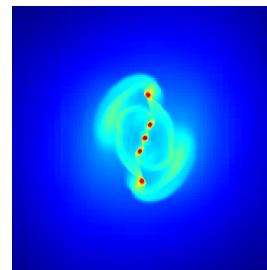
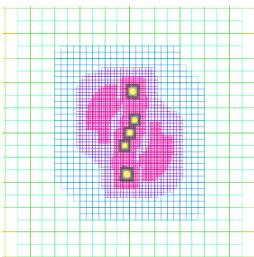


## Radiative and magnetic feedbacks on small scale collapse and fragmentation



**Commerçon Benoît**

Max Planck Institut fuer Astronomie, Heidelberg  
**Collaborators:** Patrick Hennebelle (LRA/ENS Paris),  
Gilles Chabrier (CRAL/ENS Lyon),  
Edouard Audit, Romain Teyssier (SAp,CEA Saclay)

## Outlines

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### 1. Introduction

### 2. Model

- Numerical method

### 3. Hydro collapse

- Fragmentation
- Entropy content

### 4. Magnetized collapse

- Moderate magnetic field
- First steps to synthetic observations

## Physics for star formation

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- Gravity: **Poisson equation**
- Hydrodynamics: **Euler equations**
- Radiative transfer: **Radiation hydrodynamics**
  - Barotropic EOS ( $T=f(\rho)$ )
  - Moment models: M1 (**HERACLES** code, González *et al.* 2007), Flux Limited Diffusion (FLD, e.g. Minerbo 1978)
- Magnetic field: **Magneto-Hydrodynamics**
  - Ideal
  - Ambipolar diffusion, Ohmic dissipation
- H<sub>2</sub> dissociation
- Chemistry
- Etc .....

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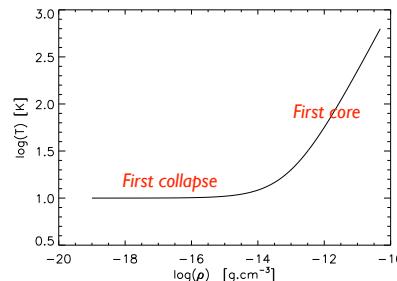
## Approximate radiative transfer

⇒ Barotropic EOS

2 regimes: isotherm and adiabatic

$$\frac{P}{\rho} = c_s^2 = c_0^2 \left[ 1 + \left( \frac{\rho}{\rho_c} \right)^{2/3} \right] \propto \rho^{\gamma-1}$$

- $\gamma_{\text{eff}} = 1$  if  $\rho \ll \rho_c \rightarrow \text{ISOTHERM}$
- $\gamma_{\text{eff}} = 5/3$  if  $\rho \gg \rho_c \rightarrow \text{ADIABATIC}$



⇒ Grey Flux Limited Diffusion

Optically thick (mean free path << L<sub>sys</sub>) ==> diffusion approximation:  $P_r = 1/3 E_r \partial_t F_r = 0$

==> Solve a diffusion equation on the radiative energy:

$$\frac{\partial E_r}{\partial t} - \nabla \cdot \left( \frac{c\lambda}{\rho\kappa_R} \nabla E_r \right) = \kappa_P \rho (4\pi B - cE_r)$$

Flux limiter (e.g. Minerbo 78)

## Flux Limited Diffusion in RAMSES

- ✓ **RAMSES code** (Teyssier 2002): 2nd order Godunov scheme, Adaptive Mesh Refinement, ideal MHD (Fromang et al. 2006)

- ✓ **RHD solver in the comoving frame using the grey Flux Limited Diffusion approximation** (Commerçon et al., submitted):

$$\begin{cases} \partial_t \rho + \nabla [\rho \mathbf{u}] = 0 \\ \partial_t \rho \mathbf{u} + \nabla [\rho \mathbf{u} \otimes \mathbf{u} + (P + 1/3E_r)\mathbb{I}] = -(\lambda - 1/3)\nabla E_r \\ \partial_t E_T + \nabla [\mathbf{u}(E_T + P + 1/3E_r)] = -(\lambda - 1/3)\nabla(\mathbf{u}E_r) + \nabla \cdot \left( \frac{c\lambda}{\rho\kappa_R} \nabla E_r \right) \\ \partial_t E_r + \nabla [\mathbf{u}E_r] = -\mathbb{P}_r : \nabla \mathbf{u} + \kappa_P \rho c (a_R T^4 - E_r) + \nabla \cdot \left( \frac{c\lambda}{\rho\kappa_R} \nabla E_r \right) \end{cases}$$

Riemann solver - explicit      Corrective terms - explicit      Coupling + Diffusion - implicit

- ✓ **Largest fan of solution with speeds:** 
$$\begin{cases} u - \sqrt{\frac{\gamma P}{\rho} + \frac{4E_r}{9\rho}} \\ u \\ u + \sqrt{\frac{\gamma P}{\rho} + \frac{4E_r}{9\rho}} \end{cases}$$

- ✓ **Implicit solved with an iterative conjugate gradient algorithm**

- ✓ Linearize emission term  $(T^{n+1})^4 = 4(T^n)^3 T^{n+1} - 3(T^n)^4$

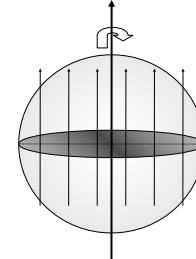
## Initial conditions

$1 M_{\odot}$  isolated dense core: uniform density and temperature (10 K), solid body rotation ( $\beta = E_{\text{rot}}/E_{\text{grav}}$ ),  $m=2$  density perturbation (amplitude 10%)  
==> Small-scale fragmentation

★ Ideal MHD <=> flux freezing:  $\varphi \propto BR^2$   
Magnetic field lines are twisted and compressed:

==> Outflow (e.g. Machida et al., Banerjee & Pudritz 06, Hennebelle & Fromang 08)

$\mu = (\varphi/M)_{\text{crit}} / (\varphi/M)$  (observations  $\mu \sim 2-5$ )



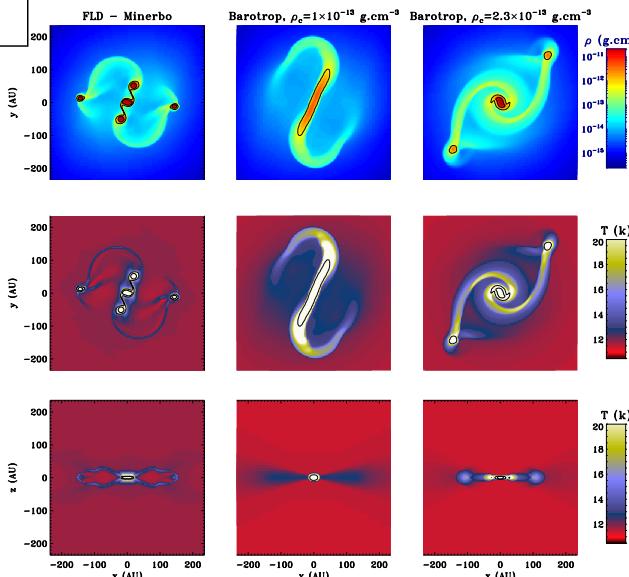
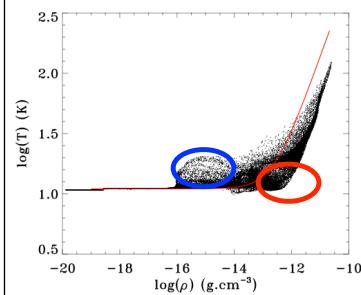
★ Radiative transfer: efficient cooling (Attwood et al. 09) and heating (Krumholz et al. 09, Bate 09). Grey opacities from Semenov et al. 03.

## Radiation-HydroDynamics calculations

$$\alpha = 0.50, \beta = 0.04, m=2, A=0.1$$

**FLD:** more fragments, gas cools efficiently in the vertical direction

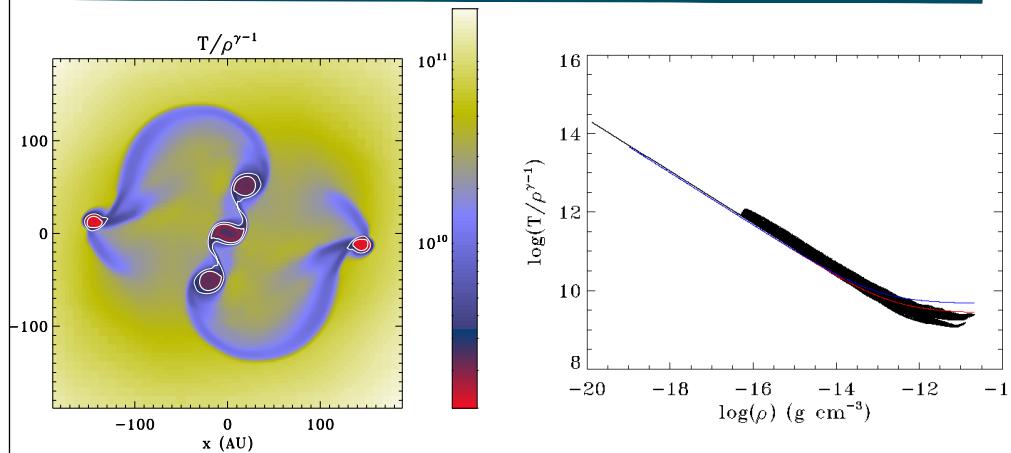
==> lower Jeans mass



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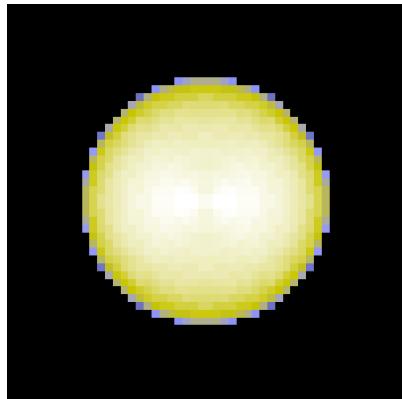
## Radiation-HydroDynamics calculations



Entropy content of the fragments depends on their location and time of formation. This may have a strong influence for the PMS evolution (entropy sets the radius)

## Radiation-HydroDynamics calculations

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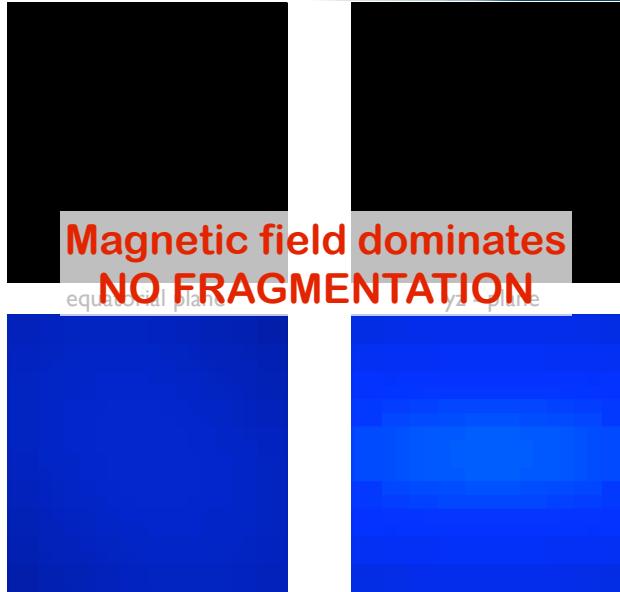
But dense core are **magnetized** (e.g *Heiles & Crutcher 2005*)

+ Magnetic field **inhibits** fragmentation (*Hennebelle & Teyssier 2008*)

=> Does the efficient cooling found with the FLD helps to fragment in presence of a magnetic field?

## Moderate magnetized case, $\mu=5$ , RMHD

Temperature



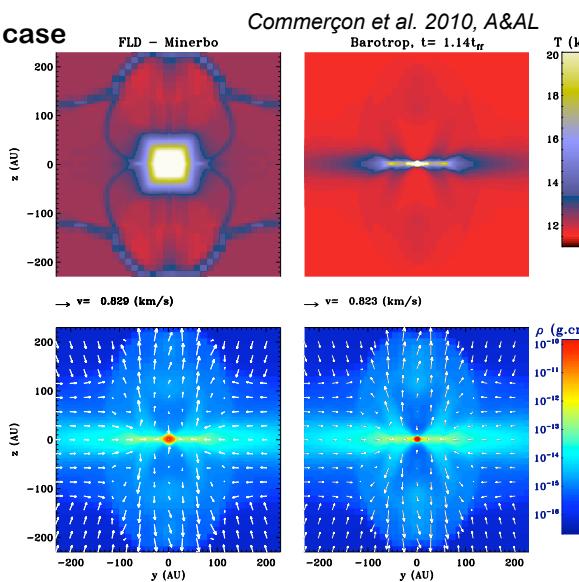
Density

## Moderate magnetized case, $\mu=5$ , RMHD

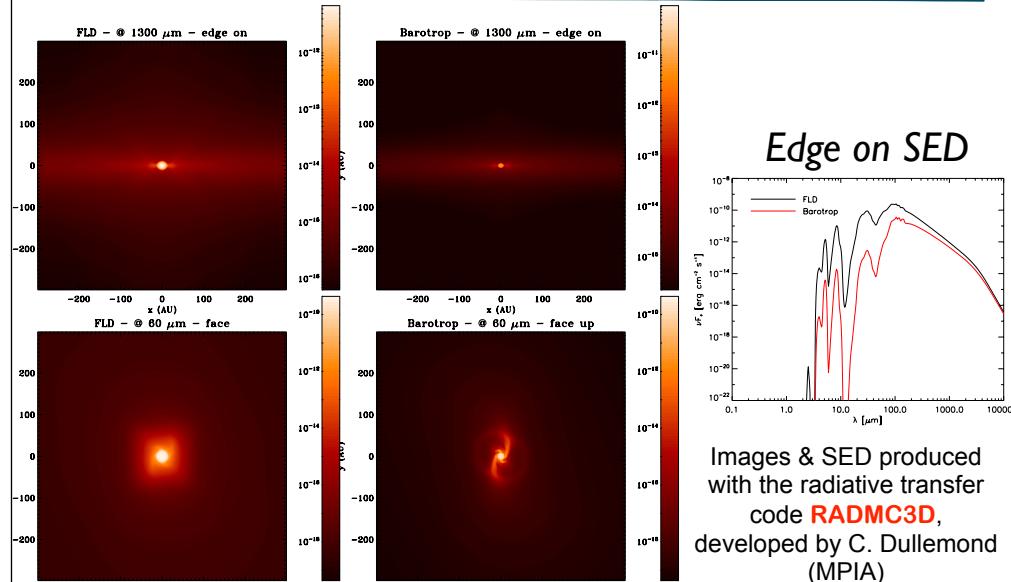
### Comparison to the barotropic case

- Density set by magnetic field
- Similar outflow velocity
- Significant differences in the temperature distribution

<=> observations



## Dust continuum emission maps & SED



Images & SED produced  
with the radiative transfer  
code **RADMC3D**,  
developed by C. Dullemond  
(MPIA)

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## Conclusion & prospects

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- Radiation-Magneto-Hydrodynamic solver with **AMR**
- First** full RMHDs calculations of dense core collapse at small scales (see also **Tomida** poster)
- Entropy of the first cores different => 2<sup>nd</sup> collapse?
- Magnetic field **inhibits** small-scale fragmentation, even with radiative transfer
- Magnetic braking **favors** radiative feedback (see *Commerçon et al. 2010*)
- ★ Effect of the angle rotational axis/magnetic field (*Hennebelle & Ciardi 2009*)?
- ★ Synthetics maps and SED for **HERSCHEL** and **ALMA** prediction (waiting for data of first cores!)
- ★ Combined effect of magnetic field and radiative feedback in massive star formation?

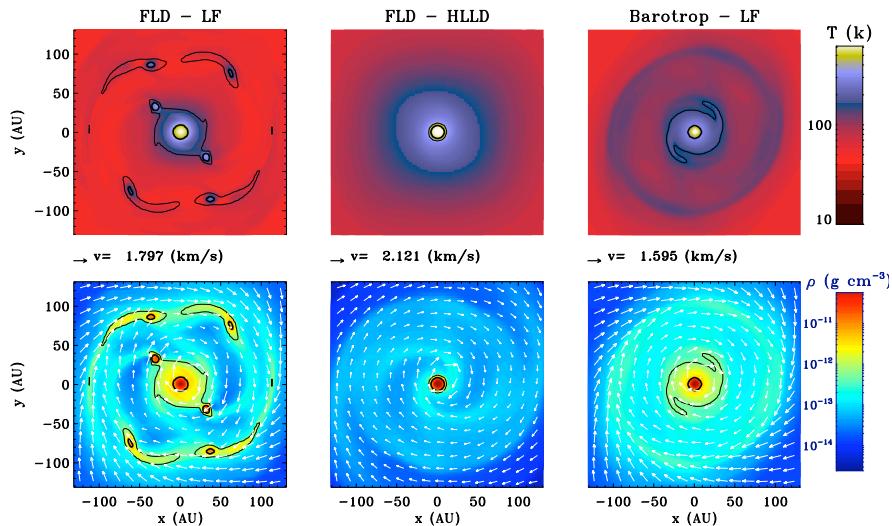
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# **THANK YOU**

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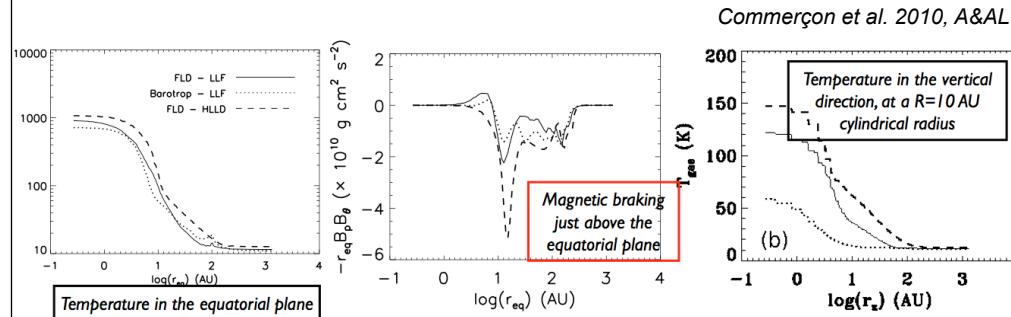
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## Intermediate case, $\mu=20$ - Numerical issue



Commerçon et al. 2010, A&AL

## Intermediate case, $\mu=20$ - Numerical issue



- ✓ **Diffusivity** of the solver => 2 effects that favor fragmentation:
  - inefficient magnetic braking
  - more massive disk
- ✓ Radiative feedback depends on the magnetic braking:  $L_{\text{acc}} \propto V_{\text{inf}}^3$  (**supercritical radiative shock**)!