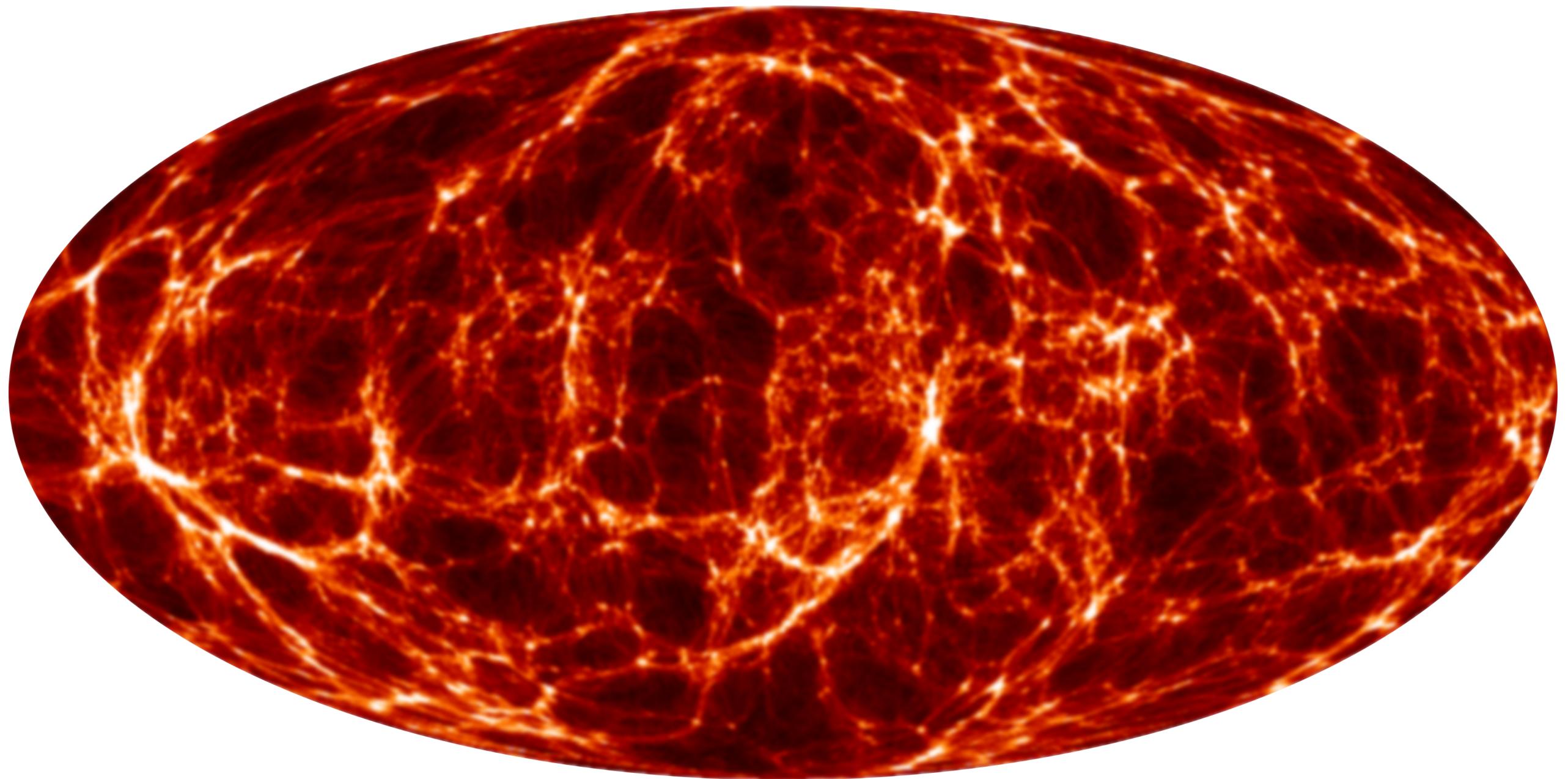
- We can efficiently model structure formation with Augmented Lagrangian Perturbation Theory → saves computational time
- We can use an effective statistical biasing description (nonlinear, stochastic, scale-dependent) → saves memory requirements (factor about 50)
- This statistical description can be used for Bayesian inference!
- We have done more than 1000 mocks for BOSS (Scoccola et al in prep)**
- PATCHY caveats: PDF still not perfectly fit; needs to be calibrated for each halo population from N-body simulations; not predictive!



real observations!



mean over an ensemble of ALPT reconstruction!



high resolution constrained N-body simulation!

# Modelling redshift space distortions

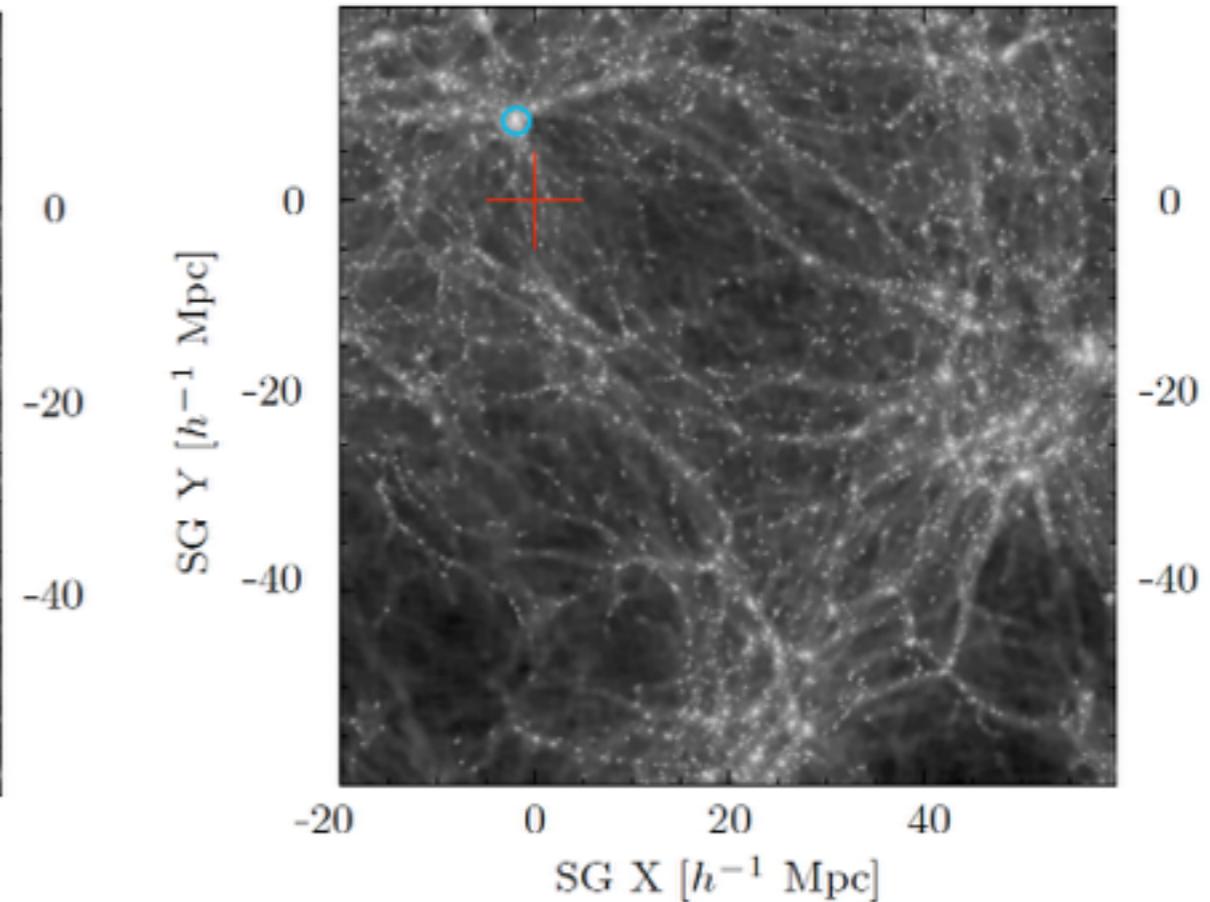
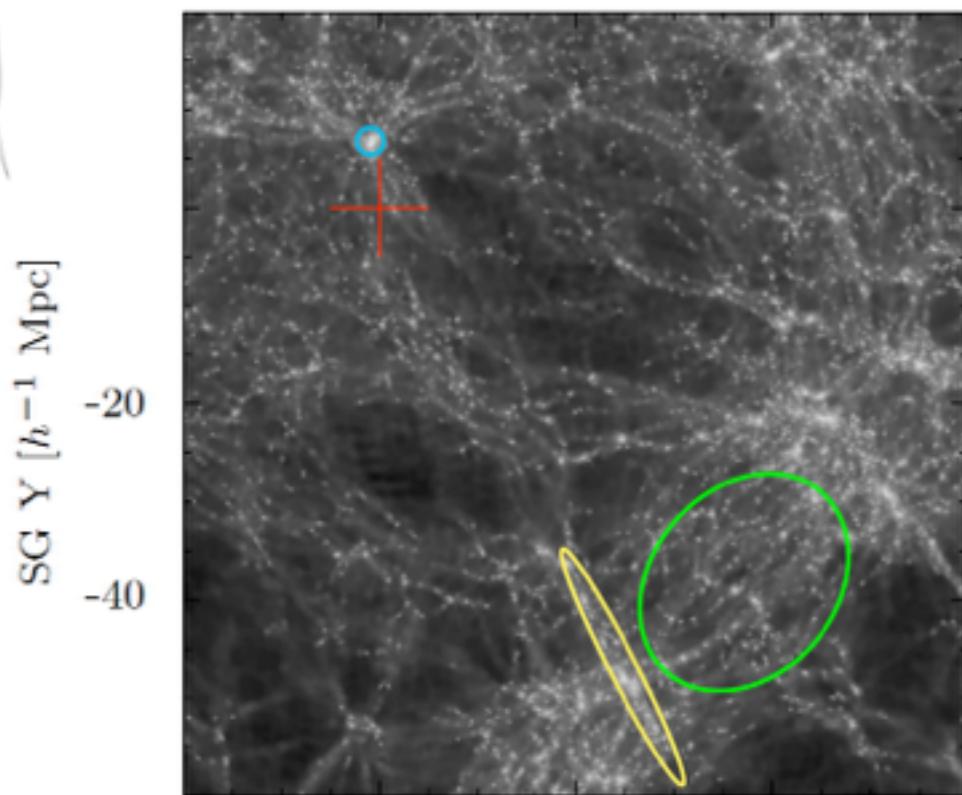
Kitaura F. S. PhD 2007 from MR sim (Hess & Kitaura in prep)

Kitaura, Yepes & Prada 2014, MNRAS

$$\mathbf{v} = \mathbf{v}^{\text{coh}} + \mathbf{v}^{\sigma}$$

$$\mathbf{v}_r^{\sigma} \equiv (\mathbf{v}^{\sigma} \cdot \hat{\mathbf{r}}) \hat{\mathbf{r}} / (Ha) = \mathcal{G} \left( g \times \left( 1 + b^{\text{ALPT}} \delta^{\text{ALPT}}(\mathbf{x}) \right)^{\gamma} \right) \hat{\mathbf{r}}$$

Application of KIGEN to 2MRS: constrained simulations



Left: constrained simulation based on 2LPT and compressed fogs

Right: constrained simulation based on ALPT modelling fogs