

High Precision Foreground Modeling Using Current And Future Multi-frequency Microwave Maps

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Motivation:

- **Conventional methods** rely on **simple parametrizations** of different **foreground** components or are **blind (variance minimization)**.
- For B-mode and spectral distortions measurements we are entering a “new era” : No signal dominated channels! **Will these methods work as well?**
 - **Yes!** Are we sure? Are we using sufficiently realistic simulations for foregrounds? How might we generate more realistic simulations?
 - **No!** We need new techniques for modeling foregrounds !

Outline:

- What are moments? **J. Chluba, J. C. Hill & M. H. Abitbol, MNRAS, Vol. 472, Iss. 1, 1195-1213**
- An example demonstrating bias in inferred cosmology.
- How well in-principle can we do with moment expansions?
- Measuring moments from Planck maps.

Scope

Moments are new observables

Signals

Foregrounds

Separations methods

Parametric

Non-Parametric

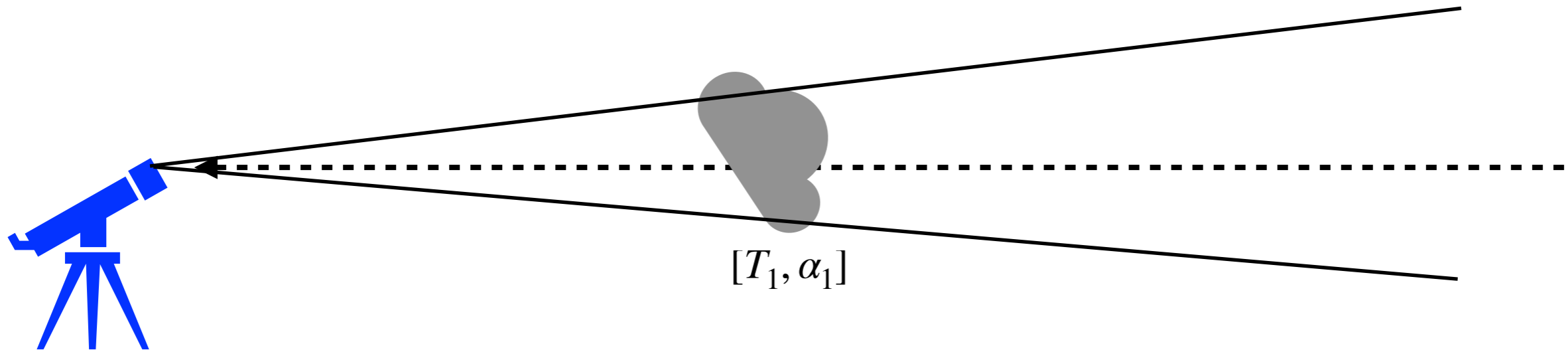
New foreground cleaning method

Connection between parametric and non-parametric methods?

Observers assumption (current)

Each cloud emits a modified black body spectrum.

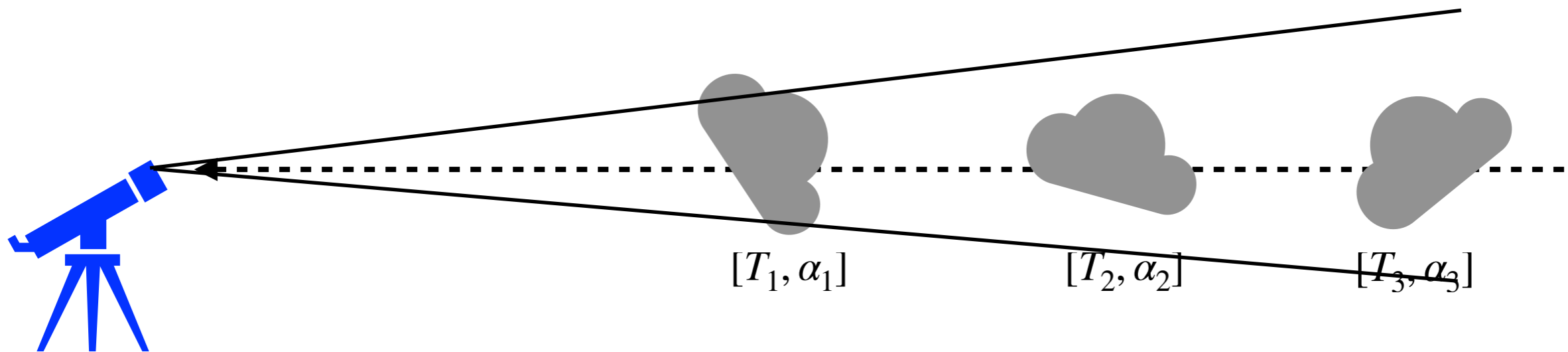
$$B_\nu(\alpha, T) = A \frac{2h\nu^3}{c^2} \left(\frac{\nu}{\nu_0} \right)^\alpha \frac{1}{e^{\frac{h\nu}{kT}} - 1}$$



Nature

Each cloud emits a modified black body spectrum.

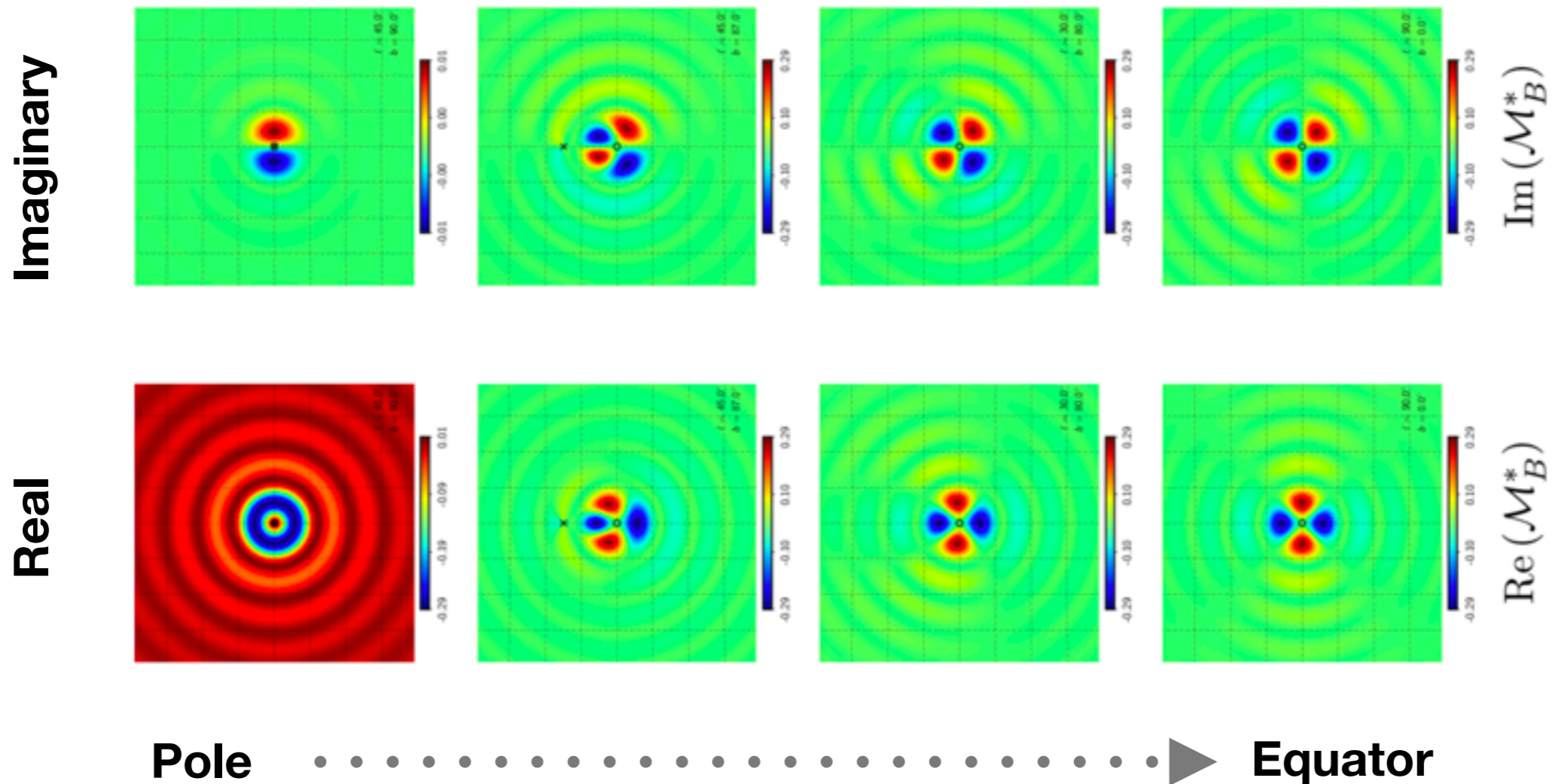
$$B_\nu(\alpha, T) = \frac{2h\nu^3}{c^2} \left(\frac{\nu}{\nu_0} \right)^\alpha \frac{1}{e^{\frac{h\nu}{kT}} - 1}$$



$$S_\nu = \int \frac{dI}{ds} ds \neq B_\nu(\alpha', T')$$

An un-avoidable averaging in Polarization analysis

Complex real space beam : Q/U \rightarrow E/B



What are moments?

Describing SED resulting from sum of modified black bodies:

$$S_\nu = \int \frac{dI}{ds} ds = \int B_\nu(\alpha, T) P(\alpha, T) d\alpha dT$$

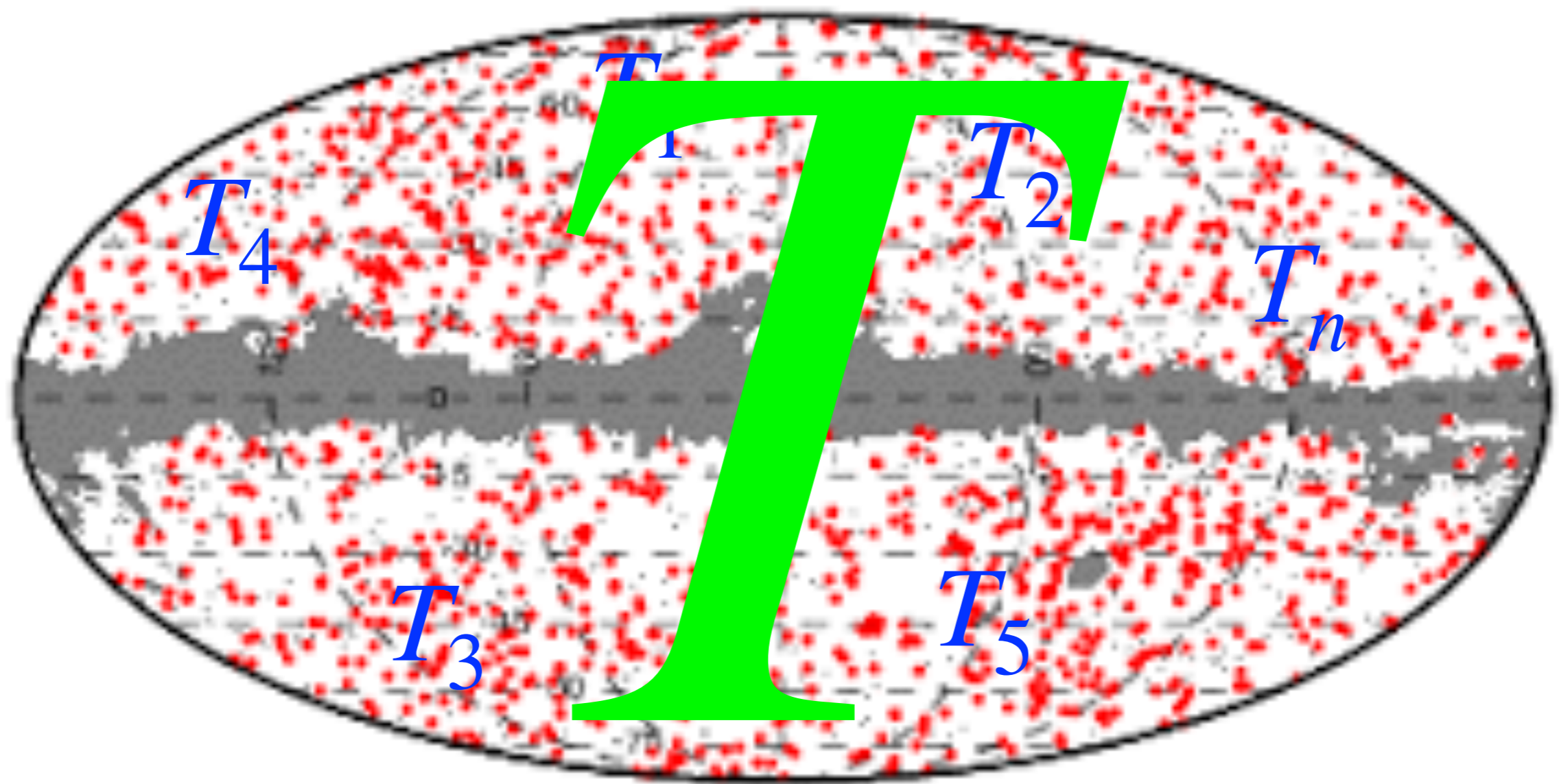
Building on top of the simple parametrization:

$$S_\nu = \sum_{m,n} \partial_\alpha^m \partial_T^n B_\nu(\alpha_0, T_0) \int (\alpha - \alpha_0)^m (T - T_0)^n P(\alpha, T) d\alpha dT$$

Moments of the distribution function

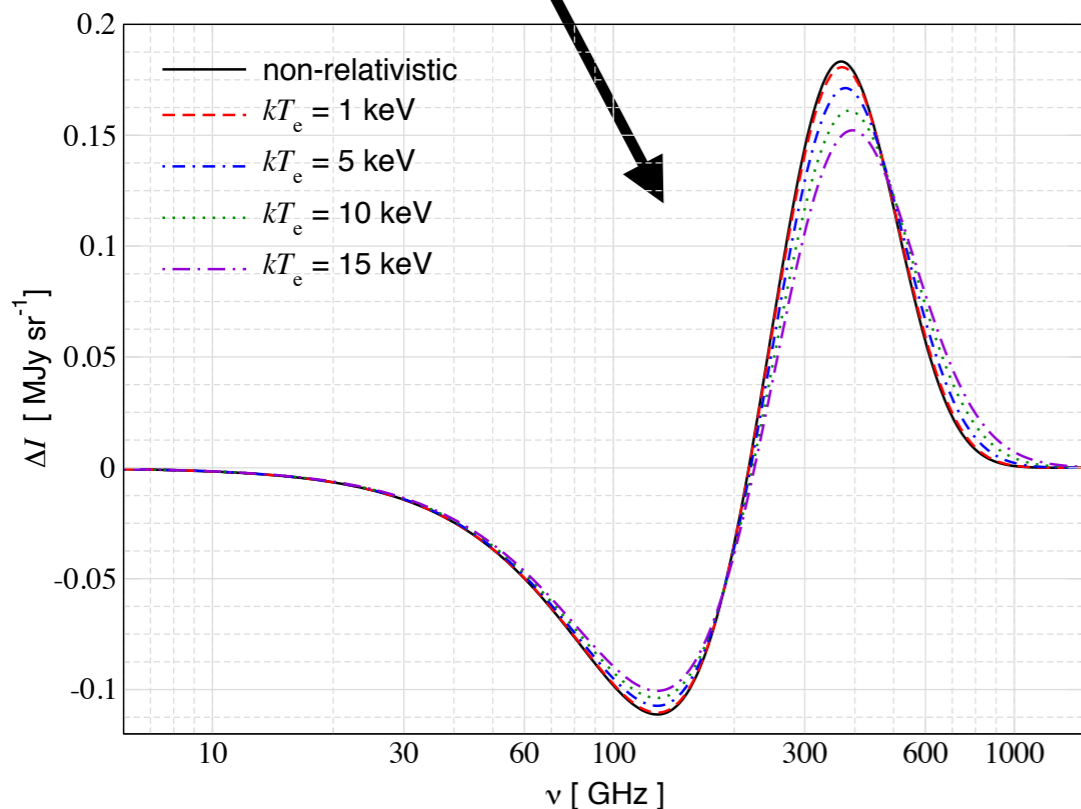
$$\begin{aligned} S_\nu(\alpha_0, T_0, A, p_\alpha, p_T, p_{\alpha\alpha}, p_{\alpha T}, p_{TT}, \dots) &\simeq AB_\nu(\alpha_0, T_0) \\ &+ p_\alpha \partial_\alpha B_\nu(\alpha_0, T_0) + p_T \partial_T B_\nu(\alpha_0, T_0) \\ &+ p_{\alpha\alpha} \partial_\alpha^2 B(\alpha_0, T_0) + p_{\alpha T} \partial_\alpha \partial_T B(\alpha_0, T_0) + p_{TT} \partial_T^2 B(\alpha_0, T_0) \\ &+ \dots \end{aligned}$$

Moments in the thermal SZ analysis

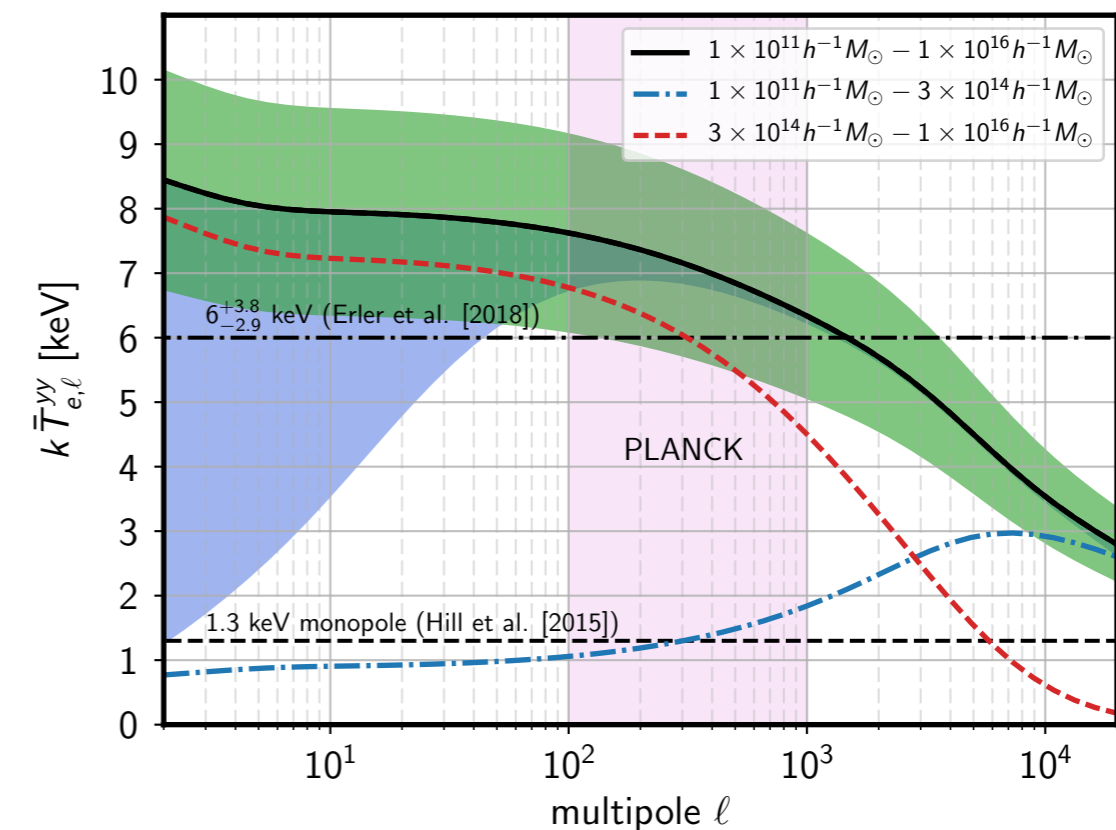


Moments in the thermal SZ analysis

$$y^{tSZ}(\nu, \hat{n}) = Y_{(0)}(\nu, \bar{T})y(\hat{n})$$



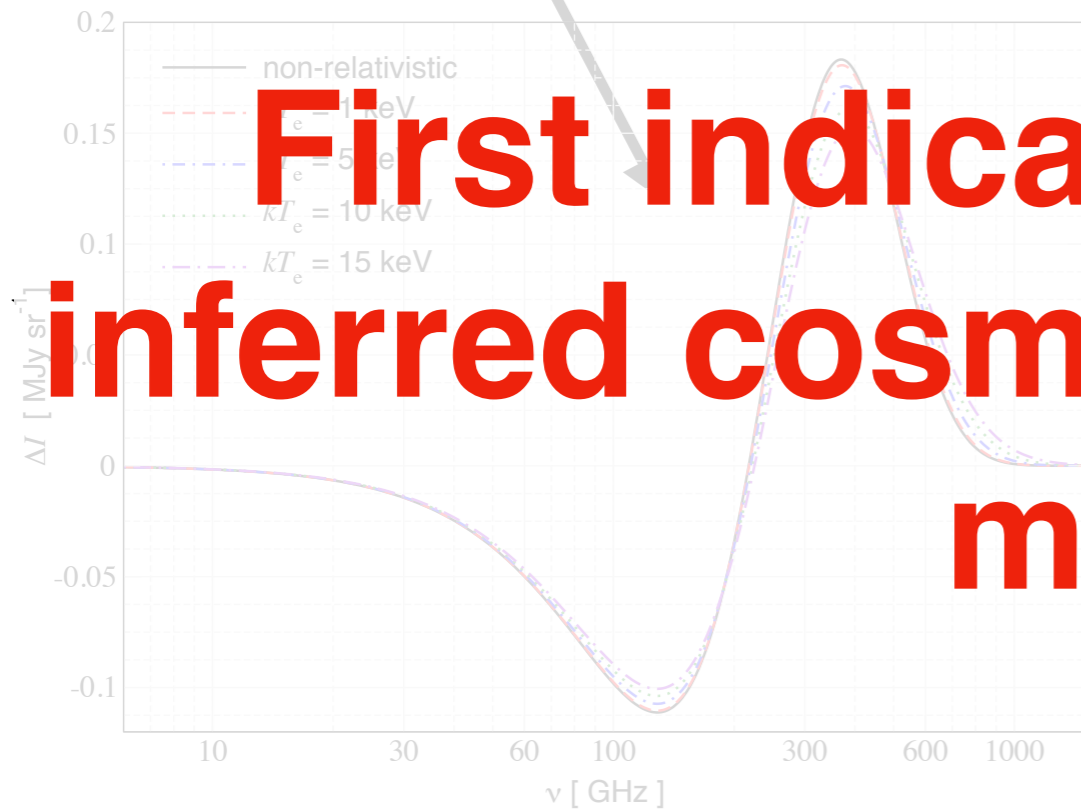
Effective change in the amplitude of the matter power spectrum for **Planck**



$$\Delta\sigma_8/\sigma_8^* \simeq 0.019 \left[\frac{k\bar{T}_e}{5 \text{ keV}} \right]$$

Moments in the thermal SZ analysis

$$y^{SZ}(\nu, \hat{n}) = Y_{(0)}(\nu, \bar{T})y(\hat{n}) + \sum_{i=1}^{N(\hat{n})} \frac{Y_{(i)}(\nu, \bar{T})(T_c(\hat{n}) - \bar{T})^i}{i!} y(\hat{n}) \Rightarrow k\bar{T}_{e,l}^{yy} = \frac{\langle kT_e(M, z) |y_\ell|^2 \rangle}{\langle |y_\ell|^2 \rangle} = \frac{C_l^{T_e,yy}}{C_l^{yy}}$$



First indications of biases in inferred cosmology from ignoring moments!



Effective change in the amplitude of the matter power spectrum for **Planck**

$$\Delta\sigma_8/\sigma_8^* \simeq 0.019 \left[\frac{k\bar{T}_e}{5 \text{ keV}} \right]$$

Measuring moments

Spectro-Spatial

$$S_\nu(\alpha_0, T_0, A, p_\alpha, p_T, p_{\alpha\alpha}, p_{\alpha T}, p_{TT}, \dots) = \vec{B}_{\nu i}(\alpha_0, T_0) \mathcal{M}_i + \epsilon_i$$



Think of this as a multi-parameter function: **optimize for the best fit parameters** given some measured SED!

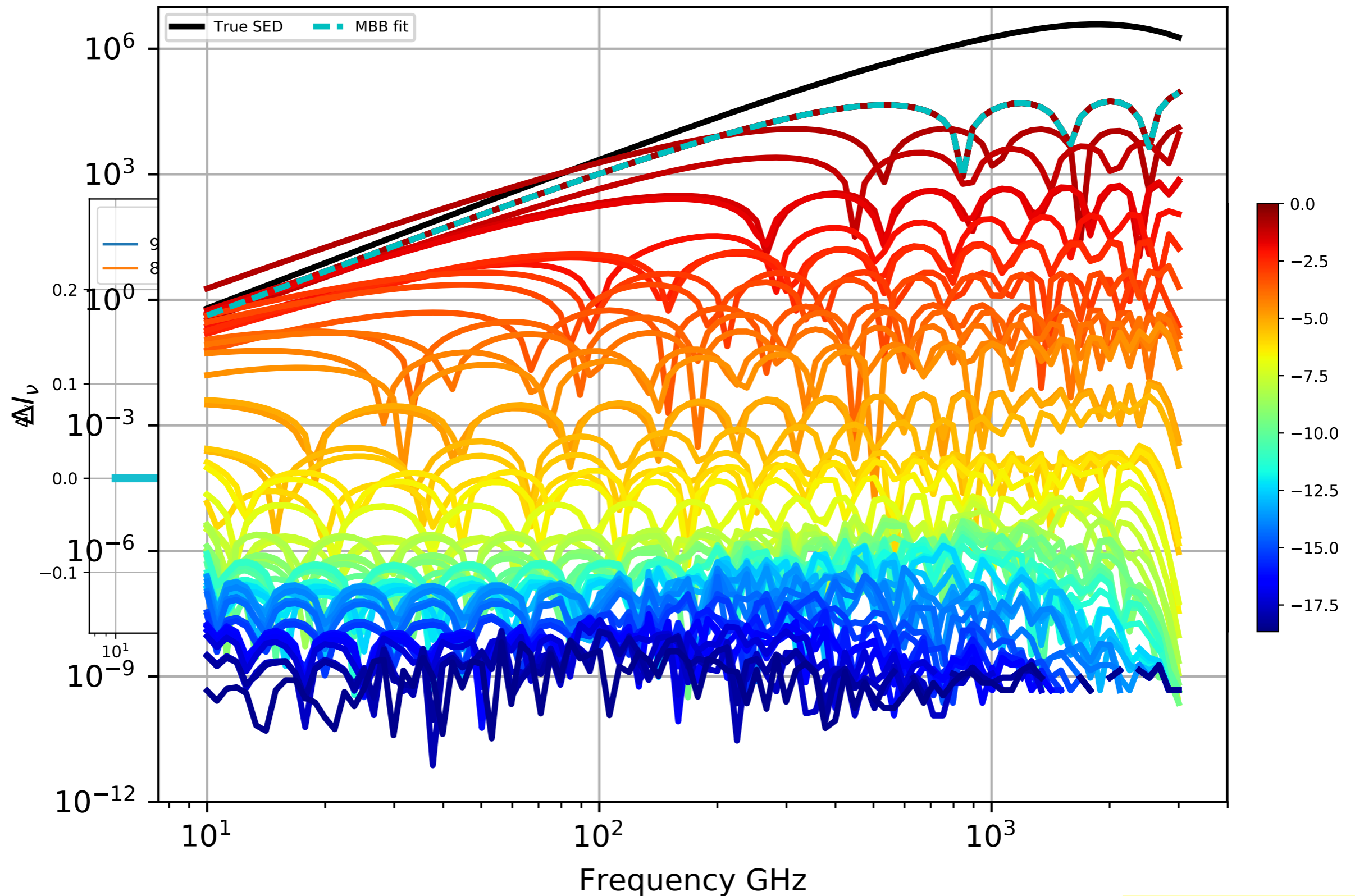


Gram - Schmidt orthogonalize and find coefficients of these vectors. Those are related to moment maps



Maximum likelihood methods: inverting the matrix equation taking into account the error in the measured SED.

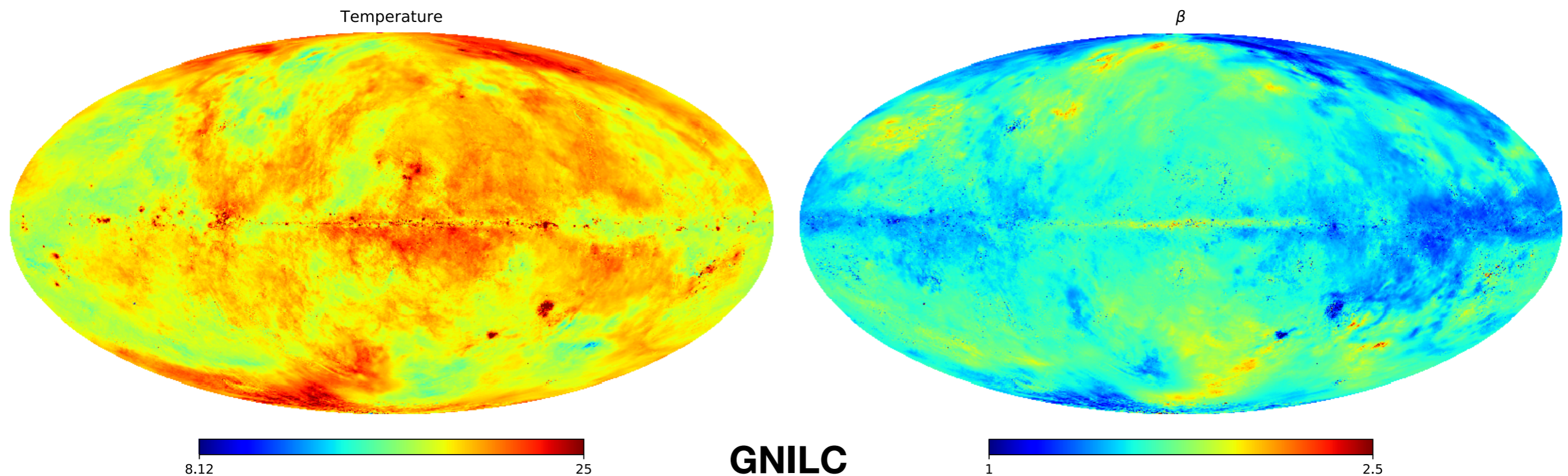
Gram-Schmidt orthogonal basis



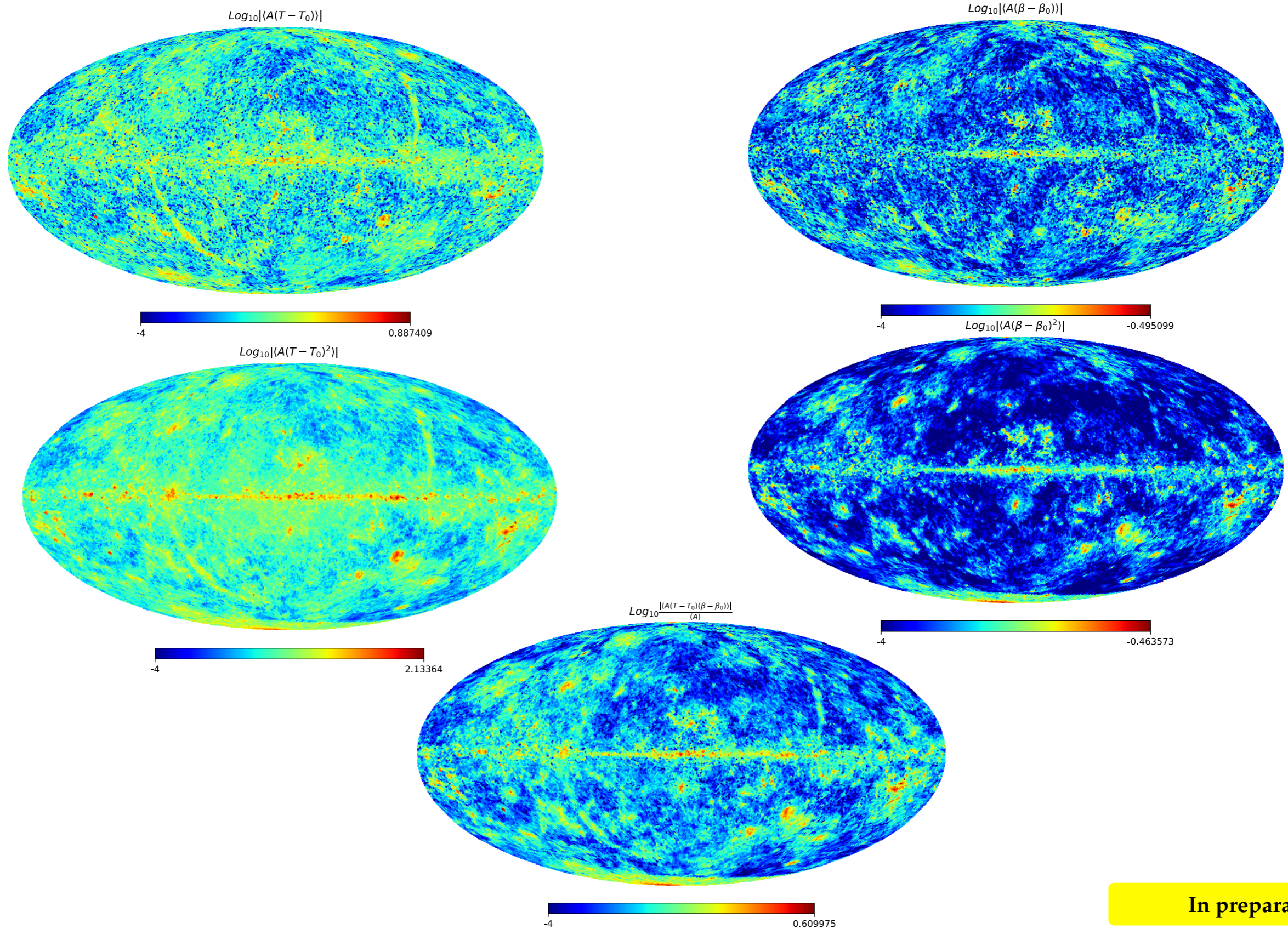
Two component MBB: [9.75 K, 1.63] + [15.7, 2.82]

In preparation

What moments do we expect from galactic dust emission?

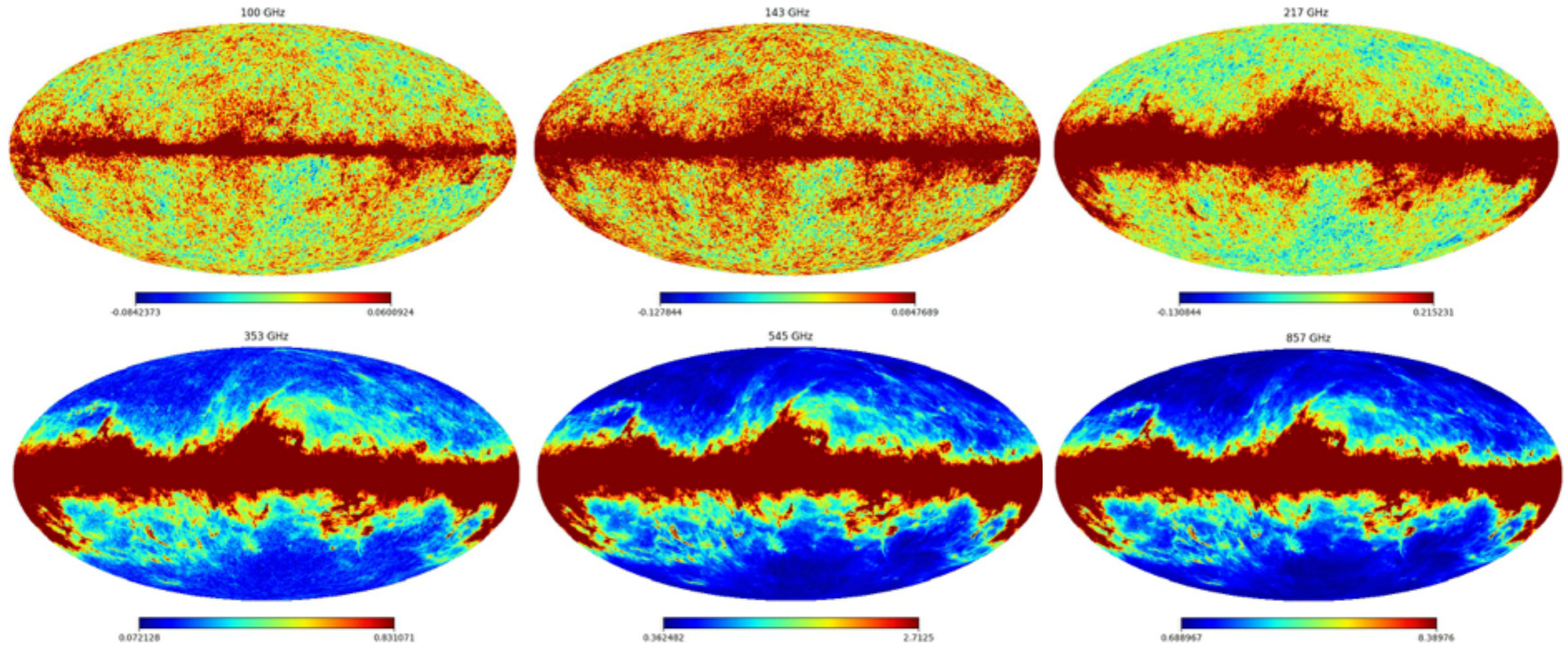


Expected dust moments



In preparation

Planck HFI - CMB

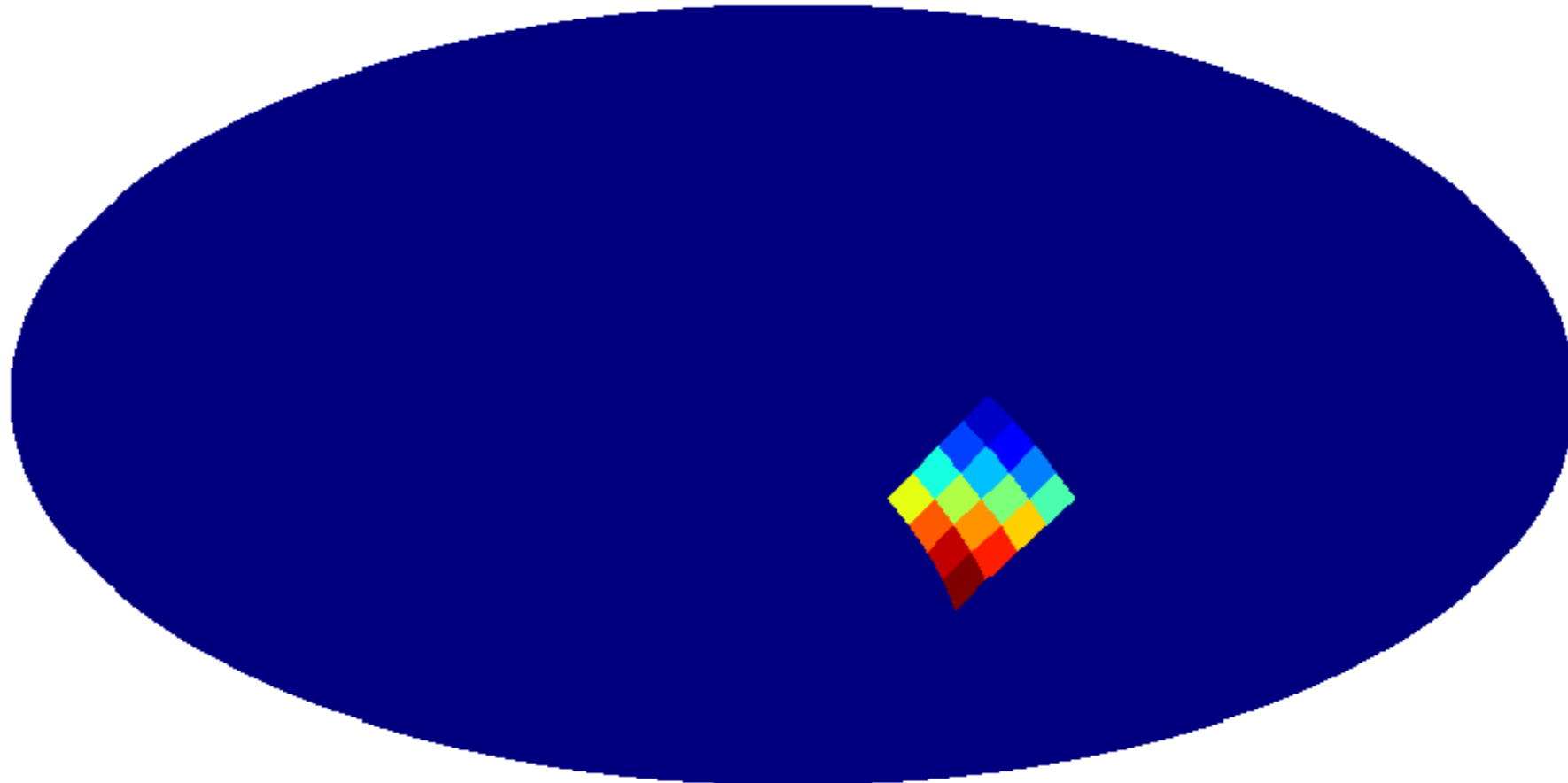


Analysis strategy

Solve for the frequency dependent part in coarser **parent pixels**

Fit a modified black body: $B_\nu(\alpha, T) = \frac{2h\nu^3}{c^2} \left(\frac{\nu}{\nu_0} \right)^\alpha \frac{1}{e^{\frac{h\nu}{kT}} - 1}$

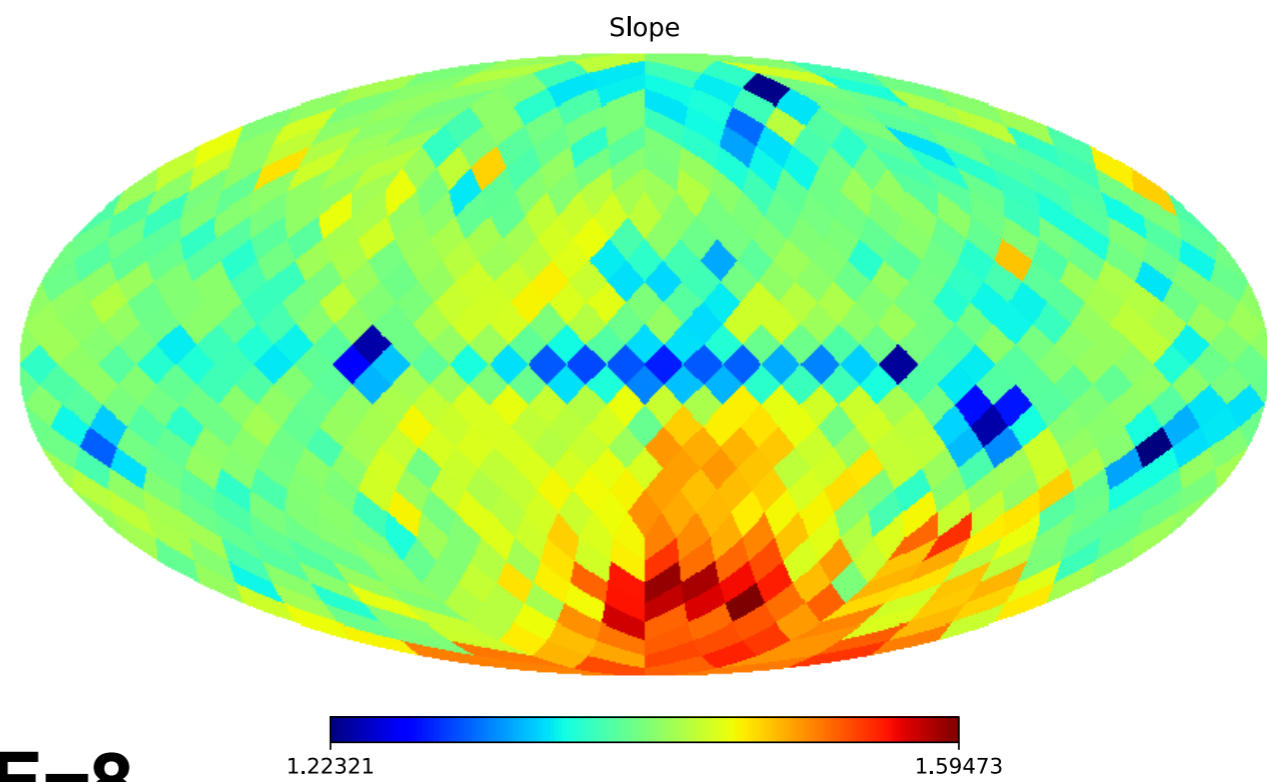
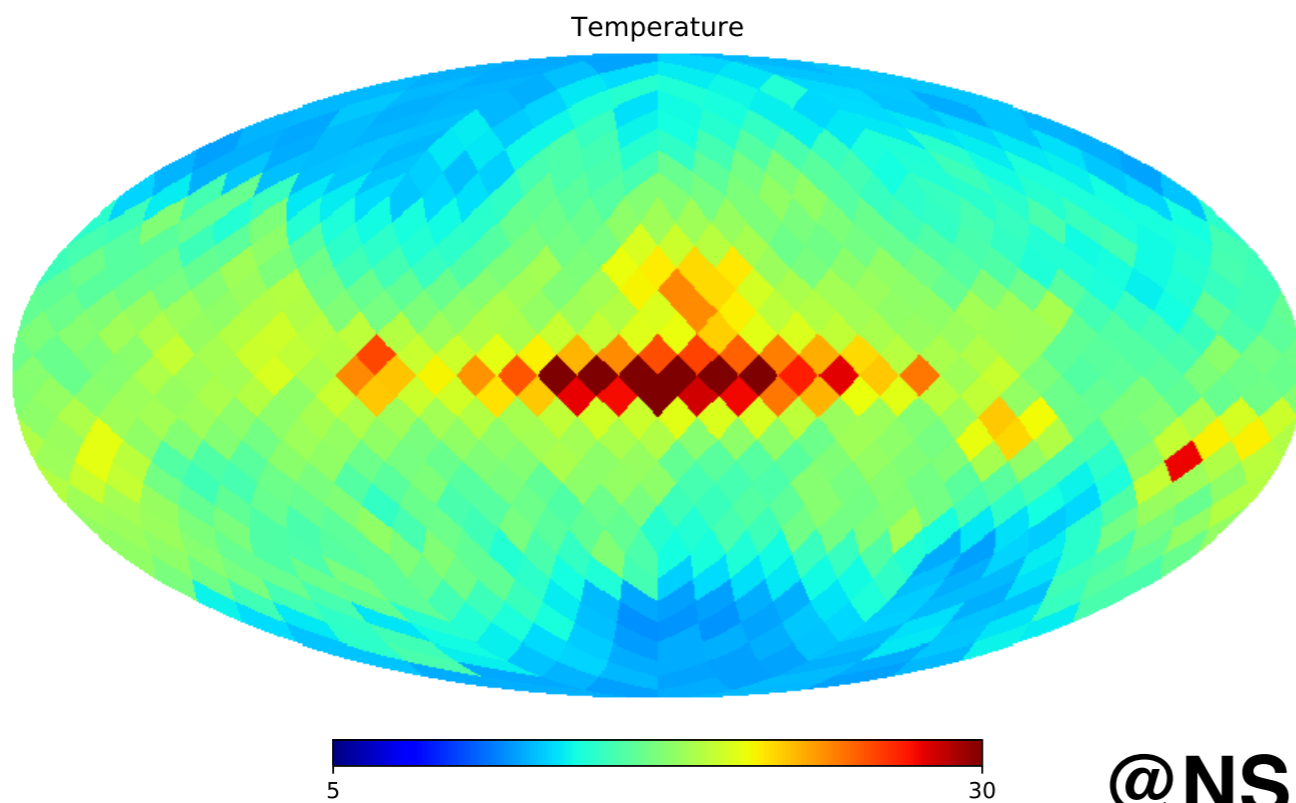
Parent pixel



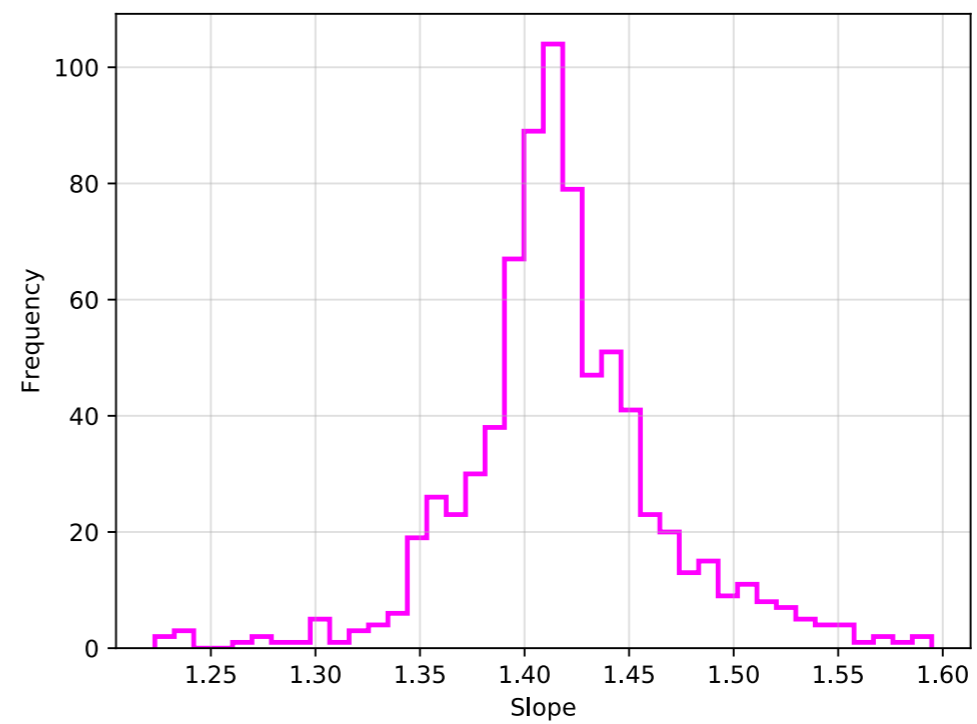
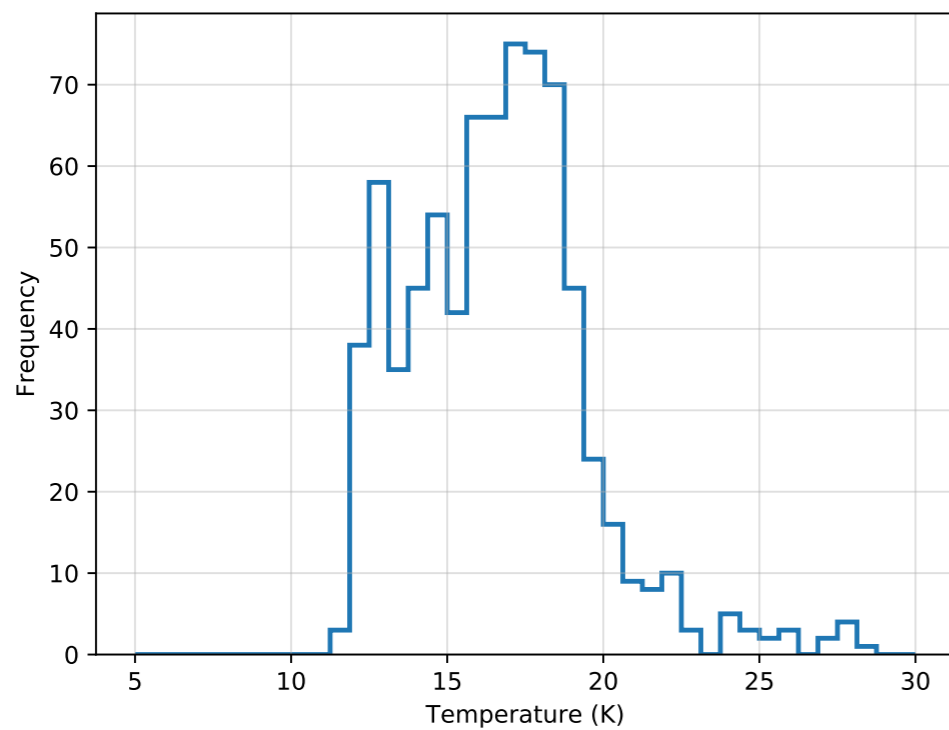
Solve for spatially varying moments in the **children pixels**

$$\mathcal{M} = [B^T N^{-1} B] B^T N^{-1} S_{nu} \quad C_{\mathcal{M}\mathcal{M}'} = [B^T N^{-1} B]^{-1}$$

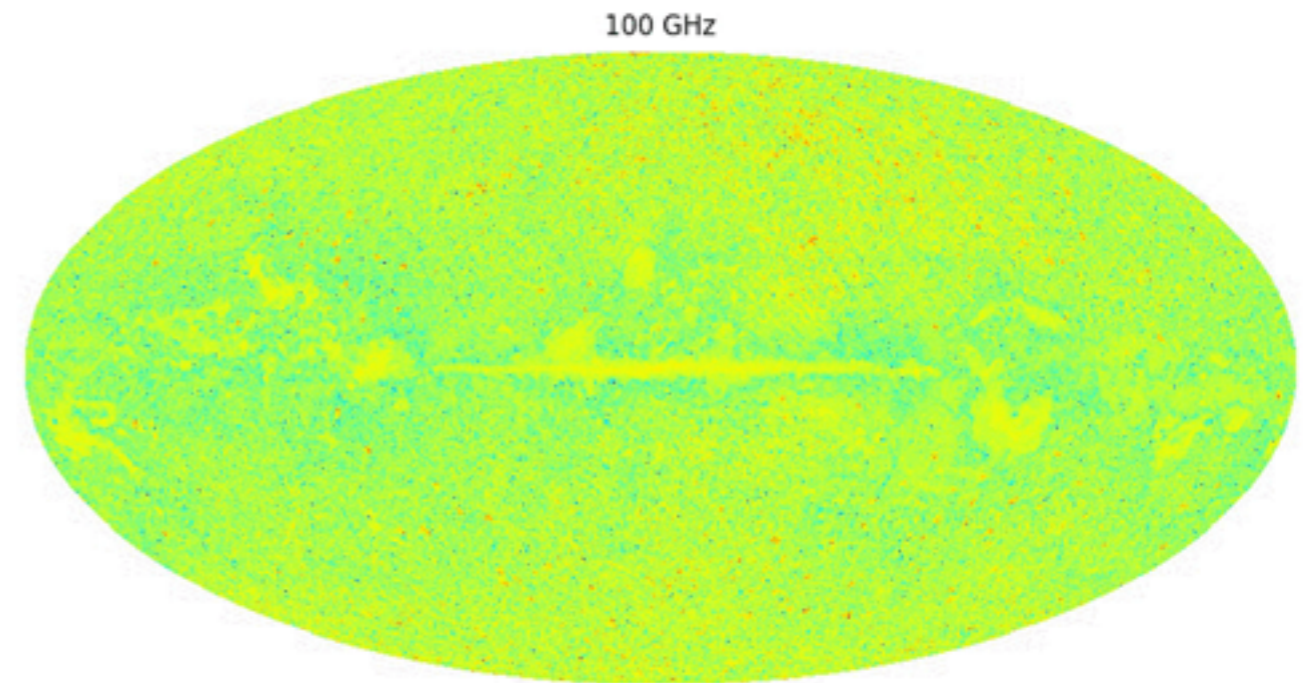
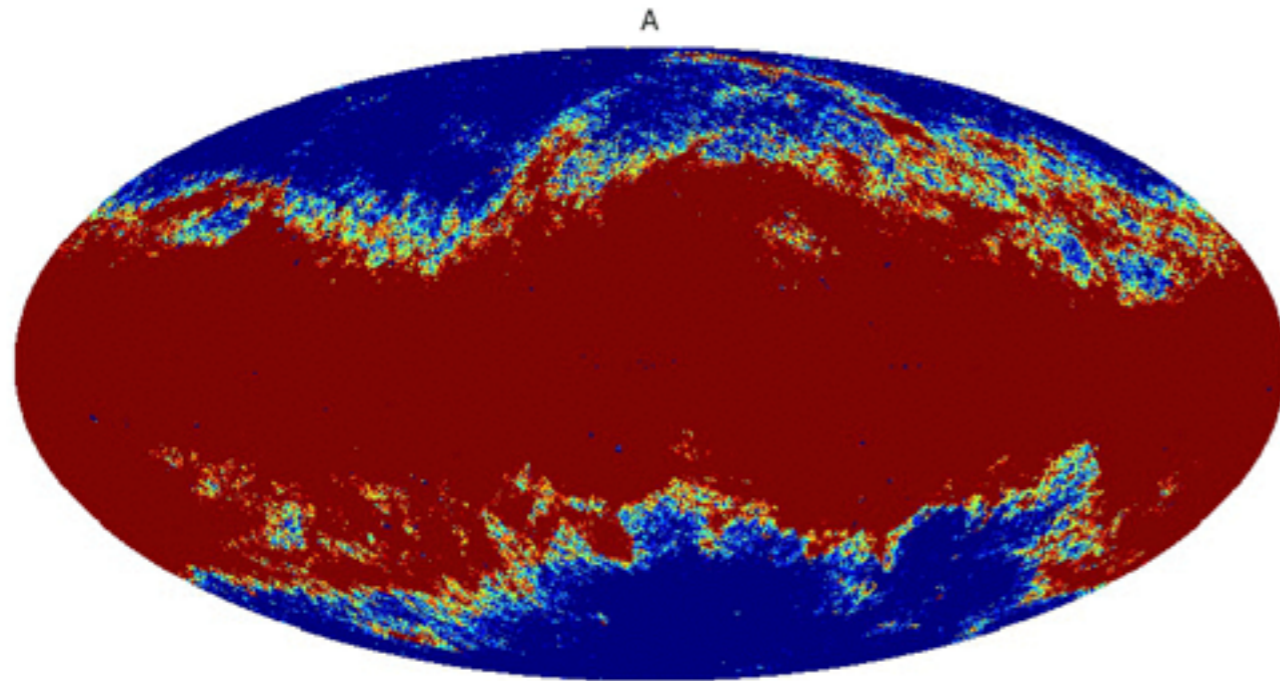
Fitting a MBB



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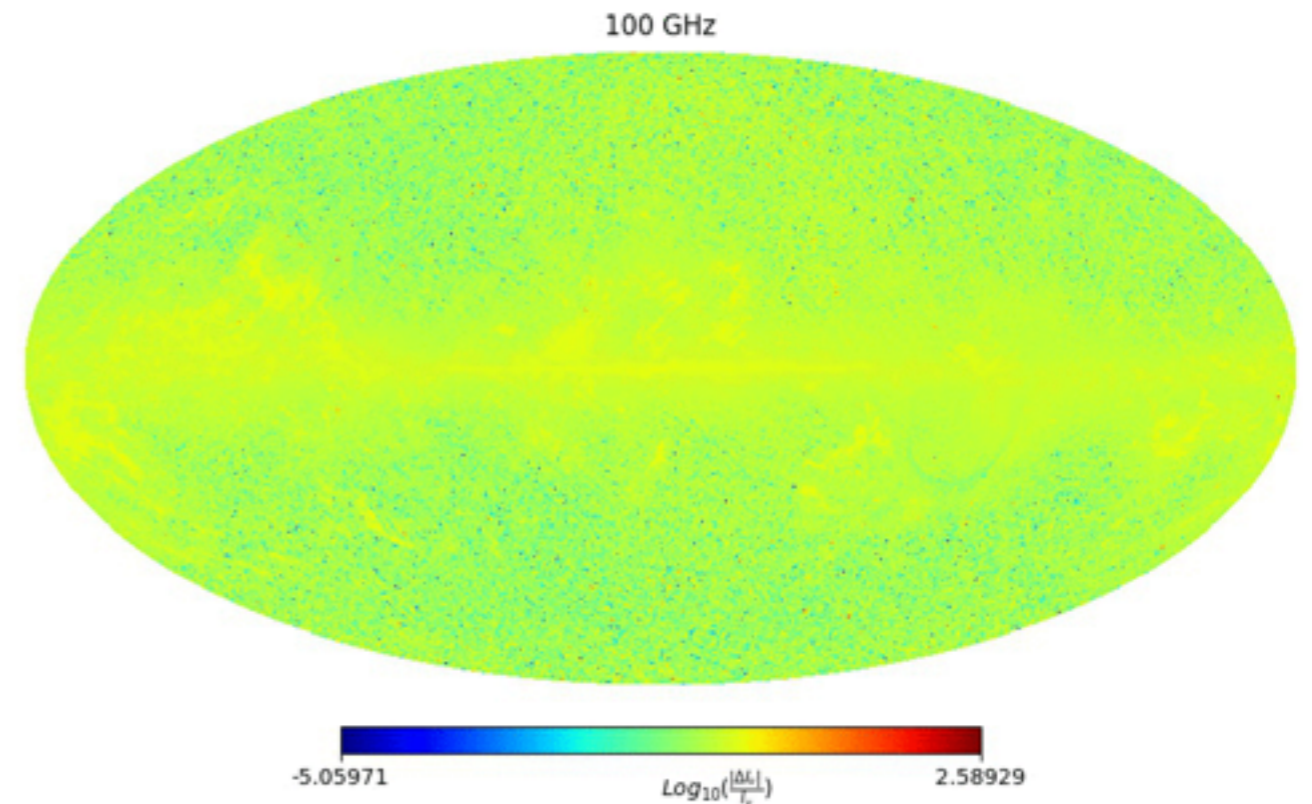
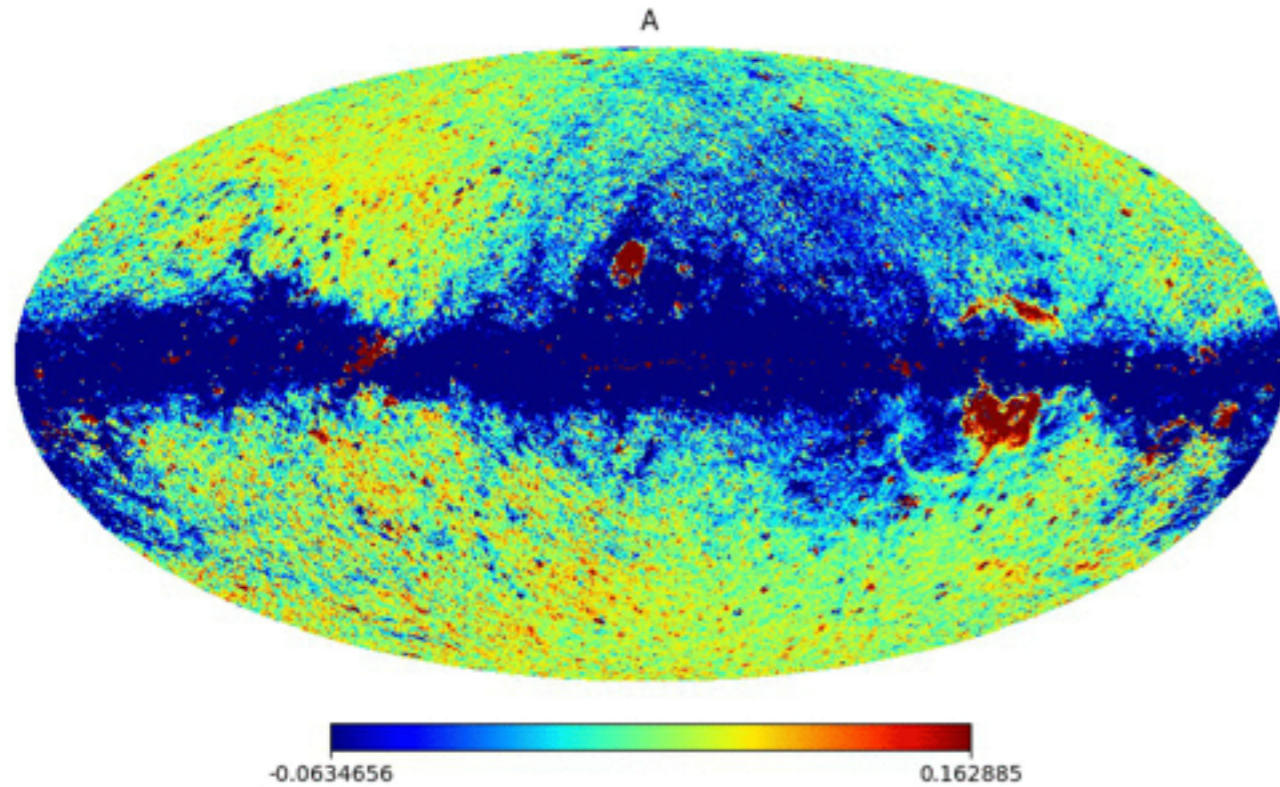


Moments maps measured from Planck HFI (3 moments)



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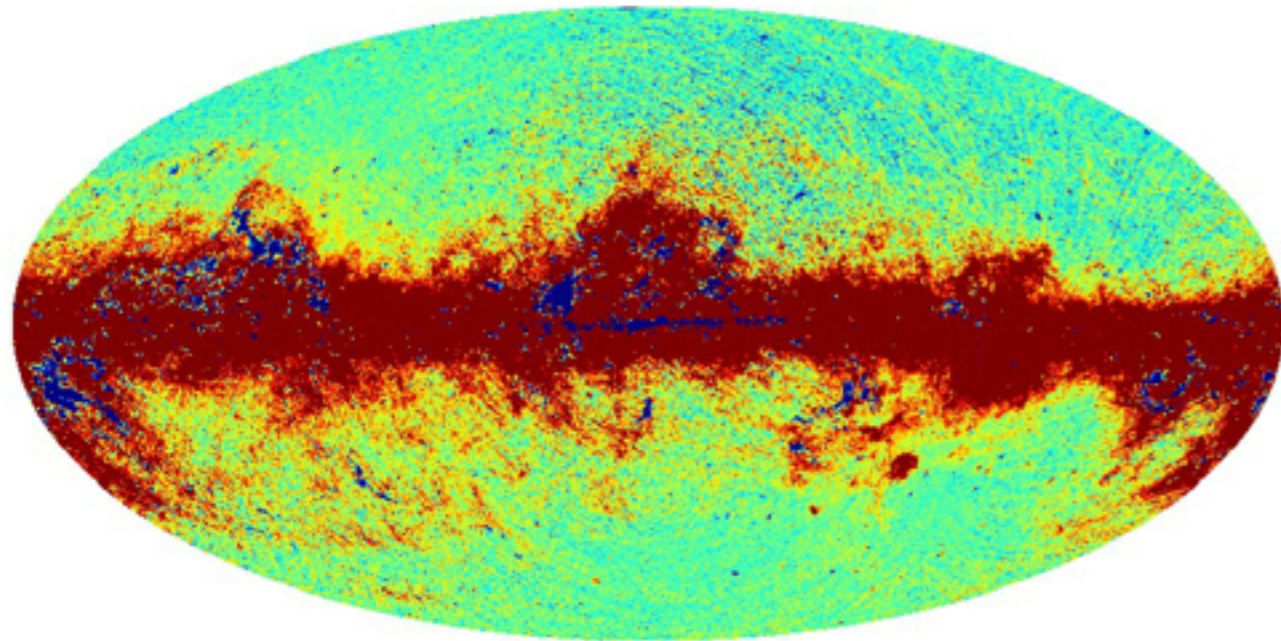
Moments maps measured from Planck HFI (4 moments)



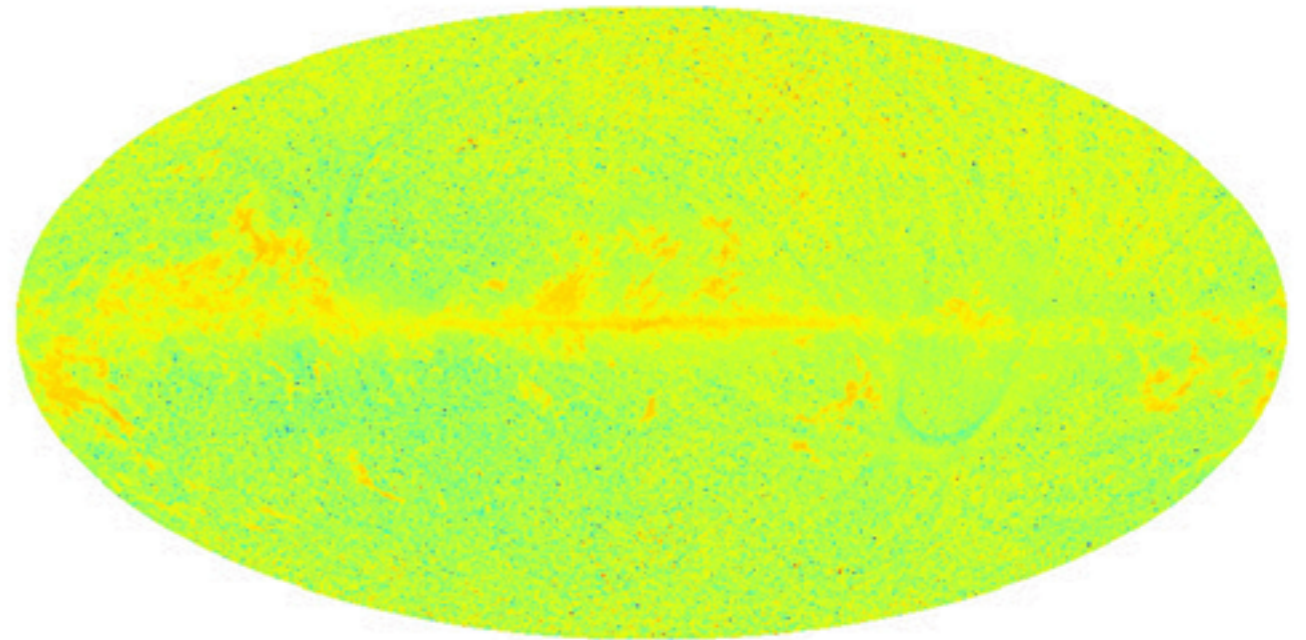
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Moments maps measured from Planck HFI (5 moments)

A



100 GHz



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Summary:

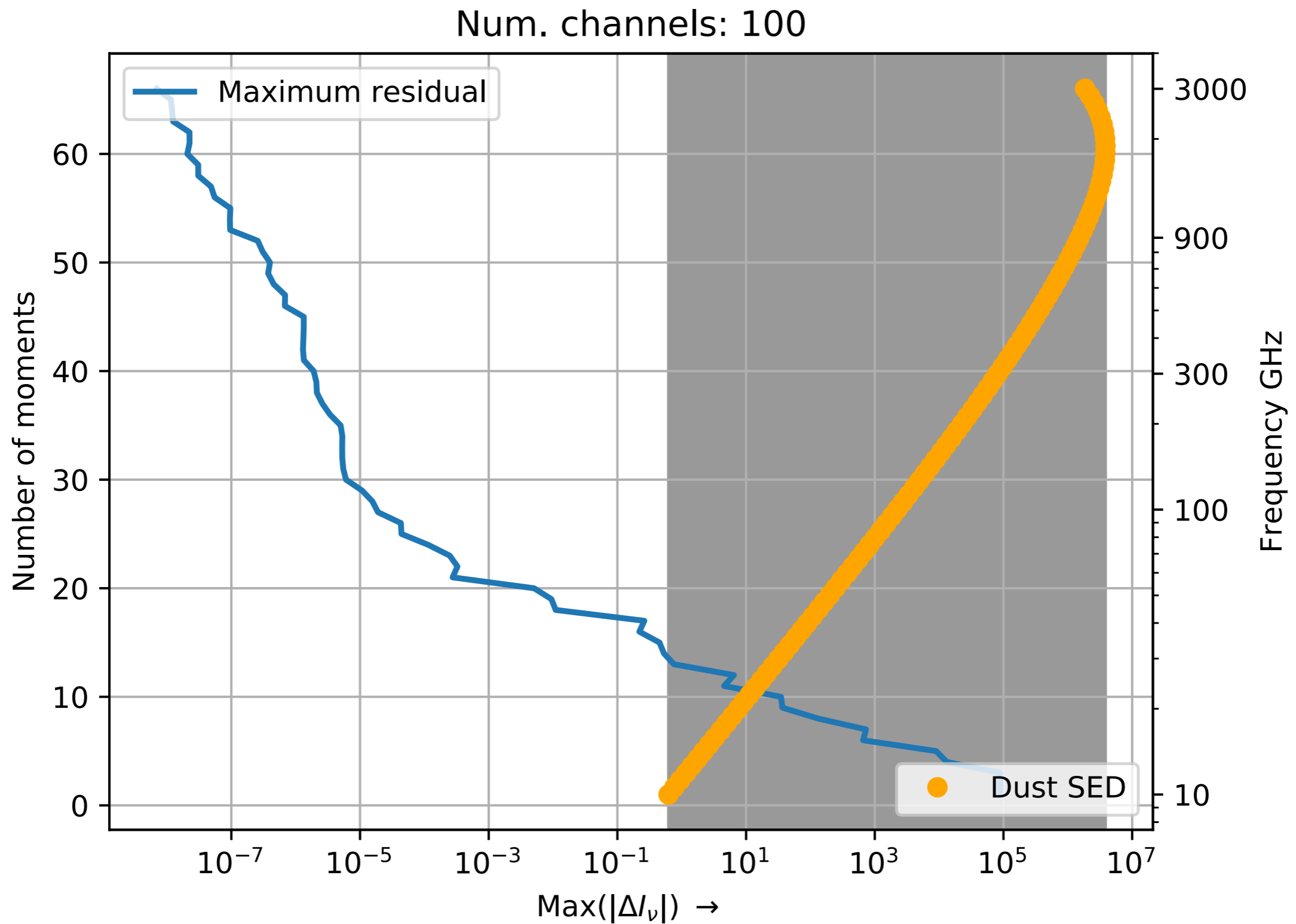
- **Due to averaging processes, simple foreground models are expected to fail at some sensitivity!**
- **The moment expansion can in principle be used to model the foregrounds to any desired accuracy** - of course at the **cost** of having a some **minimum number of frequency channels** - **determined by the desired accuracy** - and the **foreground complexity**.
- **Performed the first moment analysis on Planck HFI maps to derive constraints on higher moment maps. [PRELIMINARY]**

Ongoing:

- **Moment analysis on other components (dust, synchrotron, free-free, AME etc.) for intensity data.**
- **Extending the moment formalism for polarization.**

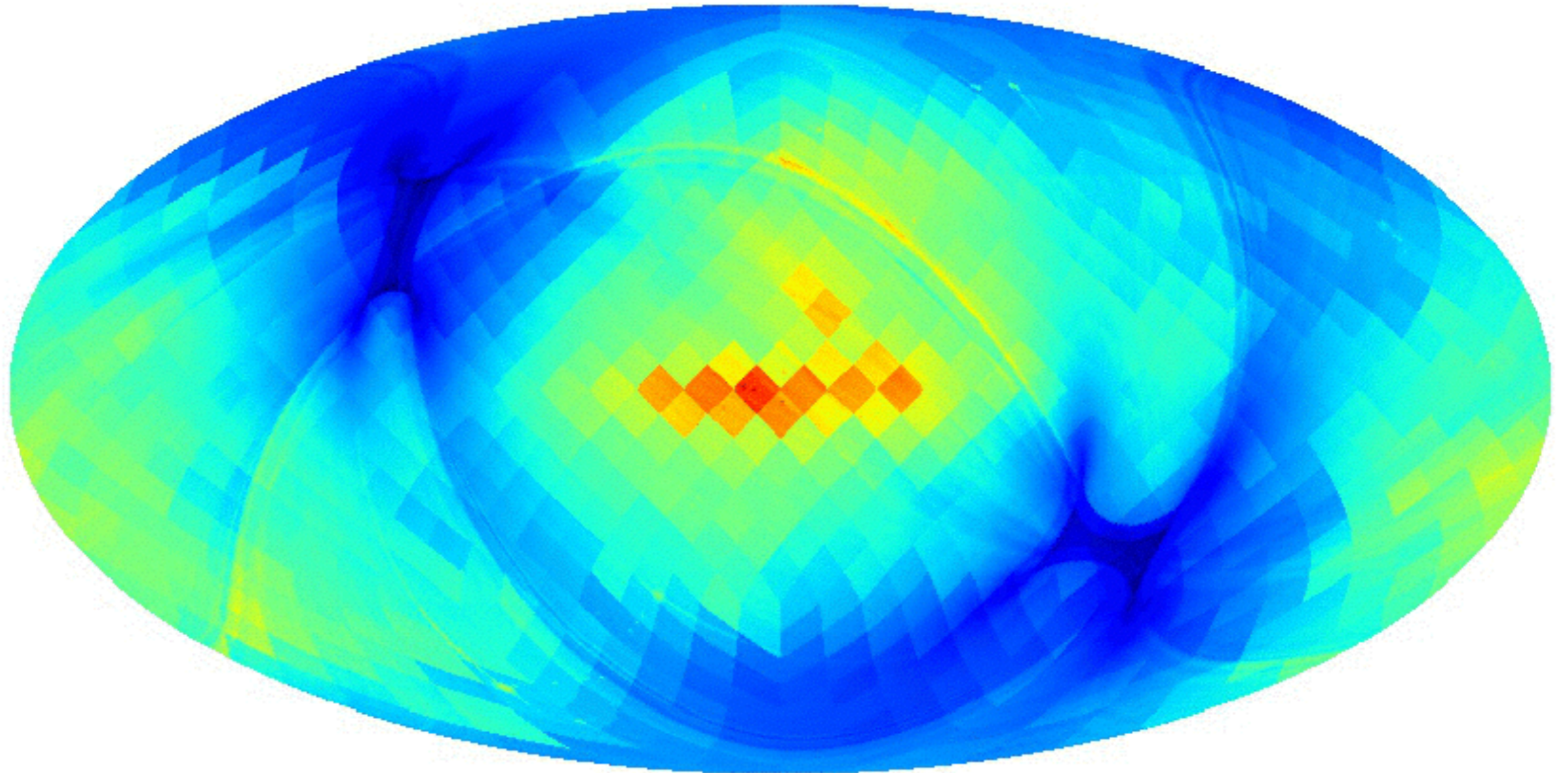
Supplementary slides

An alternate view



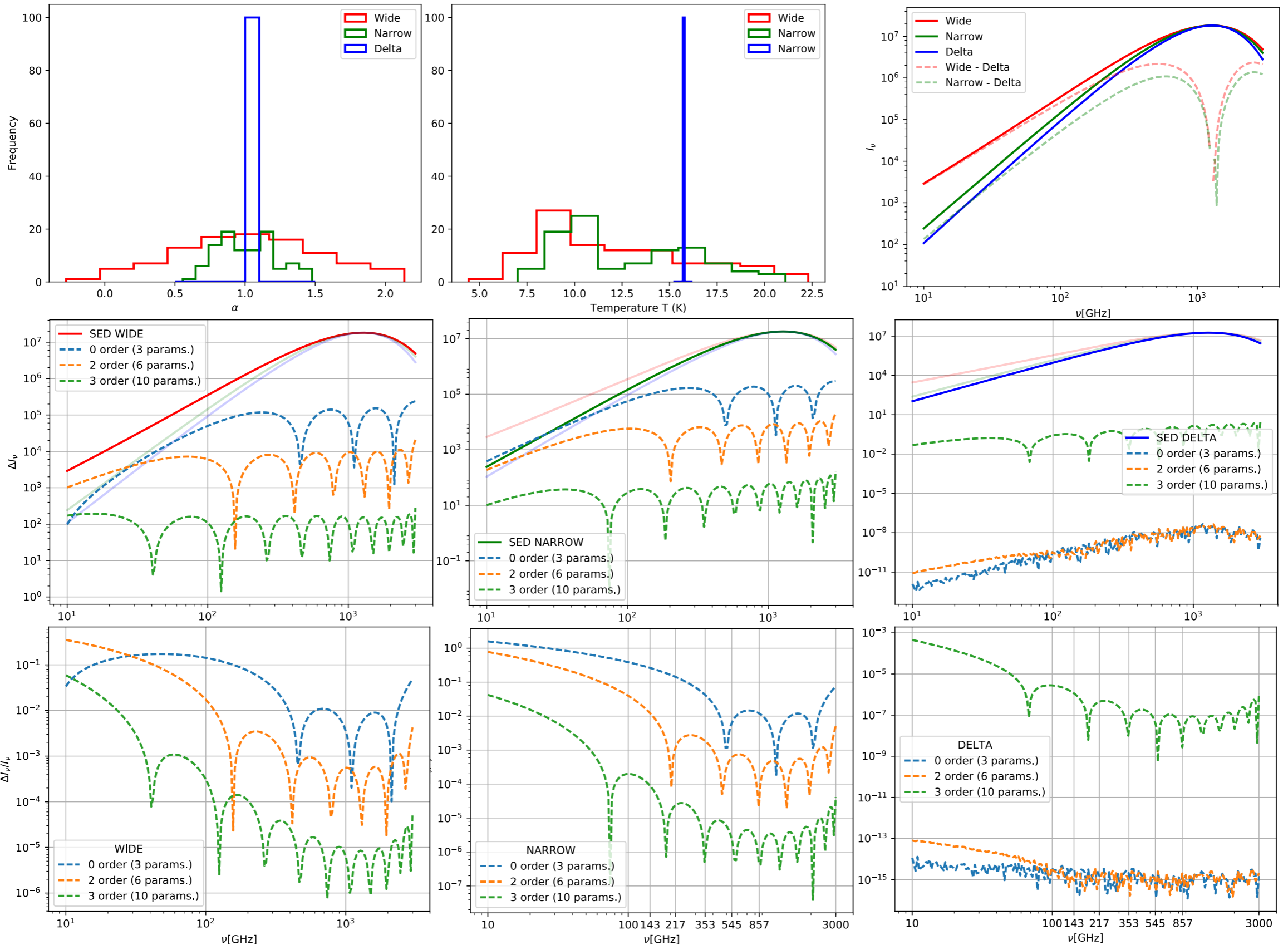
Moment statistics

A covariance



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Toy model SED's

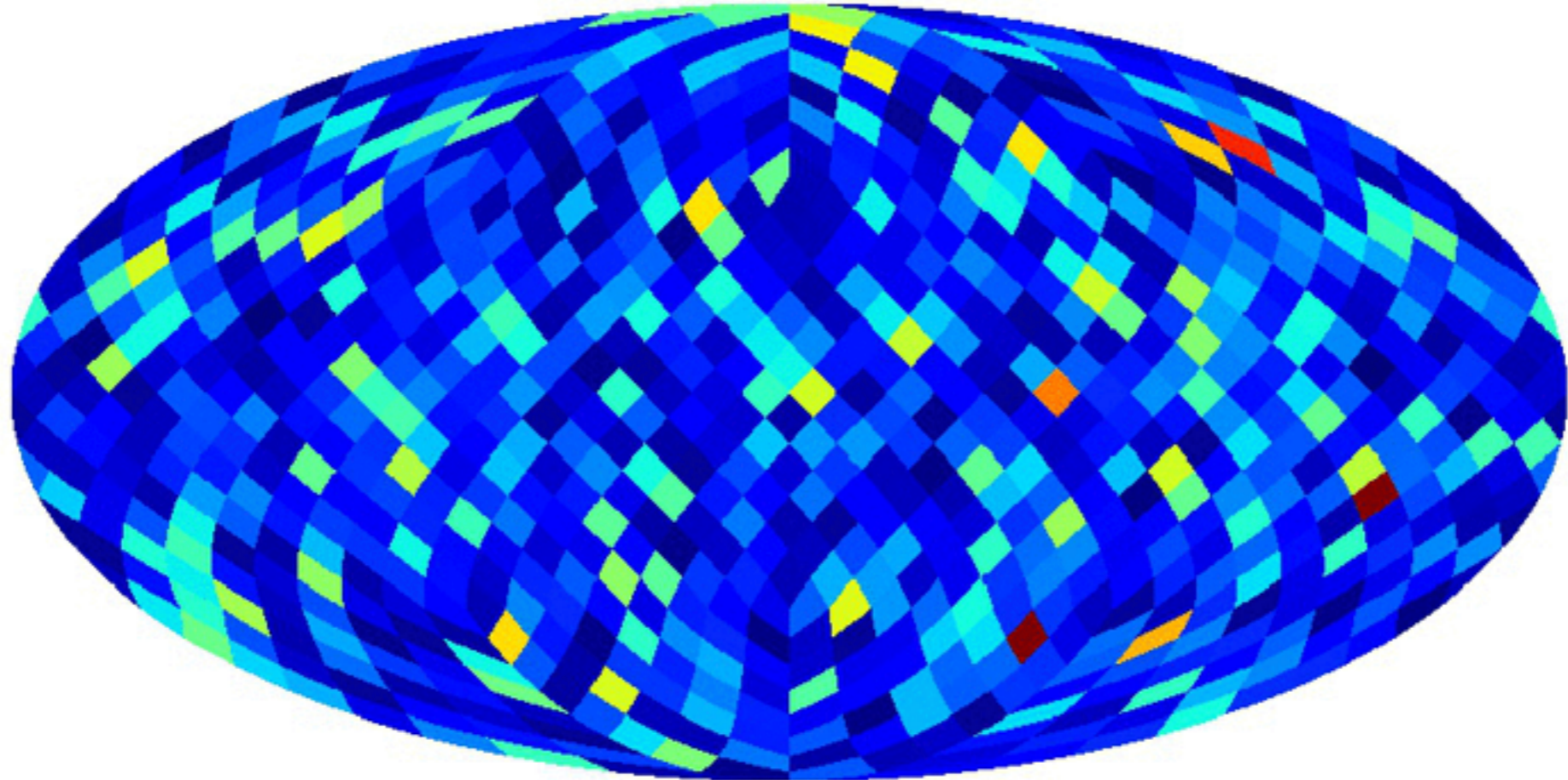


The path to connecting parametric and non-parametric methods

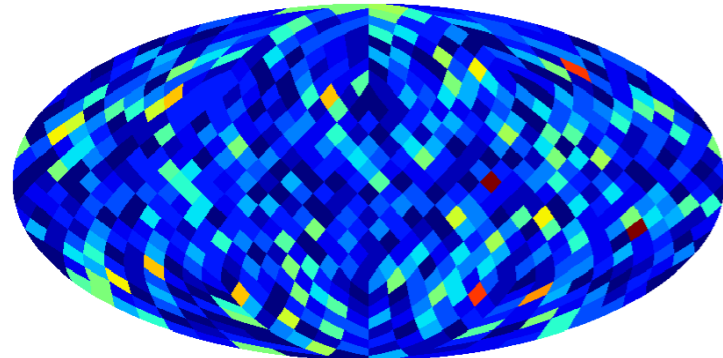
$$C_{\ell}^{\bar{\nu}} = F_{\bar{\mu}}^{\bar{\nu}}(\vec{p}_{\ell}) C_{\ell}^{\bar{\mu}} + n_{\ell}^{\bar{\nu}}$$

Model: $\sigma_T = 5, \sigma_\alpha = 0.2, N = \text{Chi}^2(5)$

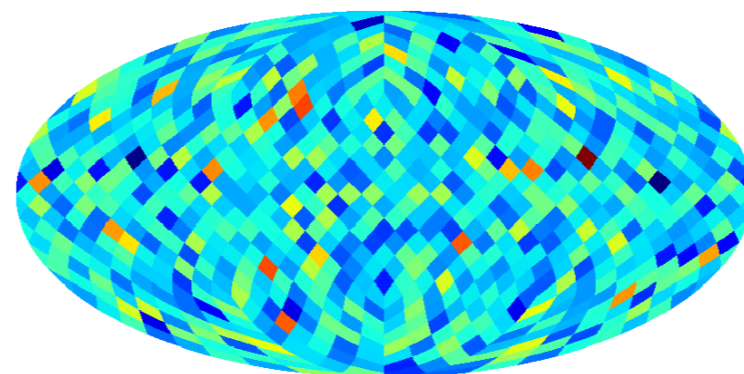
10.0 GHz



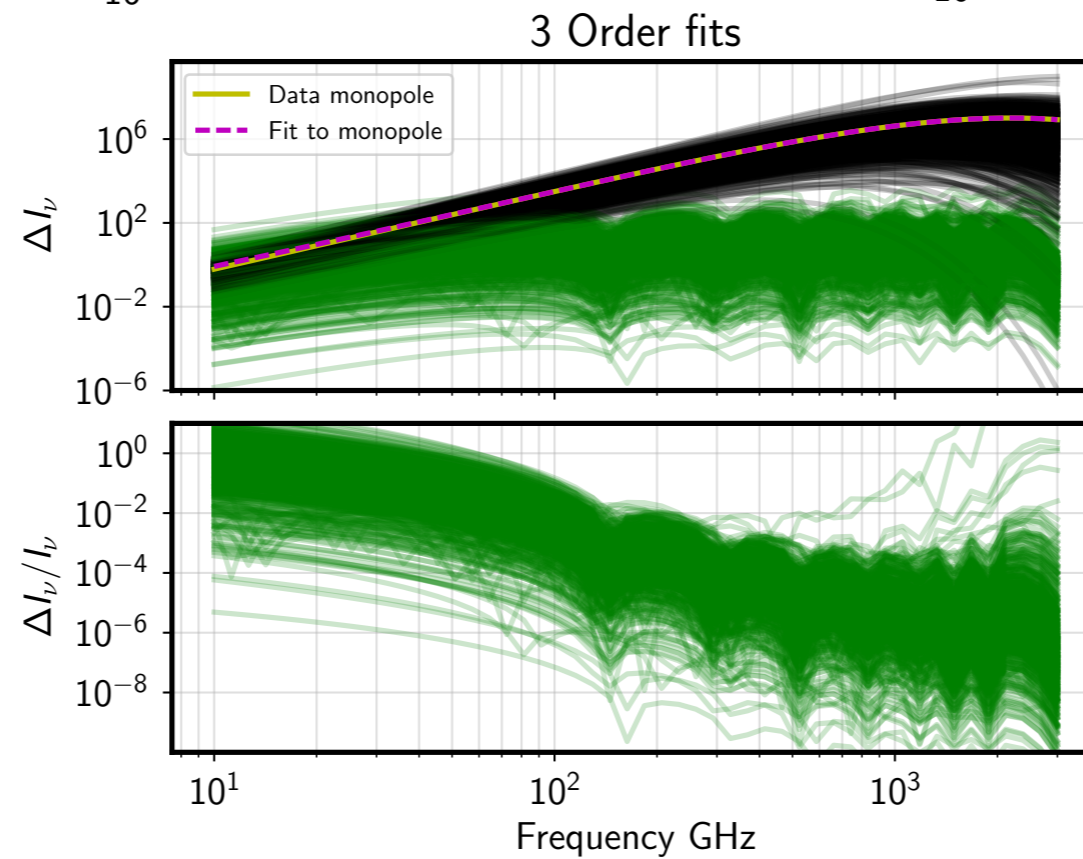
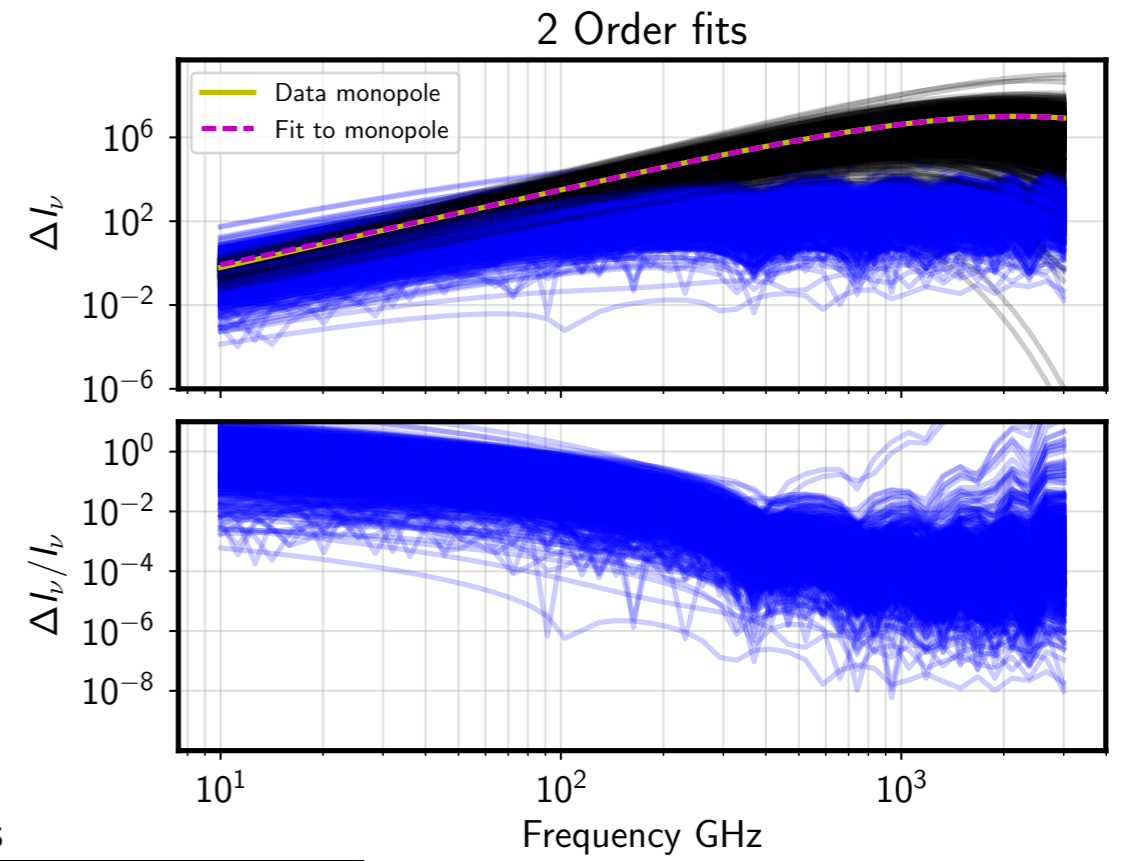
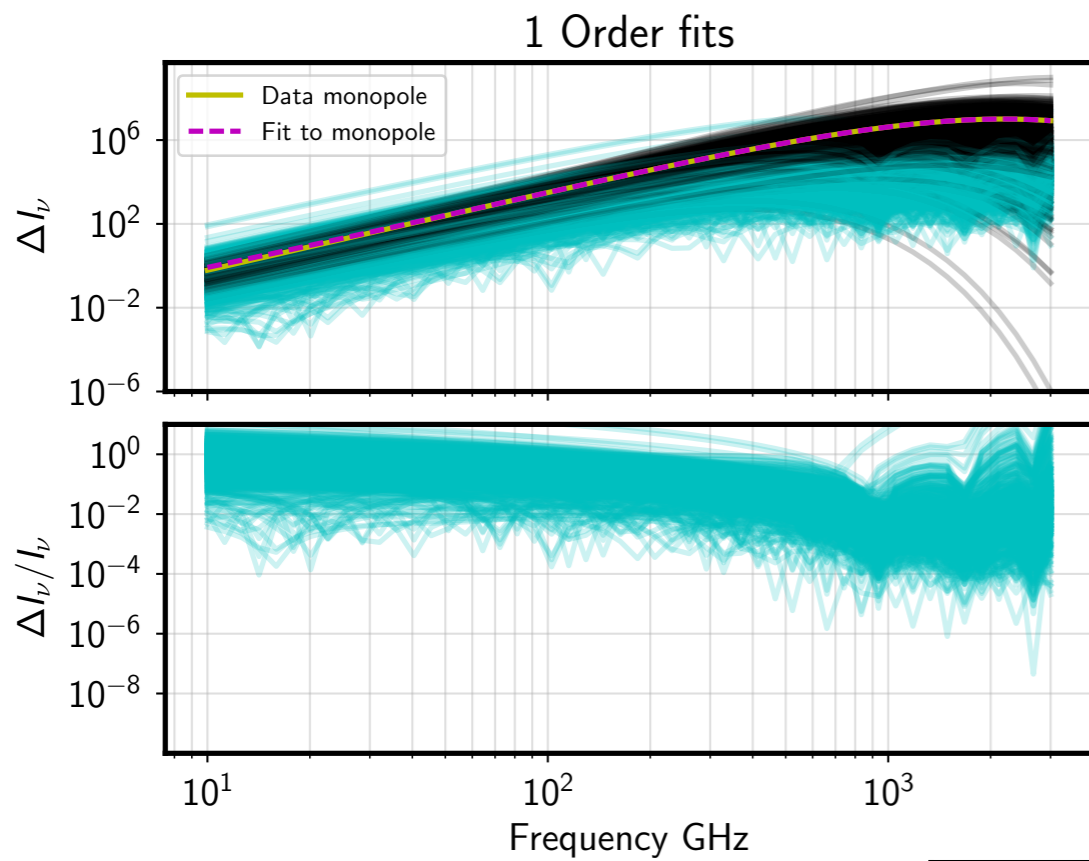
Number of emitters



Mean slope α



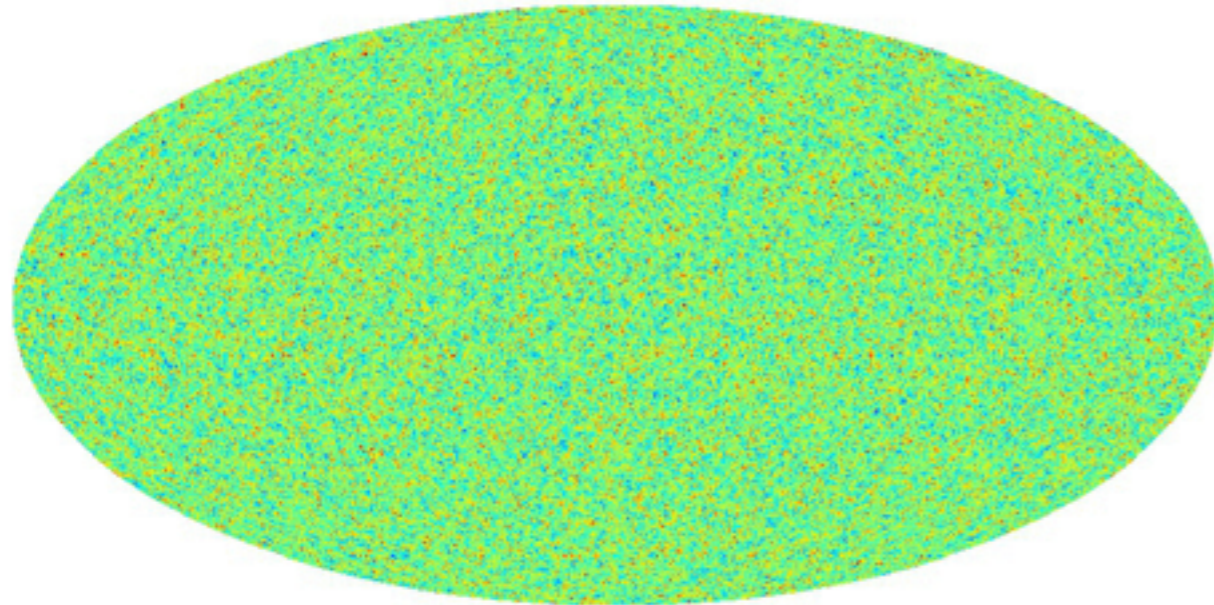
Moment fits



Visualizing moments

Data

100 GHz
[Mean = 2.30e-03 ; Std. dev. = 1.15e-04]



Moments

Moment 0 [T=13.049; $\alpha=1.717$]
Median: 1.26e+00 ; Mean: 1.26e+00 ; Std. dev.: 6.14e-02

